

# The Case for the Axion.

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Colloquium  
NIKHEF  
Amsterdam  
The Netherlands  
27 January 2017

# Strong Case for Particles Beyond the Standard Model

- > Discovery of Higgs boson marks completion of SM particle content

Drei Generationen  
der Materie (Fermionen)

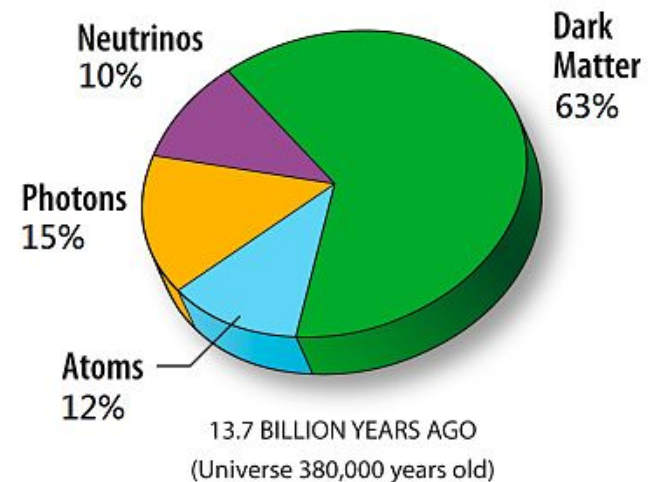
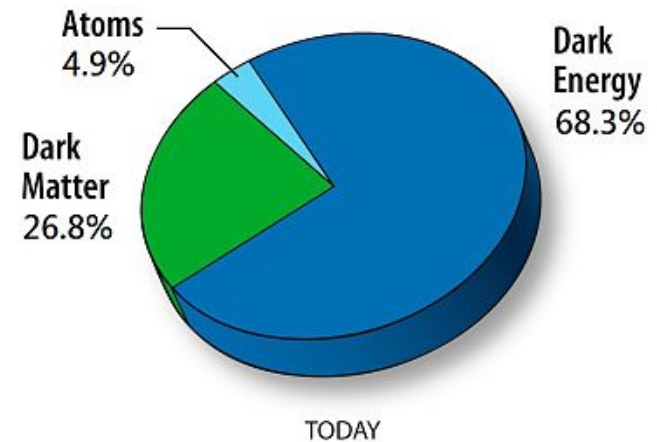
	I	II	III		
Masse →	2,3 MeV	1,275 GeV	173,07 GeV	0	125,9 GeV
Ladung →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
Spin →	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
Name →	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>γ</b> Photon	<b>H</b> Higgs Boson
				0	
	4,8 MeV	95 MeV	4,18 GeV	0	
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
<b>Quarks</b>	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b>g</b> Gluon	
	<2 eV	<0,19 MeV	<18.2 MeV	91,2 GeV	
	0	0	0	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	<b>ν<sub>e</sub></b> Elektron- Neutrino	<b>ν<sub>μ</sub></b> Myon- Neutrino	<b>ν<sub>τ</sub></b> Tau- Neutrino	<b>Z<sup>0</sup></b> Z Boson	
	0,511 MeV	105,7 MeV	1,777 GeV	80,4 GeV	
	-1	-1	-1	±1	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
<b>Leptonen</b>	<b>e</b> Elektron	<b>μ</b> Myon	<b>τ</b> Tau	<b>W<sup>±</sup></b> W Boson	<b>Eichbosonen</b>

[wikipedia]



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- > Discovery of Higgs boson marks completion of SM particle content
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  - Dark matter (DM)
  - Neutrino flavour oscillations
  - Non-observation of strong CP violation

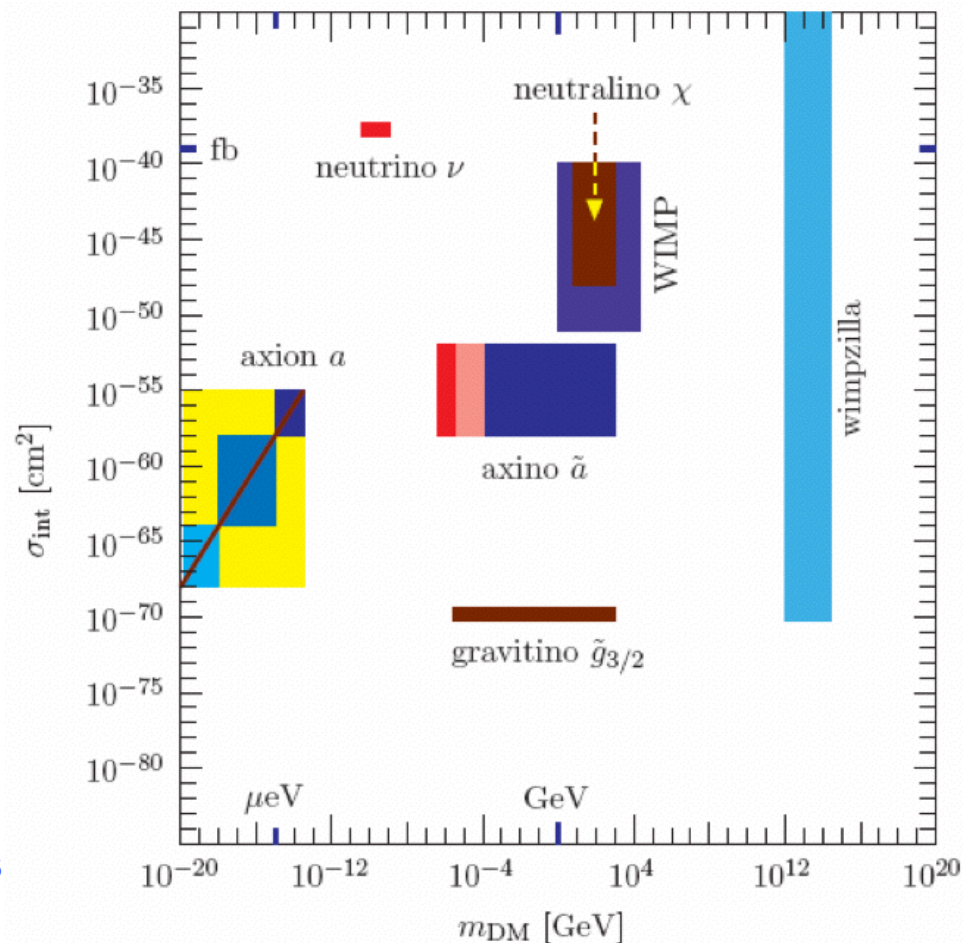


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  - Dark matter (DM)
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- Plenitude of DM candidates, e.g.:
  - Weakly Interacting Massive Particles (WIMPs), such as [neutralinos](#)
  - Very Weakly Interacting Slim (=ultra-light) Particles (WISPs), such as [axions](#)



[Kim, Carosi 10]



# Topological Theta Term and Strong CP Problem

- > Most general gauge invariant Lagrangian of QCD:

$$\mathcal{L}_{\text{QCD}} = -\frac{1}{4} G_{\mu\nu}^a G^{a,\mu\nu} + \bar{q} (i\gamma_\mu D^\mu - \mathcal{M}_q) q - \frac{\alpha_s}{8\pi} \theta G_{\mu\nu}^a \tilde{G}^{a,\mu\nu}$$

- Parameters: strong coupling  $\alpha_s$ , quark masses  $\mathcal{M}_q = \text{diag}(m_u, m_d, \dots)$  and theta angle  $\theta$  [Belavin et al. '75; 't Hooft 76; Callan et al. '76; Jackiw, Rebbi '76]

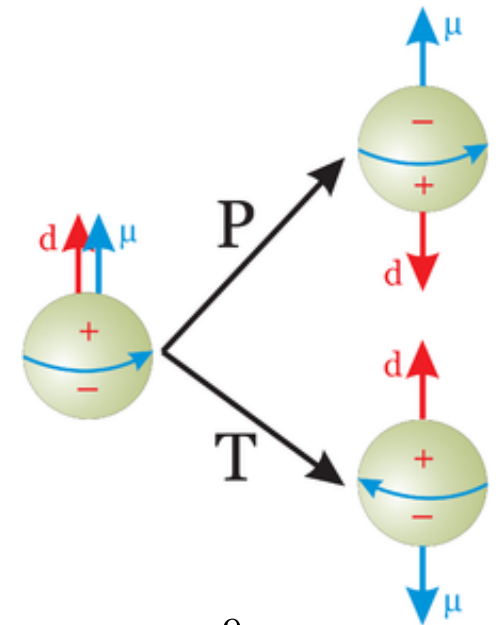
- > Topological theta term  $\propto G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} \propto \mathbf{E}^a \cdot \mathbf{B}^a$  violates P and T, and thus CP

- > Most sensitive probe of P and T violation in flavor conserving interactions: electric dipole moment of neutron; experimentally

$$|d_n| < 2.9 \times 10^{-26} \text{ e cm}$$

- > Strong CP problem:

$$d_n(\theta) \sim e \theta \frac{m_u m_d}{(m_u + m_d) m_n^2} \sim 6 \times 10^{-17} \theta \text{ e cm} \Rightarrow |\theta| < 10^{-9}$$



# Topological Theta Term and Strong CP Problem

- Theta dependence of vacuum energy density in QCD,

$$\epsilon_0(\theta) \equiv -\frac{1}{\mathcal{V}} \ln \left[ \frac{Z(\theta)}{Z(0)} \right], \quad -\pi \leq \theta \leq \pi$$

- Partition function in terms of Fourier series of Euclidean path integrals over gauge fields with fixed topological charge

$$Z(\theta) = \sum_{Q=-\infty}^{+\infty} \exp[i\theta Q] Z_Q, \quad Q = \int d^4x \frac{\alpha_s}{8\pi} G_{\mu\nu}^b \tilde{G}^{b,\mu\nu} \equiv \int d^4x q(x)$$

$$Z_Q = \int_Q [dG][dq][d\bar{q}] \exp \left[ - \int d^4x \left\{ \frac{1}{4} G_{\mu\nu}^a G_{\mu\nu}^a + i\bar{q}\gamma_\mu D_\mu q - \bar{q}_R \mathcal{M} q_L - \bar{q}_L \mathcal{M}^\dagger q_R \right\} \right]$$

