

TMDs, a 3D look at the proton

Andrea Signori

**Nikhef Jamboree
2015**



3D proton structure @ Nikhef

Piet Mulders (VU)



Amsterdam - Groningen

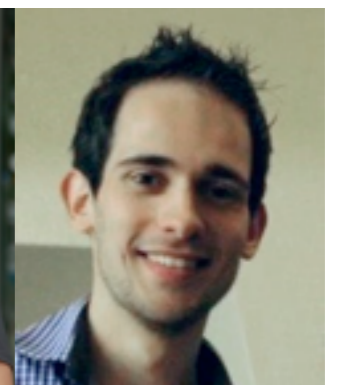


Daniel Boer (RUG)

Postdocs and
visitors



PhD students



Why the proton ..?

PROTON

p



The **PROTON** is a subatomic particle with a positive charge. Along with the neutron, it forms the nucleus of an atom. It consists of two up quarks and one down quark. The number of protons in the nucleus determines the chemical properties of the atom and which chemical element it is.

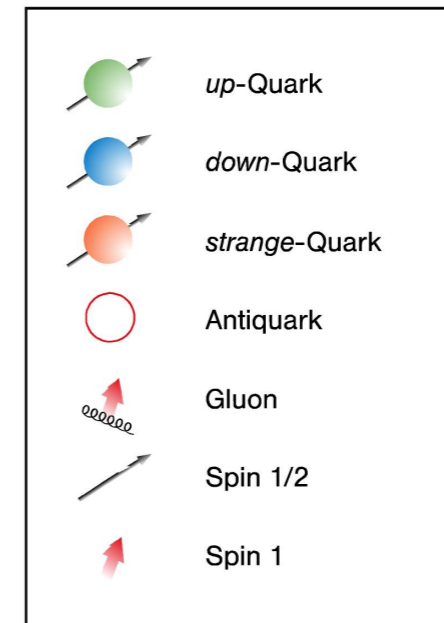
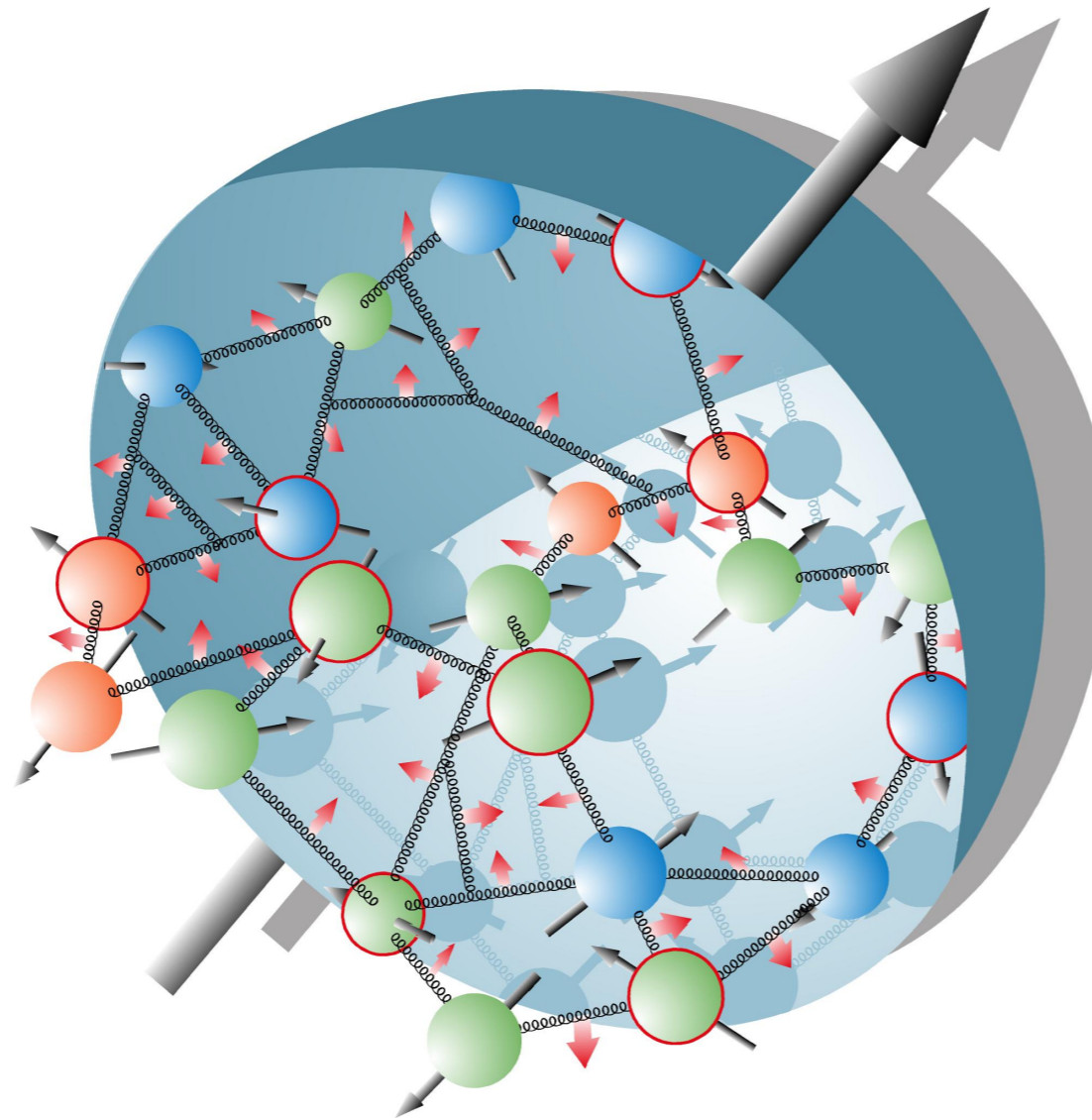
Acrylic felt & fleece with poly bead fill for medium mass.

- building blocks of our world:
~ **99.97% of the mass** of the world we live in is accounted by protons+neutrons
- **connection** between chemistry, atomic/nuclear physics and the elementary building blocks of Nature
- **field theory** : subtle role in canceling some of the divergencies of the theory

HOW CAN WE DESCRIBE IT ?

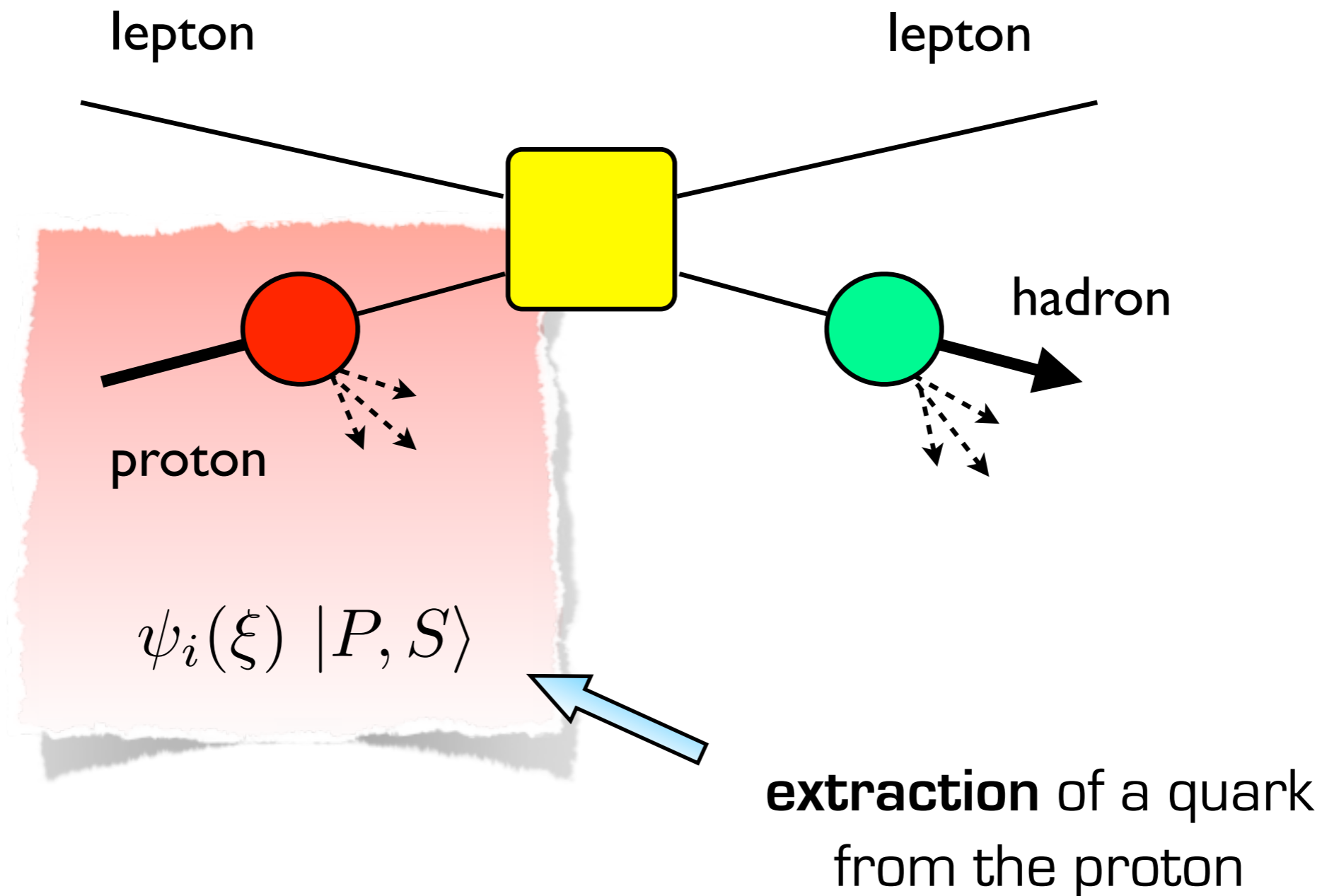
The quest for the structure

quantum field theory:
Quantum Chromodynamics



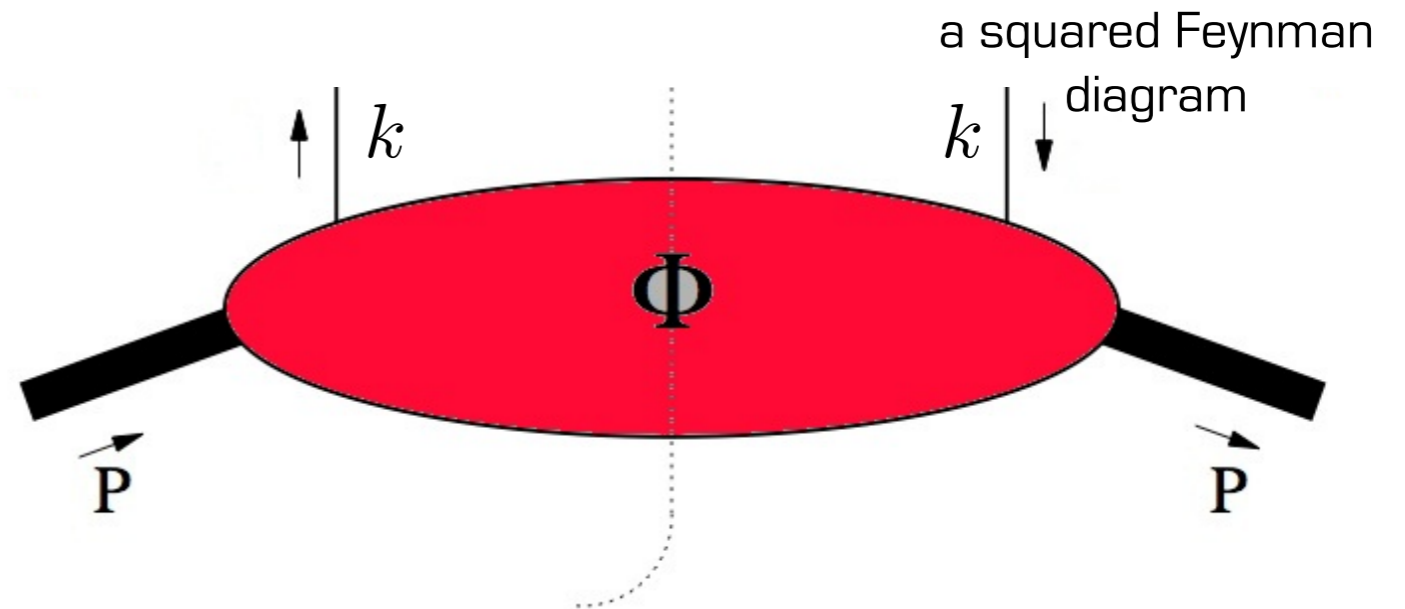
Quarks & gluons

Observing protons

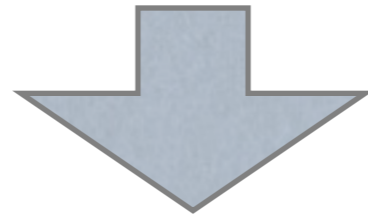


Observing protons

how can we **define**
distribution functions ?

