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A Surrogate Model to Optimize Injection Efficiency in PSI muEDM Experiment

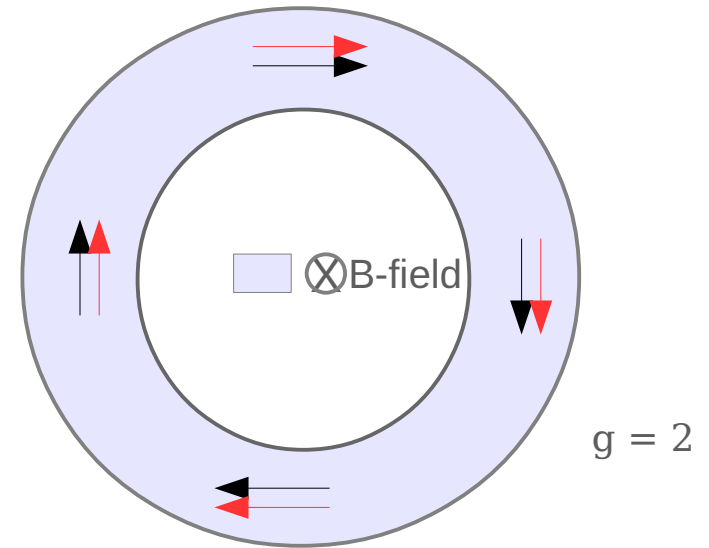
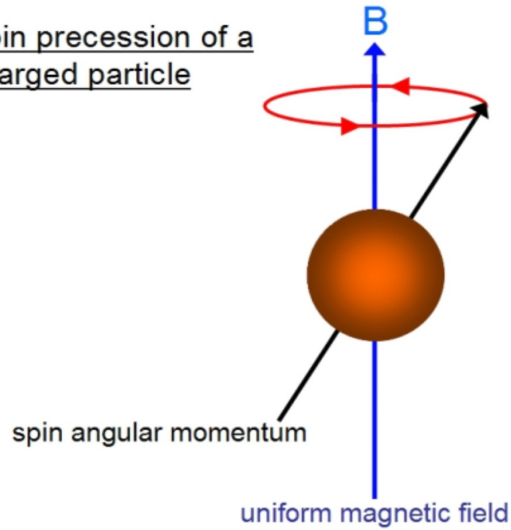
Ritwika Chakraborty (PSI)

**European AI for Fundamental Physics Conference
Amsterdam**

02.05.2024

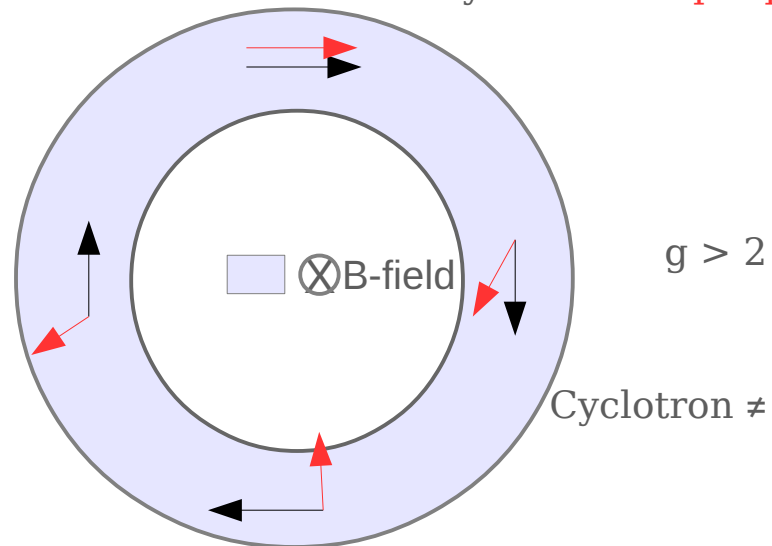
Muons in a Storage Ring

Spin precession of a charged particle



Cyclotron = spin precession

In presence of vacuum effects:



Cyclotron \neq spin precession

Frozen Spin Technique

- $E \perp B \perp \beta$

$$\vec{\Omega} = \frac{q}{m} \left[a\vec{B} - \frac{a\gamma}{(\gamma+1)} (\vec{\beta} \cdot \vec{B}) \vec{\beta} - \left(a + \frac{1}{1-\gamma^2} \right) \frac{\vec{\beta} \times \vec{E}}{c} \right] + \frac{\eta q}{2m} \left[\vec{\beta} \times \vec{B} + \frac{\vec{E}}{c} - \frac{\gamma c}{(\gamma+1)} (\vec{\beta} \cdot \vec{E}) \vec{\beta} \right]$$

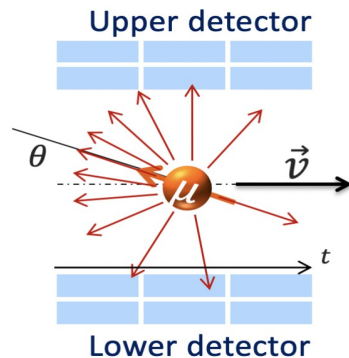
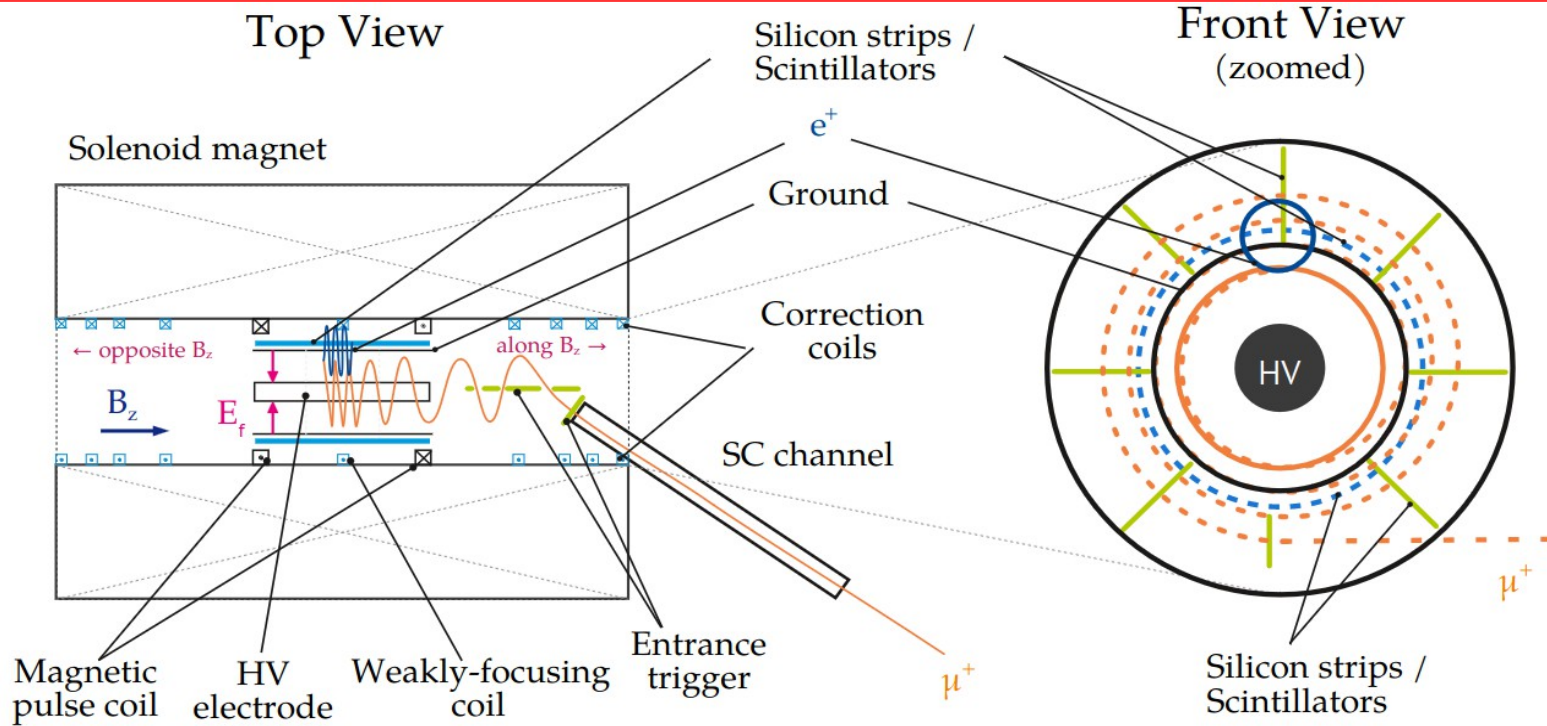
g-2 term
EDM term

- Suppress g-2 term by setting $a\vec{B} = \left(a - \frac{1}{\gamma^2 - 1} \right) \frac{\vec{\beta} \times \vec{E}}{c}$
- Radial E-field $E_f \approx aBc\beta\gamma^2$

$$\vec{\omega}_e = \frac{\eta q}{2m} \left[\vec{\beta} \times \vec{B} + \frac{\vec{E}_f}{c} \right]$$

