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pop-cosmos:

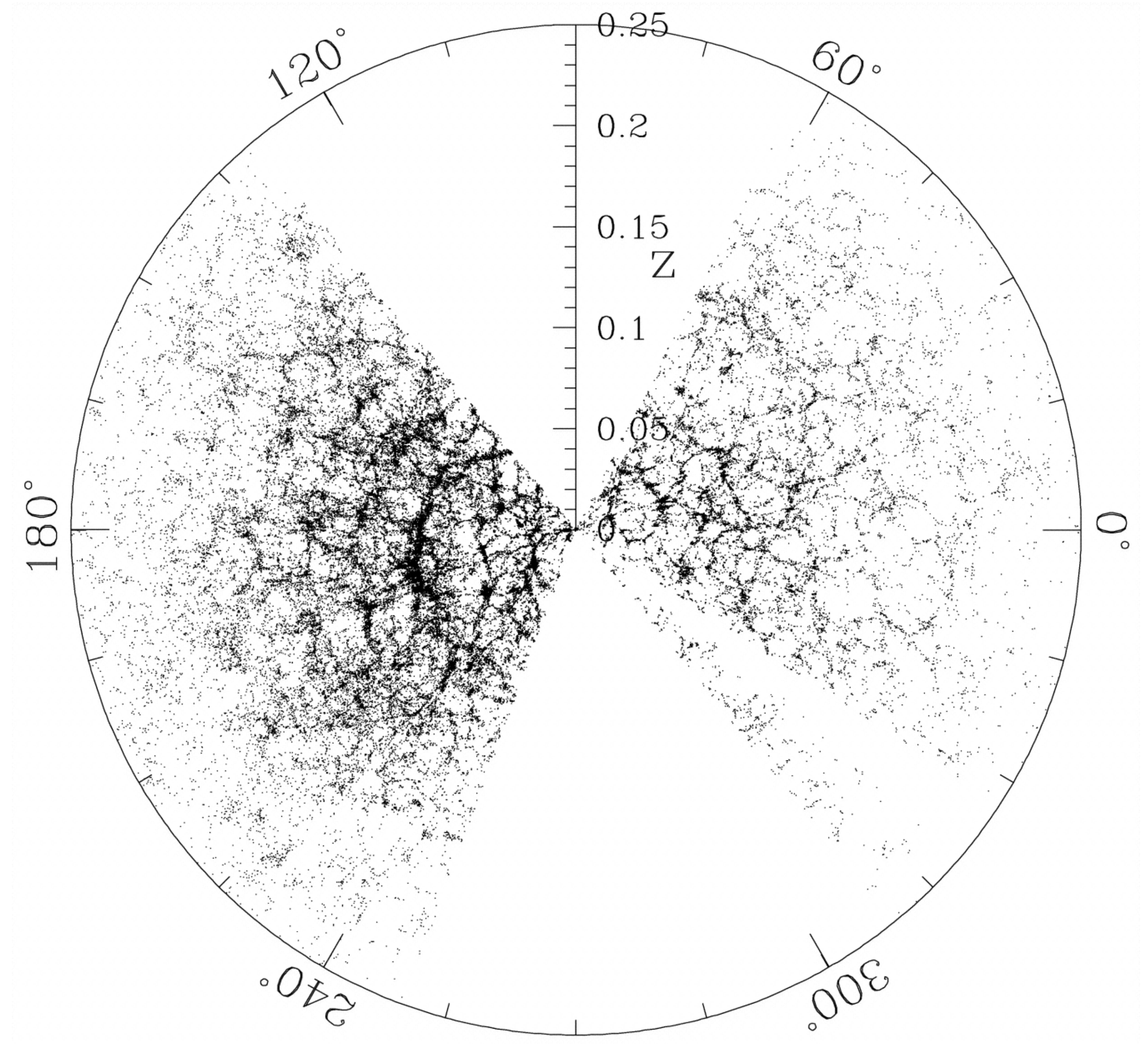
Comprehensive forward modelling of photometric galaxy surveys

Stephen Thorp, Justin Alsing, Sinan Deger, Hiranya Peiris,
Boris Leistedt, Daniel Mortlock, Joel Leja, Arthur Loureiro



Large Scale Structure Cosmology

- Map the matter distribution in the universe using spectra or photometry of galaxies
- Galaxy clustering (positions), or weak lensing (shapes) sensitive to cosmological parameters
- But... need redshifts