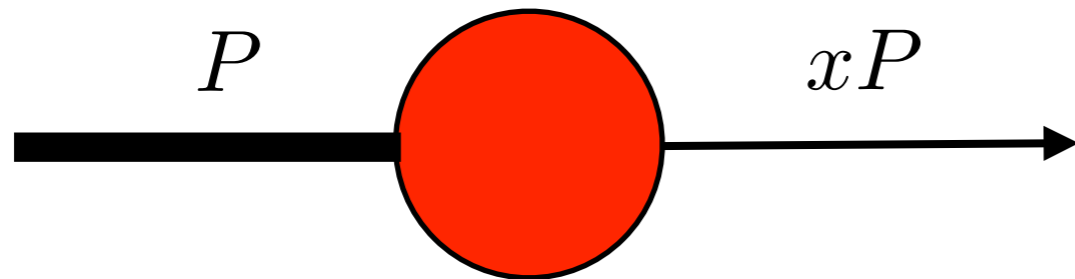


$$\Phi_{ij}(k; P, S) \sim \text{F.T.} \langle P, S | \bar{\psi}_j(0) U_{[0,\xi]} \psi_i(\xi) | P, S \rangle_{LF}$$



Dirac matrix , parametrized in terms of
quark distribution functions

Quarks in 1D - PDFs



extraction of a quark
collinear with the proton

3 parton distribution functions (PDFs)

**not computable
in pert. theory**

Proton **and** quark
spin configuration:

unpolarized longitudinal transverse

$$\{ f_1(x), g_1(x), h_1(x) \}$$

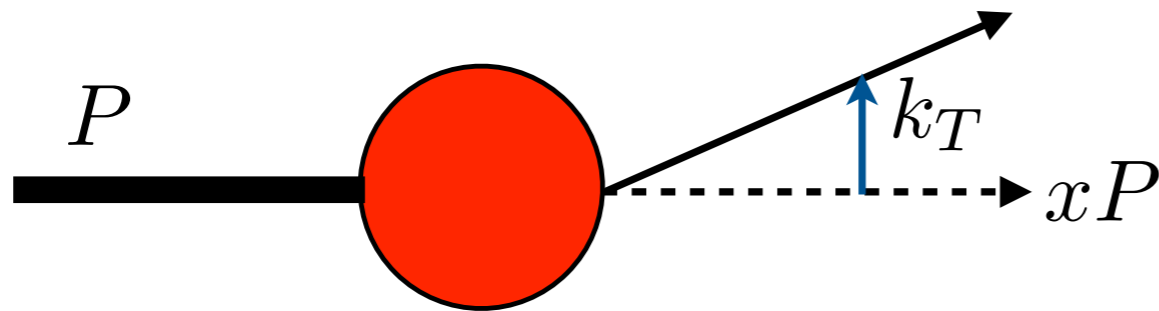
level of knowledge:

very good

getting better

basic

Quarks in 3D - TMDs



extraction of a **quark**
not collinear with the proton

partly not computable

8 transverse-momentum-dependent
parton distribution functions (TMD PDFs)

quark pol.

$f_1^q(x, \vec{k}_T)$
! 3D functions!
richer than 1D PDFs

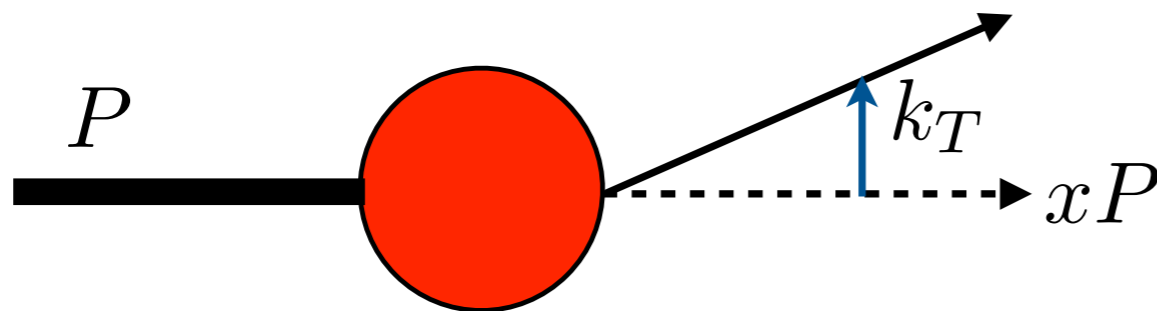
for **LHC**

nucleon pol.

	U	L	T
U	f_1		h_1^\perp
L		g_{1L}	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

Twist-2 TMDs

Gluons in 3D - TMDs



extraction of a **gluon**
not collinear with the proton

partly not computable

8 transverse-momentum-dependent
parton distribution functions (TMD PDFs)

for **LHC**

LEADING
TWIST

GLUONS	<i>unpolarized</i>	<i>circular</i>	<i>linear</i>
U	f_1^g		$h_1^{\perp g}$
L		g_{1L}^g	$h_{1L}^{\perp g}$
T	$f_{1T}^{\perp g}$	g_{1T}^g	$h_{1T}^g, h_{1T}^{\perp g}$

Mulders, Rodriguez
PRD 63 (2001)

Phenomenology of **TMDs** @ the **LHC**

useful references (Xmas reading):

AS et al. - [10.5506/APhysPolB.46.2501](#)

Echevarria, Kasemets, Mulders, Pisano

[10.1007/JHEP07\(2015\)158](#)

AS, Bacchetta, Radici, Schnell

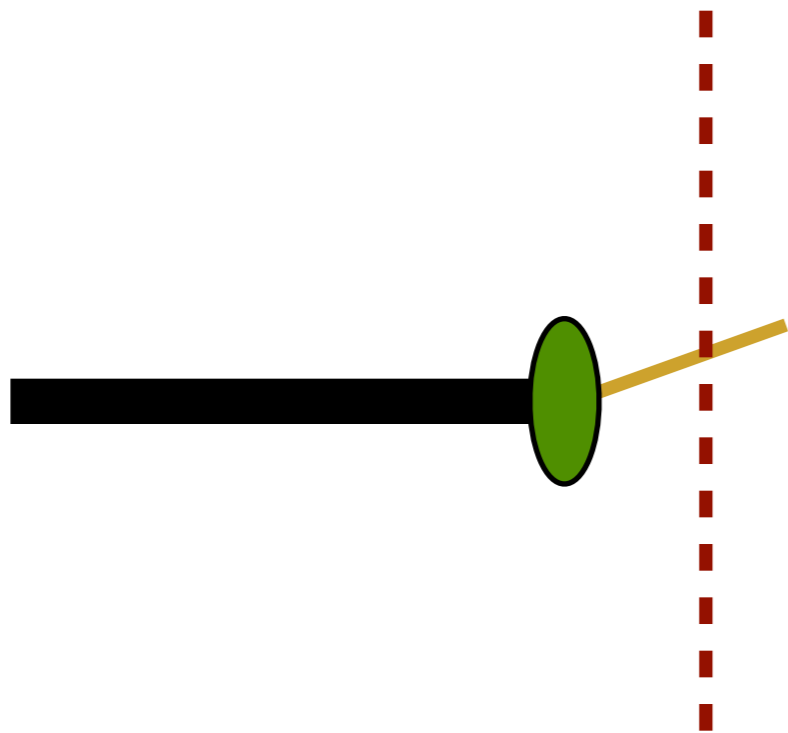
[10.1007/JHEP11\(2013\)194](#)

Bacchetta, Echevarria, Mulders, Radici, **AS**

[10.1007/JHEP11\(2015\)076](#)