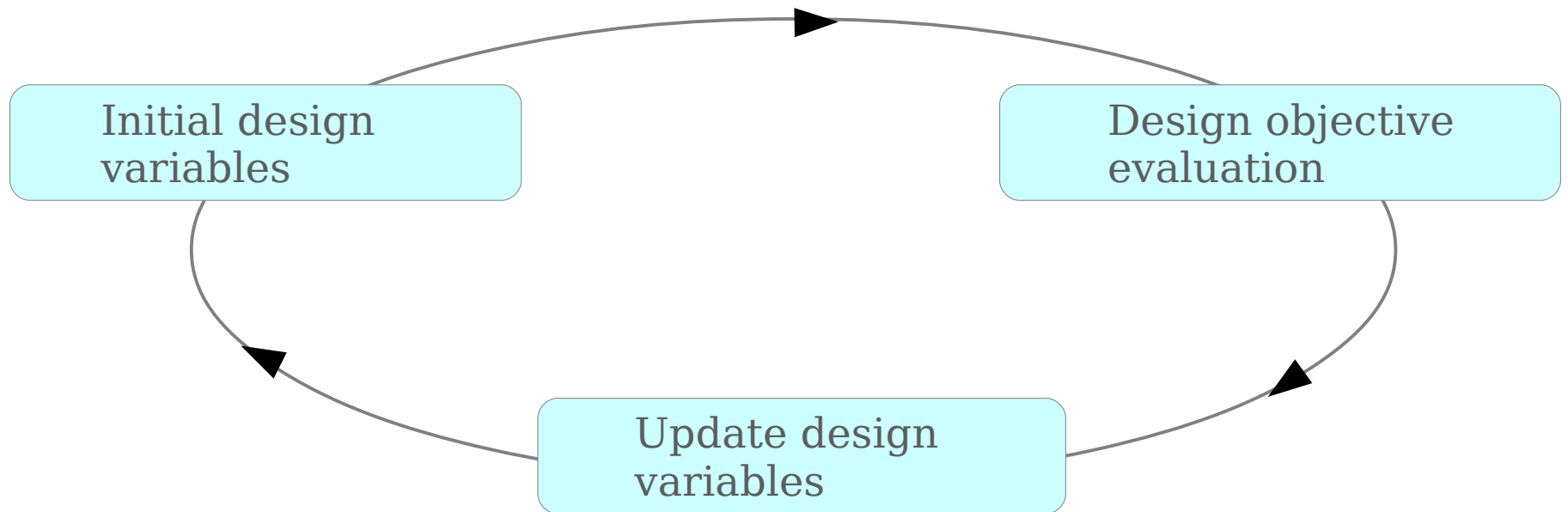
Precession frequency only due to EDM

PSI muEDM Experiment



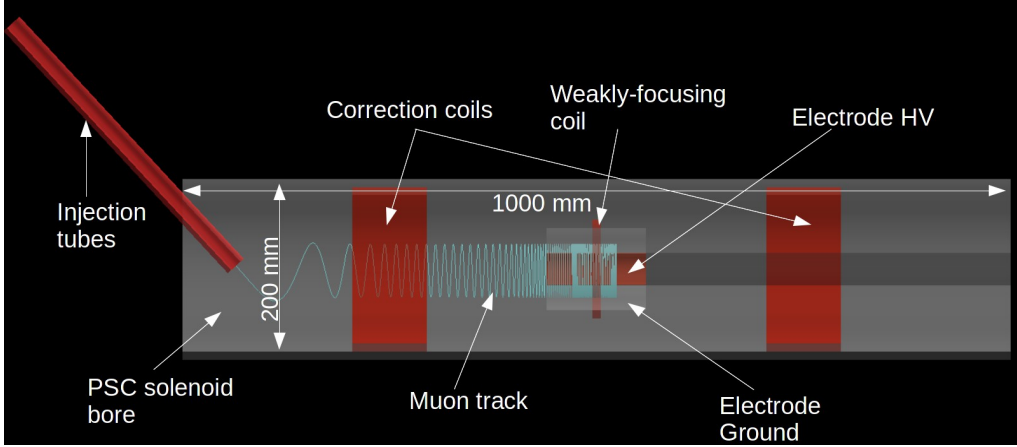
Asymmetry in number of detected positrons upstream vs downstream is proportional to EDM signal

Design Optimization Layout



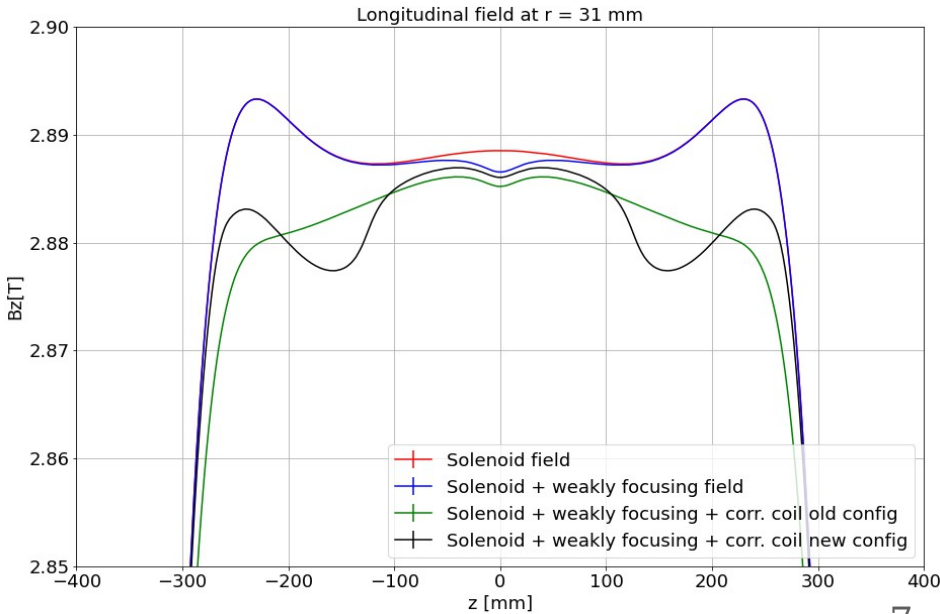
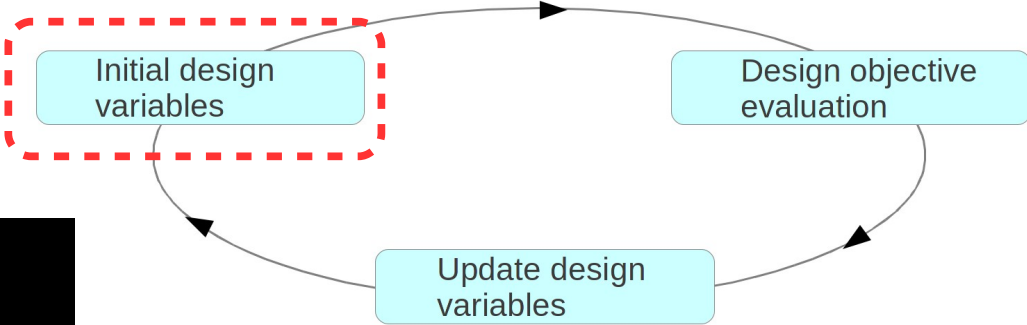
Design Optimization Layout