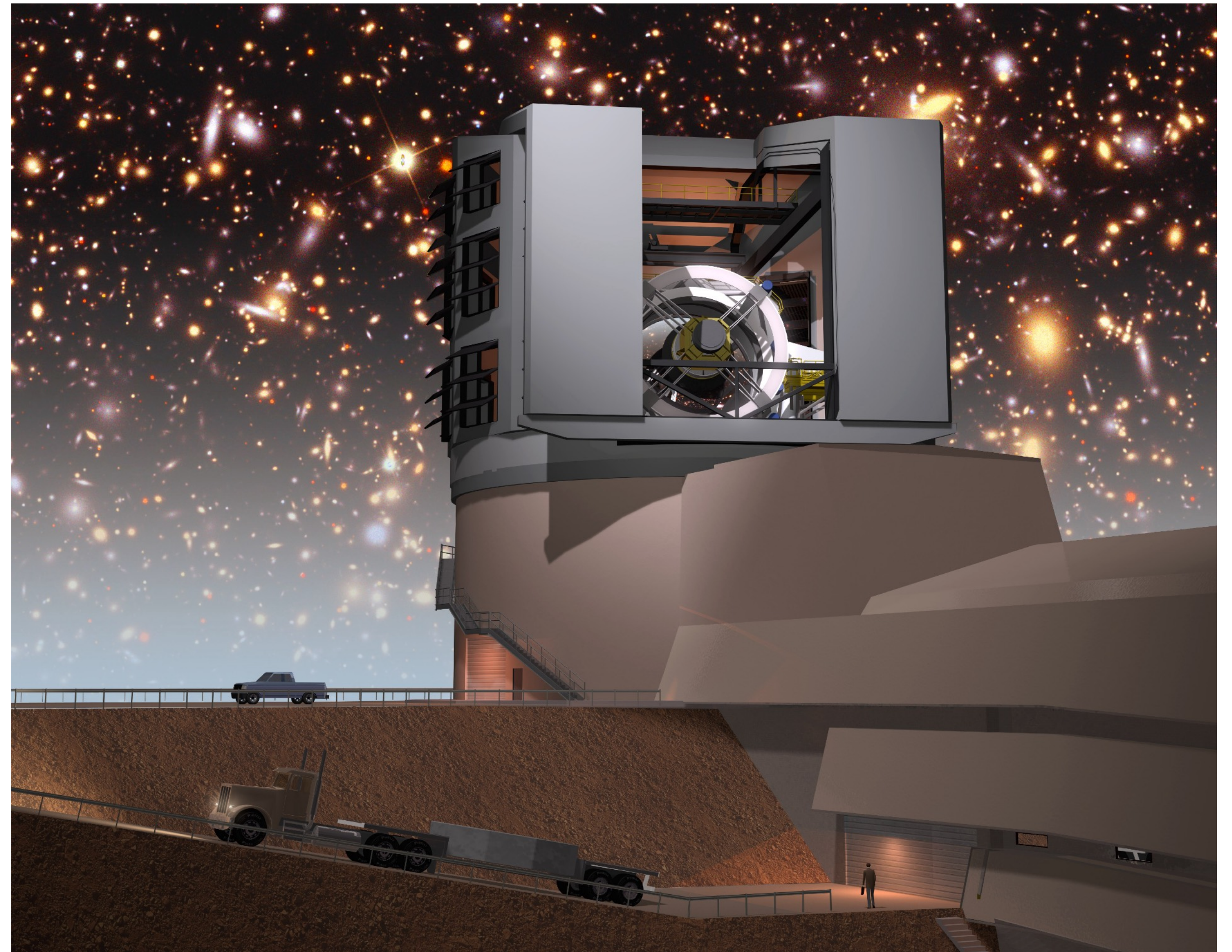


SDSS: *Blanton et al. (2003)*

Coming Soon...