TMDs - a physical picture

intrinsic
transverse
momentum

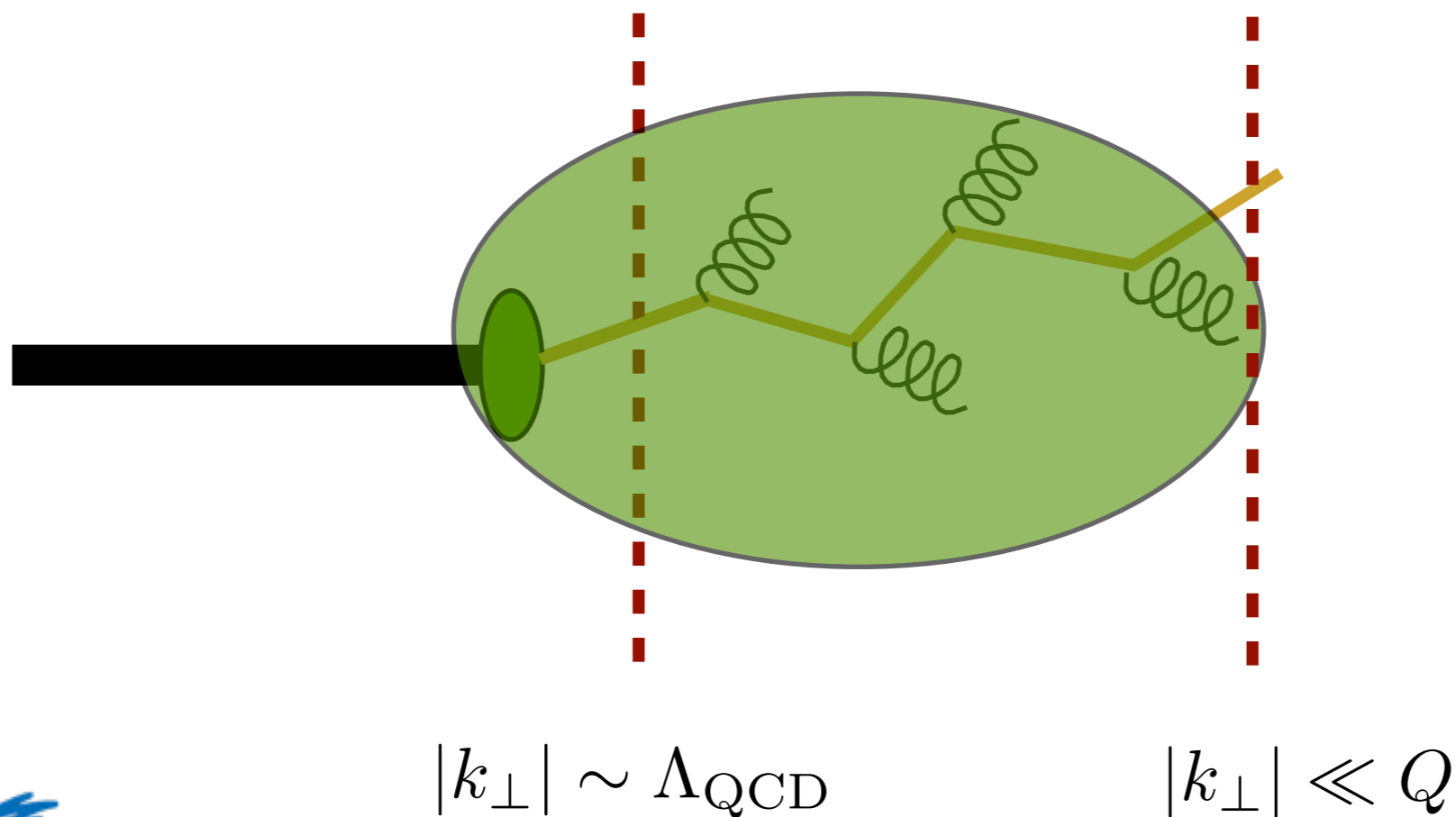


$$|k_{\perp}| \sim \Lambda_{\text{QCD}}$$

TMDs - a physical picture

intrinsic
transverse
momentum

soft and collinear
gluon radiation

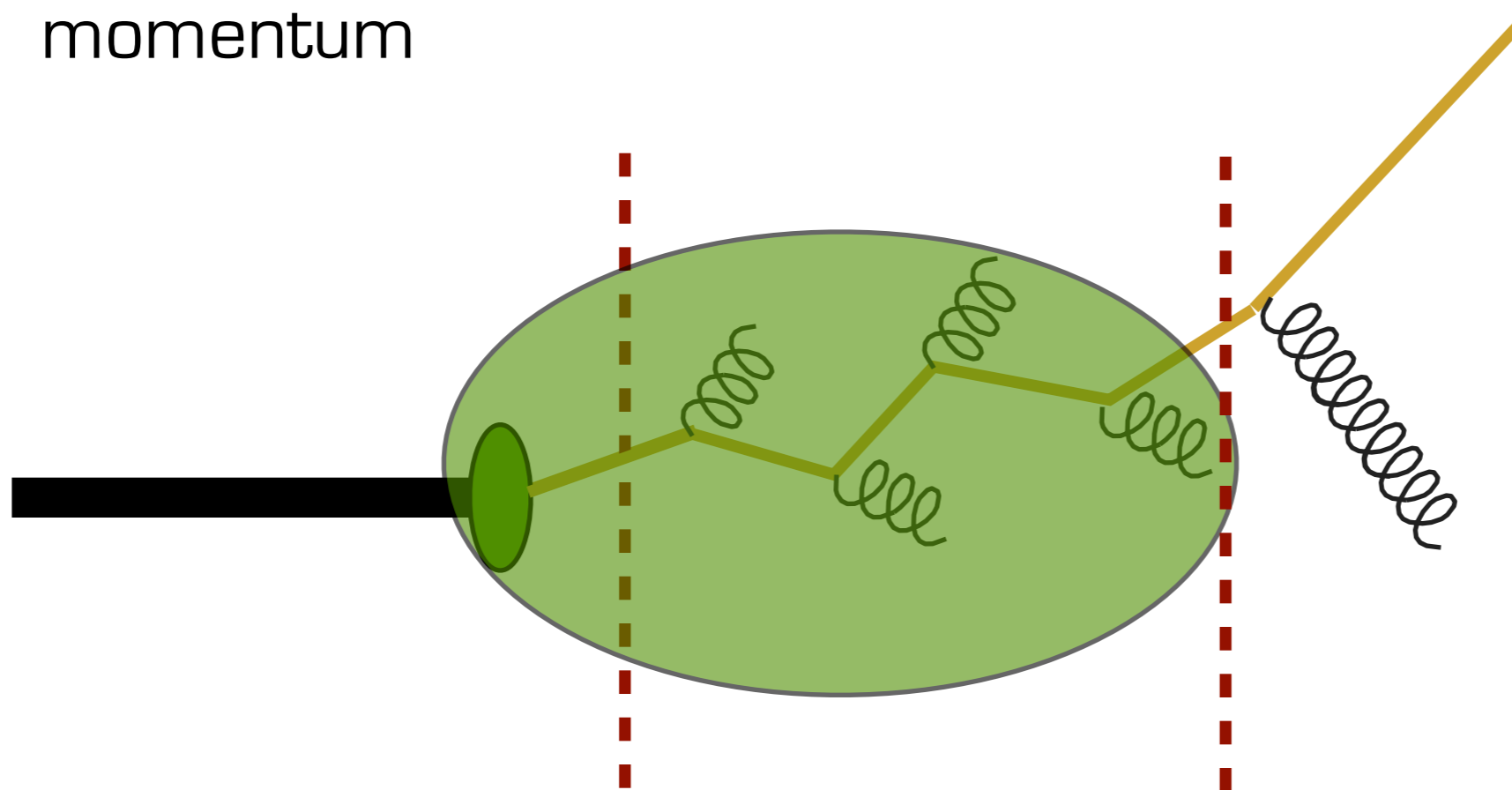


TMDs - a physical picture

intrinsic
transverse
momentum

soft and collinear
gluon radiation

hard
gluon radiation



$$|k_{\perp}| \sim \Lambda_{\text{QCD}}$$

$$|k_{\perp}| \ll Q$$

$$|k_{\perp}| \sim Q$$

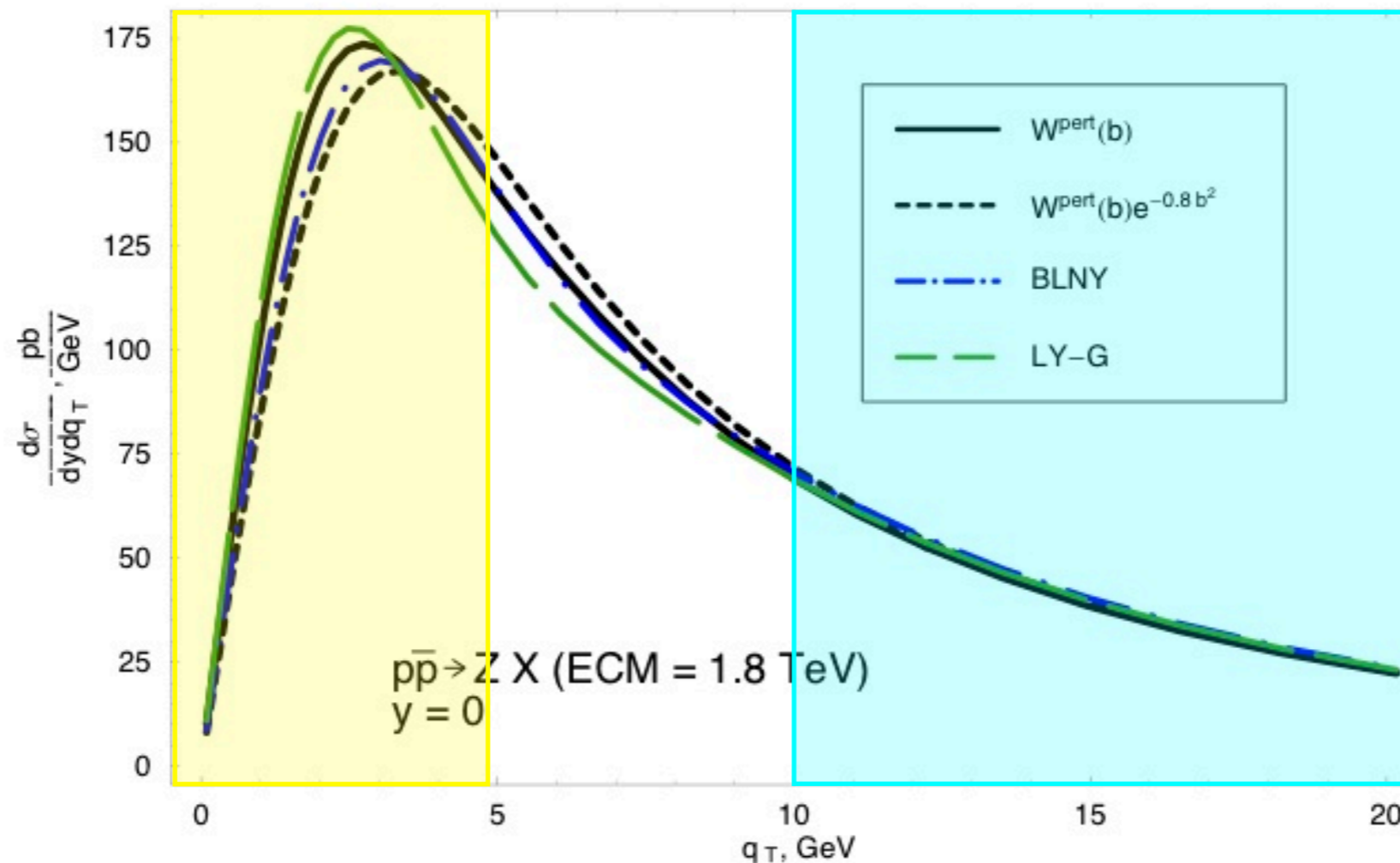
TMDs - from low to high momenta

TMDs generate the q_T dep. of cross sections : but **how in practice** ?

intrinsic momentum +
soft/coll. gluon radiation

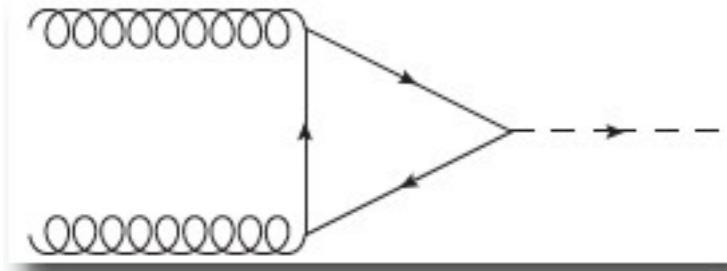
matching

hard gluon radiation



Gluons @ the LHC

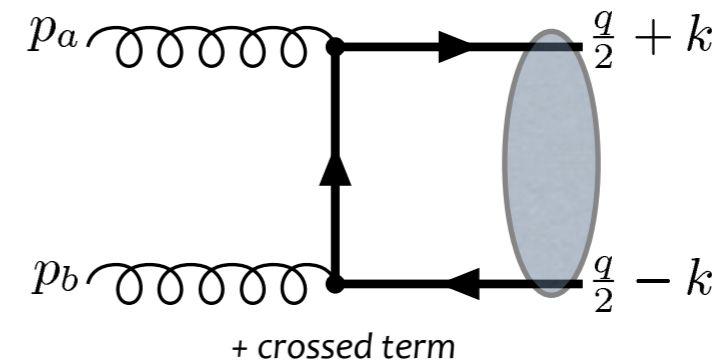
Higgs production



$$P_A + P_B \rightarrow h(q_T) + X$$

$$m_h = 125 \text{ GeV}$$

quarkonium production

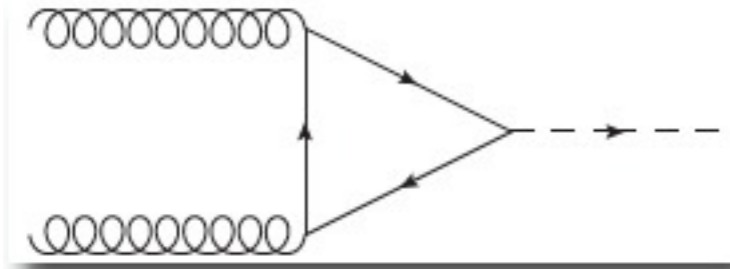


$$P_A + P_B \rightarrow \eta_b(q_T) + X$$

$$m_{\eta_b} = 9.39 \text{ GeV}$$

Gluons @ the LHC

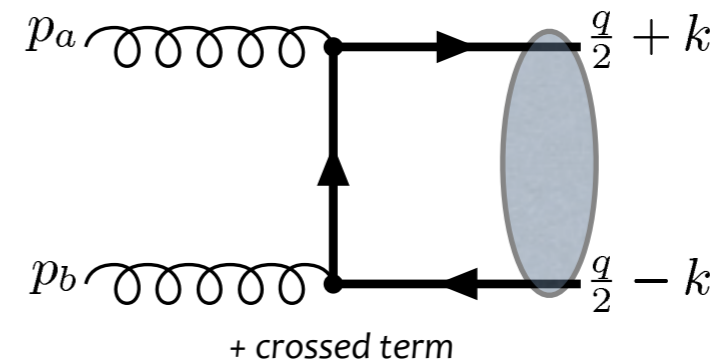
Higgs production



$$P_A + P_B \rightarrow h(q_T) + X$$

$$m_h = 125 \text{ GeV}$$

quarkonium production



$$P_A + P_B \rightarrow \eta_b(q_T) + X$$

$$m_{\eta_b} = 9.39 \text{ GeV}$$

$$\frac{d\sigma}{dq_T} \sim \Phi_A^U \Phi_B^U |\mathcal{M}|^2$$

$$\sim \mathcal{C} \left[f_1^{g/A} \quad f_1^{g/B} \right]$$

unpolarized gluons

\pm

$$\mathcal{C} \left[h_1^{\perp g/A} \quad h_1^{\perp g/B} \right]$$

lin. polarized gluons

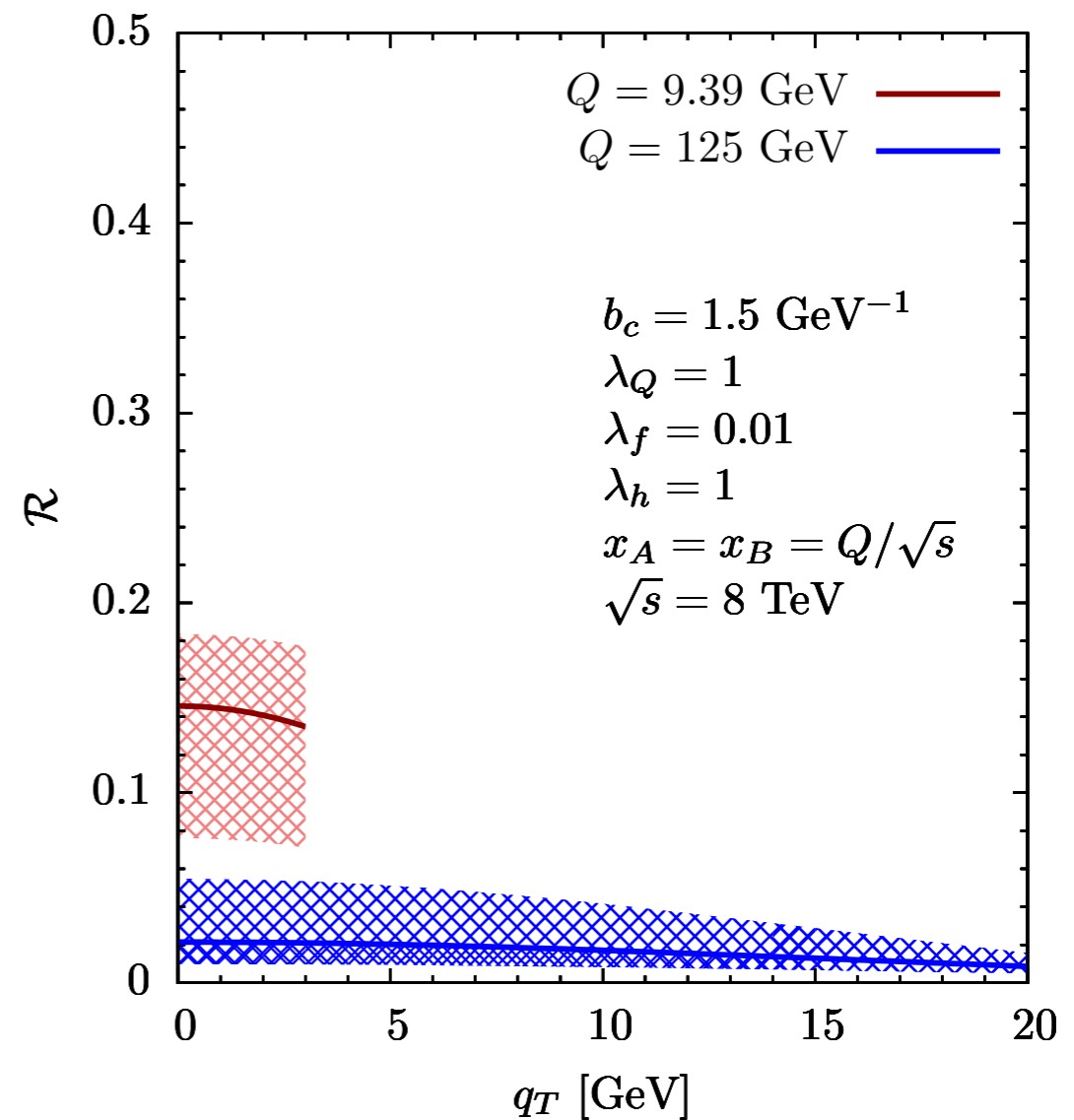
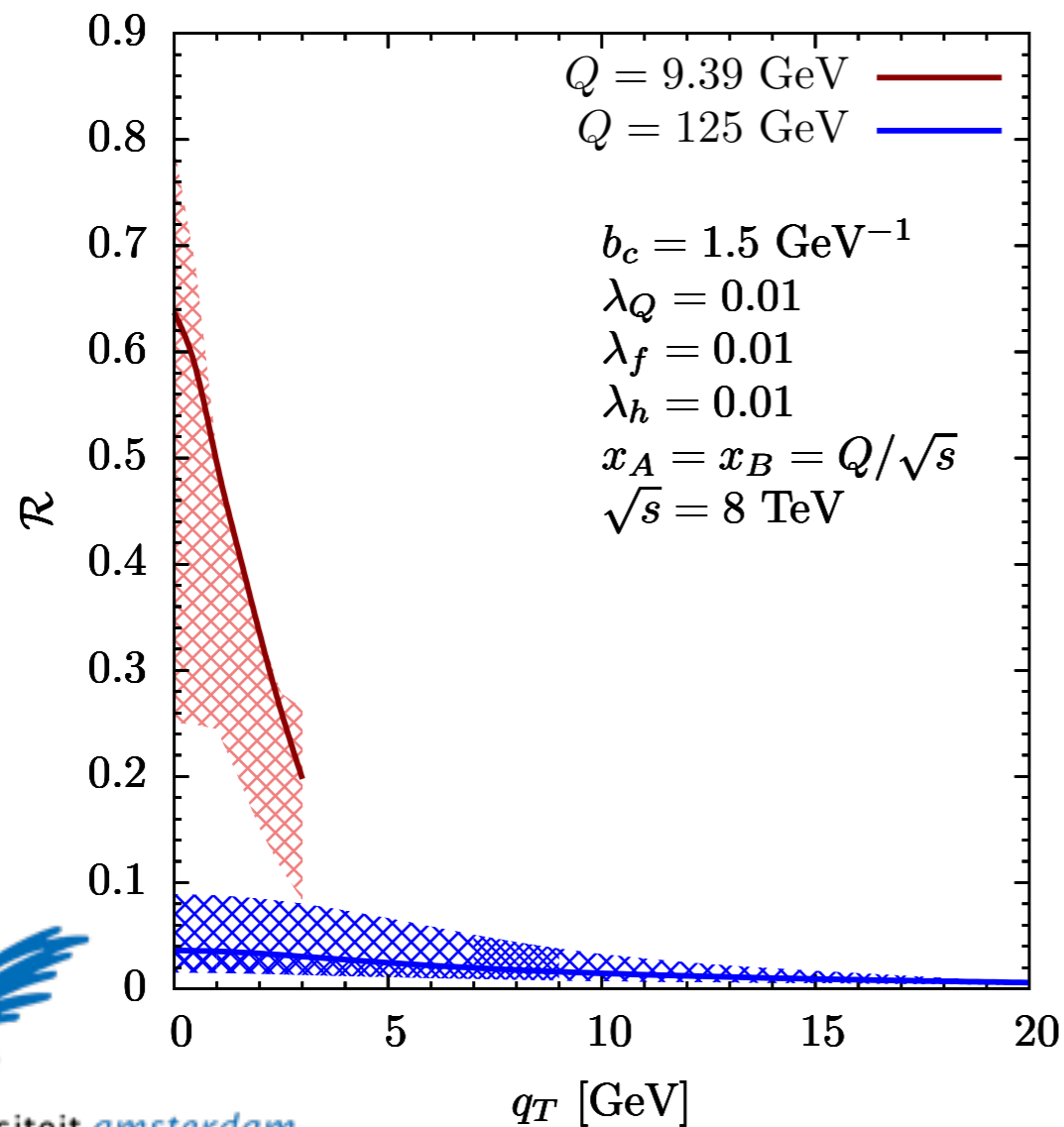