Design simulation in g4bl



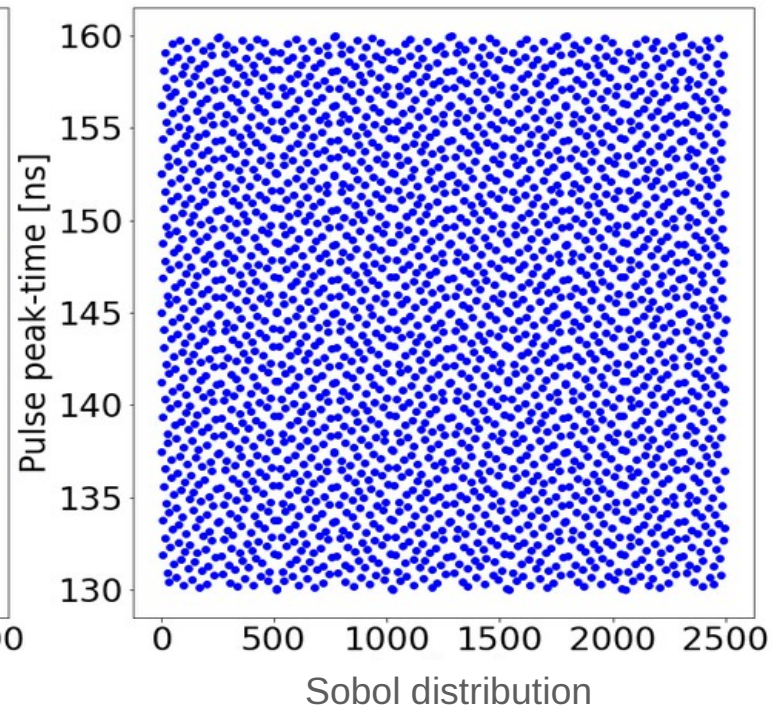
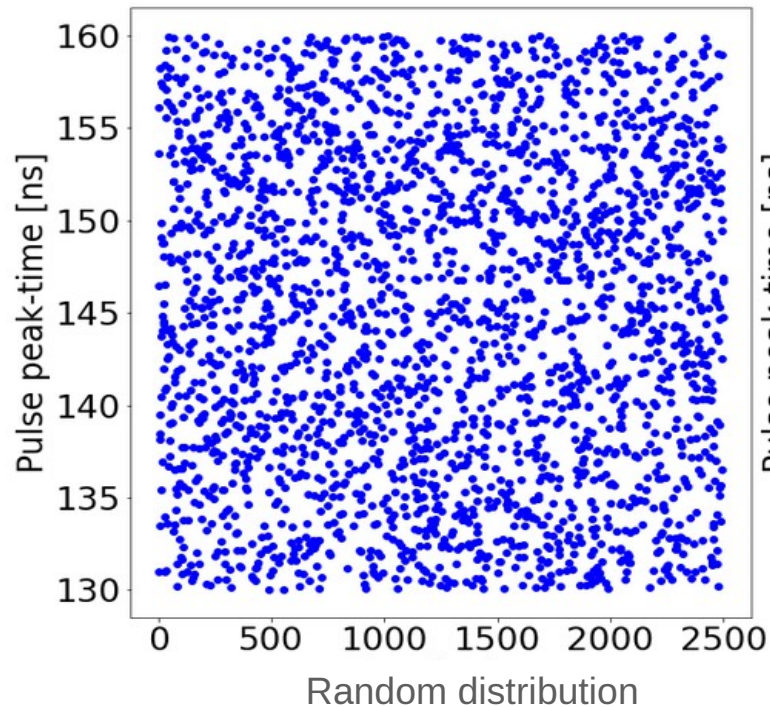
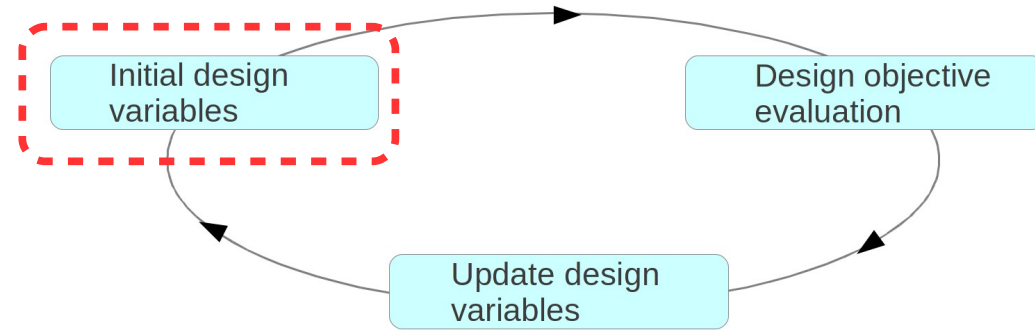
Design parameters:

- Injection coordinates
- Magnetic field strength
- Correction coil features
- Weak-focusing coil features
- Kicker pulse features
-



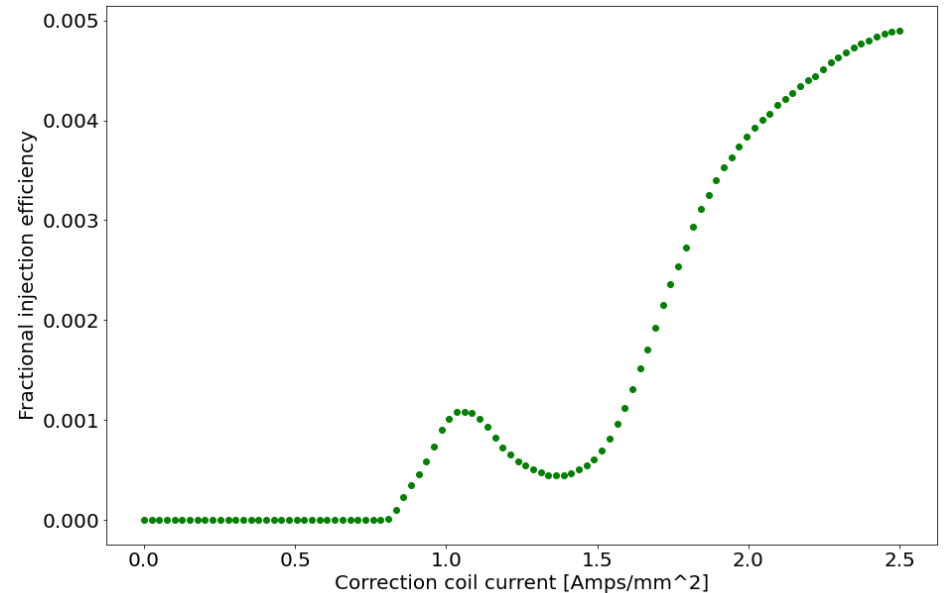
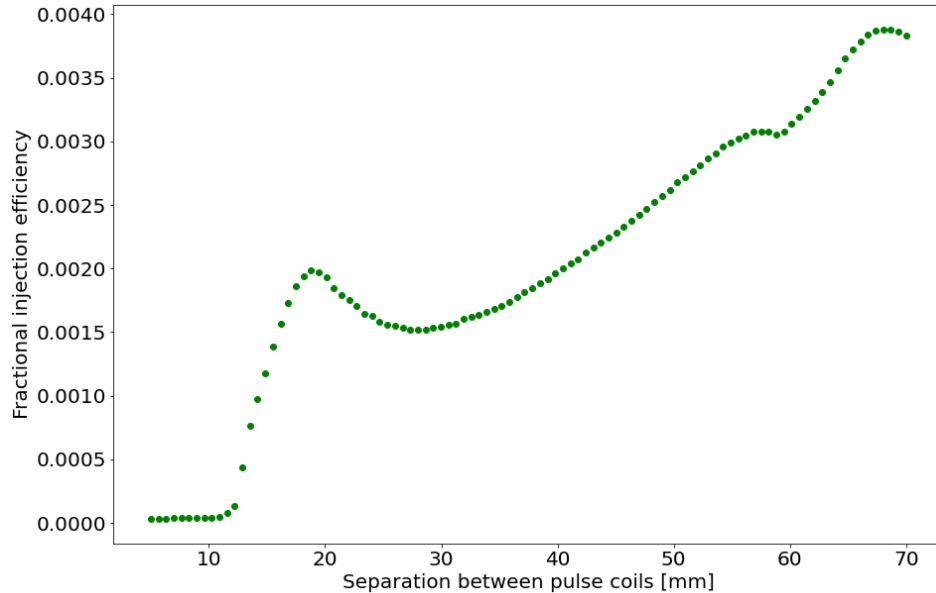
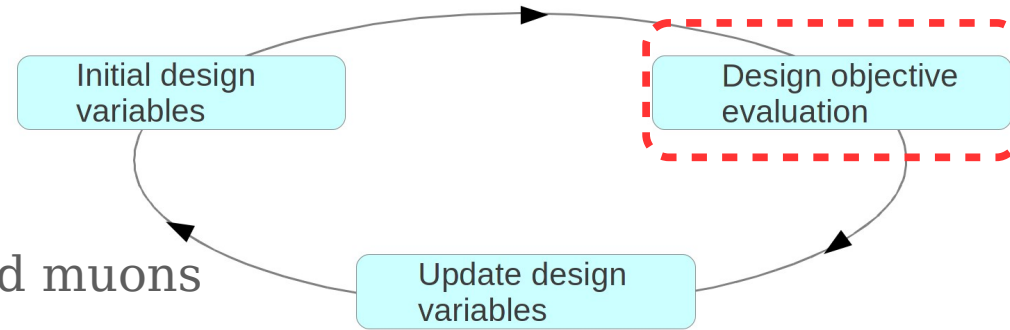
Design Optimization Layout

- Sampling input variables
- Sobol distribution (*Sobol, 1967*)
- Maximum uniform spread



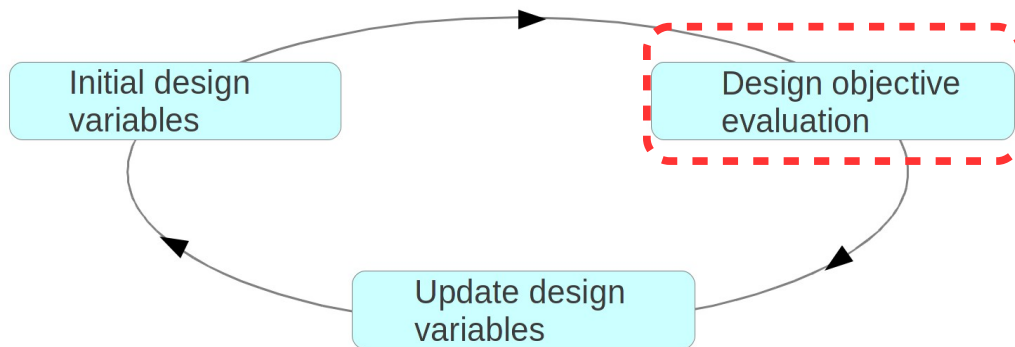
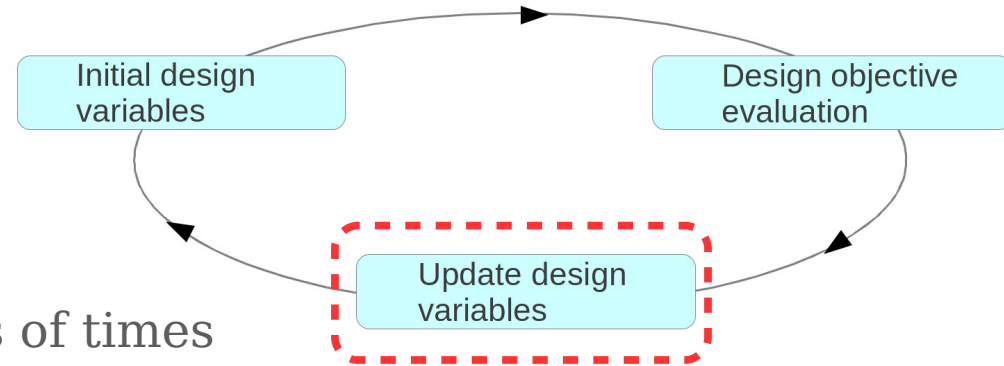
Design Optimization Layout

