Electric Dipole Moments and the search for new CP violation



Jordy de Vries, Nikhef, Amsterdam Topical Lectures on electric dipole moments, Dec. 14-16





Goals

- Goal 1: A crash course in Electric Dipole Moments
 - What are EDMs and why do people bother to find them?
 - Overview of EDM theory and experimental landscape (I'm a theorist...)
- **Goal 2:** Put EDMs in a broader context (LHC/flavor/....)
 - How do EDM measurements complement other searches ?
- Goal 3: Discuss outstanding issues/challenges/opportunities

A rough outline ...

- Part 1: What are Magnetic and Electric Dipole Moments ?
 - General introduction
 - EDMs and the CKM mechanism
- Part 2: EDMs and 'strong' CP violation
 - The QCD theta term and the strong CP problem
- Part 3: Classes of EDM experiments
 - Why are there so many experiments ??
- Part 4: EDMs in the era of the LHC

Magnetic dipole moments

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- A particle with spin (i.e. electron) in a magnetic field is described by





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 $\omega = 2\mu B\sin\theta$

• How large is the magnetic dipole moment ?

Magnetic dipole moments

• Magnetic moment from Dirac Equation (DE):

$$(i\gamma^{\mu}D_{\mu} - m)\Psi_{e}(p) = 0$$
$$D_{\mu} = \partial_{\mu} + ieA_{\mu}$$

e



• In the non-relativistic limit, the solution to DE becomes:

$$\Psi_{e}(p) \sim \begin{pmatrix} \chi \\ \frac{\vec{\sigma} \cdot \vec{p}}{2m} \chi \end{pmatrix}$$

$$A_{\mu}$$

$$\downarrow q \qquad e \bar{u}(p') \gamma^{\mu} u(p) A_{\mu} \rightarrow e \left[(\chi^{\dagger} \chi) A_{0} + \frac{i}{2m} \chi^{\dagger} \sigma^{k} \chi \epsilon^{klm} q^{l} A^{m} \right]$$

$$\downarrow p \qquad p' \qquad e \qquad q = p - p'$$

$$B^{k}$$



- g is the gyromagnetic ratio, triumph of Dirac and QM !
- Electron magnetic moment ~ $e/m_e \sim 10^{-11} e cm \sim 100 e fm$
- Nucleon magnetic moment ~ $e/m_N \sim 10^{-13} e cm \sim 1 e fm$
- By the way: do we expect for the nucleon g=2 as well?

• So Dirac predicts: $\begin{array}{c} A_{\mu} \\ e\bar{u}(p')\gamma^{\mu}u(p)A_{\mu} \rightarrow e\left[(\chi^{\dagger}\chi)A_{0} - \frac{1}{2m}\chi^{\dagger}\sigma \cdot B\chi\right] \\ H = -\frac{\mu}{2}(\vec{\sigma} \cdot \vec{B}) \quad \mu = \frac{eg}{2m} \quad g = 2 \end{array}$

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- Nucleon magnetic moment ~ $e/m_N \sim 10^{-13} e cm \sim 1 e fm$
- By the way: do we expect for the nucleon g=2 as well? (g = -3.826 for neutron and g = 5.58 for proton)
- Measurements in 1940's: $g_e = 2*(1.00118+-0.00003)....$
- Enter Quantum Field Theory

Anomalous magnetic moments

- Anomalous magnetic moment defined as a=(g-2)/2
- Calculate from loop diagrams:

$$a_e = \frac{\alpha_{em}}{2\pi} + \mathcal{O}(\alpha_{em}^2)$$



- Nowadays calculated up to **5 loops** in QED, 2 loops in electroweak
- Measurement so precise (Harvard group) that it is used to determine the fine-structure constant α_{em}
- Alternatively: take α_{em} from somewhere else (atomic spectroscopy)

$$\Delta a_e = a_e^{\exp} - a_e^{\rm SM} = -1.05(0.82) \times 10^{-12}$$

• Agreement up to 12 digits.... Quite remarkable.