Linearly polarized vs unpolarized

$$\mathcal{R}(q_T; Q) = \frac{\mathcal{C} \left[\begin{array}{cc} h_1^{\perp g/A} & h_1^{\perp g/B} \end{array} \right]}{\mathcal{C} \left[\begin{array}{cc} f_1^{g/A} & f_1^{g/B} \end{array} \right]}$$

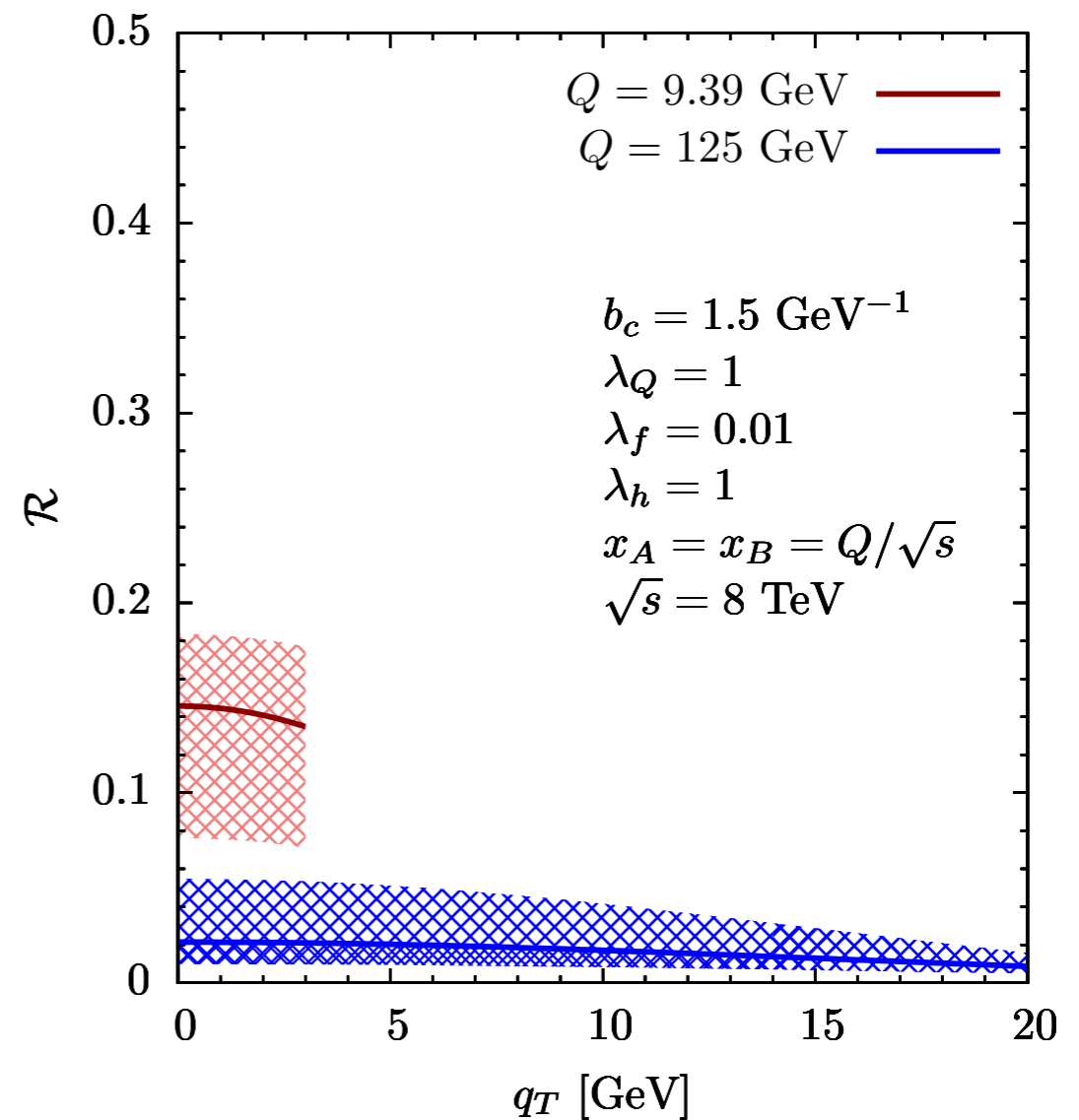
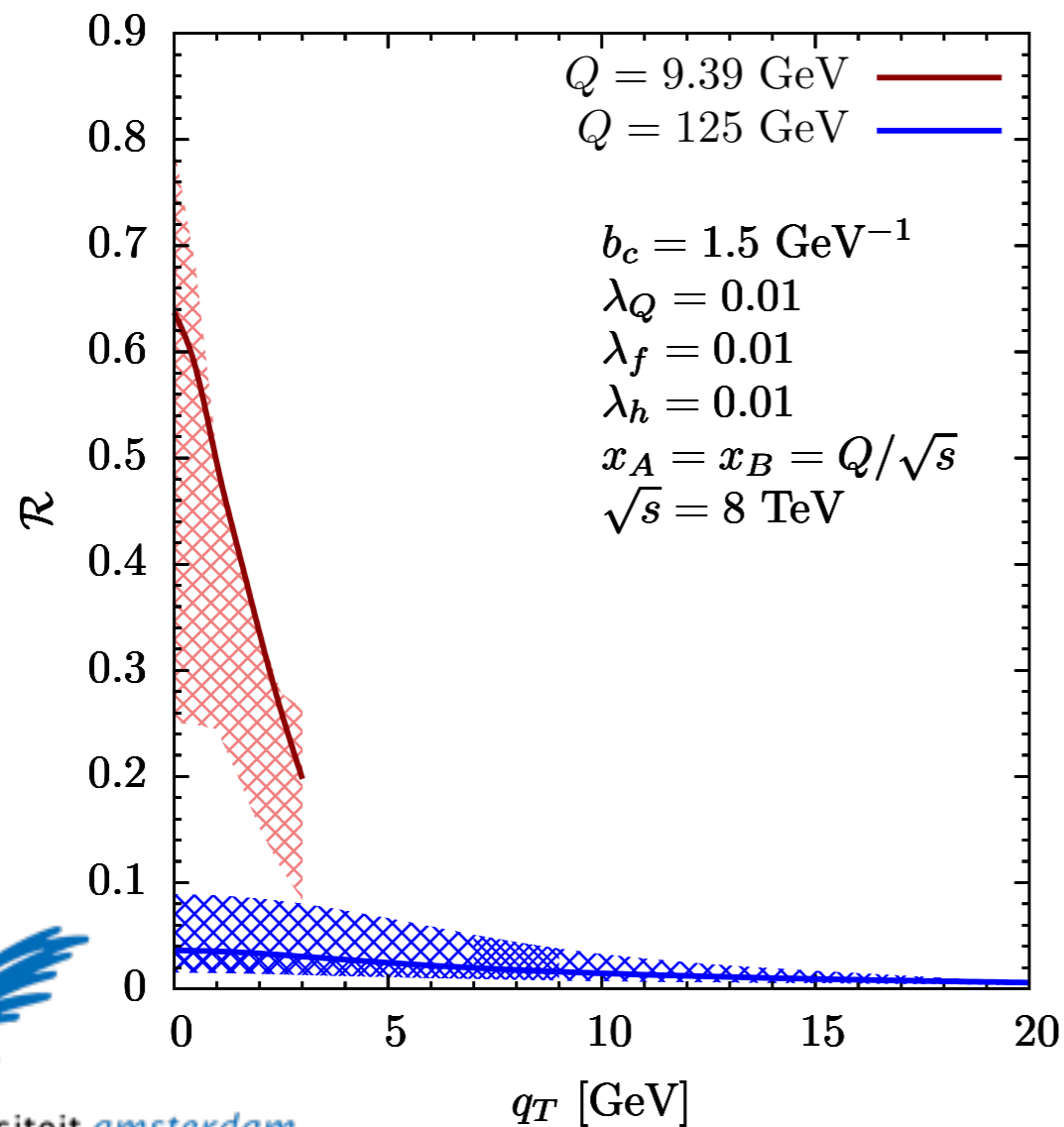
quarkonium - low energy

higgs - high energy



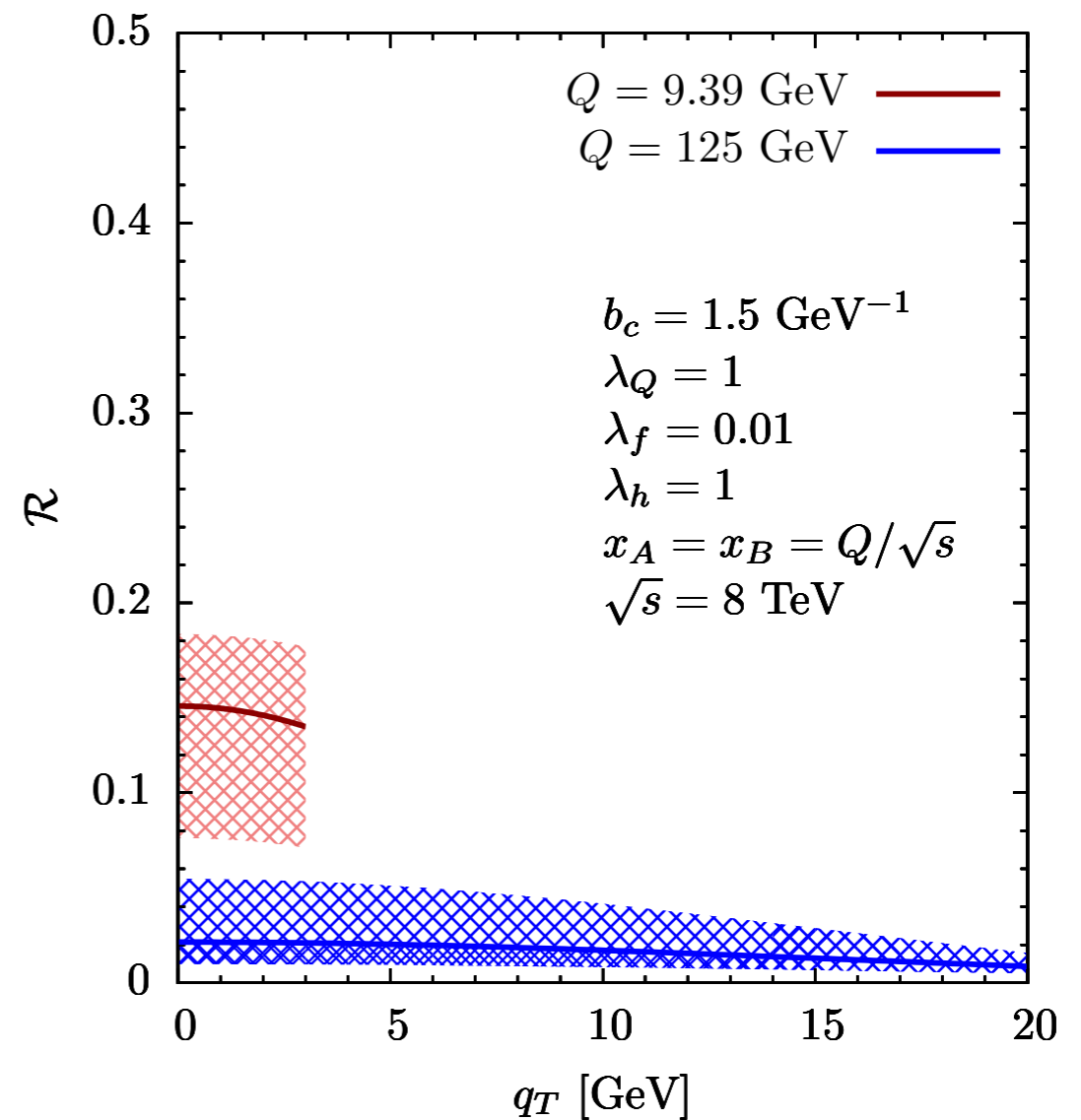
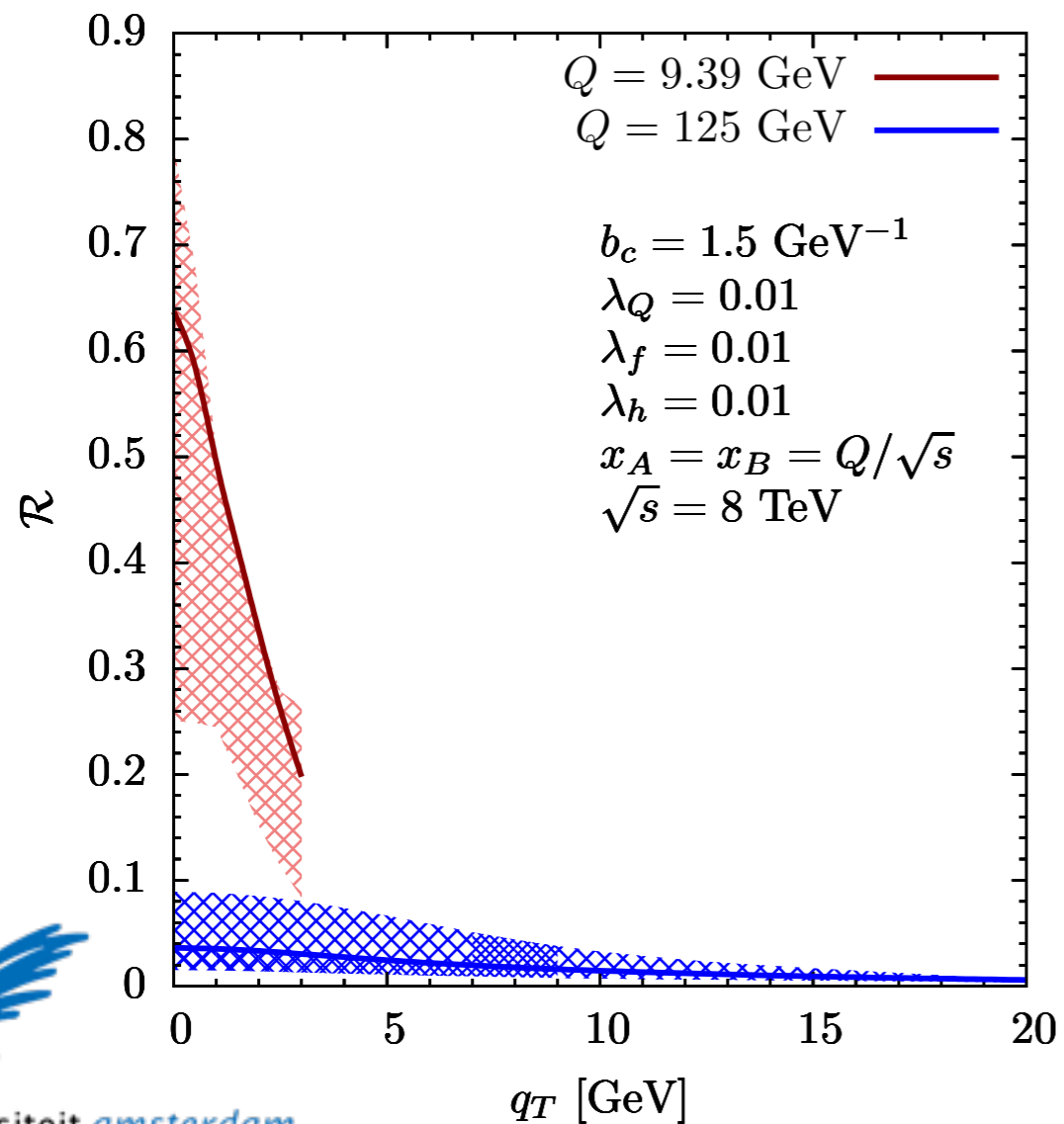
Linearly polarized vs unpolarized

