

(Exercises - day 2)

Today's exercises

ex9 – ML estimators

ex09.C

Example of Maximum Likelihood estimation

- Illustration of ML estimate on Poisson counting model

$$L(N | s) = \text{Poisson}(N | s + \tilde{b})$$

-log L(N|s) versus N [s=0,5,10,15] -log L(N|s) versus s [N=7]

- Note that Poisson model is discrete in N, but continuous in s!

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ex10 – Interval calculators

ex10_roostats_p1r_interval.C

Connection with likelihood ratio intervals

- If you assume the asymptotic distribution for t_{μ} ,
 - Then the confidence belt is exactly a box
 - And the constructed confidence interval can be simplified to finding the range in μ where $t_{\mu} = \frac{1}{2} Z^2$

→ This is exactly the MINOS error

FC interval with Wilks Theorem MINOS / Likelihood ratio interval

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ex11 – Poisson Sidebands

ex11_build_PoissonPoisson.C

The sideband measurement

- Suppose your data in reality looks like this →

Can estimate level of background in the 'signal region' from event count in a 'control region' elsewhere in phase space

$$L_{SR}(s, b) = \text{Poisson}(N_{SR} | s + b)$$

NB: Define parameter 'b' to represent the amount of bkg is the SR.

$$L_{CR}(b) = \text{Poisson}(N_{CR} | \tilde{\tau} \cdot b)$$

Scale factor $\tilde{\tau}$ accounts for difference in size between SR and CR

"Background uncertainty constrained from the data"

- Full likelihood of the measurement ('simultaneous fit')

$$L_{full}(s, b) = \text{Poisson}(N_{SR} | s + b) \cdot \text{Poisson}(N_{CR} | \tilde{\tau} \cdot b)$$

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ex12 – Subsidiary measurements

ex12_build_PoissonGaussGlobs.C

Generalizing the concept of the sideband measurement

- Background uncertainty from sideband clearly clearly not a 'systematic uncertainty'

$$L_{full}(s, b) = \text{Poisson}(N_{SR} | s + b) \cdot \text{Poisson}(N_{CR} | \tilde{\tau} \cdot b)$$

- Now consider scenario where b is not measured from a sideband, but is taken from MC simulation **with an 8% cross-section 'systematic' uncertainty**

'Measured background rate by MC simulation'

$$L_{full}(s, b) = \text{Poisson}(N_{SR} | s + b) \cdot \text{Gauss}(\tilde{b} | b, 0.08)$$

'Subsidiary measurement' of background rate

- We can model this in the same way, because the cross-section uncertainty is also (ultimately) the result of a measurement

Generalize: 'sideband' → 'subsidiary measurement'

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Today's exercises

ex13 – template models

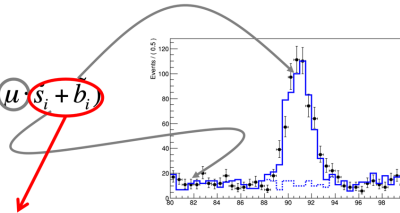
ex13_build_binned.C

The imperfect experiment

- When relying on simulation templates to build models, a whole world of problems awaits when considering that simulation predictions have many systematic uncertainties associated with them?

$$L(\vec{N} | \mu) =$$

$$\prod_{bins} \text{Poisson}(N_i | \mu \cdot (s_i + b_i))$$



Signal and background predictions
are affected by (systematic) uncertainties