- Maximize injection efficiency
- Minimize power dissipation of setup
- Minimize polarization spread in stored muons
-



Design Optimization Layout

- Update design variables based on objective evaluation
- Repeat until optimal solution found
- Required to run simulation thousands of times → computationally expensive
- Replace physics simulation with approximation → surrogate model



Surrogate model for objective evaluation
→ Many ways
→ PCE and NN models explored

PCE Surrogate Model

- Polynomial Chaos Expansion (PCE) :

$$Y = \sum_{i=0}^{\infty} \alpha_i \Psi_i (\vec{x})$$

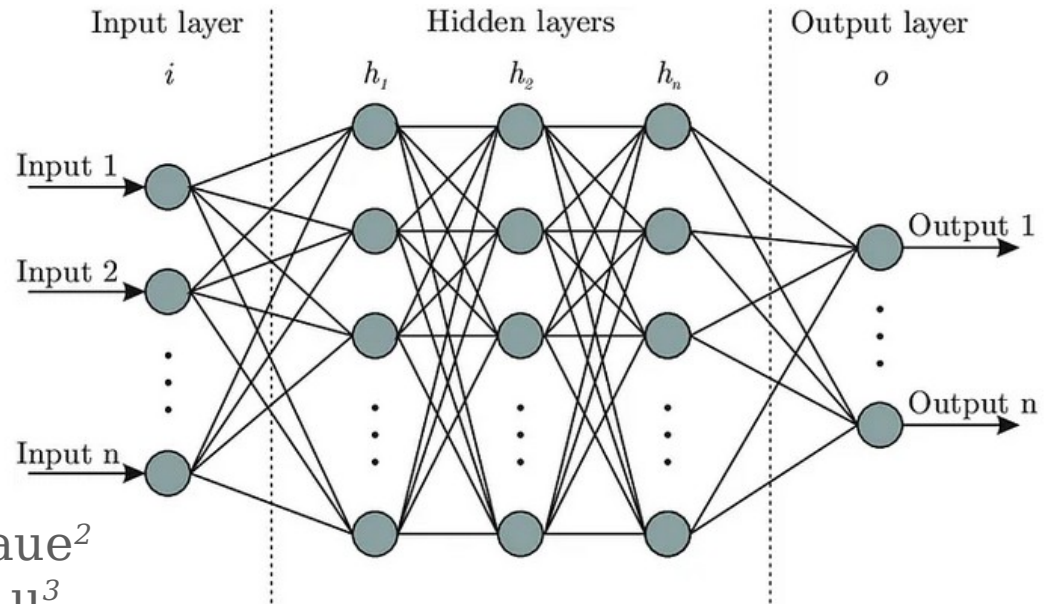
Y → Model response (injection efficiency), Ψ_i → Orthogonal polynomials
 x → input variables, α_i → expansion coefficients

- Polynomial basis based on input variable distribution
- Coefficients determined using regression based methods

$$\vec{\alpha} = \text{Argmin} \frac{1}{N} \sum_{j=1}^N \left\{ f(\vec{\xi}^j) - \sum_{i=0}^{P-1} \alpha_i \Psi_i (\vec{x}^j) \right\}^2$$

NN Surrogate Model

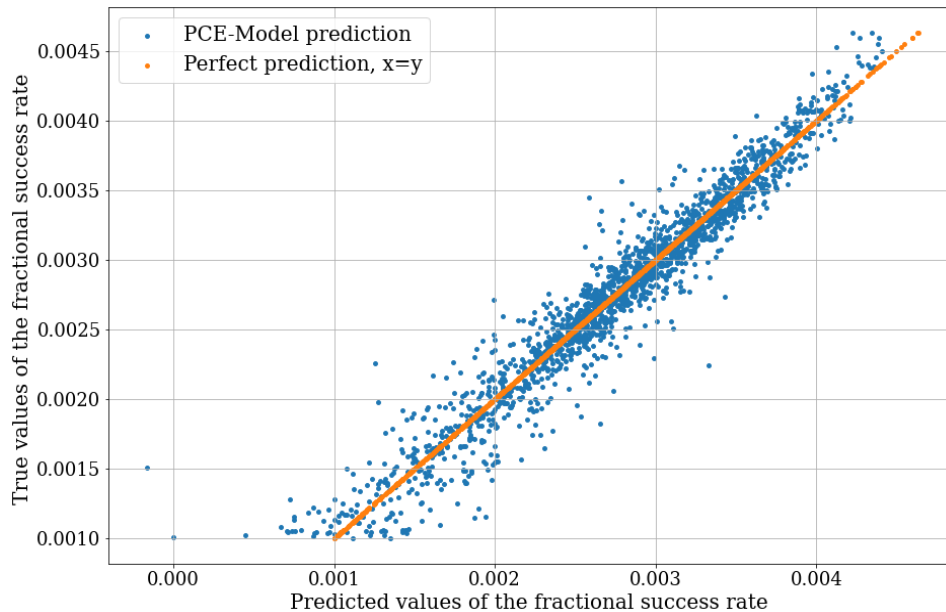
- Use the input (design) and output (objective) to train a neural network
- Hyper parameters:
 - no. of hidden layers = 8
 - no. of neurons/layer = 500
 - learning rate = 0.001
 - optimizer: Adam¹
 - scheduler: ReduceLROnPlateau²
 - activation function: LeakyReLU³



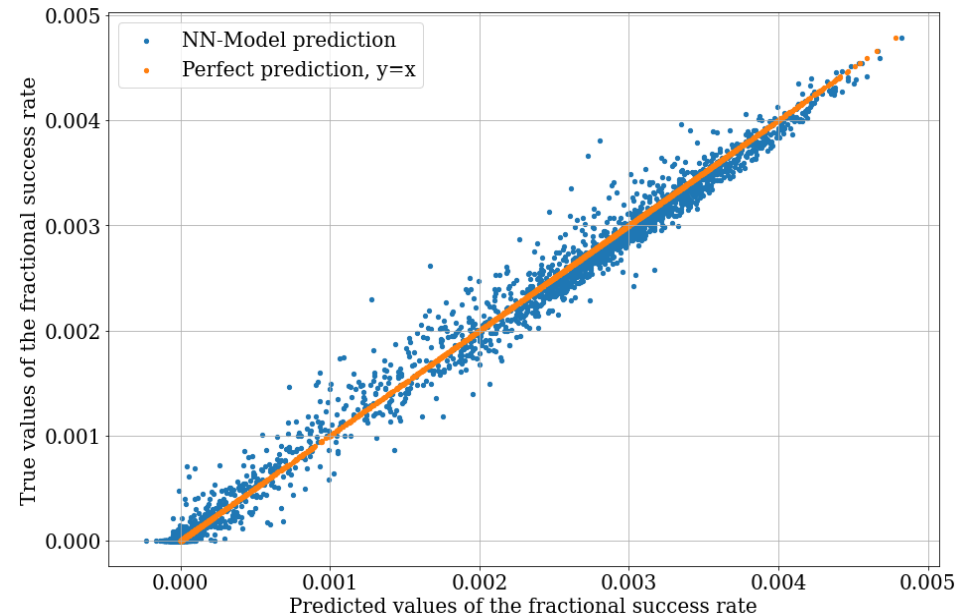
¹ Kingma and Ba, 2014 ² Maas, 2013 ³ K Developers, 2019

Surrogate Model Performance

Model performance for a 6 dimensional input space
(Kicker timing, Kicker strength, Corr coil position, Corr coil length, Corr coil thickness and Corr coil radius)