- Since  $Z_Q$  positive, the vacuum energy density has absolute minimum at  $\theta = 0$  [Vafa, Witten '84]
- If theta were a dynamical field, its vacuum expectation value would be zero: strong CP problem solved



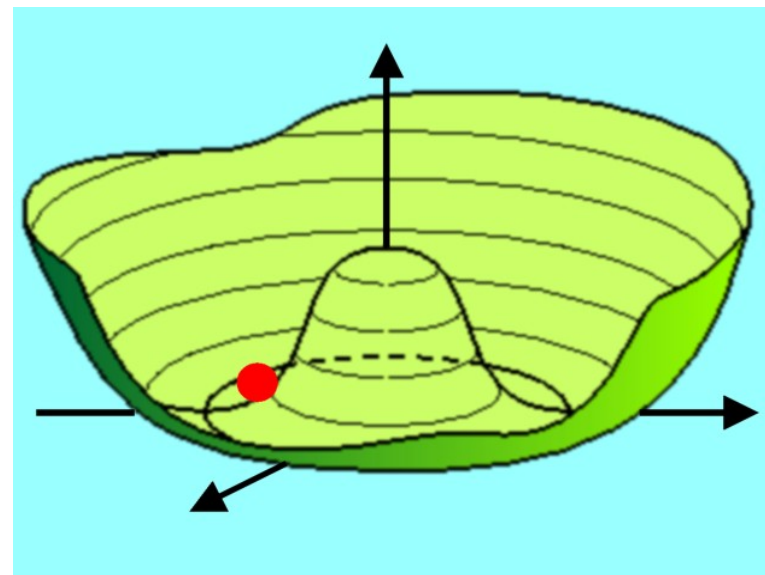
# Axionic Solution of Strong CP Problem

➤ A singlet complex scalar field  $\sigma$  featuring a global  $U(1)_{PQ}$  symmetry is added to SM

➤ Symmetry is broken by vev  $\langle \sigma \rangle = v_{PQ}/\sqrt{2}$

$$\sigma(x) = \frac{1}{2} (v_{PQ} + \rho(x)) e^{iA(x)/v_{PQ}}$$

- Excitation of modulus:  $m_\rho \sim v_{PQ}$
- Excitation of angle: NGB  $m_A \ll v_{PQ}$



[Raffelt]

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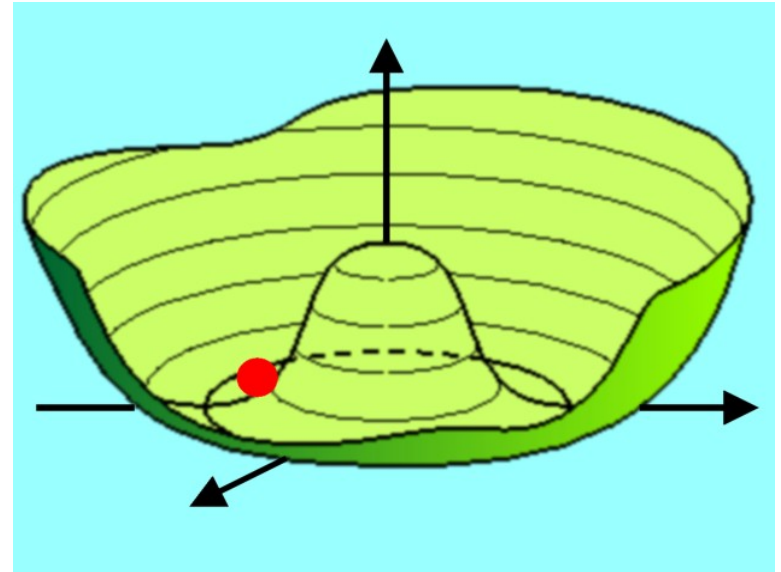
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>  $U(1)_{PQ}$  charges of quarks (SM or extra) are such that  $U(1)_{PQ} \times SU(3)_C \times SU(3)_C$  has chiral anomaly: NGB is called **axion**

[Peccei,Quinn 77; Weinberg 78; Wilczek 78]



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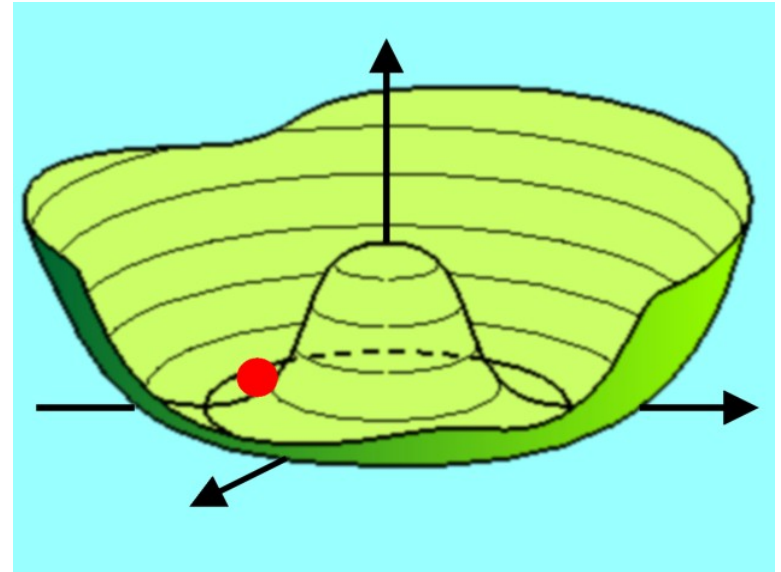
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> No strong CP problem, since axion field acts as x-dependent theta parameter

$$\mathcal{L} \supset -\frac{\alpha_s}{8\pi} \frac{A(x)}{f_A} G_{\mu\nu}^a \tilde{G}^{a\mu\nu}; \quad f_A = v_{PQ}/N_{DW}; \quad N_{DW} = \# \text{ quarks with PQ charge}$$

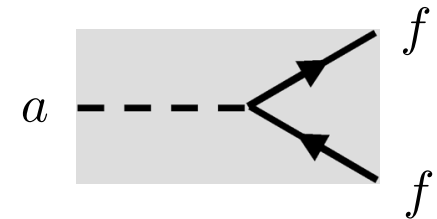
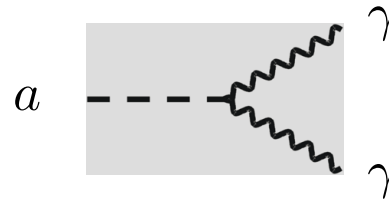
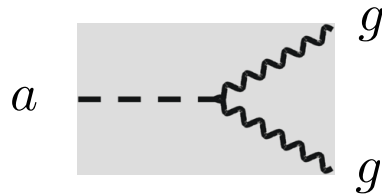
QCD dynamics:  $\langle A(x) \rangle = 0$



[Raffelt]

# Axion Couplings to SM

$$\mathcal{L} \supset -\frac{\alpha_s}{8\pi} \frac{A}{f_A} G_{\mu\nu}^a \tilde{G}^{a,\mu\nu} - \frac{\alpha}{8\pi} C_{A\gamma} \frac{A}{f_A} F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{1}{2} \frac{C_{Af}}{f_A} \partial_\mu A \bar{\psi}_f \gamma^\mu \gamma_5 \psi_f$$



- > Couplings of axion to SM suppressed by powers of

$$f_A = v_{PQ}/N_{DW} \gg v = 246 \text{ GeV}$$

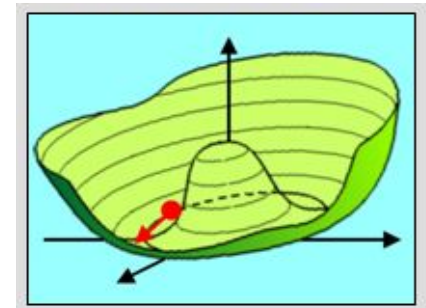
rendering the axion „invisible“

[Kim 79; Shifman, Vainshtein, Zakharov 80; Zhitnitsky 80; Dine, Fischler, Srednicki 81; ...]

- > Axion acquires a small mass from gluonic topological fluctuations:

[Weinberg '78; Wilczek '78; ... Borsanyi et al. '16]

$$m_A = \frac{\sqrt{\int d^4x \langle q(x)q(0) \rangle}}{f_A} \equiv \frac{\sqrt{\chi_0}}{f_A} = 57.0(7) \left( \frac{10^{11} \text{ GeV}}{f_A} \right) \mu\text{eV}$$