Nonperturbative physics
enhanced at low Q



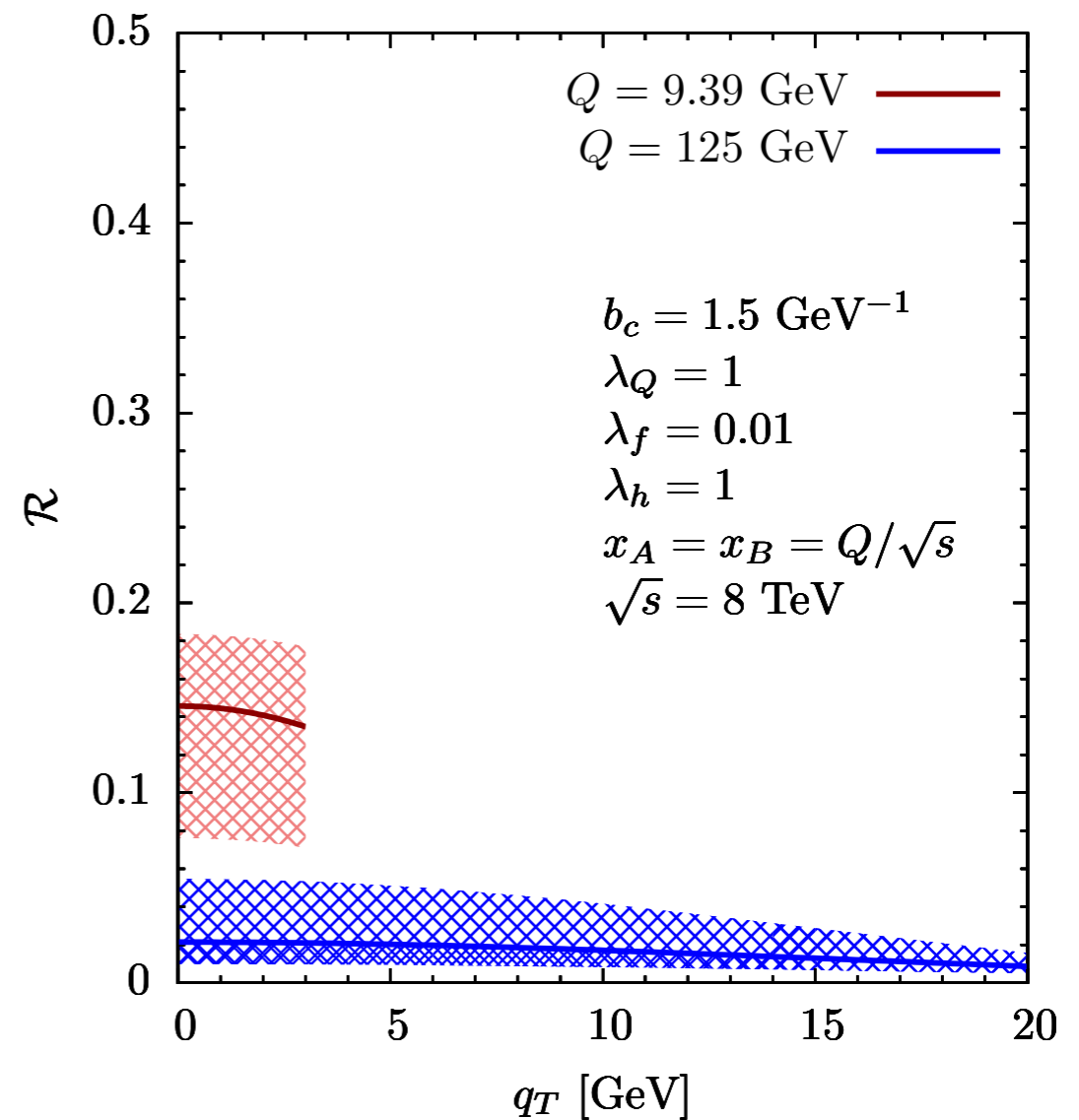
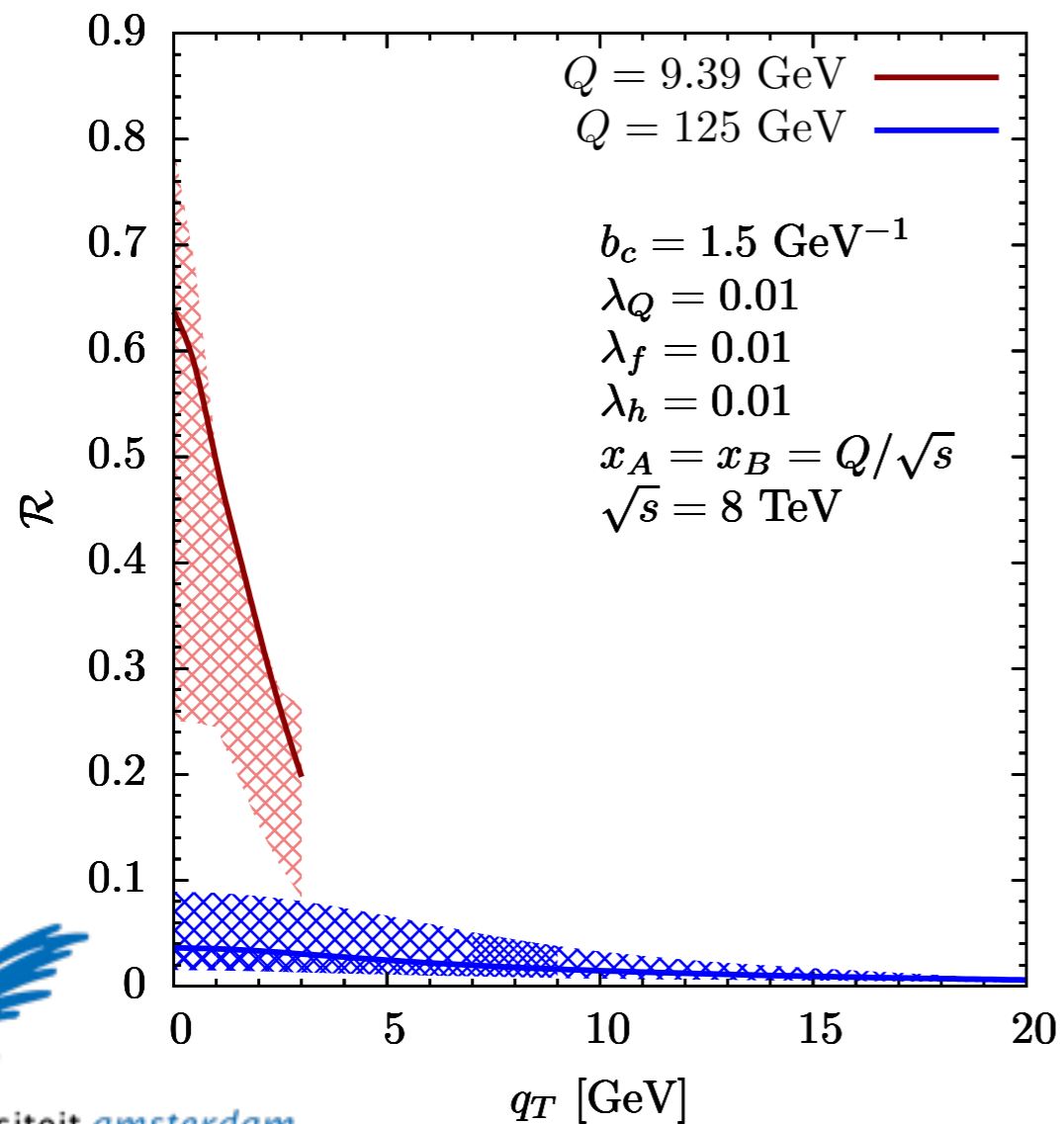
Linearly polarized vs unpolarized

lin. pol. gluons :
10% - 70% at low Q



Linearly polarized vs unpolarized

lin. pol. gluons :
1% - 9% at high Q



Gluons @ the LHC - take home

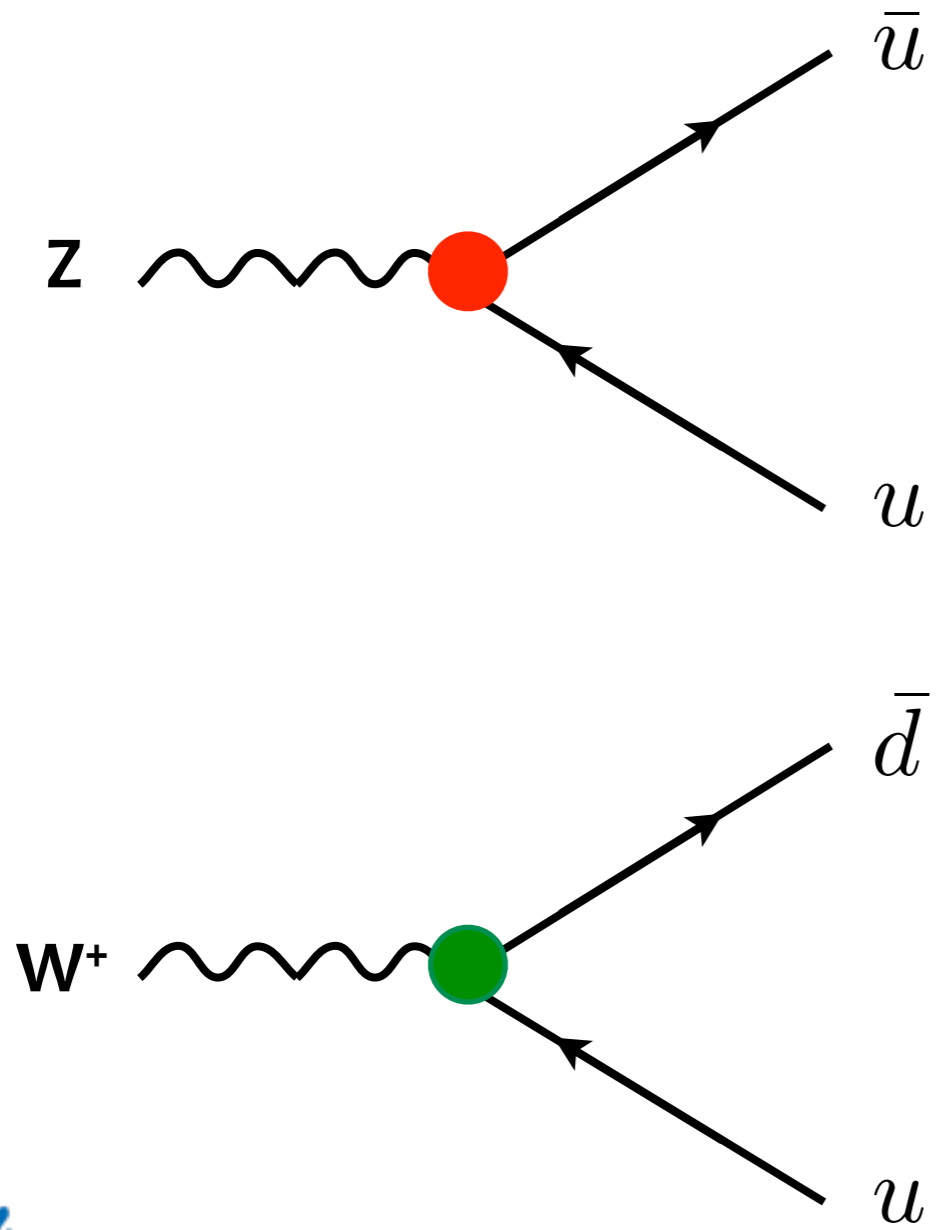
Lin. polarized gluons
are **not negligible**
when studying
TMD observables!