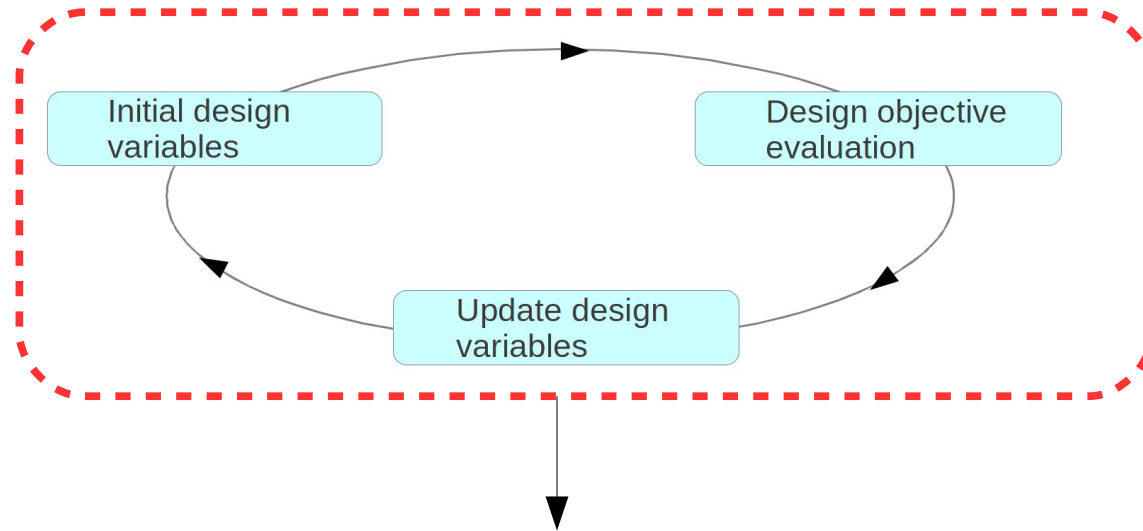


PCE Mean Square Error: $3.47 \text{ e-}08$



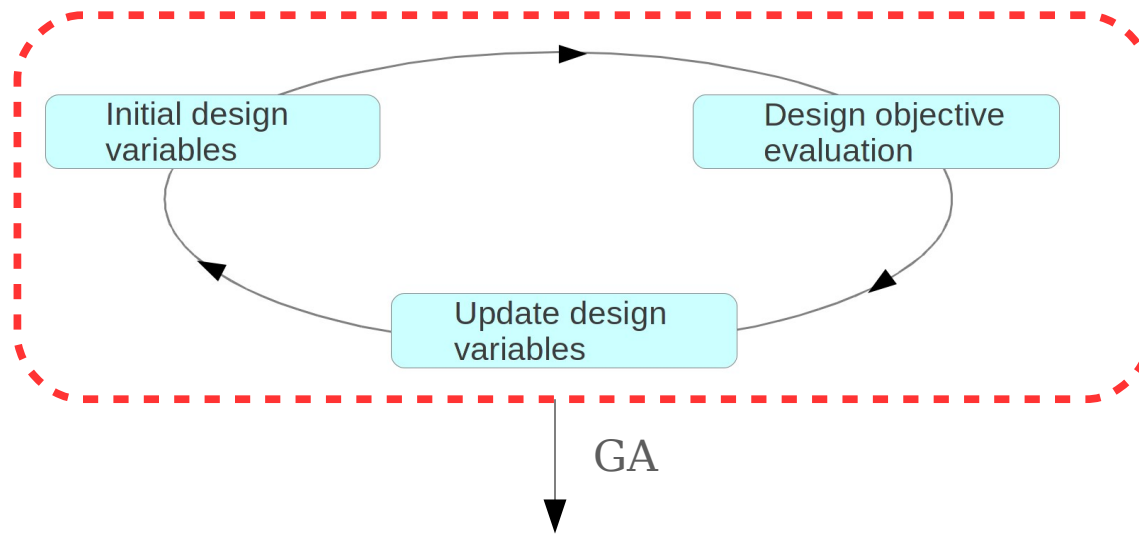
NN Mean Square Error: $1.88 \text{ e-}08$

Multi-objective Optimization



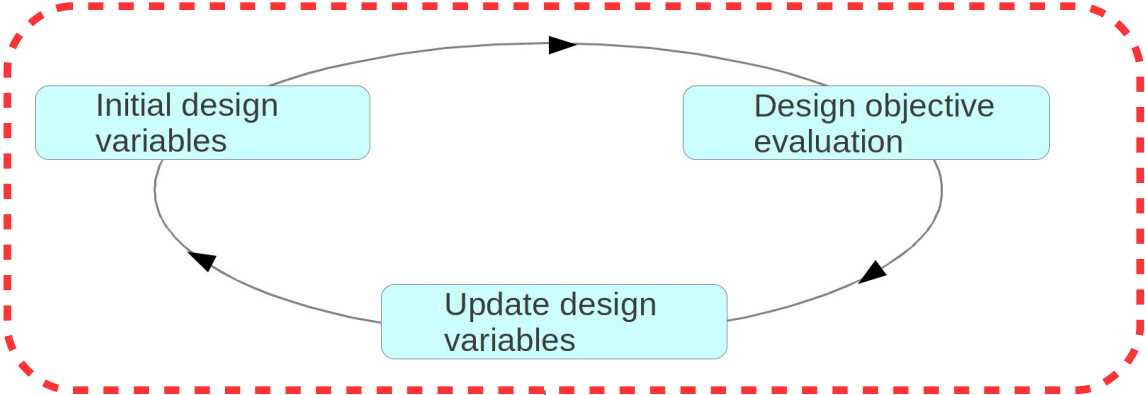
Genetic Algorithms (GA)

Genetic Algorithm

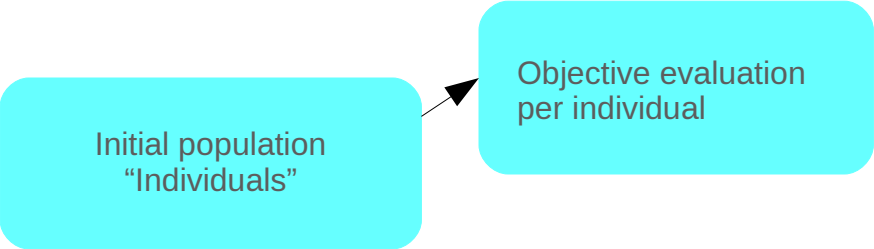


Initial population
"Individuals"