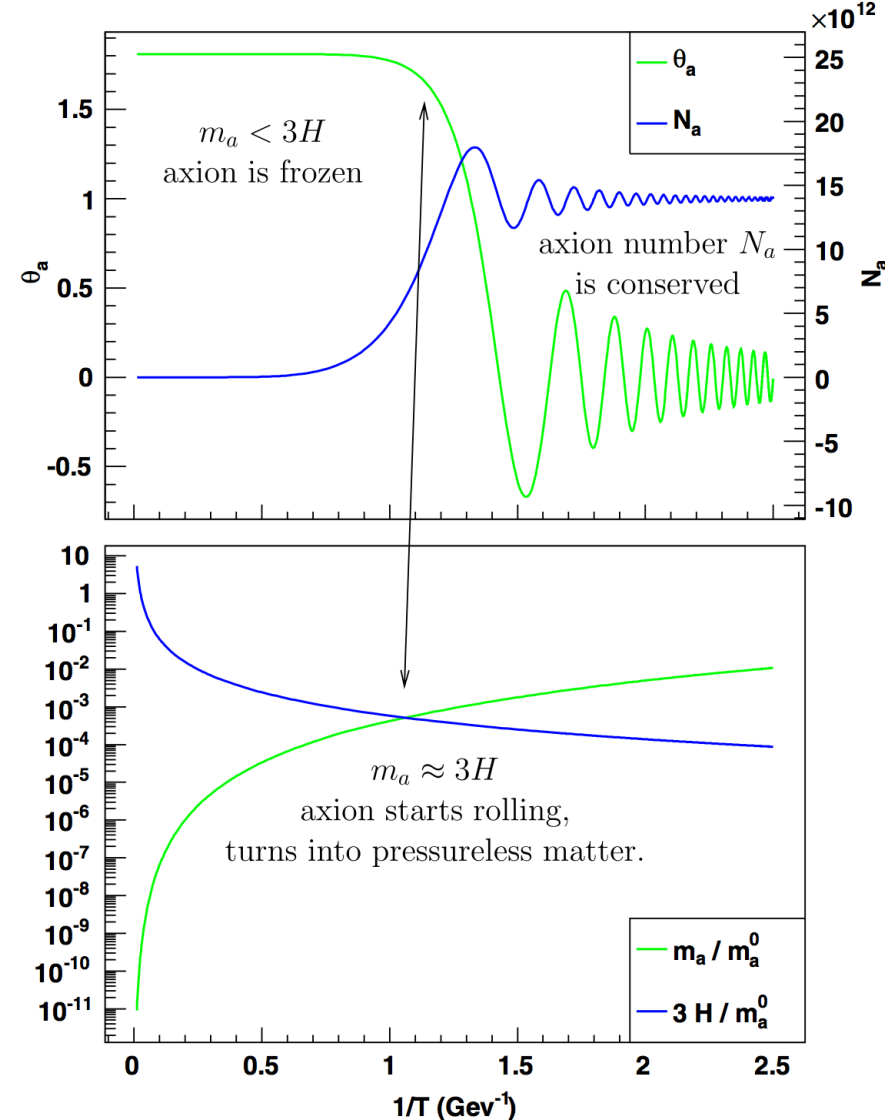


# Axion Dark Matter

## > DM from vacuum realignment:

[Preskill,Wise,Wilczek 83; Abbott,Sikivie 83; Dine,Fischler 83,...]

- In early universe, axion frozen at random initial value
- Later, field feels pull of mass towards zero and oscillates around it
- Spatially uniform oscillating classical field = coherent state of many, extremely non-relativistic particles = CDM



[Wantz,Shellard `09]



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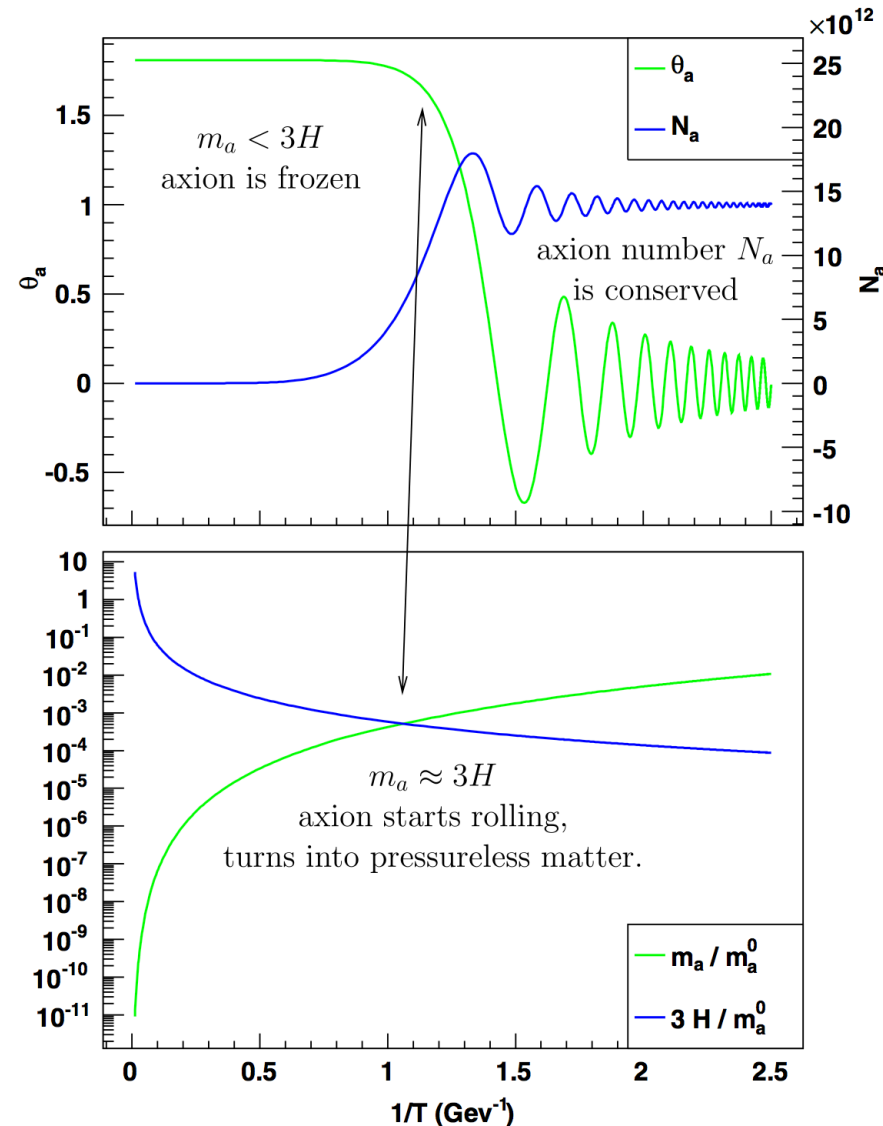
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## > Crucial QCD input for prediction of axion DM abundance:

- Equation of state at temperatures around 1 GeV: determines  $H(T)$
- Topological susceptibility:

$$\chi(T) \equiv \int d^4x \langle q(x)q(0) \rangle_T$$

determines  $m_A^2(T) = \chi(T)/f_A^2$



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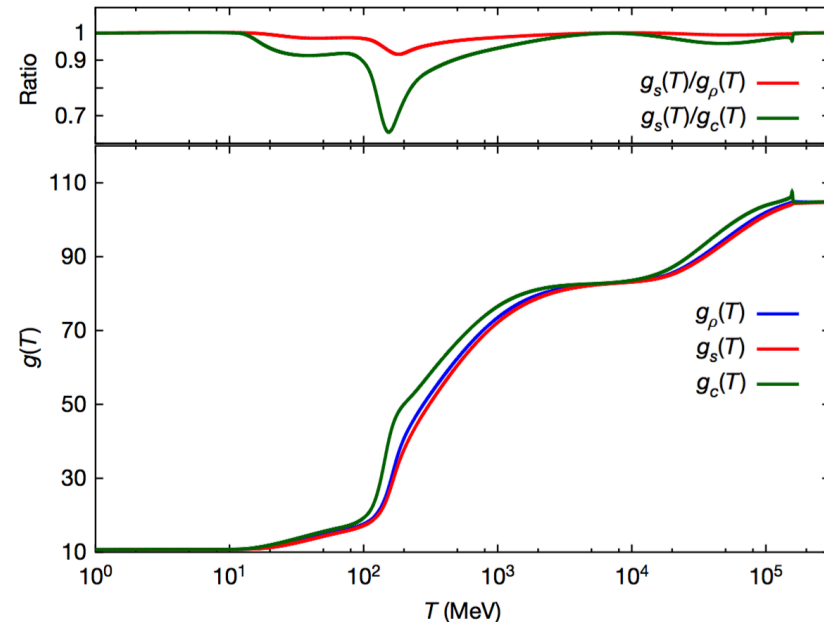
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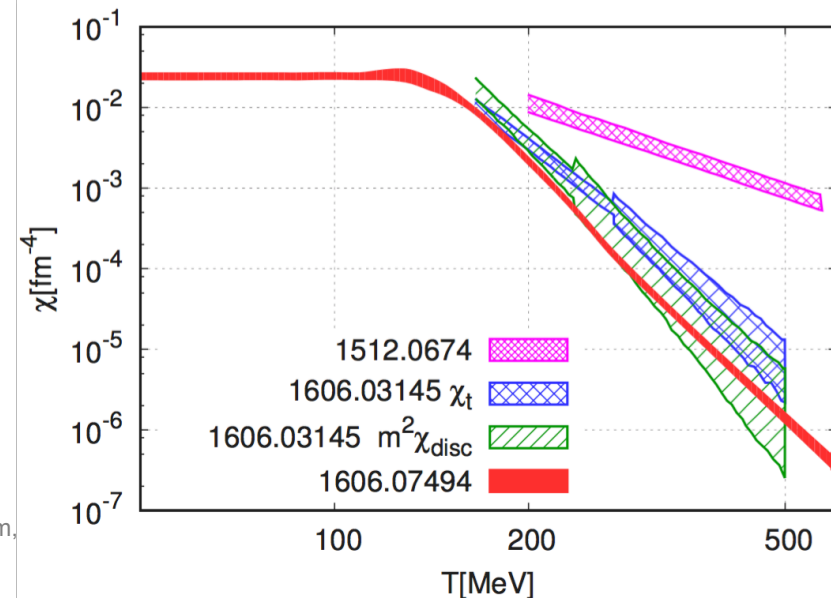
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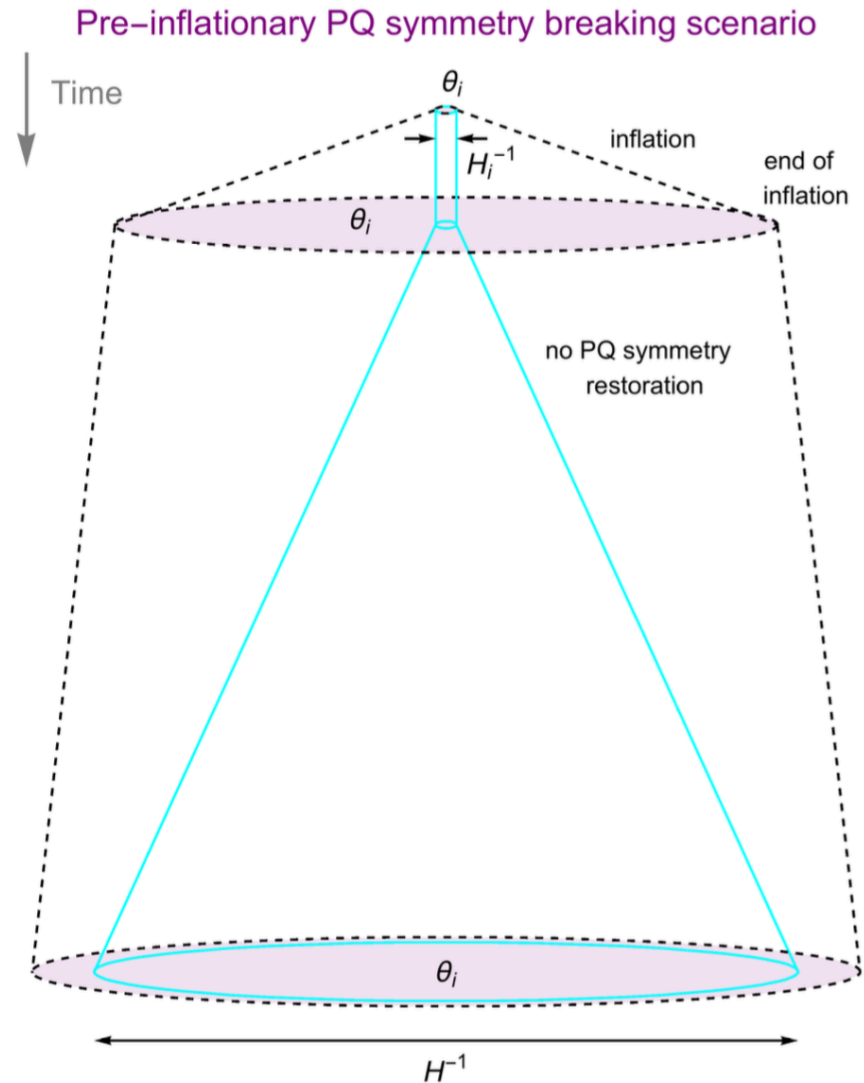