puzzling interplay :
the proton structure
manifests in different ways

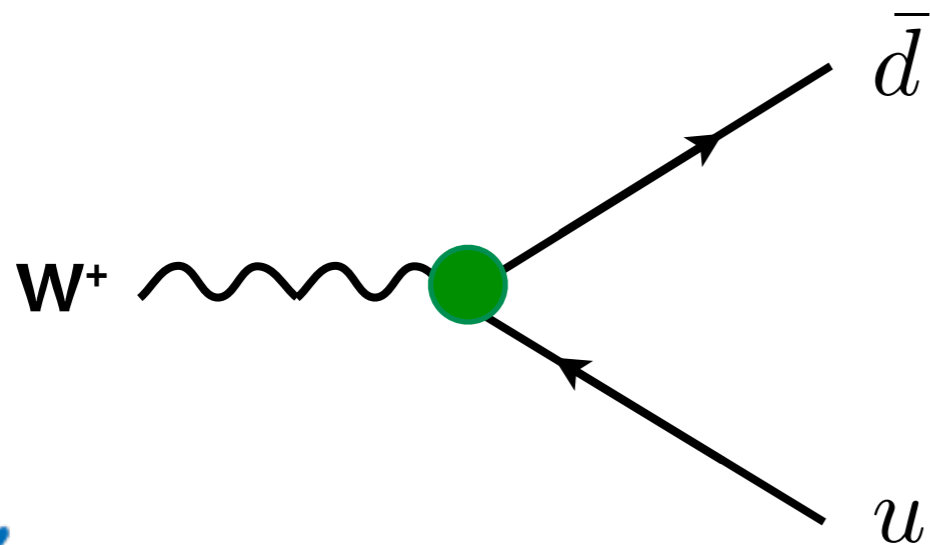
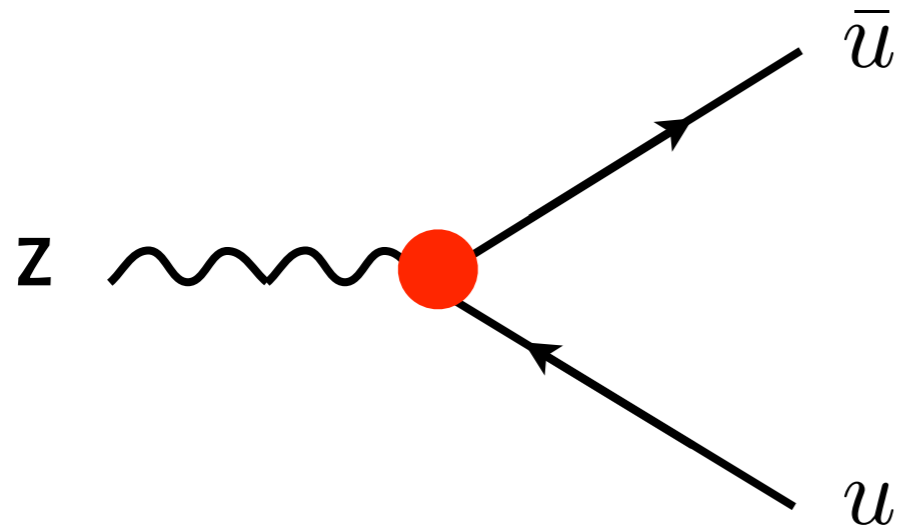
**ITS PHENOMENOLOGY
IS NOT UNIQUE**



Quarks @ the LHC



Quarks @ the LHC

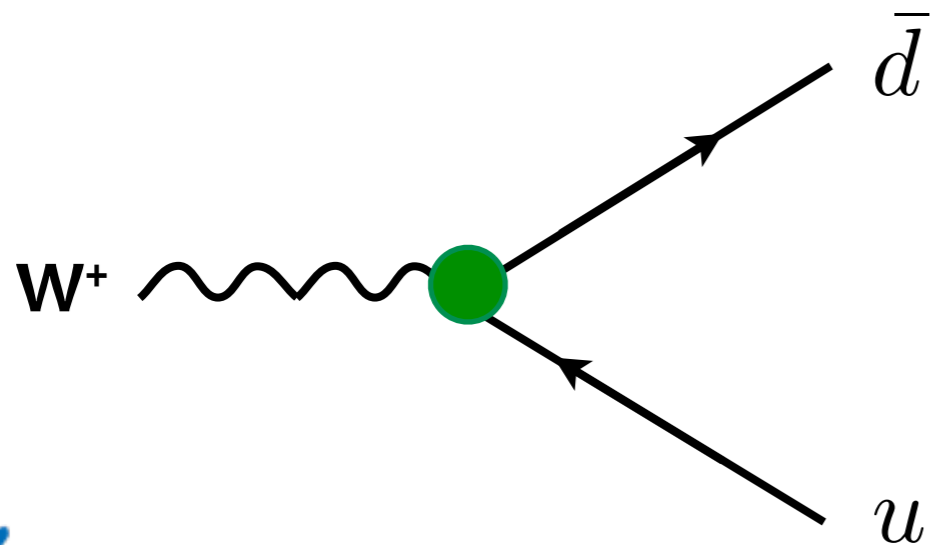
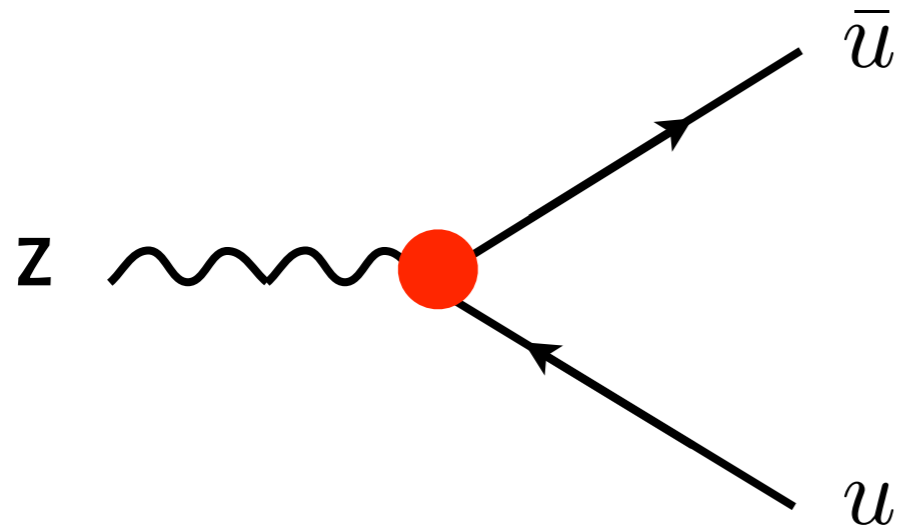


$$\frac{d\sigma}{dq_T} \sim \Phi_A^U \Phi_B^U |\mathcal{M}|^2$$

$$\sim \mathcal{C} \left[\begin{array}{cc} f_1^{q/A} & f_1^{q/B} \end{array} \right] \pm \mathcal{C} \left[\begin{array}{cc} h_1^{\perp q/A} & h_1^{\perp q/B} \end{array} \right]$$

unpolarized quarks
transv. polarized quarks

Quarks @ the LHC



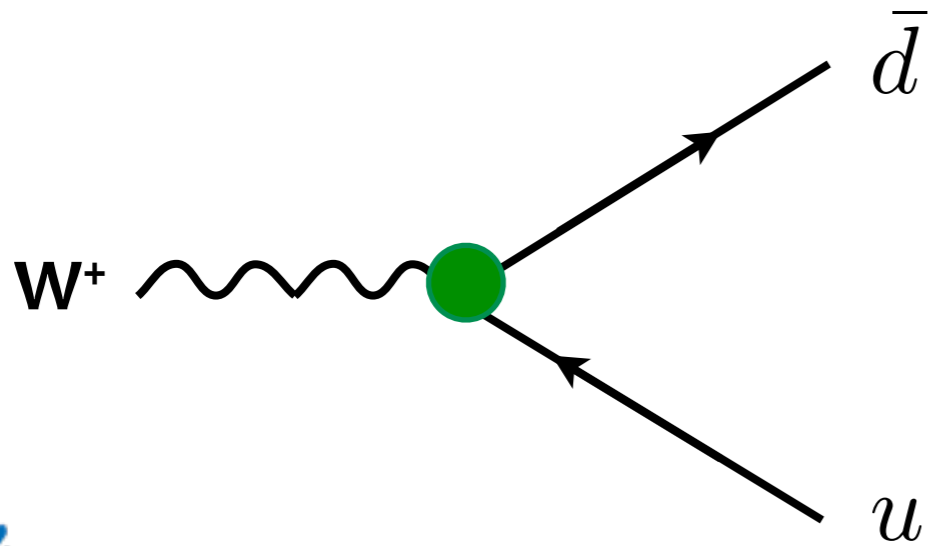
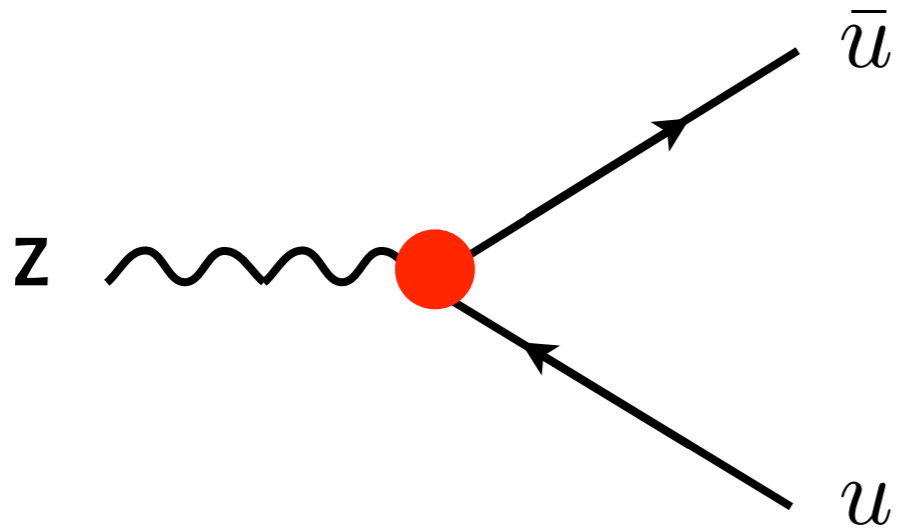
$$\frac{d\sigma}{dq_T} \sim \Phi_A^U \Phi_B^U |\mathcal{M}|^2$$

$$\sim \mathcal{C} \left[\begin{array}{cc} f_1^{q/A} & f_1^{q/B} \end{array} \right] \pm \mathcal{C} \left[\begin{array}{cc} h_1^{\perp q/A} & h_1^{\perp q/B} \end{array} \right]$$

unpolarized quarks
transv. polarized quarks

no sufficient knowledge

Quarks @ the LHC



$$\frac{d\sigma}{dq_T} \sim \Phi_A^U \Phi_B^U |\mathcal{M}|^2$$

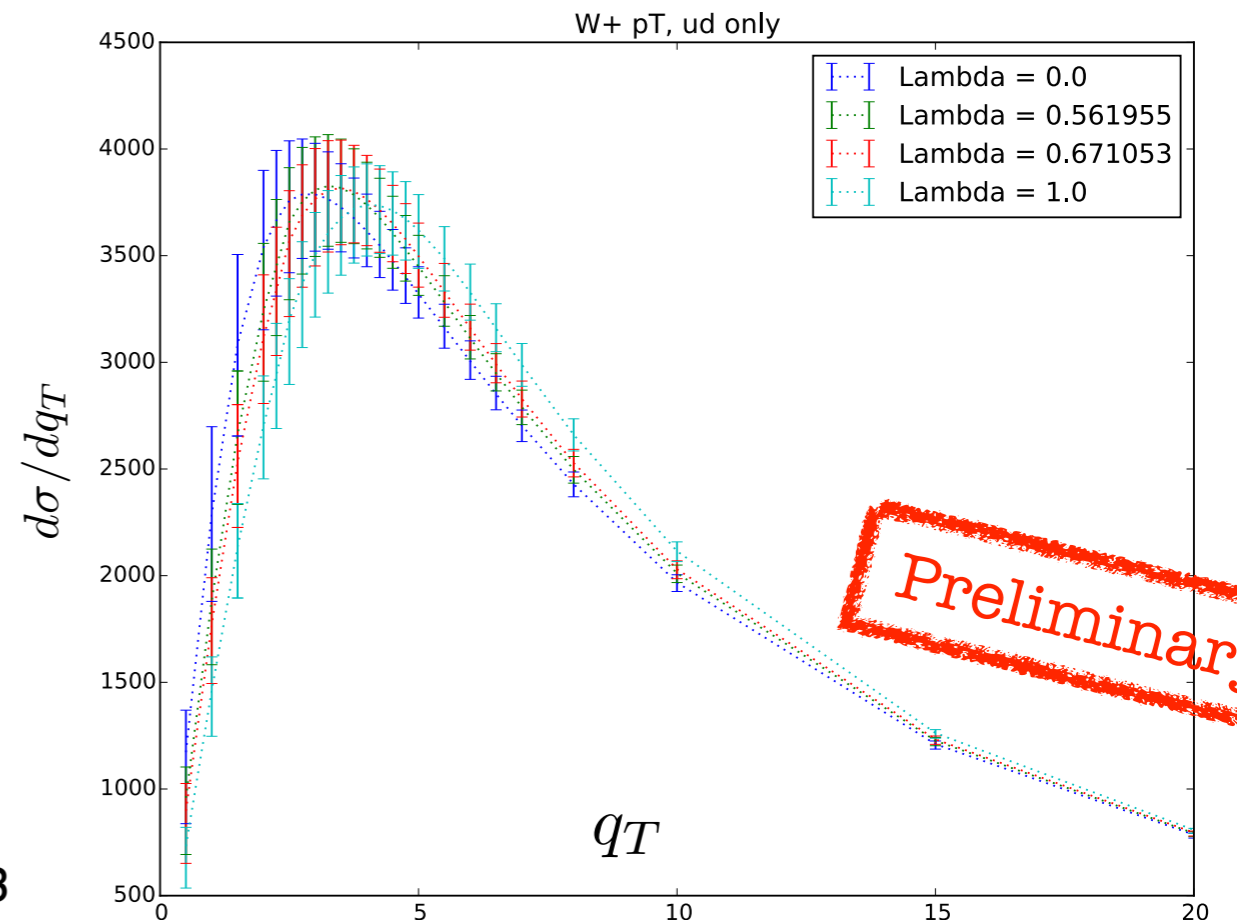
$$\sim \mathcal{C} \left[\begin{matrix} f_1^{q/A} & f_1^{q/B} \end{matrix} \right] \pm \mathcal{C} \left[\begin{matrix} h_1^{\perp q/A} & h_1^{\perp q/B} \end{matrix} \right]$$

unpolarized quarks

transv. polarized quarks

focus on the
flavor structure
of the NP part

~~no sufficient knowledge~~



Conclusions

1) We are opening a window on the **structure of the proton in 3D** momentum space

2) It's an interesting endeavor , with very **close connections between theory and experiments** - also with the LHC

3) Questions? Interested? Come to the 3rd floor !