Trouble in paradise

- The muon is elementary too !
- Measure its g-2 as well @ Brookhaven

 $\Delta a_{\mu} = a_{\mu}^{\exp} - a_{\mu}^{\rm SM} = 2.88(0.63)(0.49) \times 10^{-9}$

- Some tension with SM predictions ~ 3 sigma
- Larger theory uncertainties from hadronic effects...





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- Larger theory uncertainties from hadronic effects...
- Say it is true, what does it mean? A new term in the QED Lagrangian !

$$\mathcal{L} = \bar{\Psi}_{\mu} (i\gamma^{\mu} D_{\mu} - m_{\mu}) \Psi_{\mu} - C_{\mu} m_{\mu} \bar{\Psi}_{\mu} \sigma^{\mu\nu} \Psi_{\mu} F_{\mu\nu}$$

• 'new physics' contribution $\Delta a_{\mu} = m_{\mu}^2 C_{\mu}$ $C_{\mu} \sim \alpha_{em} \frac{1}{\Lambda_{BSM}^2}$ $\Lambda_{BSM} \sim \frac{m_{\mu} \sqrt{\alpha_{em}}}{\sqrt{\Delta a_{\mu}}} \sim 100 \,\text{GeV}$ A bit low.....





Magnetic Electric dipole moments

- Let's remind ourselves about electric dipole moments
- A particle with spin (i.e. neutron) in an **electric** field is described by





• The **E-field** puts a torque on the system \rightarrow spin precession

 $\omega = 2\mu E \sin \theta \qquad \omega = 2dE \sin \theta$

• How large is the **electric** dipole moment ?

- We already exhausted the Dirac equation... No EDM there ?
- Can we understand this ?

$$H = -\mu(\vec{S} \cdot \vec{B}) - d(\vec{S} \cdot \vec{E})$$

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• Perform a Time-reversal (T) transformation

$$\vec{S} \rightarrow -\vec{S}$$
Spin like angular momentum ~ $\vec{L} \sim \vec{r} \times \vec{p}$

$$\vec{B} \rightarrow -\vec{B}$$

$$\vec{E} \rightarrow \vec{E}$$
Spin like angular momentum ~ $\vec{L} \sim \vec{r} \times \vec{p}$

$$\vec{B} \propto \varepsilon^{ijk} F_{jk} \sim \partial_j A_k \rightarrow (+\partial_j)(-A_k)$$

$$\vec{E} \propto F_{0i} \sim \partial_0 A_i \rightarrow (-\partial_0)(-A_i)$$

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$$H = -\mu(\vec{S} \cdot \vec{B}) - d(\vec{S} \cdot \vec{E})$$

• Perform a Parity (P) transformation

$$\vec{S} \to \vec{S}$$
Spin like angular momentum ~ $\vec{L} \sim \vec{r} \times \vec{p}$
 $\vec{B} \to \vec{B}$
 $\vec{E} \to -\vec{E}$
Spin like angular momentum ~ $\vec{L} \sim \vec{r} \times \vec{p}$
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- EDMs violate T and P symmetry ! But QED is P-invariant !
- CPT theorem: **T-violation = CP violation** !
- So if we measure a nonzero EDM this means CP (or CPT...) violation!
- Two major questions should pop up:
 - 1. Uuuuh, what about H_2O or NH_3 molecules. HUGE EDMs. ~ 10⁻⁸ e cm
 - 2. What about CP violation in the SM ?

Other electric dipole moments

- Take a classical dipole configuration
- Electric dipole ~ d ~ q r
- Does not violate anything



- So we mean with an EDM: the coupling of **spin** and the **E-field**.
- For electron, neutron, atom, the only quantity available is the spin.
 So there is no 'r' around
- So where does the non-CPV EDM of molecules come from ?