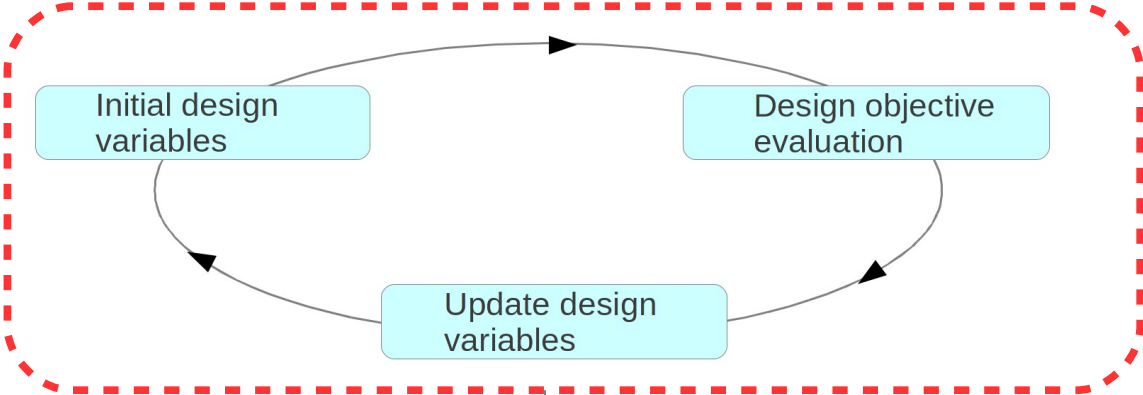
Genetic Algorithm



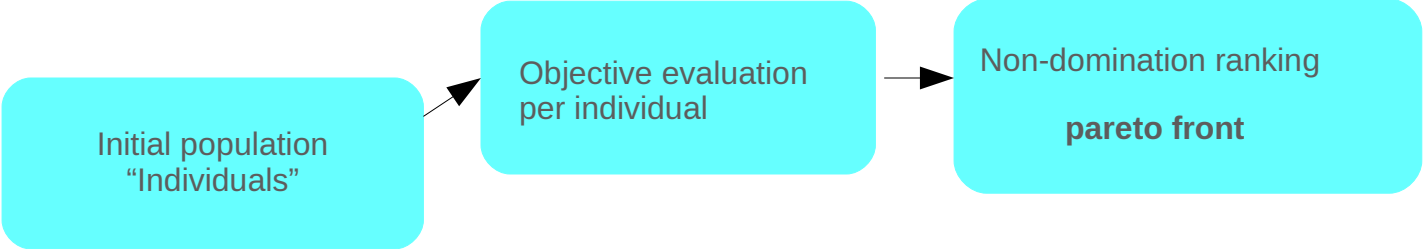
GA



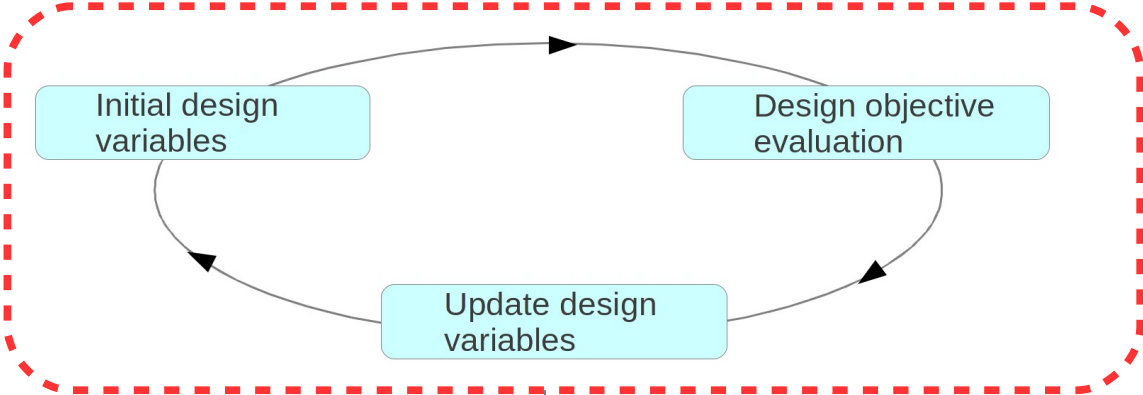
Genetic Algorithm



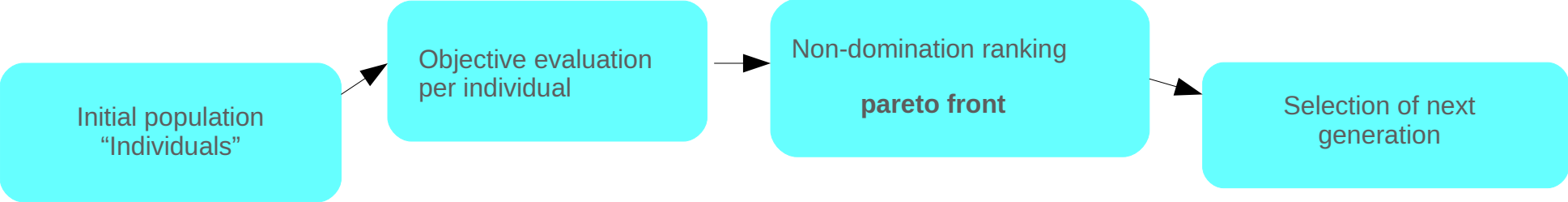
GA



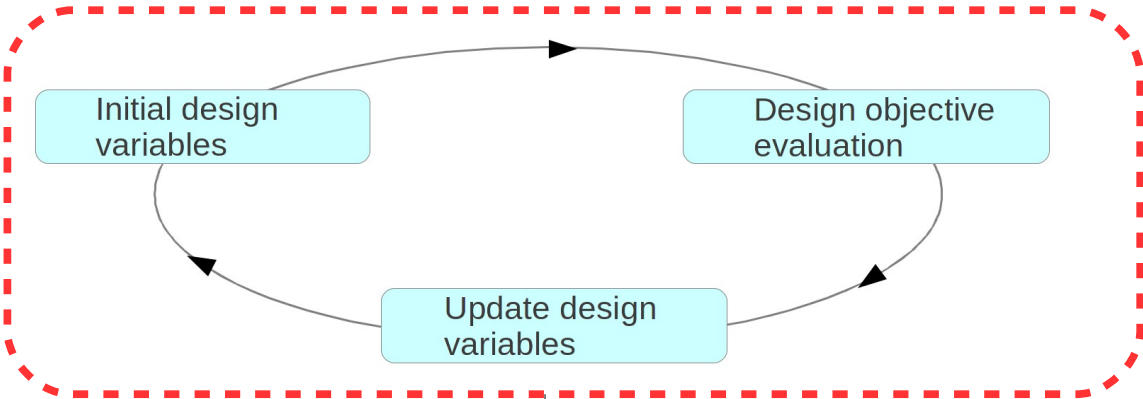
Genetic Algorithm



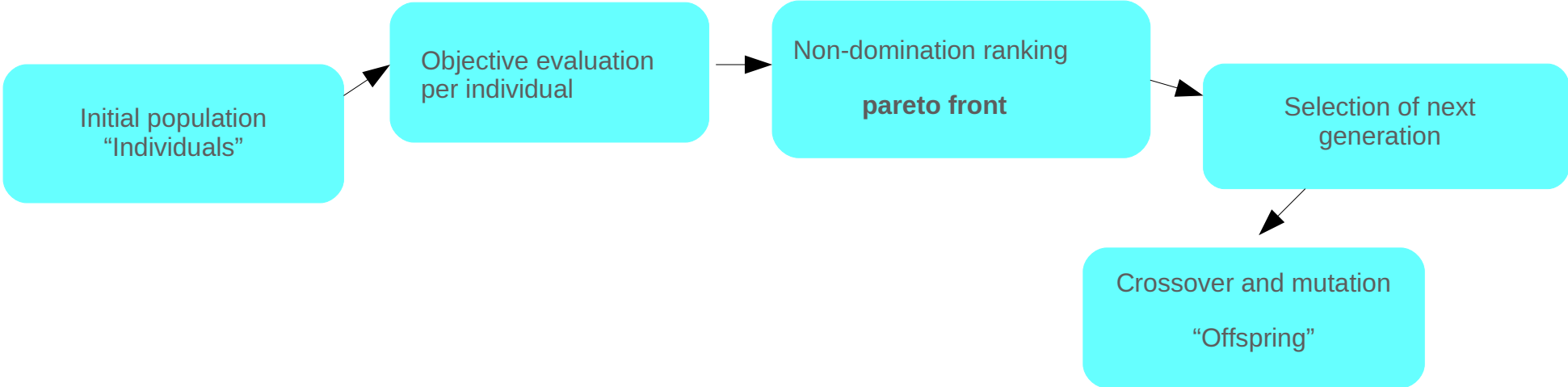
GA



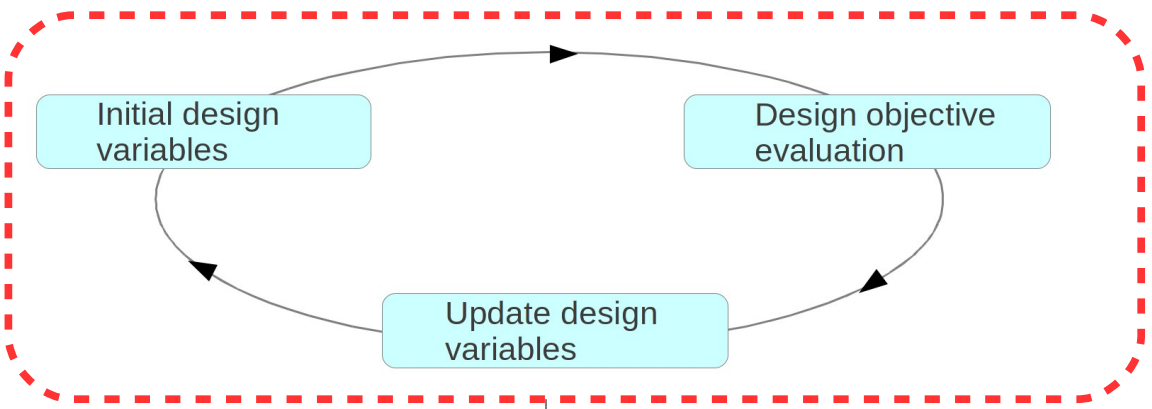
Genetic Algorithm



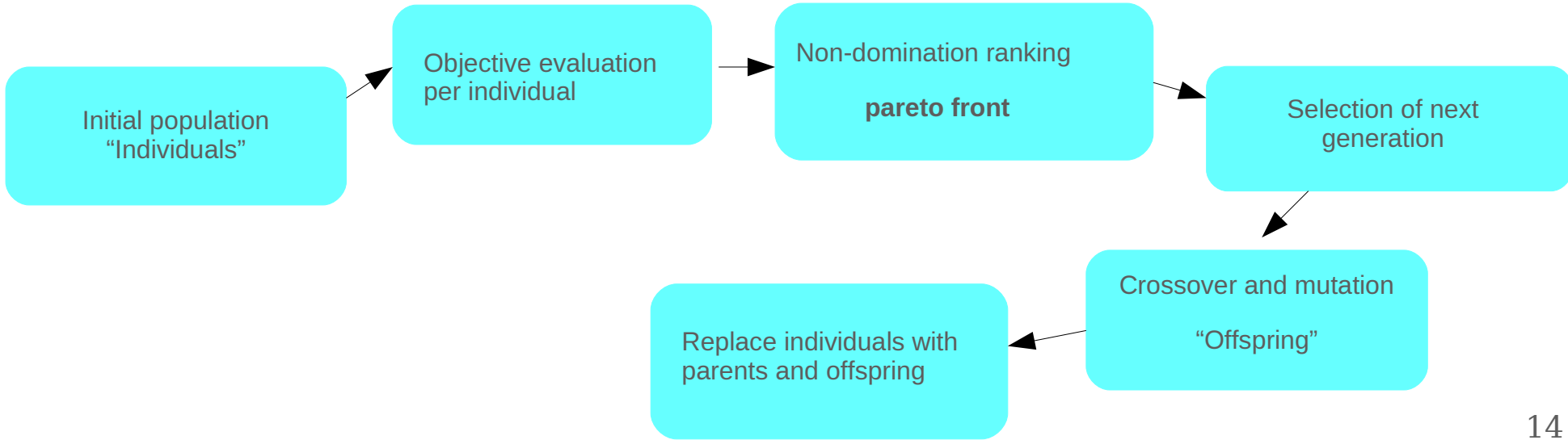
GA