[Borsanyi et al., Nature `16 [1606.0794]]



# Axion Dark Matter

- > If U(1) symmetry broken during inflation and not restored afterwards (pre-inflationary SB breaking scenario):
  - Axion CDM density depends on single initial angle during inflation and  $f_A$

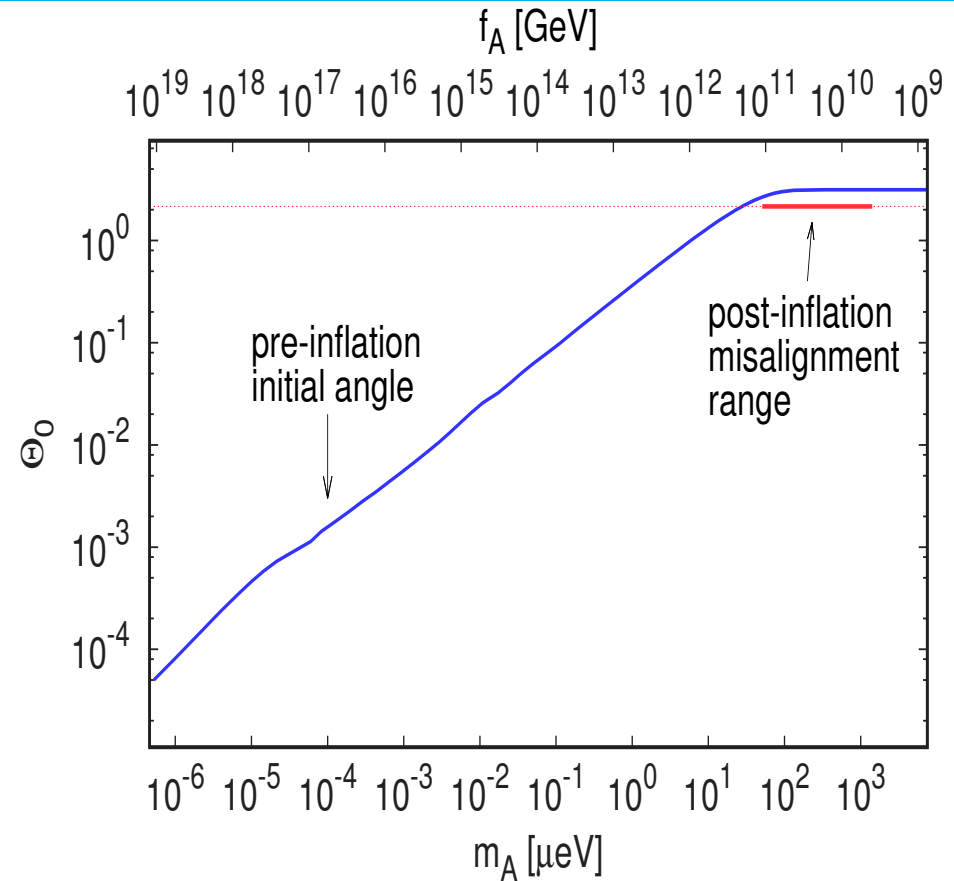


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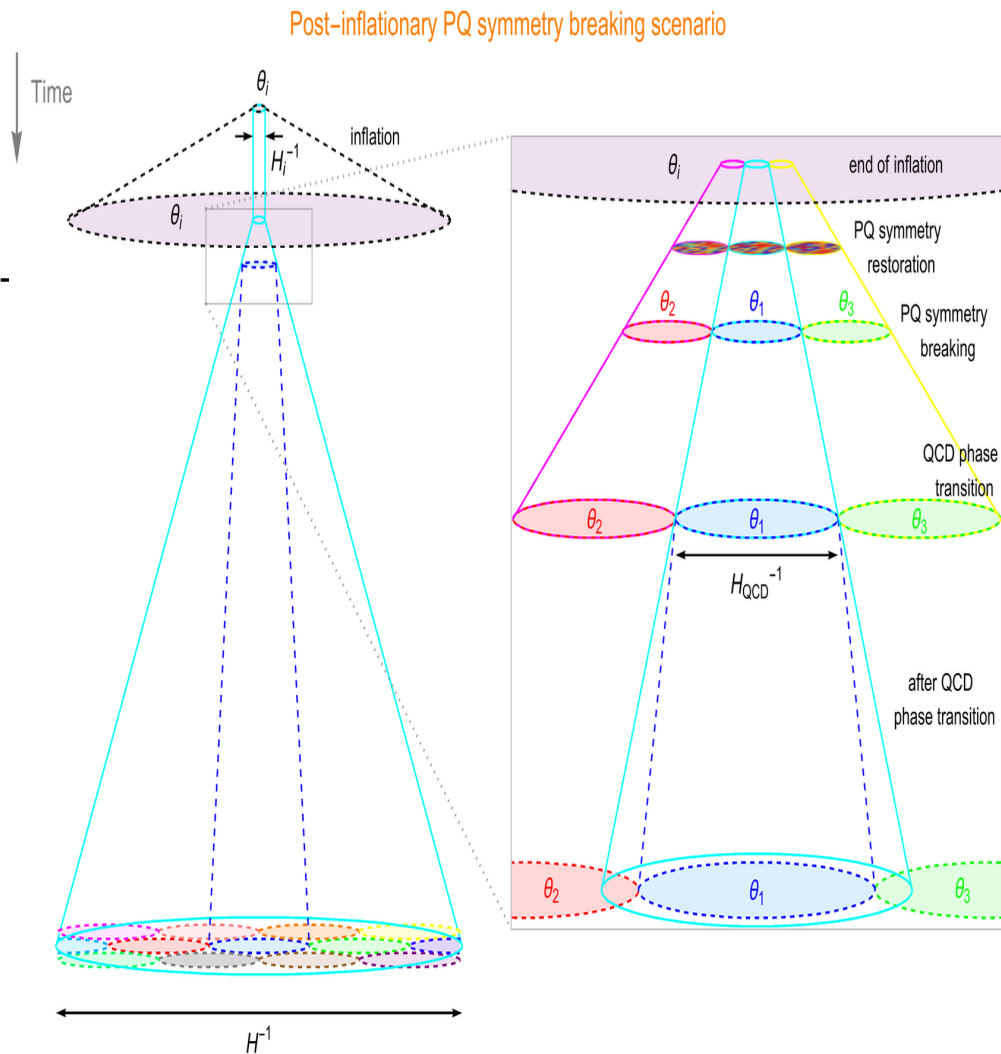
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[Saikawa]

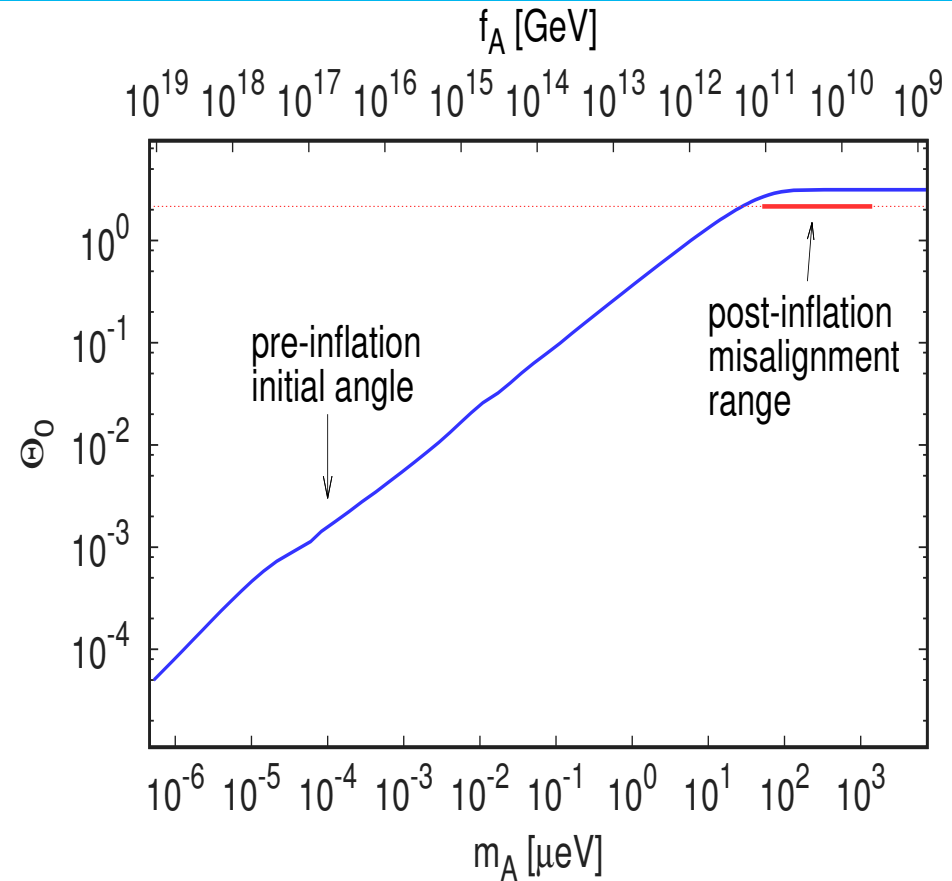




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  - Upper limit on  $f_A$  from requirement that realignment contribution should not exceed DM abundance leads to:

$$m_A > 28(2) \mu\text{eV}$$

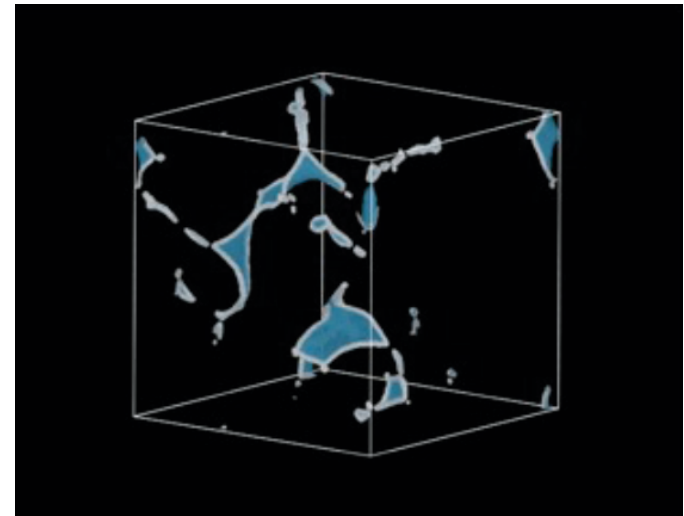
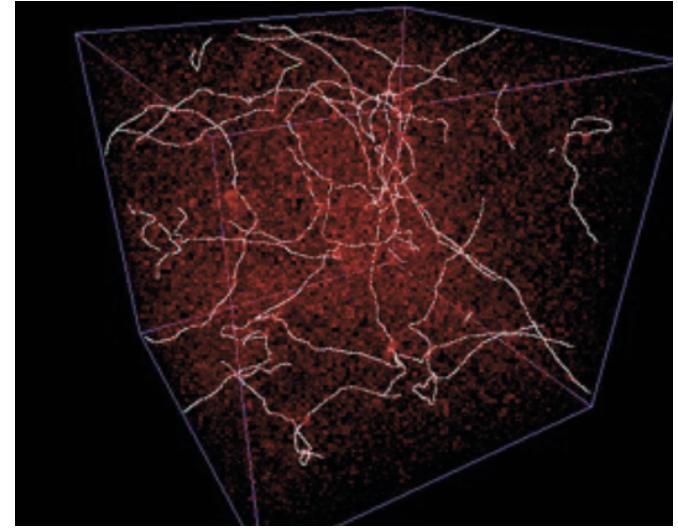


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  - Additional contributions arise from decay of topological defects



[Hiramatsu et al. 12]

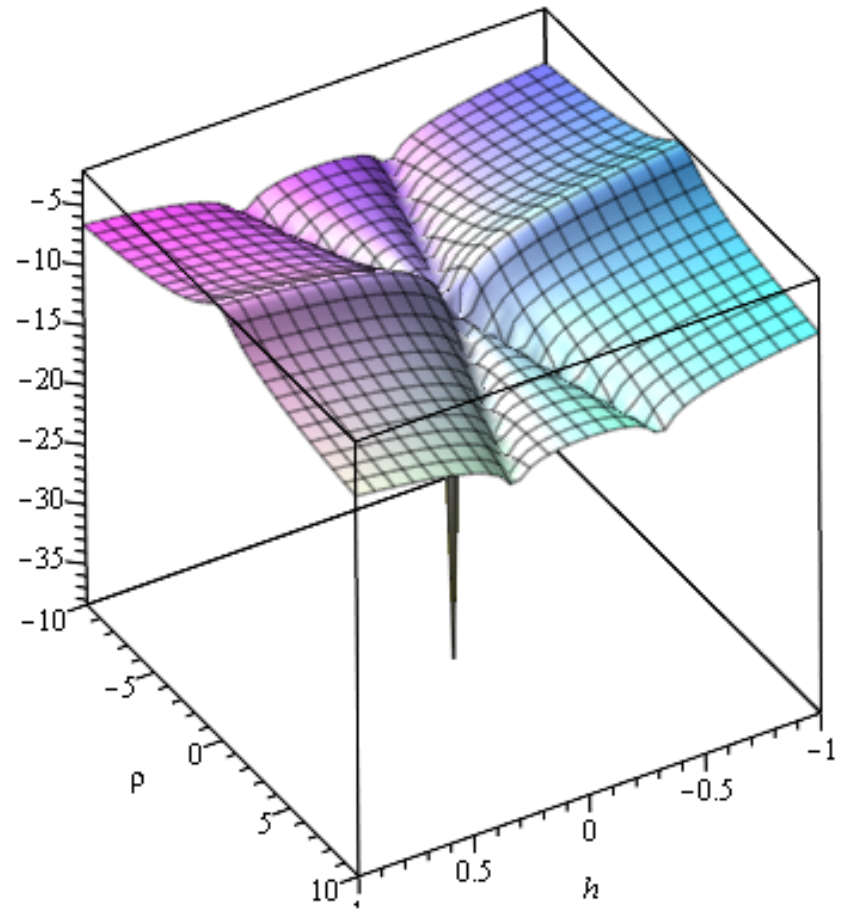
# One SM\*A\*S\*H to rule them all ...

- $|\sigma| = \rho/\sqrt{2}$  or mixture with Higgs modulus may play role of inflaton, if it has non-minimal coupling to gravity,

[Fairbairn et al. '14]

$$S \supset - \int d^4x \sqrt{-g} \left[ \frac{M^2}{2} + \xi_\sigma \sigma^* \sigma \right] R$$

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[Ballesteros, Redondo, AR, Tamarit, 1610.01639]

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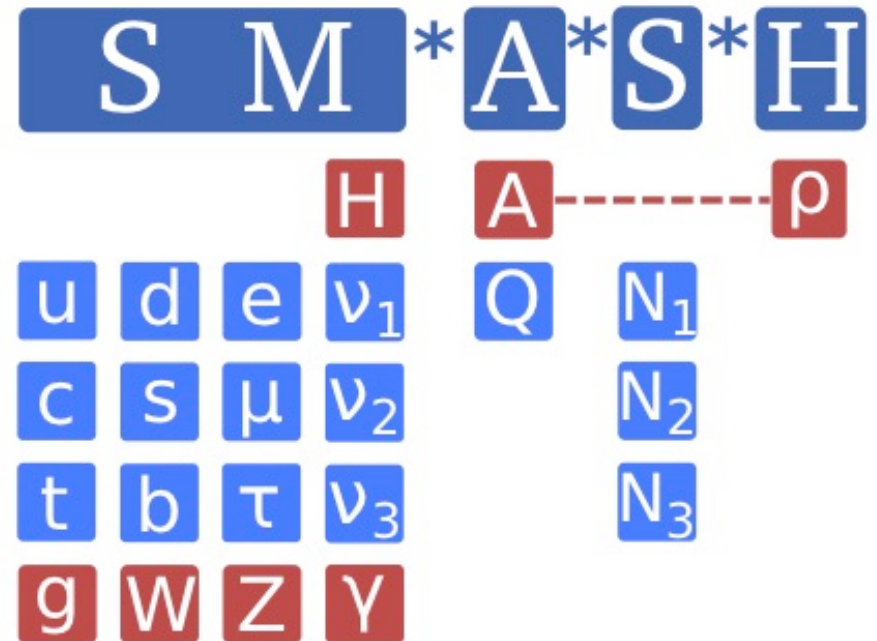
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- > Augmenting axion models with three RH singlet neutrinos, getting their Majorana masses also through the vev  $v_\sigma$

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[Dias et al. '14; Ballesteros et al. '16]



[Tamarit '17]