Backup slides

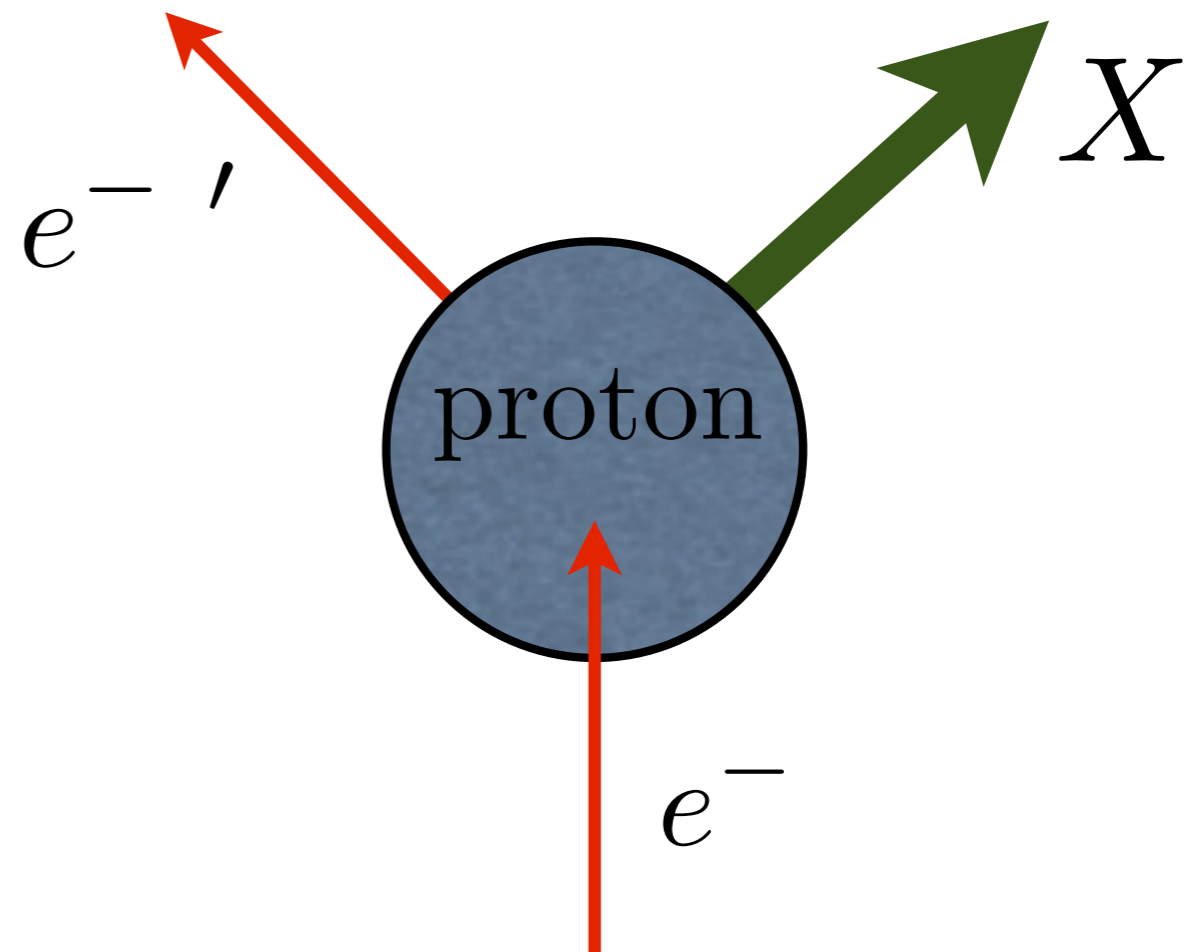
The quest for the structure

Electron-proton deep inelastic scattering
(MIT/SLAC -1960)
to test the
inner structure of the proton

scattering techniques

what happened ..?

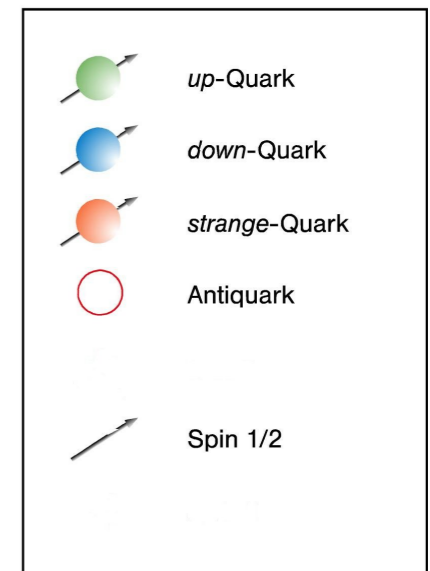
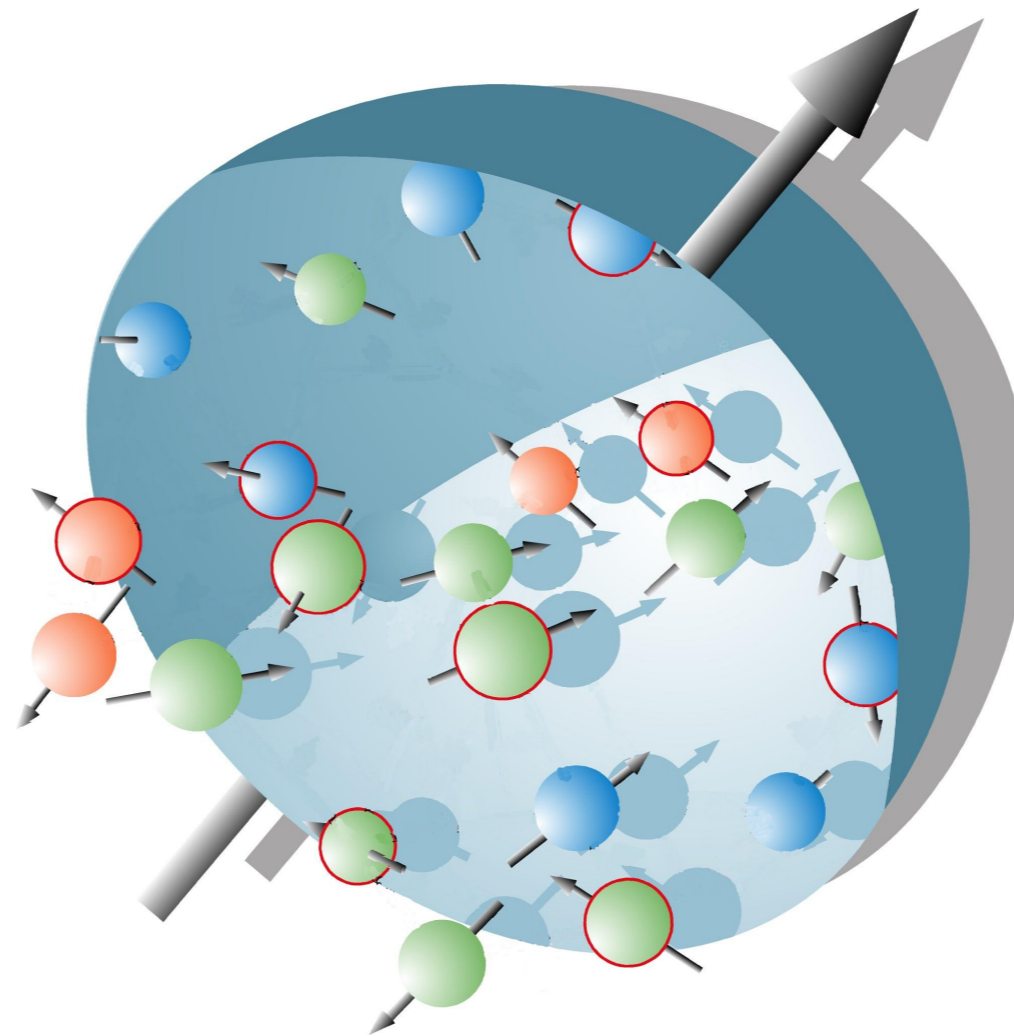
$$e^{-} P \rightarrow e^{-}' X$$



The quest for the structure

Experimental data are compatible with elastic scattering off **pointlike, free, spin $1/2$ particles**

The partons
[Feynman, Bjorken]

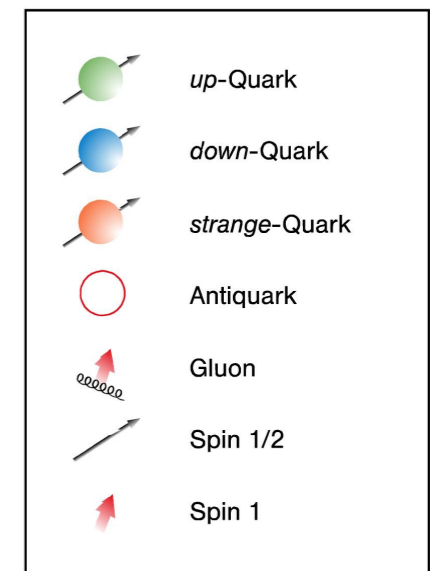
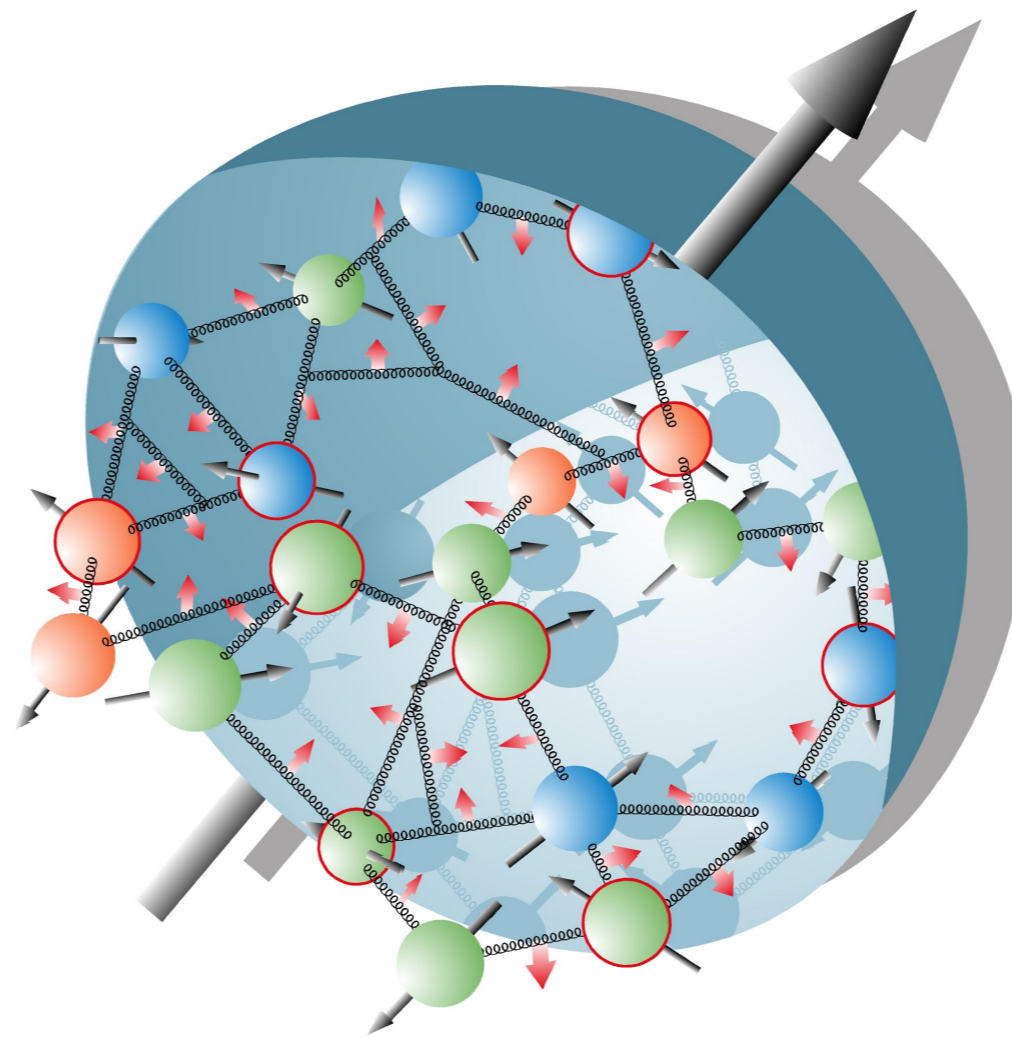


The quest for the structure

Experimental data are compatible with elastic scattering off **pointlike, free, spin 1/2 particles**

The partons
[Feynman, Bjorken]