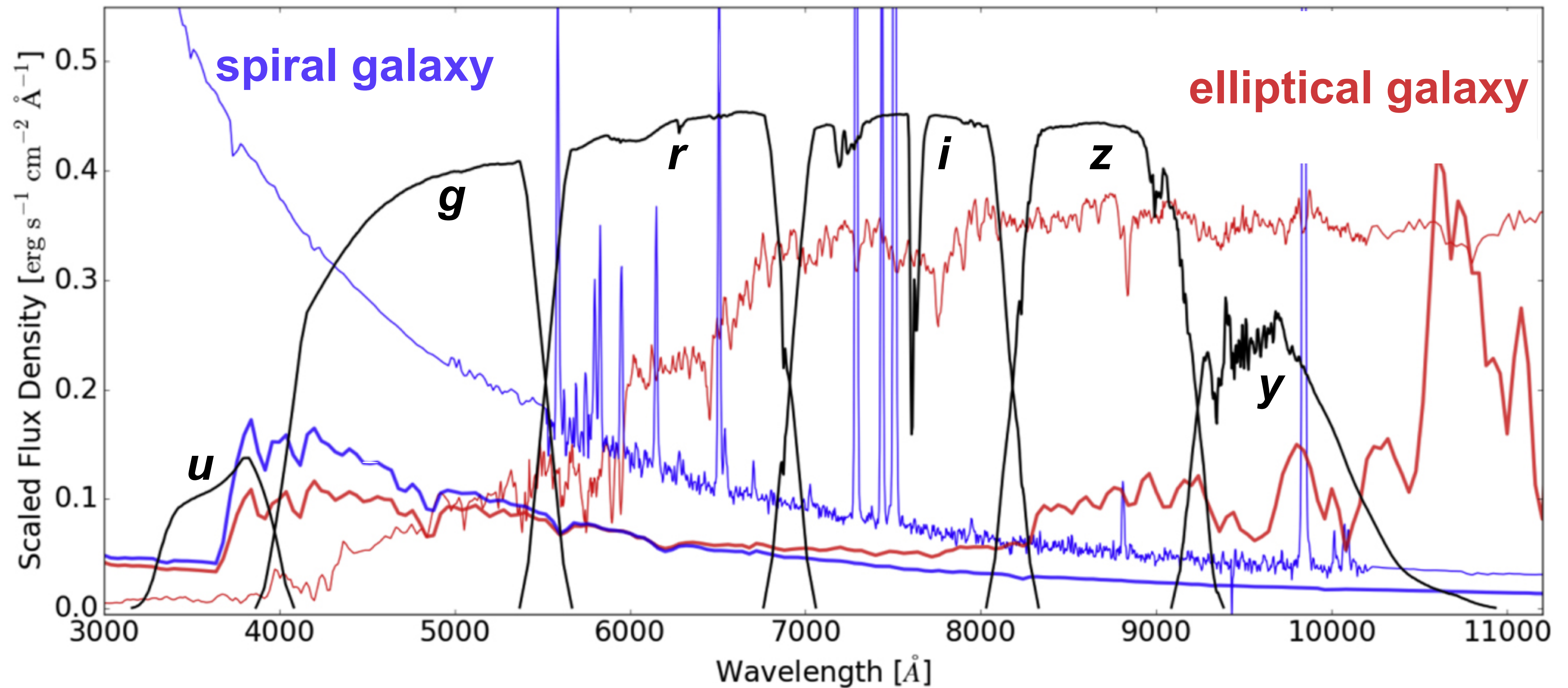


- 18,000 deg²
- Deep imaging in *ugrizy*
- 10 year LSST survey
- Single epoch: $r \lesssim 24$ mag;
10 year co-add: $r < 26.9$ mag
- Billions of galaxies: impossible to get spectra
- Need *photometric* redshifts