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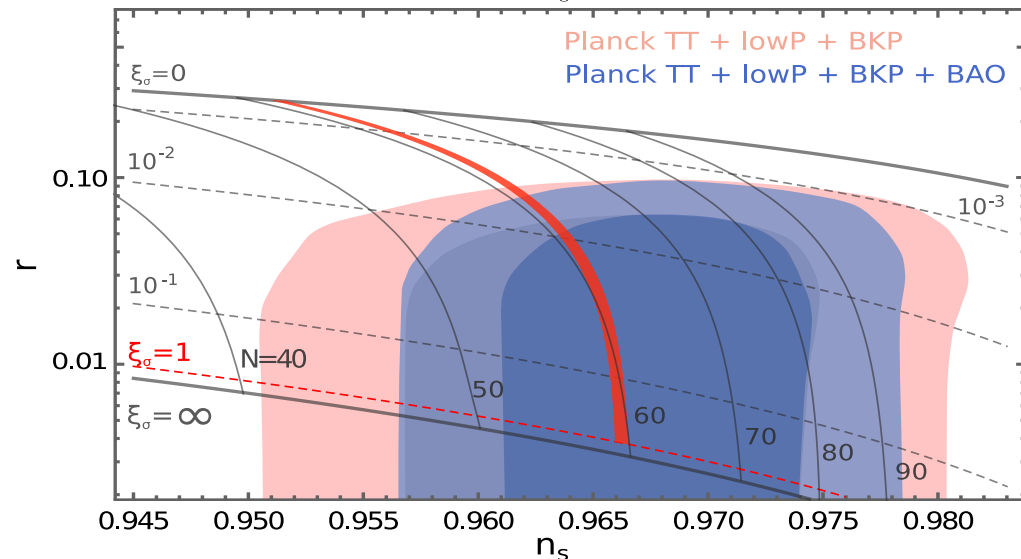
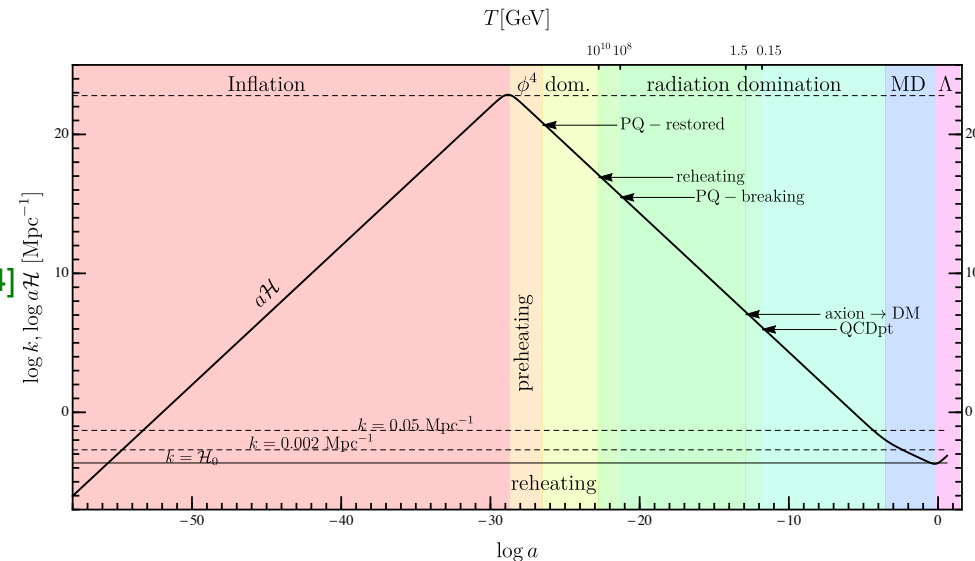
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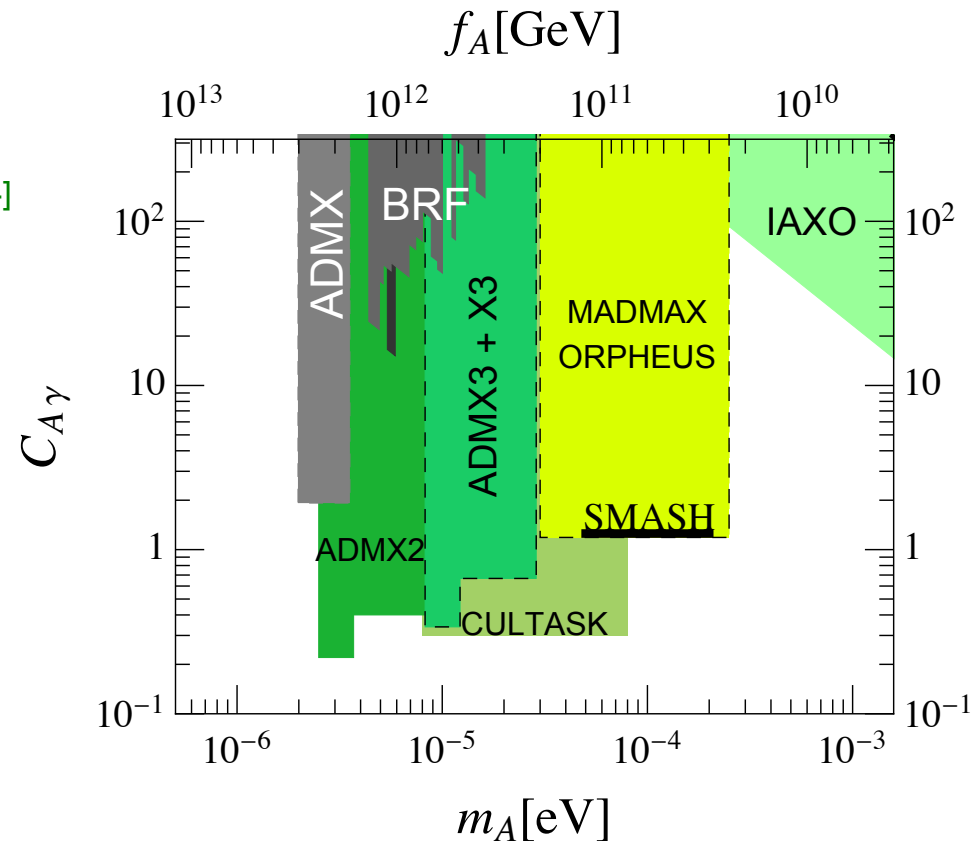
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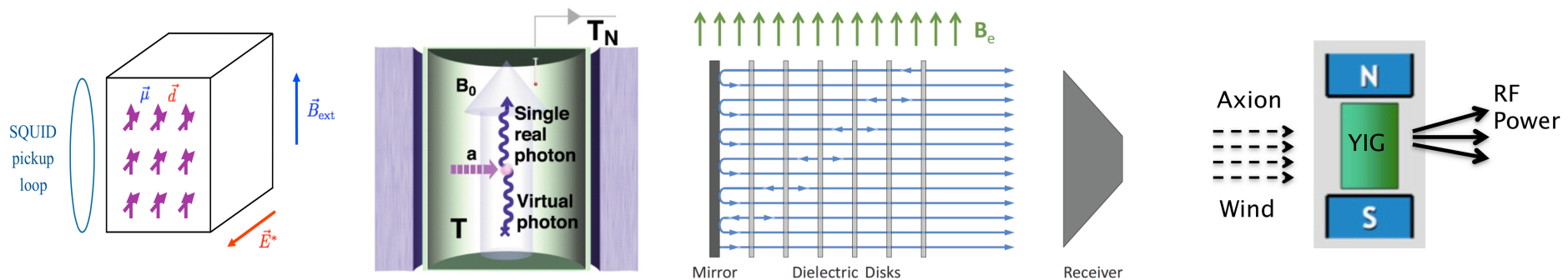
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# Axion Dark Matter Experiments

➤ Upcoming generation of axion dark matter experiments can probe sizeable portion of axion mass range relevant for DM:

- $m_A \ll \mu\text{eV}$ : searches for oscillating nuclear electric dipole moments exploiting nuclear magnetic resonance techniques ([CASPER](#)); searches via LC circuit ([ABRACADABRA](#))
- $\mu\text{eV} \lesssim m_A \lesssim 0.1 \text{ meV}$ : searches for excitations of electromagnetic resonances due to axion photon conversion in microwave cavities in superconducting solenoids ([ADMX](#), [X3](#), [CULTASK](#), ...)
- $30 \mu\text{eV} \lesssim m_A \lesssim 0.3 \text{ meV}$ : searches for electromagnetic excitation in open dielectric/Fabry-Perot resonator in a strong magnetic field ([MADMAX/ORPHEUS](#), ...)
- $0.3 \text{ meV} \lesssim m_A \lesssim 10 \text{ meV}$ : searches exploiting dish antenna or electron spin precession in galactic axion wind ([QUAX](#))

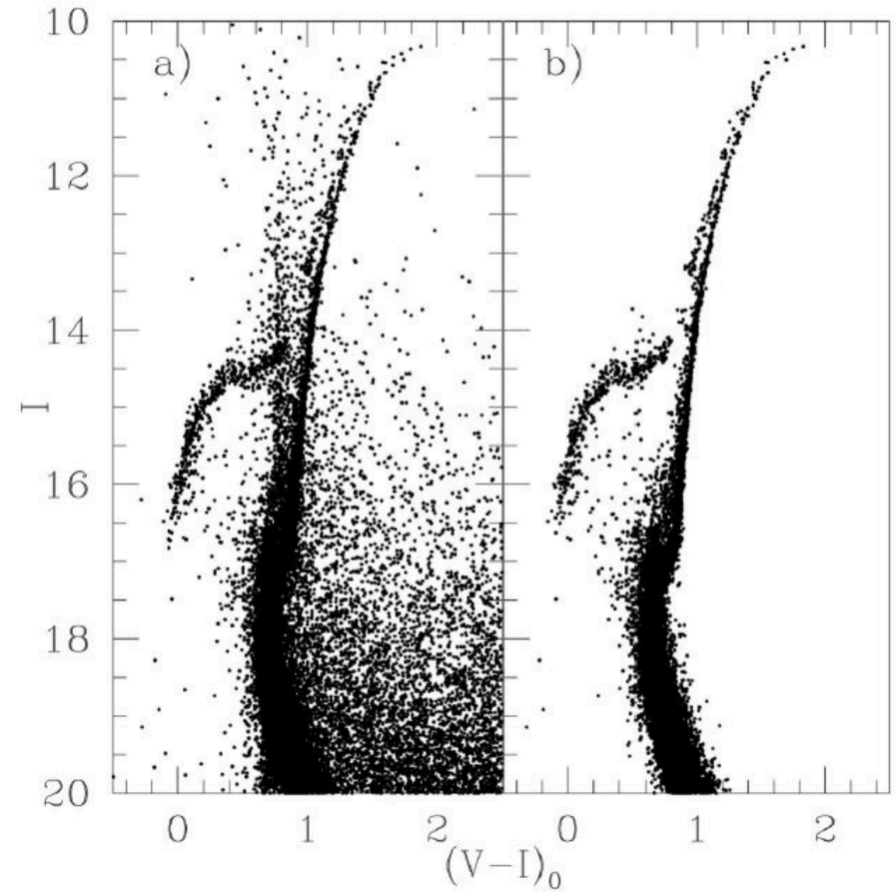




# Astro-Hints for the Axion: Energy Losses of Stars?

- RG cooling excess: Brightness of tip of RG branch in color-magnitude diagram of globular cluster