Double-well potential

- Analogy take a double-well potential
- If V_0 is very small, get usual solutions

$$\psi_n(x) = \begin{cases} \sqrt{\frac{2}{a}} \sin\left(\frac{n\pi x}{a}\right) & \text{if } 0 < x < a, \\ 0 & \text{otherwise,} \end{cases}$$



V

Double-well potential

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- With nonzero V₀, two solutions appear with different parity and a small enery difference (tunneling effect !). E₊ E₋ ~ b
- A molecule like water has indeed a nearly-degenerate ground state with opposite parity

Fake EDMs

- So we have 2 states which we call $|\pm\rangle$
- Turn on Electric Field E (mixing of states)

$$H = \left(\begin{array}{cc} \mathcal{E}^+ & 0\\ 0 & \mathcal{E}^- \end{array}\right) + \left(\begin{array}{cc} 0 & Eb\\ Eb & 0 \end{array}\right)$$

• Diagonalize matrix to get energy eigenvalues

$$\mathcal{E}_{1,2} = \frac{1}{2}(\mathcal{E}_{+} + \mathcal{E}_{-}) \pm \sqrt{(\mathcal{E}_{+} - \mathcal{E}_{-})^{2}/4 + E^{2}b^{2}}$$

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• If the E field is smaller than the energy gap

$$\mathcal{E}_{1,2} = \frac{1}{2}(\mathcal{E}_{+} + \mathcal{E}_{-}) \pm \frac{1}{2}(\mathcal{E}_{+} - \mathcal{E}_{-})\left(1 + \frac{2E^{2}b^{2}}{(\mathcal{E}_{+} - \mathcal{E}_{-})^{2}}\right)$$

- The energy shift is quadratic in the E field !! So no P or T violation
- If the E field is larger than the gap: degenerate ground state

$$\mathcal{E}_{1,2} = \frac{1}{2}(\mathcal{E}_+ + \mathcal{E}_-) \pm Eb$$

EDM theorem

- Nonzero EDMs imply P and T (and CP) violation if the system has a **nondegenerate ground state**
- Note: all subatomic particles are non-degenerate
 - 1. Uuuuh, what about H₂O or NH₃ molecules. HUGE EDMs. ~ 10^{-8} e cm

Degenerate ground states, no signal for CP violation !

2. What about CP violation in the Standard Model (SM) ? How large are EDMs expected to be ?

CP violation in the Standard Model

• **Two** sources of CPV in the Standard Model

$$L_{CPV} = L_{CKM} + L_{theta}$$



- Three real (CP-conserving) mixing angles and one CPV phase
- Appears in charged weak interactions. In diagonal-mass basis

$$\frac{-g}{\sqrt{2}}(\bar{u}_L, \, \bar{c}_L, \, \bar{t}_L)\gamma^{\mu}V_{CKM} \begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix} W^+_{\mu} + \text{h.c.}$$

- Note, CPV phase is not small at all: $Sin(\delta_{13}) \sim O(1)$
- But the off-diagonal elements are small: $s_{13} \sim 10^{-3}$ (not understood)

• Analogously to g-2 magnetic moment corrections we can calculate SM EDMs.

$$L_{dip} = -\frac{1}{2} \overline{\Psi} \sigma^{\mu\nu} (\mu + i\gamma^5 d) \Psi F_{\mu\nu}$$



$$\mu = \frac{e}{2m_e} \frac{\alpha_{em}}{2\pi} \qquad d = 0$$
Why

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$$\mu = \frac{e}{2m_e} \frac{\alpha_{em}}{2\pi} \qquad d = 0$$
Why



$$\mu \propto \frac{m_d}{m_W^2} \frac{\alpha_{weak}}{2\pi} (V_{qd} V_{qd}^*)$$
$$d = 0 \qquad \text{Why ?}$$

- At two loops: individual diagrams contribute but the sum vanishes
- $d_q (2 \text{ loops}) = 0$, this was unexpected !