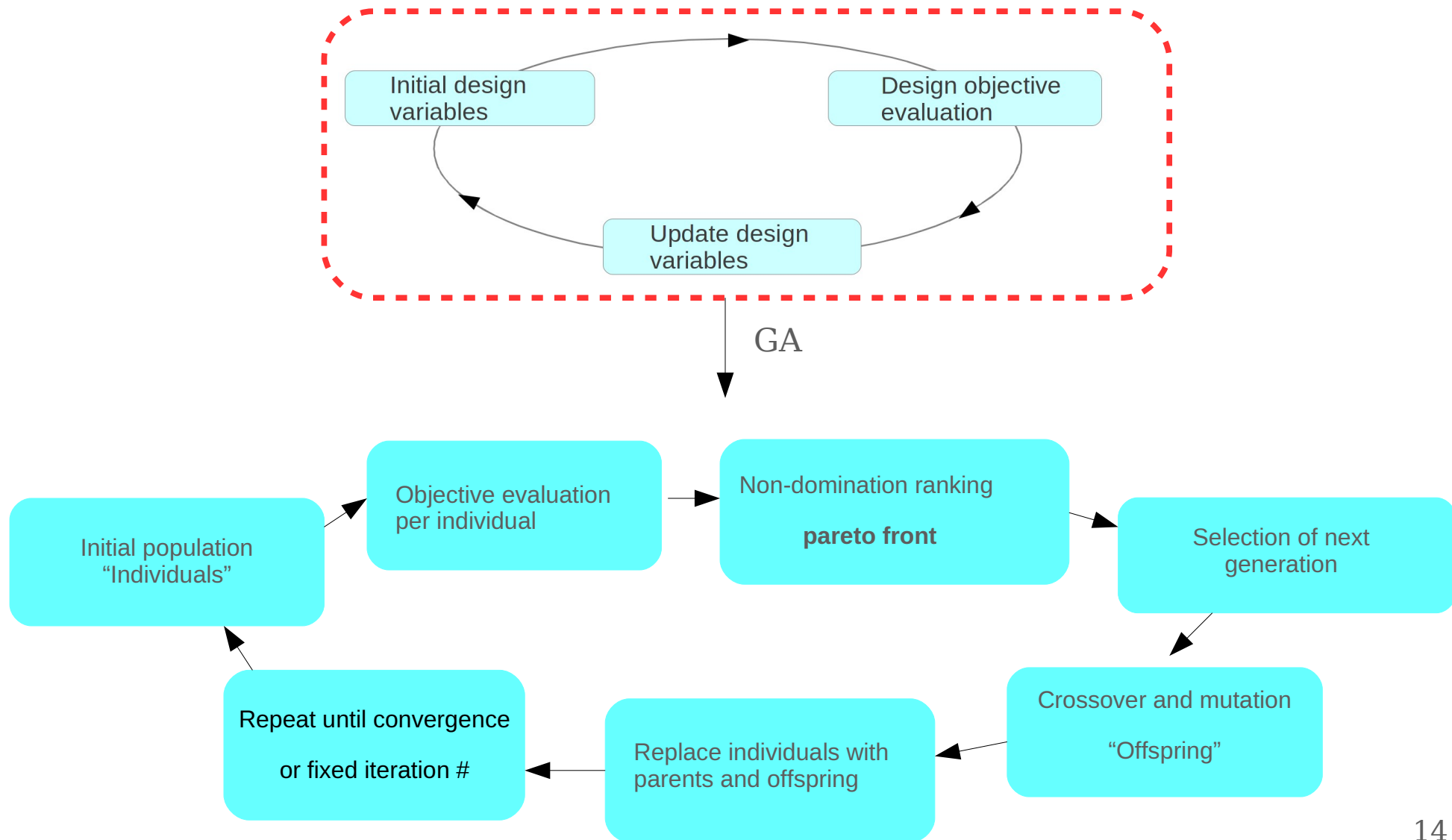
Genetic Algorithm



GA

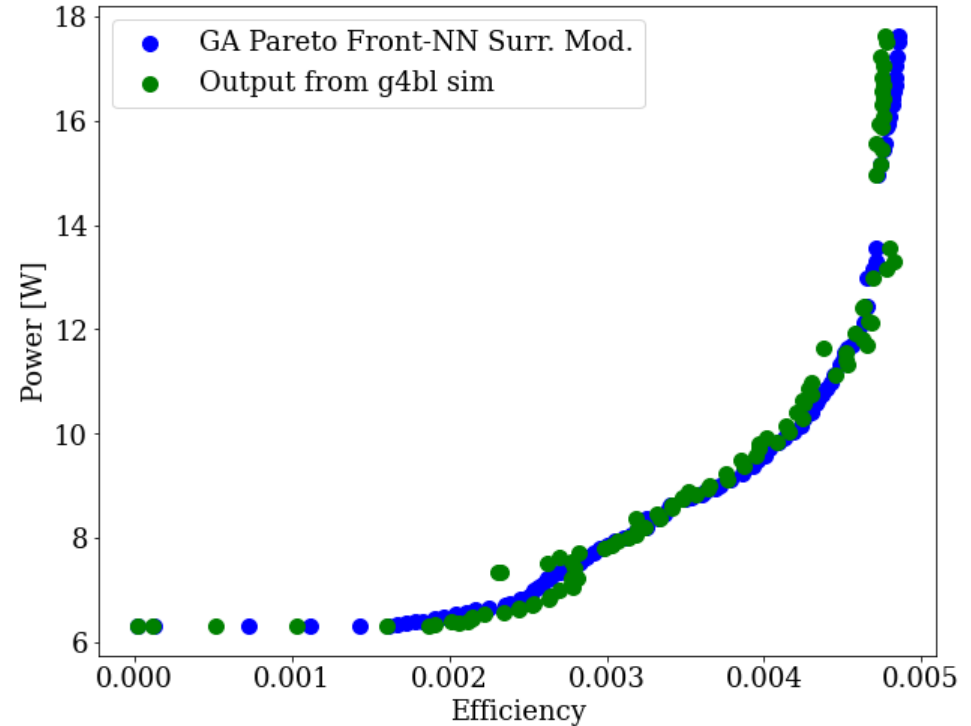
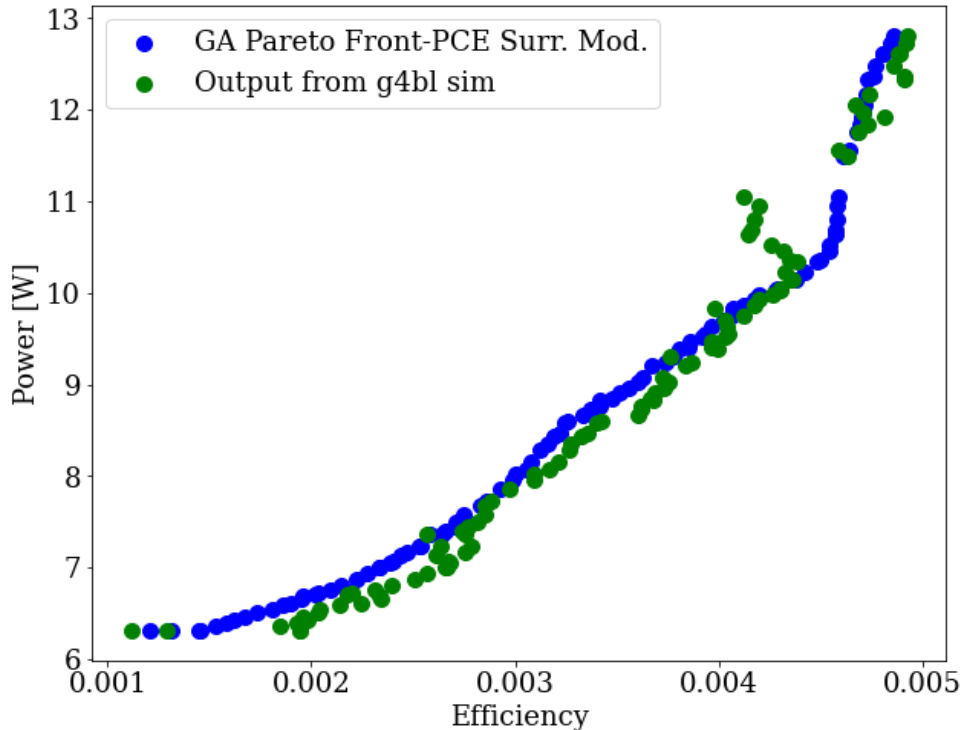


Genetic Algorithm



Surrogate model based NSGA-II¹ performance

Optimization to maximize Injection Efficiency/minimize Power Dissipation



- 10^3 speed up for PCE Surr and 10^4 speed up for NN Surr
- Agreement within 5% vs 2% for PCE/NN based GA performance for average injection efficiency of 0.35%