[Viaux et al. 13]

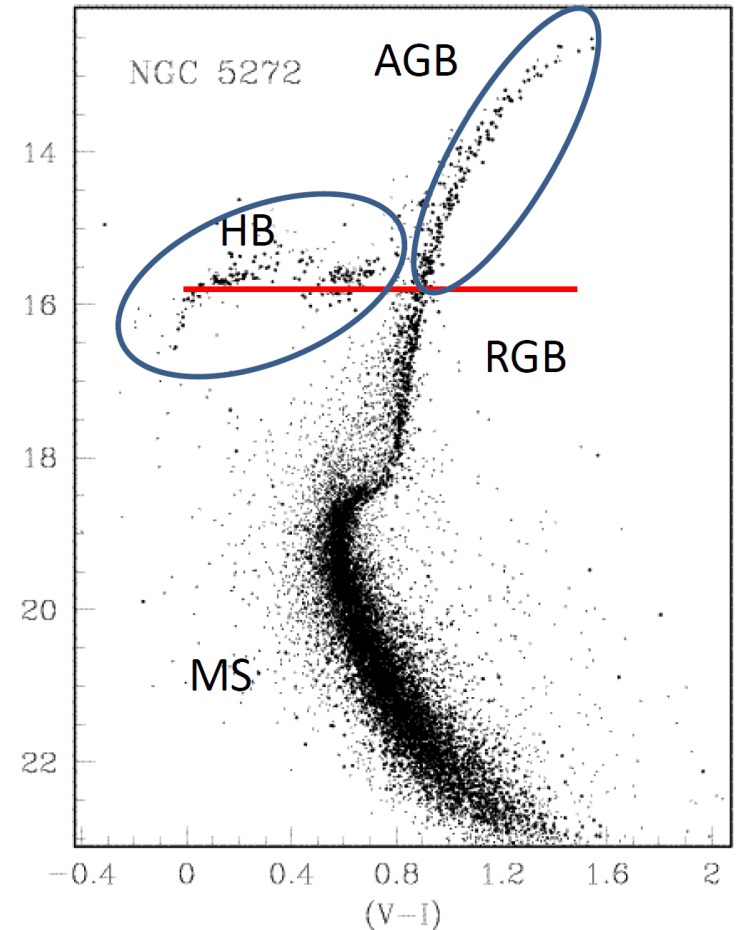


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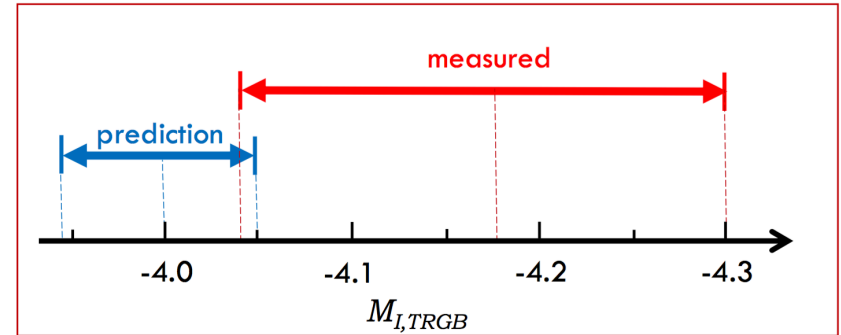


[Giannotti '16]

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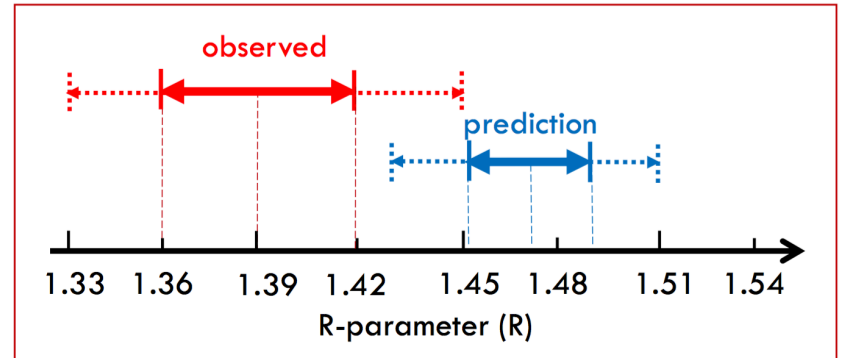
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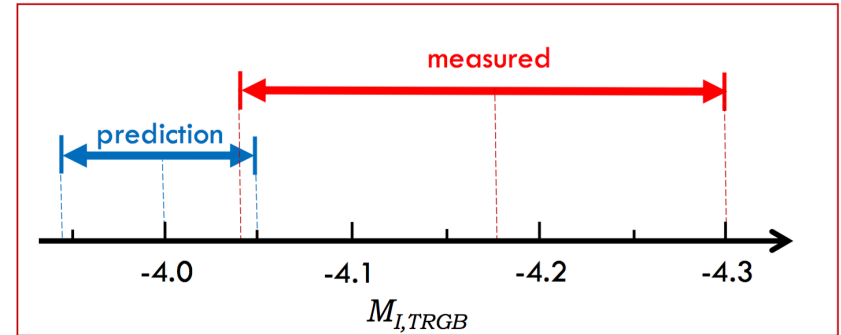
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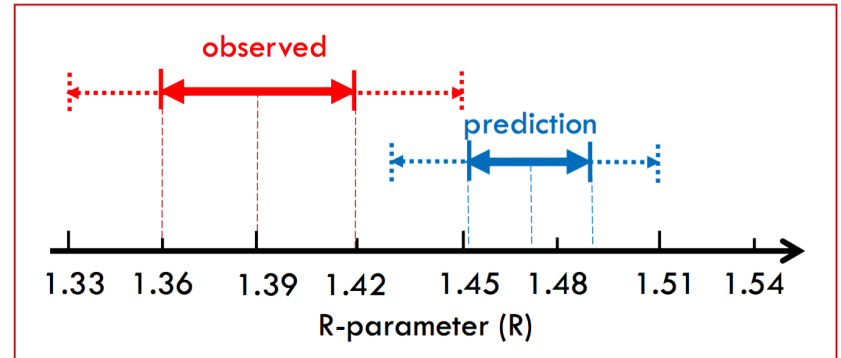
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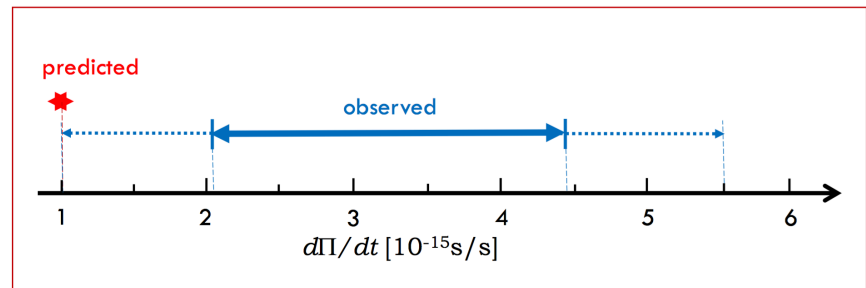
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- > WD cooling excess:

- Period decrease of variable WDs [Kepler et al. 91,...]



[Giannotti 15]



# Astro-Hints for the Axion: Energy Losses of Stars?

> RG cooling excess: Brightness of tip of RG branch in color-magnitude diagram of globular cluster

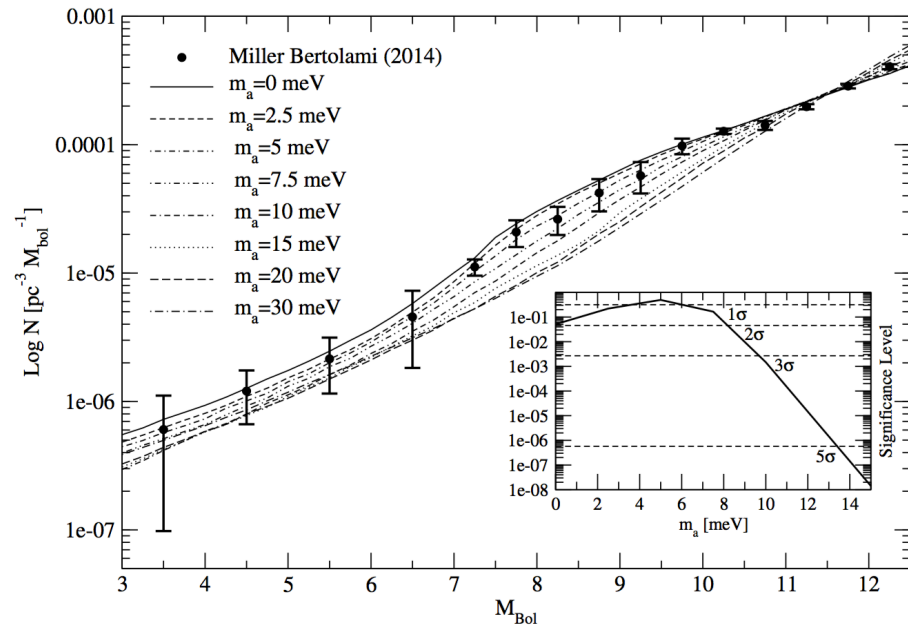
[Viaux et al. 13]

> HB cooling excess: Number of HB stars vs. number of RGs in color-magnitude diagram of globular cluster

[Ayala et al. 14]

> WD cooling excess:

- Period decrease of variable WDs [Kepler et al. 91,...]
- White dwarf luminosity function (WDLF) [Isern et al. 08-12]