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- At three loops: $d_d \simeq m_d \frac{m_c^2 \alpha_s G_F^2}{108\pi^5} \mathcal{J}_{CP} \simeq 10^{-21} \, e \, \mathrm{fm}$ $\mathcal{J}_{CP} = c_{12} c_{23} c_{13}^2 s_{12} s_{23} s_{13} \sin \delta \simeq 3 \cdot 10^{-5}$
- Electron EDM at 4 loops $d_e \simeq 10^{-26} \, e \, {\rm fm}$
- Compare with magnetic moment: $\mu_e \simeq 100 \, e \, \mathrm{fm}$
- CKM EDMs are really **very very very small**

Measuring EDMs

• General idea now. Later more.



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• Note

 $d = 10^{-28} e \ cm \qquad E = 100 \ kV \ / \ cm$ $\delta \omega \sim 10^{-7} \ rad \ / \ s \sim 1 \ rad \ / \ year$

It's hopeless.....

System	Current limit	CKM contribution	
Neutron	< 10 ⁻²⁶ e cm	10 ^{-31,-32} e cm	
¹⁹⁹ Hg	< 10 ⁻²⁹ e cm	10 ^{-33,-35} e cm	
Electron	< 10 ⁻²⁸ e cm	10 ^{-38,-39} e cm	

- Systems with strongest experimental limits
- CKM contributions are many orders of magnitude away

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- Systems with strongest experimental limits
- CKM contributions are many orders of magnitude away
- Some questions for later: why neutron, Hg, and electron ?
- Why is the CKM contribution to Hg smaller than to neutron?
- What do these bounds mean for BSM CP violation ?

Standard Model suppression



5 to 6 orders **below** upper bound \longrightarrow **Out of reach!**

With linear extrapolation: CKM neutron EDM in 2075....

Other sources of CP violation

- Another SM source of CP violation (QCD theta term)
- Discussed in next lecture

- CKM EDMs are small because of the peculiar SM flavor structure
- Only CPV in flavor-changing transitions + 3 loops
- NOT GENERAL at all. In many BSM models, EDMs at tree- or one-loop level. Much larger EDMs !
- These lectures will not discuss BSM models in any detail, **but just to** illustrate

The MSSM

The MSSM can contain many new sources of CP violation

Higgsino and Higgs masses \rightarrow 2 phases

squark and slepton masses \rightarrow 15 phases

gaugino masses \rightarrow 3 phases

trilinear couplings \rightarrow 27 phases

 $\mu \tilde{H}_{u} \tilde{H}_{d} + \frac{B \mu H_{u} H_{d}}{H_{d}} + \frac{m_{H_{u}}^{2}}{H_{u}}|^{2} + \frac{m_{H_{d}}^{2}}{H_{d}}|^{2}$

$$\begin{split} m_Q^2 \tilde{Q}_L^{\dagger} \tilde{Q}_L + m_U^2 \tilde{U}_R^{\dagger} \tilde{U}_R + m_D^2 \tilde{D}_R^{\dagger} \tilde{D}_R \\ + m_L^2 \tilde{L}_L^{\dagger} \tilde{L}_L + m_E^2 \tilde{E}_R^{\dagger} \tilde{E}_R \end{split}$$

 $m_1 \tilde{B}\tilde{B} + m_2 \tilde{W}\tilde{W} + m_3 \tilde{g}\tilde{g}$

 $\textbf{A}_{u} \ \textbf{H}_{u} \tilde{\textbf{Q}}_{L}^{\dagger} \tilde{\textbf{U}}_{R} + \textbf{A}_{d} \ \textbf{H}_{d} \tilde{\textbf{Q}}_{L}^{\dagger} \tilde{\textbf{D}}_{R} + \textbf{A}_{\ell} \ \textbf{H}_{d} \tilde{\textbf{L}}_{L}^{\dagger} \tilde{\textbf{E}}_{R}$

not all phases are physical! (like in the case of the CKM matrix)

2 phases can be rotated away...