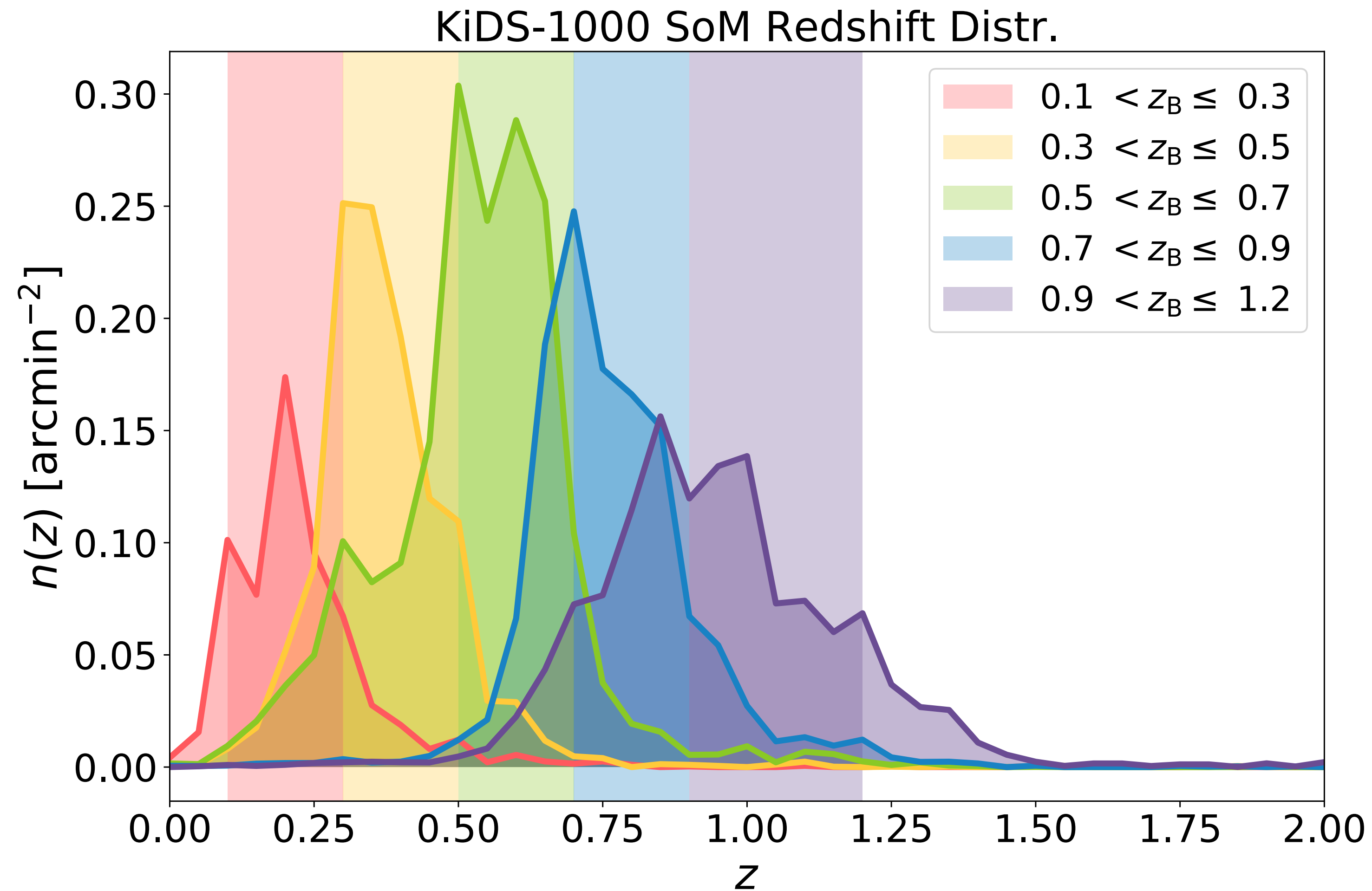
Credit: Rubin Observatory

Photometry

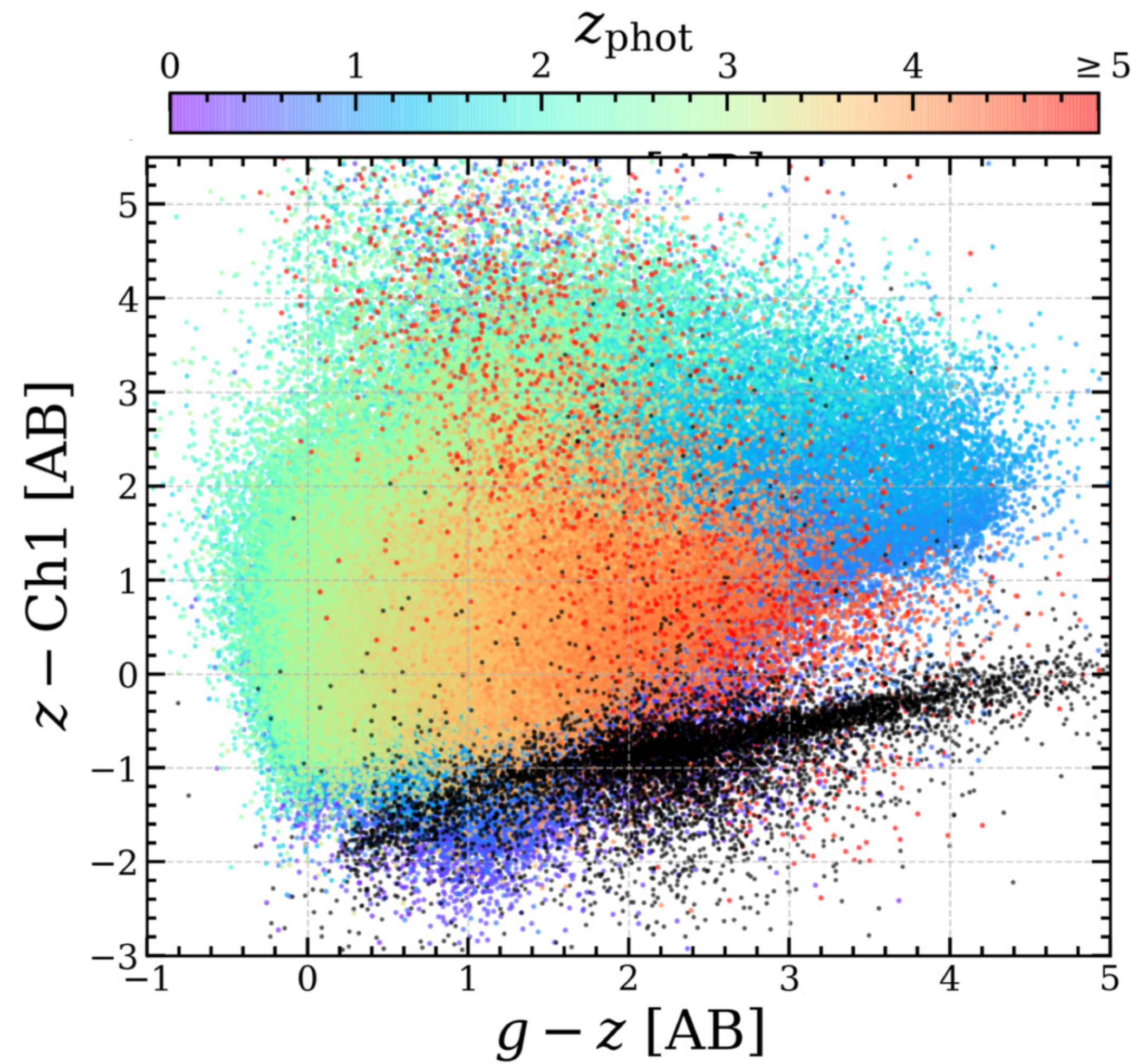