Summary

- PSI muEDM experiment will be most precise muon EDM measurement to date → setup needs to be carefully optimized
- Running simulations iteratively is bottleneck in optimization process
- Orders of magnitude speed up can be achieved by replacing physics simulation by surrogate model
- Genetic algorithm NSGA-II used to run multi-objective optimization
- PCE and NN surrogate models based GA investigated; $\sim 10^3$ speed up for PCE, $\sim 10^4$ for NN
- Plan to expand into Bayesian optimization where higher dimensional input space can be implemented with straightforward uncertainty quantification techniques

Acknowledgments



The muEDM Collaboration
(Spring meeting 2024)

- Computational resources: PSI Local High Performance Computing cluster, Merlin6, Siyuan-1 cluster supported by the Center for High Performance Computing at Shanghai Jiao Tong University and the Euler cluster operated by the High Performance Computing group at ETH Zürich.
- Accelerator Modeling and Advanced Simulations (AMAS) group at PSI: A. Adelman, S. Heinekamp and P. Juknevičius
- NN surrogate starting point: A. Holmberg Bachelor's Thesis ETH Zurich 2021

Project funded by



Schweizerische Eidgenossenschaft
Confédération suisse
Confederazione Svizzera
Confederaziun svizra

Swiss Confederation

Federal Department of Economic Affairs,
Education and Research EAER
**State Secretariat for Education,
Research and Innovation SERI**

Extra

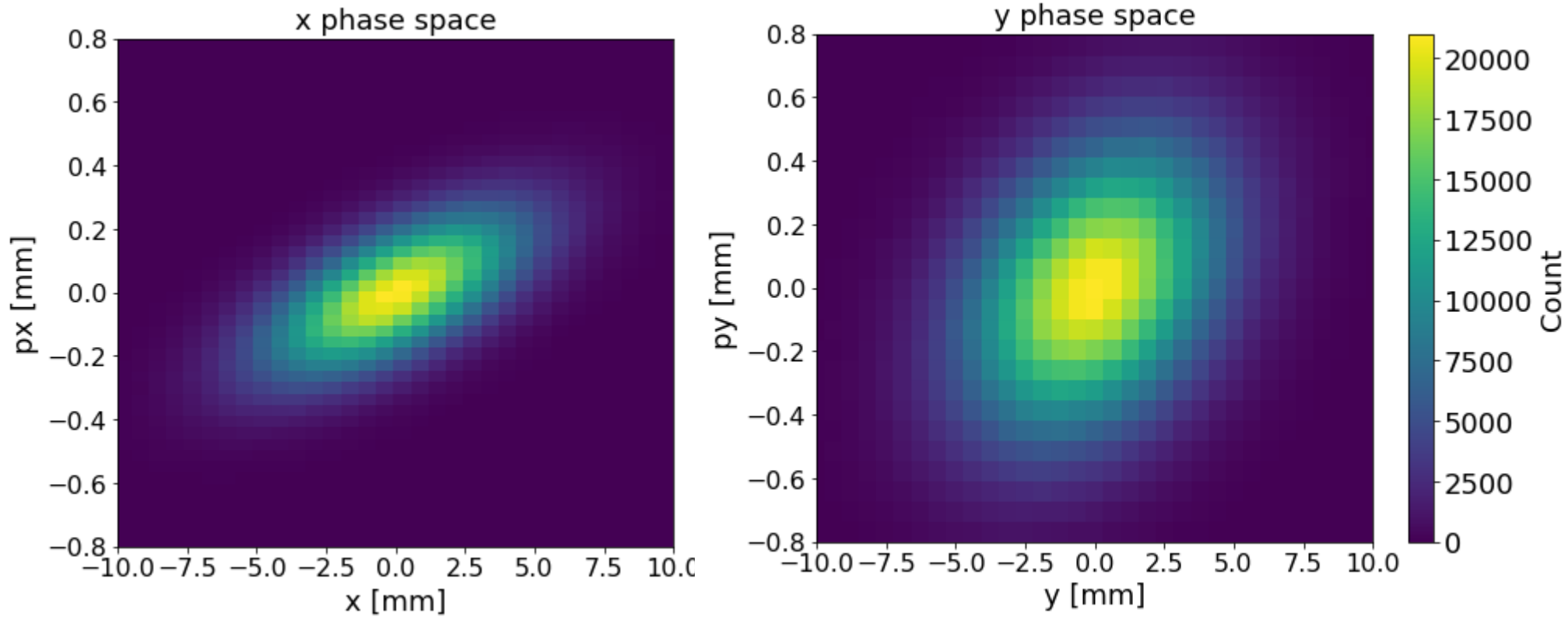
Polynomial Chaos Orthogonal Basis

The correspondence of the types of Wiener–Askey polynomial chaos and their underlying random variables ($N \geq 0$ is a finite integer).

	Random variables ζ	Wiener–Askey chaos $\{\Phi(\zeta)\}$	Support
Continuous	Gaussian gamma beta uniform	Hermite-chaos Laguerre-chaos Jacobi-chaos Legendre-chaos	$(-\infty, \infty)$ $[0, \infty)$ $[a, b]$ $[a, b]$
Discrete	Poisson binomial negative binomial hypergeometric	Charlier-chaos Krawtchouk-chaos Meixner-chaos Hahn-chaos	$\{0, 1, 2, \dots\}$ $\{0, 1, \dots, N\}$ $\{0, 1, 2, \dots\}$ $\{0, 1, \dots, N\}$

(Xiu and Karniadakis, 2002)

Total phase space after collimation



Neural Net hyperparameters

```
def __init__(self, input_dimension, output_dimension, n_hidden_layers,
             neurons, regularization_param, regularization_exp):
    super(net, self).__init__()
    # Number of input dimensions n
    self.input_dimension = input_dimension
    # Number of output dimensions m
    self.output_dimension = output_dimension
    # Number of neurons per layer
    self.neurons = neurons
    # Number of hidden layers
    self.n_hidden_layers = n_hidden_layers
    # Activation function
    self.activation = nn.LeakyReLU()
    #
    self.regularization_param = regularization_param
    #
    self.regularization_exp = regularization_exp

    self.input_layer = nn.Linear(self.input_dimension, self.neurons)
    self.hidden_layers = nn.ModuleList([nn.Linear(self.neurons, self.neurons) for _ in range(n_hidden_layers)])
    self.output_layer = nn.Linear(self.neurons, self.output_dimension)

    self.dropout = nn.Dropout(0.1)
```

```
# Model definition
my_network = net(input_dimension=x_train_norm.shape[1], output_dimension=y_train_norm.shape[1],
                 n_hidden_layers=8, neurons=512, regularization_param=0,
                 regularization_exp=0) #2 1e-5

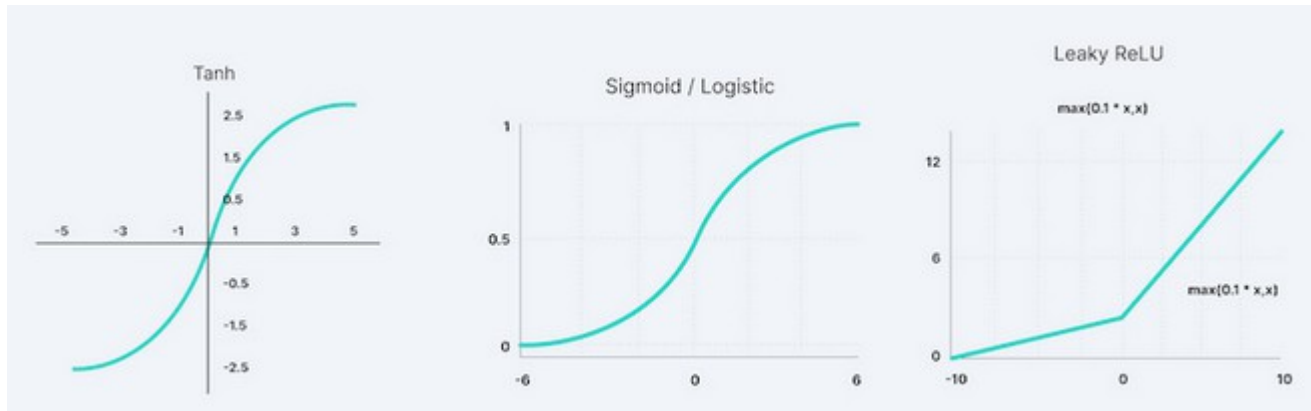
# Random Seed for weight initialization
retrain = 134
# Xavier weight initialization
init_xavier(my_network, retrain)

optimizer_ = optim.Adam(my_network.parameters(), lr=1e-3)#, weight_decay=1e-5)
#optimizer_ = optim.LBFGS(my_network.parameters(), lr=0.1, max_iter=1,
#                          max_eval=50000, tolerance_change=1.0 * np.finfo(float).eps)

scheduler = optim.lr_scheduler.ReduceLROnPlateau(optimizer_, mode='min', factor=0.5, patience=500000)
#scheduler = optim.lr_scheduler.StepLR(optimizer=optimizer_, step_size=50, gamma=0.5)

n_epochs = 200
```

Neural Net activation function



6-d optimization parameter bounds

```
bounds = {"T_Offset": [80, 98],  
         "BPI": [0.35, 0.80],  
         "CC_Len": [88, 150],  
         "CC_Ir": [40, 84],  
         "CC_Thick": [7, 15],  
         "CC_Pos": [166, 241]}
```