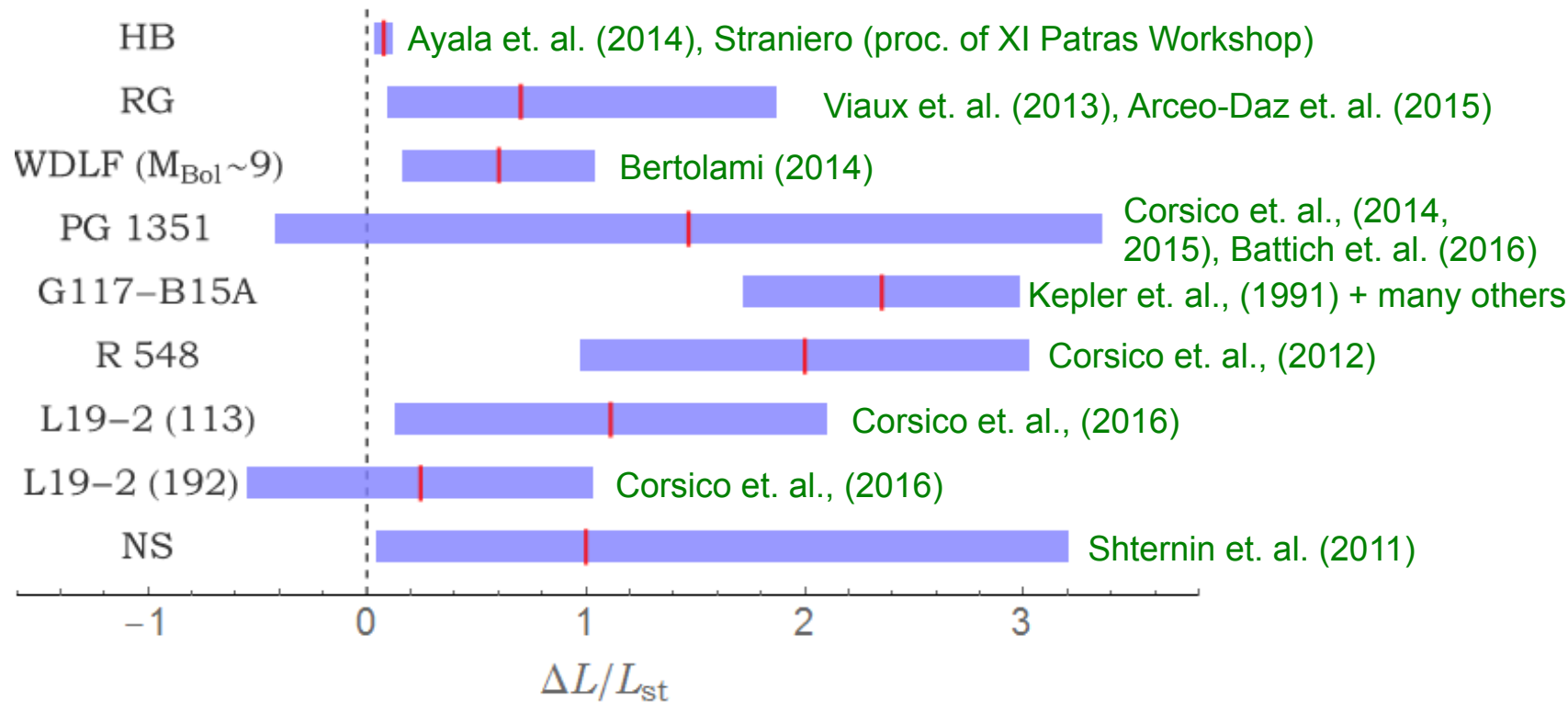


[Bertolami et al. 15]



# Astro-Hints for the Axion: Energy Losses of Stars?

- Practically every stellar systems seems to be cooling faster than predicted by models

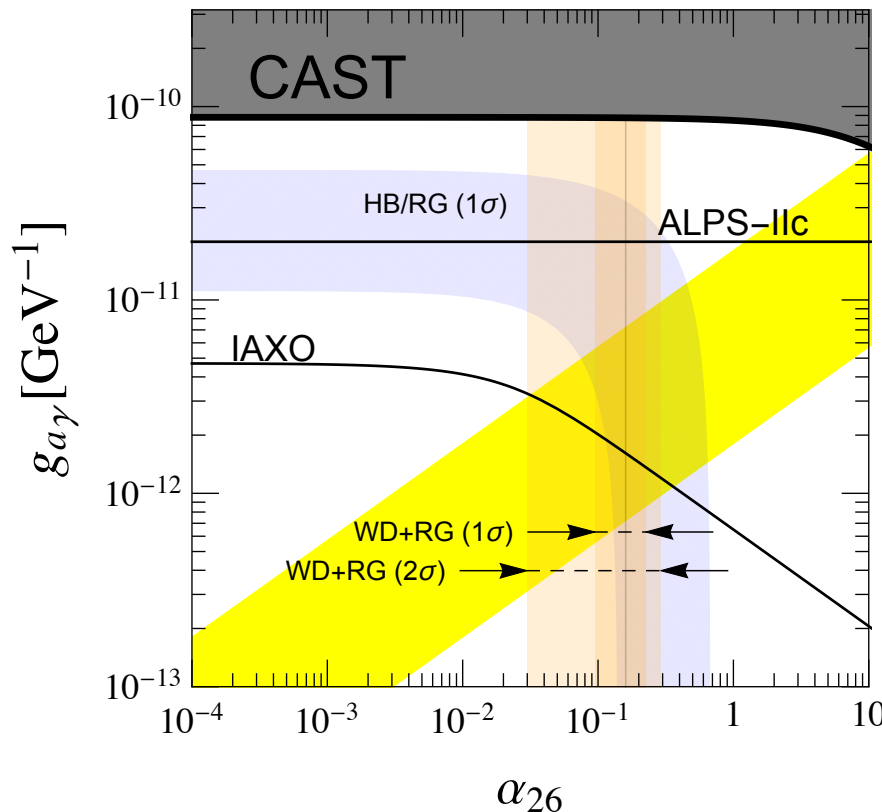


[Giannotti, Irastorza, Redondo, AR (2015); Giannotti, Irastorza, Redondo, AR (in preparation)]

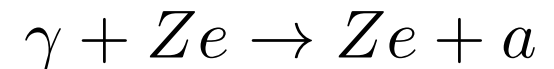


# Astro-Hints for the Axion: Energy Losses of Stars?

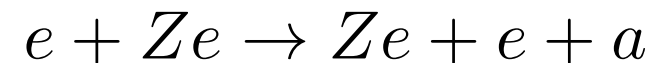
- Excessive energy losses of HBs, RG, WDs can be explained at one stroke by production of axion/ALP with coupling to photons and electrons and probed by photon regeneration experiments (ALPS II, IAXO):



$$g_{a\gamma} = C_{a\gamma}\alpha/(2\pi f_a)$$



$$g_{ai} = C_{ai}m_i/f_a$$



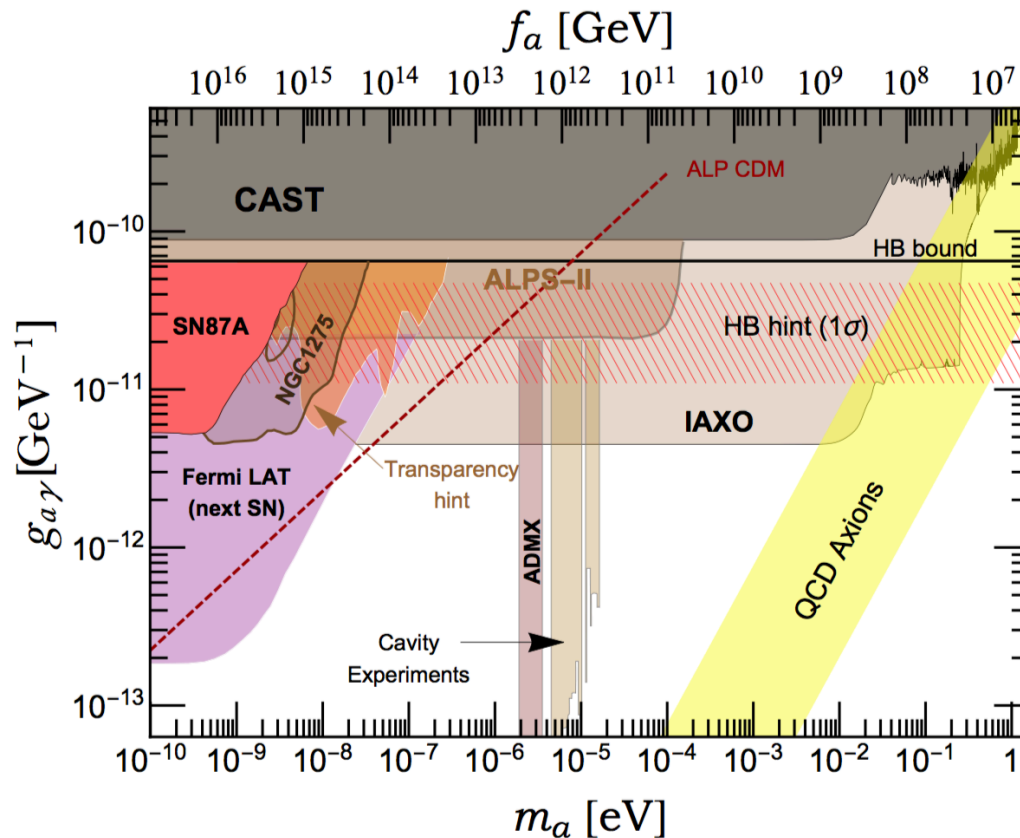
$$\alpha_{26} = g_{ae}^2/(4\pi)/10^{-26}$$

[Giannotti,Irastorza,Redondo,AR `16]



# Astro-Hints for the Axion: Energy Losses of Stars?

- Excessive energy losses of HBs, RG, WDs can be explained at one stroke by production of axion/ALP with coupling to photons and electrons and probed by photon regeneration experiments (ALPS II, IAXO):



[Giannotti, Irastorza, Redondo, AR, in preparation]



# Conclusions

- > Strong physics case for the axion:
  - Solution of strong CP problem
  - Candidate for dark matter
  - Explanation of astrophysical hints on excessive energy losses of stars
- > Strong motivation for experimental searches of the axion