Photometric Redshifts

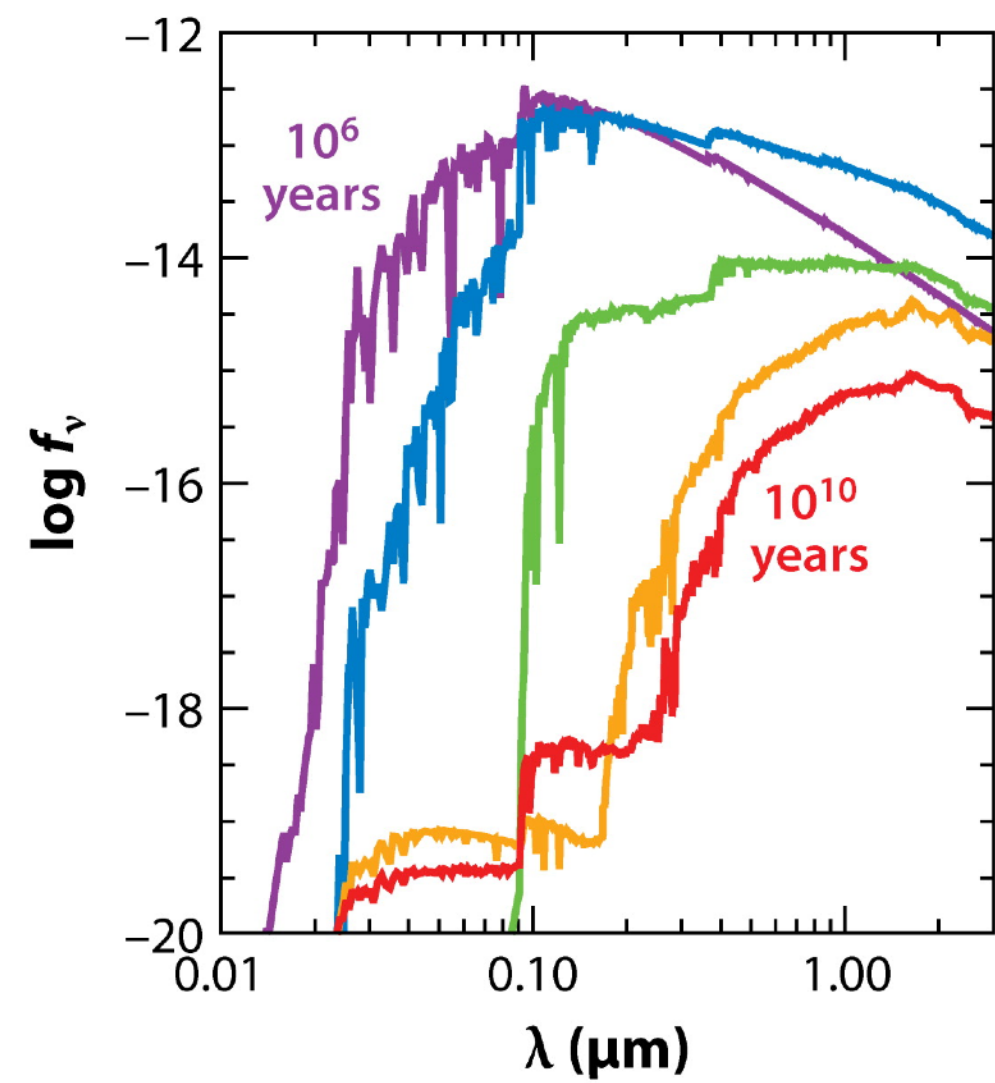
We need accurate characterisation of $n(z)$ in tomographic bins