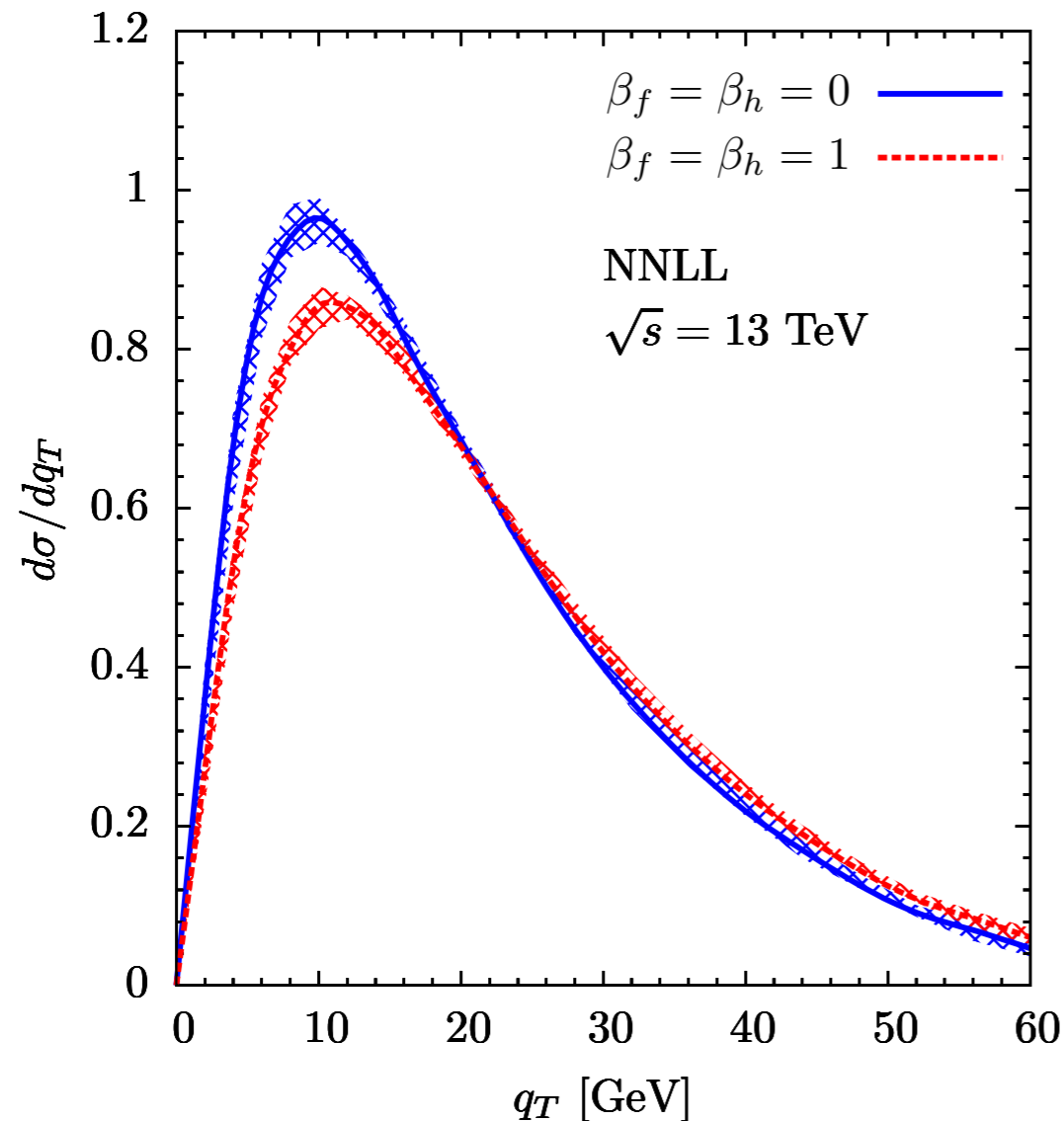
Quantum Chromodynamics:
they are the physical degrees of freedom of the theory at high-energies



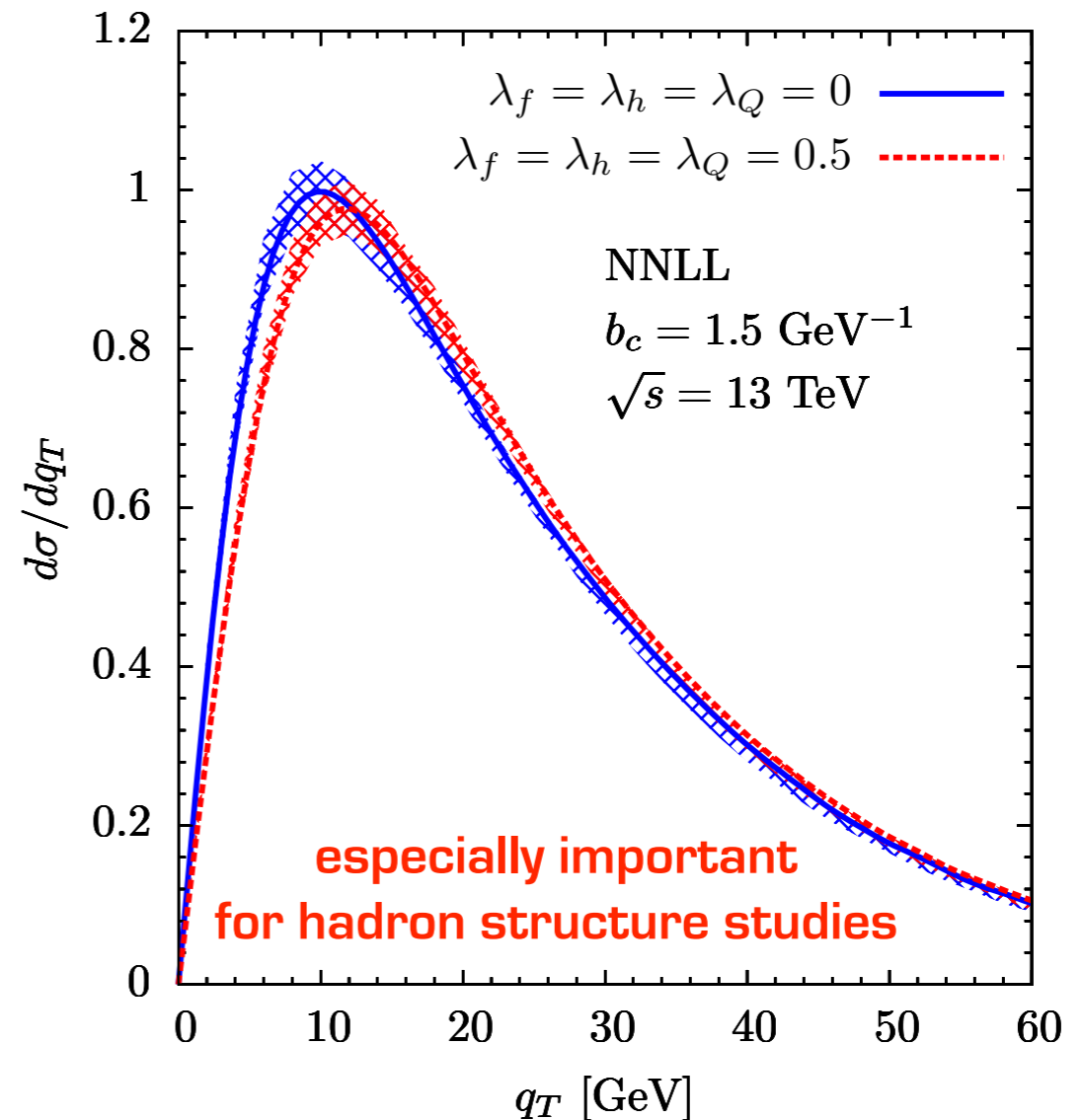
Quarks & gluons

Perturbative & nonperturbative

momentum space resummation



position space resummation



“freedom” in the perturbative part leads to
different descriptions of the NP part (the core of proton structure)

Philosophy of TMD phenomenology

REMEMBER :

dependence on non-perturbative parameters vanishes in the limit
 $Q/\Lambda_{QCD} \rightarrow \infty$ (Parisi, Petronzio 1979).

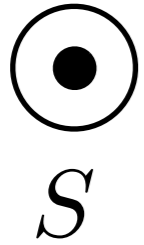
If we want to explore effects at low q_T we should look at
relatively low Q values.

BUT not too low: problems with factorization and/or
pollution from higher twist effects

At medium values of Q we could appreciate and
extract the low q_T effects applying TMD evolution properly

“in medio stat virtus”

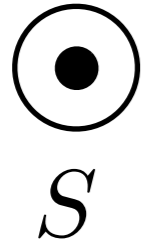
The Sivers effect



$$f_{1T}^{\perp}$$

interaction between **spin of the proton** and **OAM of the quark**

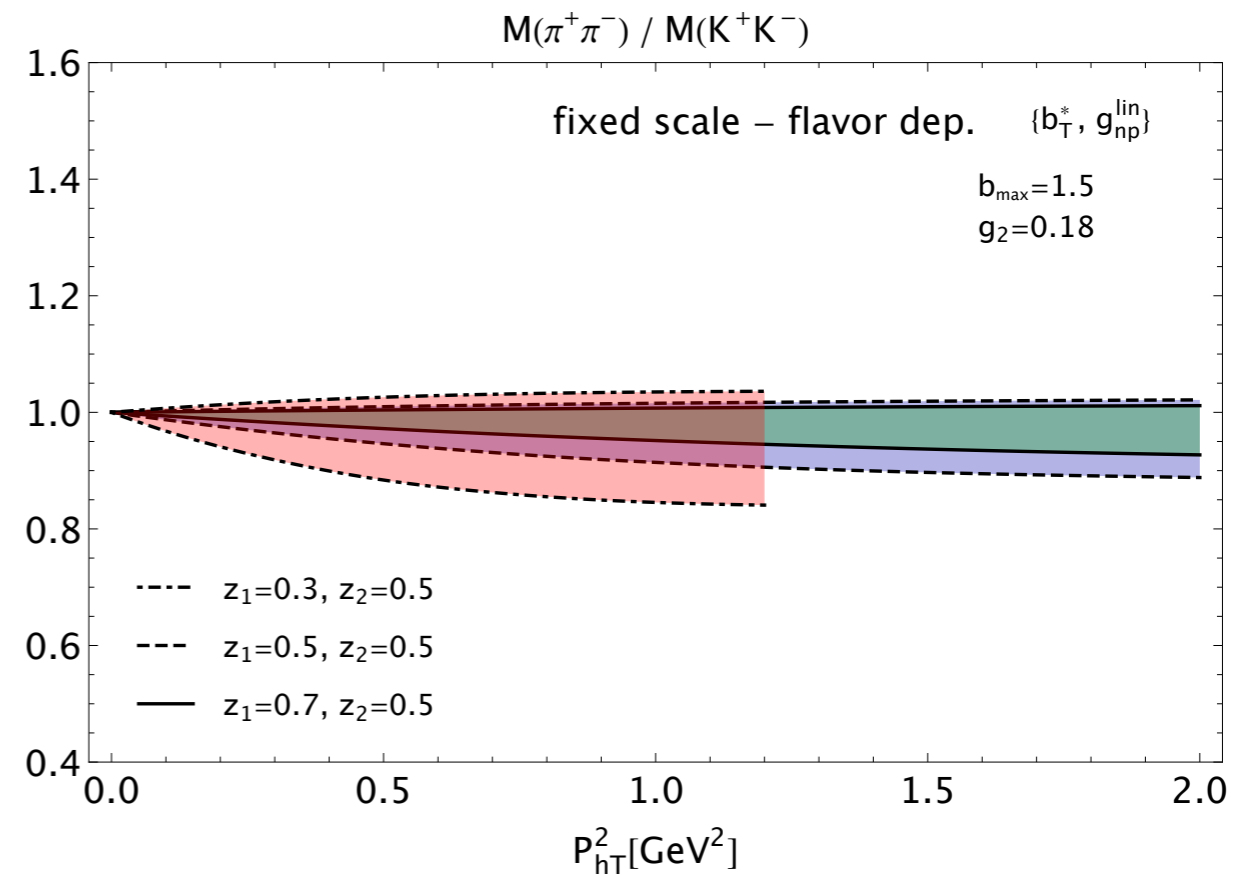
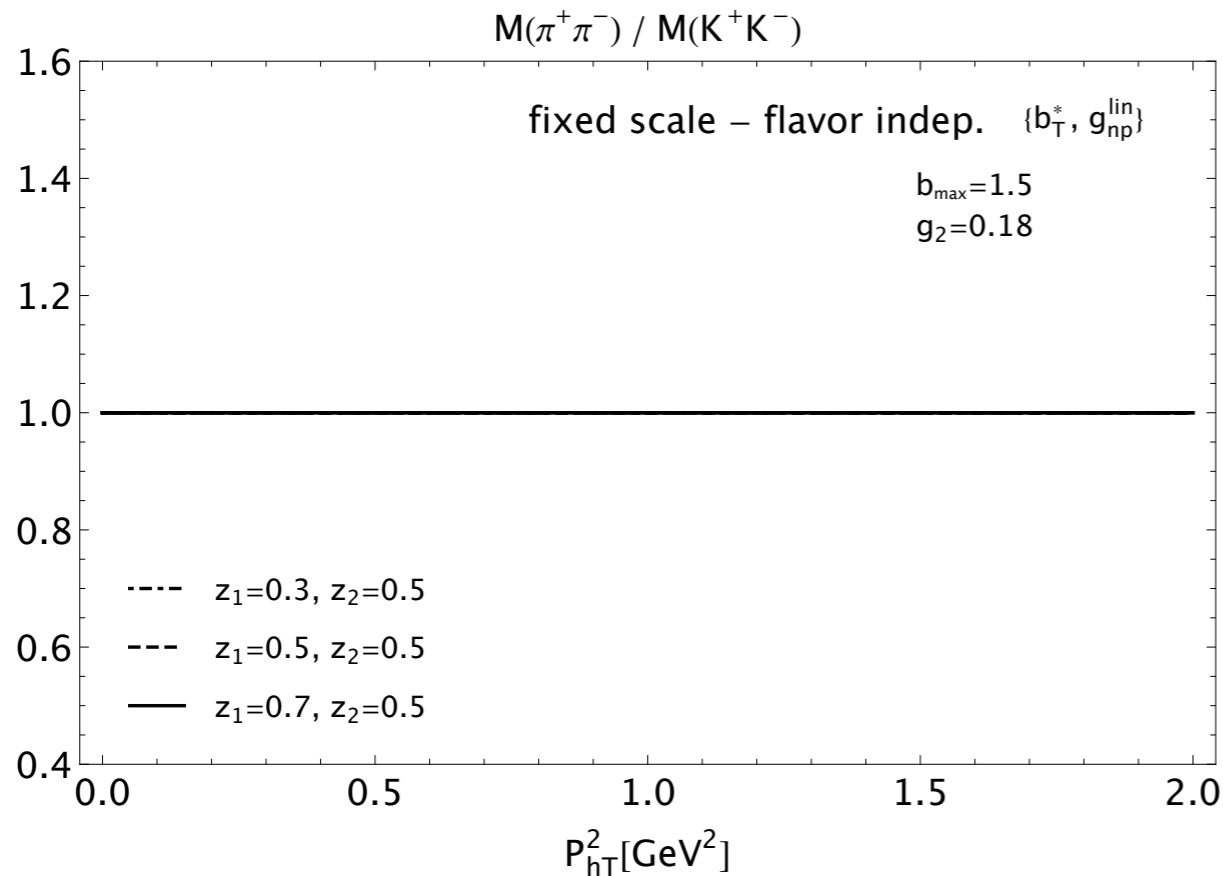
The Sivers effect



$$f_{1T}^{\perp}$$

interaction between **spin of the proton** and **OAM of the quark**

Quarks @ e^+e^- colliders - TMD FFs



Estimated **impact of flavor dependent intrinsic transverse momentum**
on electron-positron annihilation into two hadrons

Gluon correlator

$$\Phi^{\mu\nu}(k; P, S) \sim \text{F.T.} \langle P, S | F^{+\mu}(0) U_{[0,\xi]} F^{n\nu}(\xi) U'_{[\xi,0]} | P, S \rangle_{LF}$$

This is a **Lorentz matrix** ,
parametrized in terms of gluon
distributions