Slide from Altmannshofer, 2014

The SUSY CP problem

Example 1: Bino-Higgsino loop contribution to the electron EDM



- CPV phase already at one-loop !
- Typical size of EDM

$$d_e \sim \left(\frac{\alpha_{em}}{\pi}\right)^n \frac{m_e}{\Lambda^2} \sin\phi$$

If phase = O(1):
$$\Lambda > 10 \text{ TeV} (n=1)$$

- MSSM was pushed above 1 TeV well before the LHC was turned on
- Usual solution: ignore CPV phases... (pMSSM, cMSSM, ...)
- 'Solutions' to the problem exist (decouple sfermions, cancellations, ...)

Matter-Antimatter asymmetry







Observed:

 $\frac{n(b)}{n(\gamma)} \approx 10^{-9}, \quad n(\overline{b}) \approx 0$

Expected:

$$\frac{n(b)}{n(\gamma)} \approx \frac{n(b)}{n(\gamma)} \approx 10^{-18}$$

Sakharov Conditions

Standard Model

- Baryon number violation :
- C & CP violation:
- Out of equilibrium (or CPT violation)

Yes ! (sphalerons) Yes, but too small No



Scenarios: Leptogenesis, **Electroweak baryogenesis**, Affleck-Dine, Asymmetric Dark Matter, whatever-you-can-come-up-with-genesis

• In many models, EDMs are not linked to the asymmetry





It's hopeless..... But that is nice !

Why are EDMs interesting to measure?



A search for new physics which is Many beyond-the-SM models predict large EDMs: Matter/Antimatter asymmetry requires more CPV:

'background free'
CKM too small

Complementary to LHC search EDMs are good probes, but NO direct link

Very active experimental field

	System	Group	Limit	C.L.	Value	Year
ſ	²⁰⁵ Tl	Berkeley	1.6×10^{-27}	90%	6.9(7.4) × 10 ⁻²⁸	2002
	YbF	Imperial	10.5×10^{-28}	90	$-2.4(5.7)(1.5) \times 10^{-28}$	2011
l	ThO	ACME	8.7×10^{-29}	90	$-2.1(3.7)(2.5) \times 10^{-29}$	2014
-	n	Sussex-RAL-ILL	3.0×10^{-26}	90	$0.2(1.5)(0.7) \times 10^{-26}$	2006
	¹²⁹ Xe	UMich	6.6×10^{-27}	95	$0.7(3.3)(0.1) \times 10^{-27}$	2001
	¹⁹⁹ Hg	UWash	7.4×10^{-30}	95	$-2.2(2.8)(1.5) \times 10^{-30}$	2016
	²²⁵ Ra	Argonne	1.4×10^{-23}	95	$-0.5(1.5)(0.01) \times 10^{-23}$	2016
	muon	E821 BNL g-2	1.8×10^{-19}	95	$0.0(0.2)(0.9) \times 10^{-19}$	2009

• Why do experiments on all these systems?

е

- How do the experiments compare? What does $dn/dHg \sim 10^{-3,-4}$ imply?
- Are there new systems that would be interesting to study ?

Race for an EDM



• And new experiment at Groningen/Nikhef using BaF molecule

EDMs are a multi-scale problem



Intermediate summary

• Electric dipole moments are probes of P and T and CP violation

$$H = -\mu(\vec{S} \cdot \vec{B}) - d(\vec{S} \cdot \vec{E})$$

- CP-violating analogue of magnetic dipole moments
- 'structural' EDMs of molecules like H2O are unrelated (no CPV)
- CPV in CKM is not 'small' but **just very inefficient** in creating EDMs
- 3 or 4 loops: orders of magnitude below experiments
- CPV beyond-the-SM is **very well motivated**
- In most BSM models EDMs are created much more efficiently
- Possible connection to **baryogenesis** (but no 1-to-1 link !)
- Forseeable future: **nonzero EDM = new CP violation**