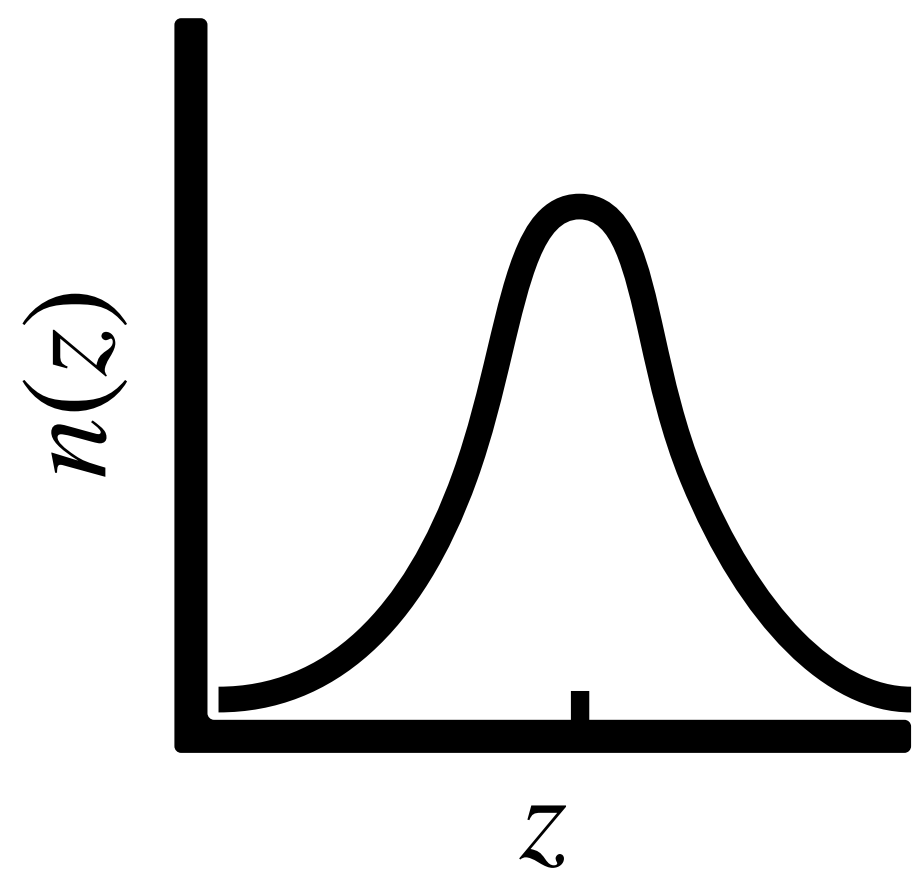
Forward Modelling a Photometric Catalog



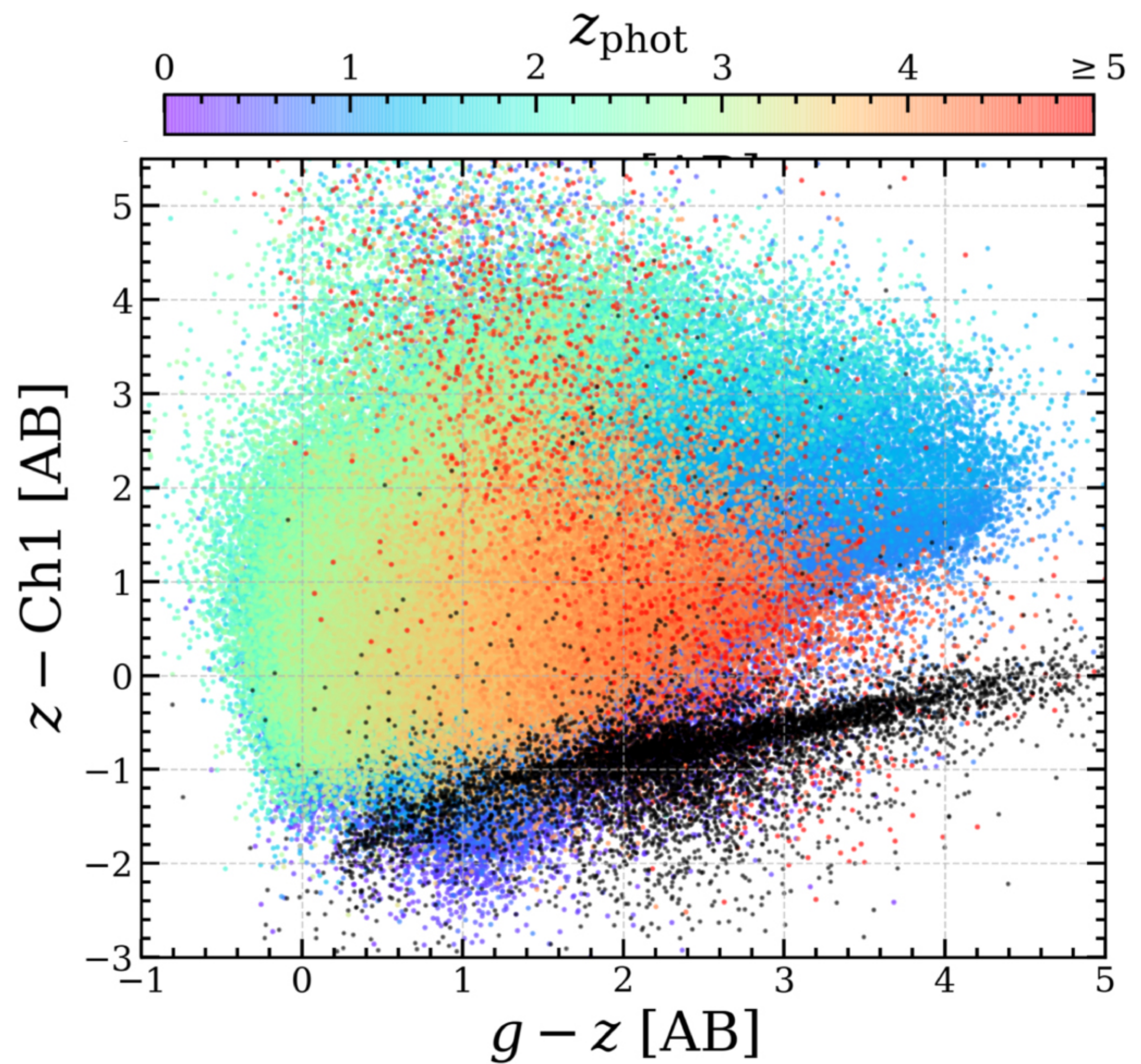
Forward Modelling a Photometric Catalog



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Forward Modelling a Photometric Catalog

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1. Draw from galaxy population distribution over physical properties and z

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Forward Modelling a Photometric Catalog

1. Draw from galaxy population distribution over physical properties and z
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4. Add noise based on the uncertainties
5. Apply selection

Forward Modelling a Photometric Catalog

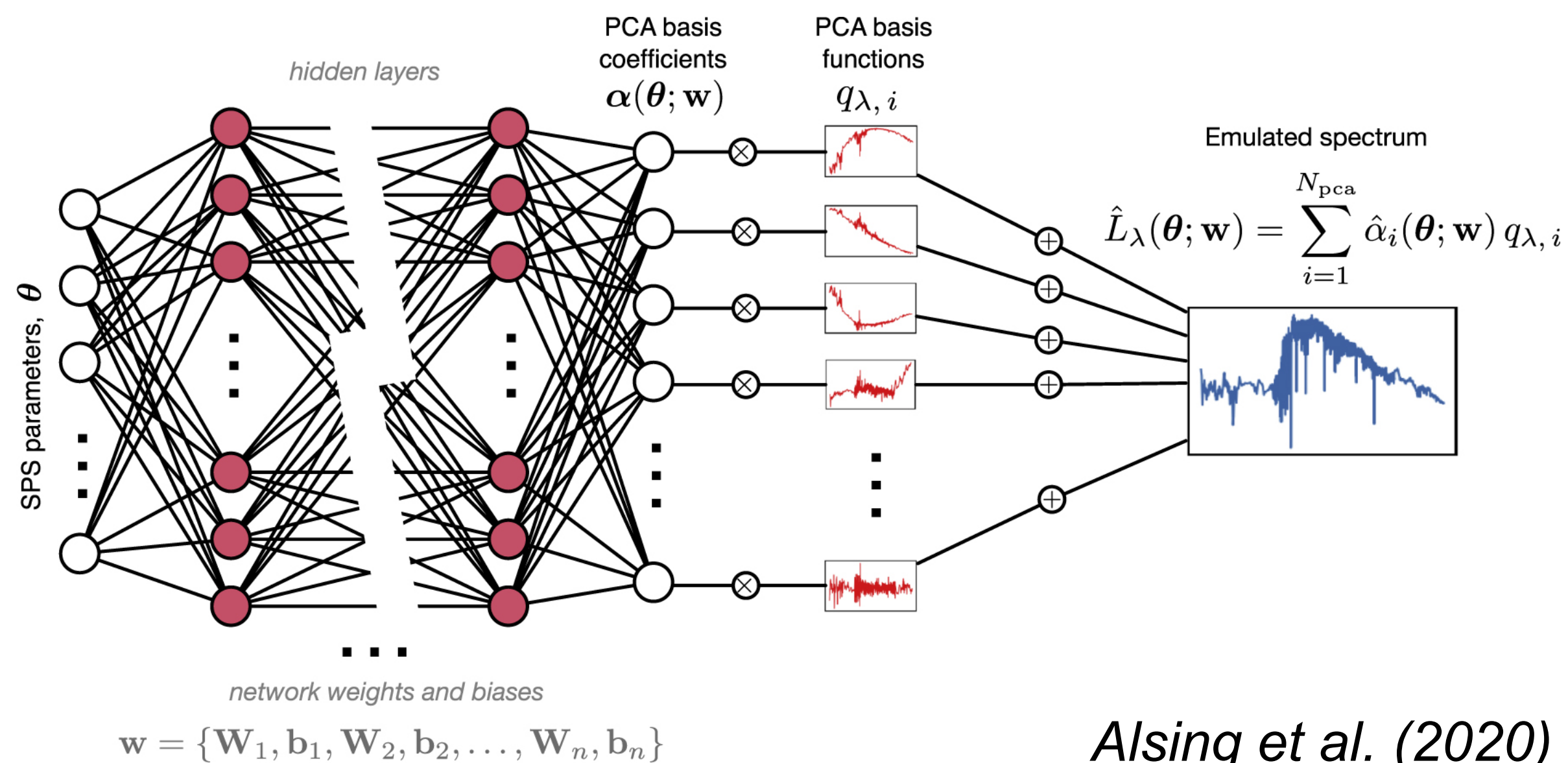
1. Draw from galaxy population distribution over physical properties and z
2. Compute fluxes via stellar population synthesis
3. Draw realistic uncertainties from an uncertainty model
4. Add noise based on the uncertainties
5. Apply selection
6. Compare model fluxes to data

pop-cosmos framework

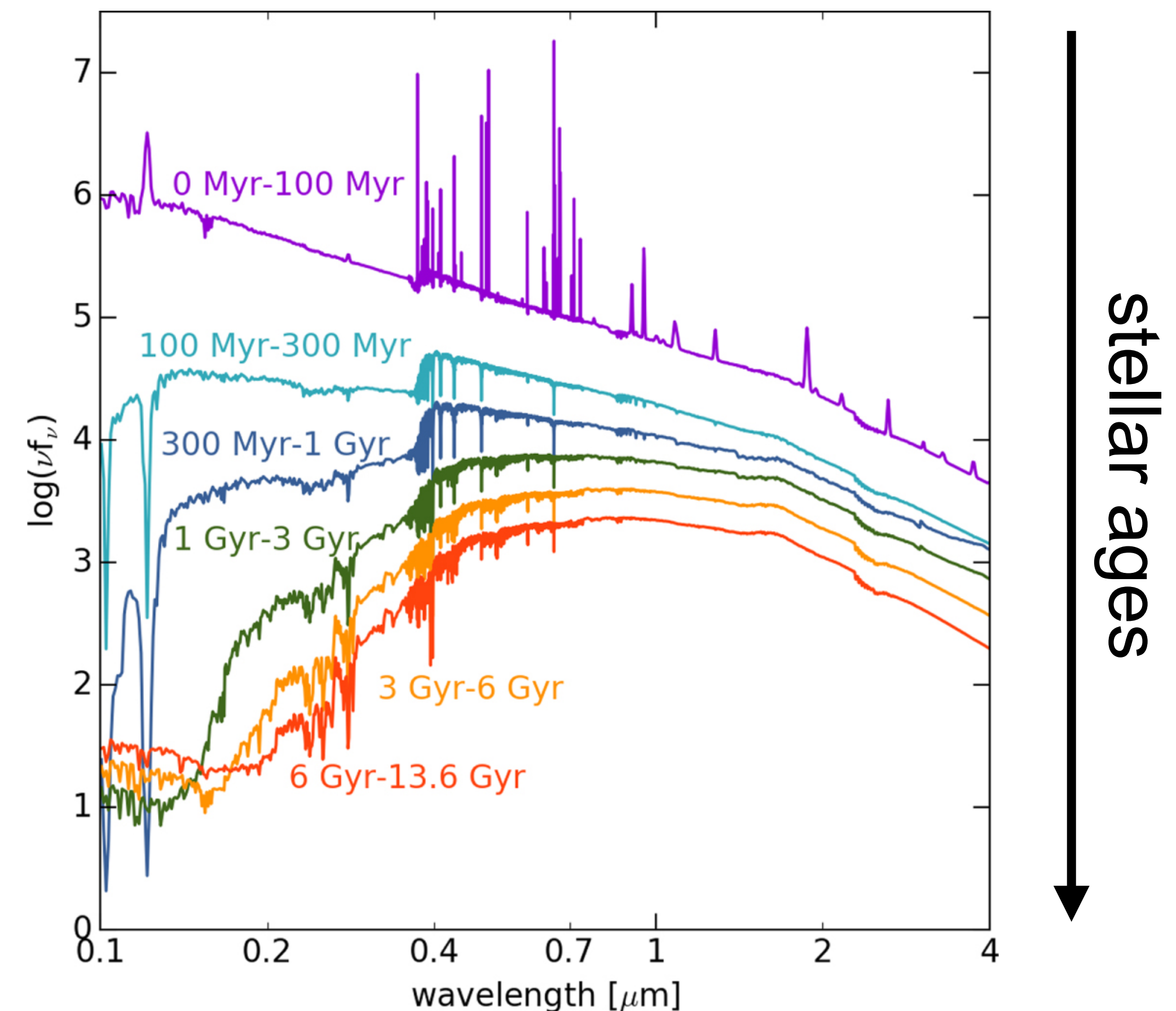
How do we represent a galaxy?

Stellar Population Synthesis (SPS)

- Builds galaxy SED from stars, gas, dust, etc.
- 16 parameters (\approx Prospector- α)
- Emulated with Speculator



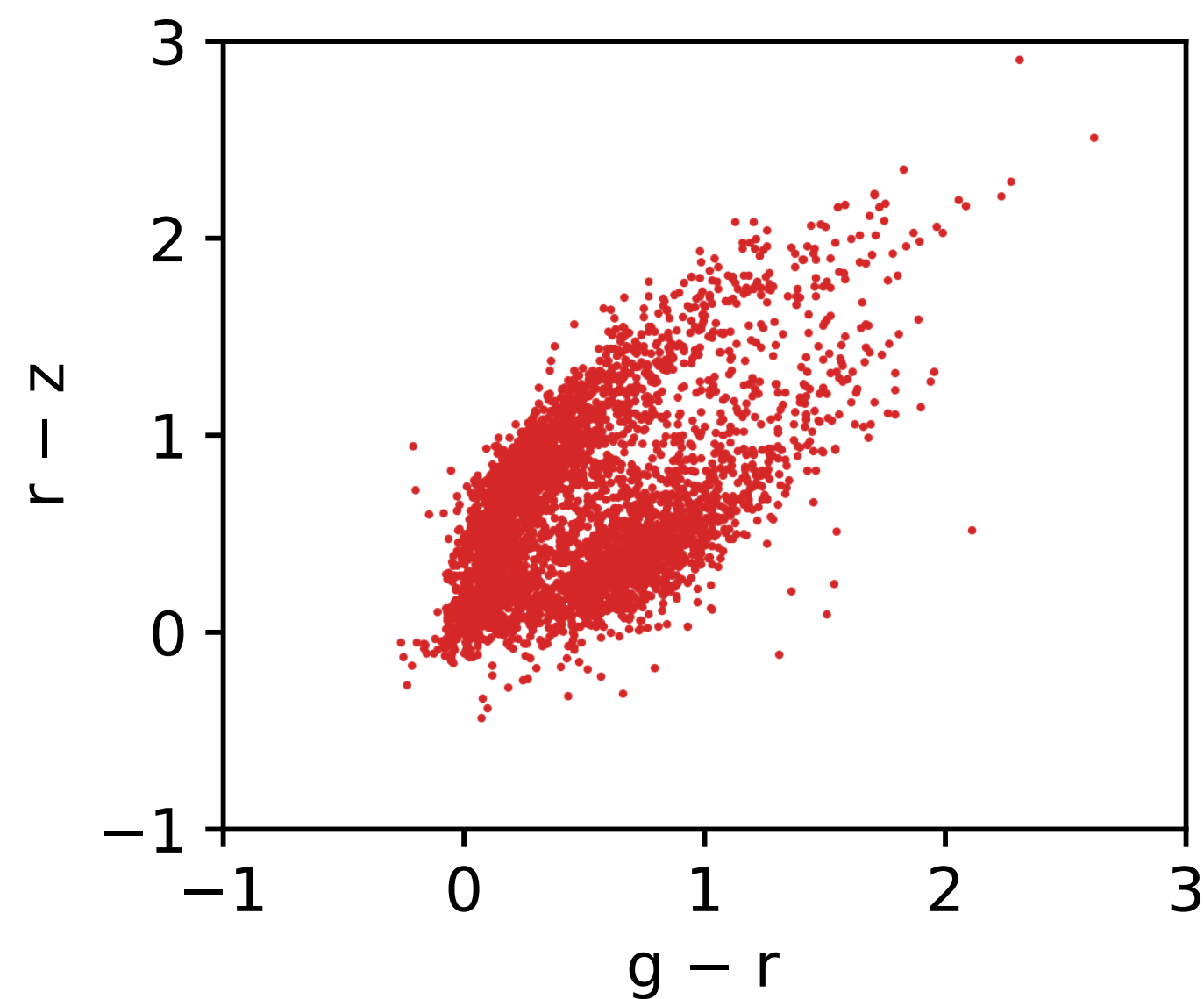
Alsing et al. (2020)



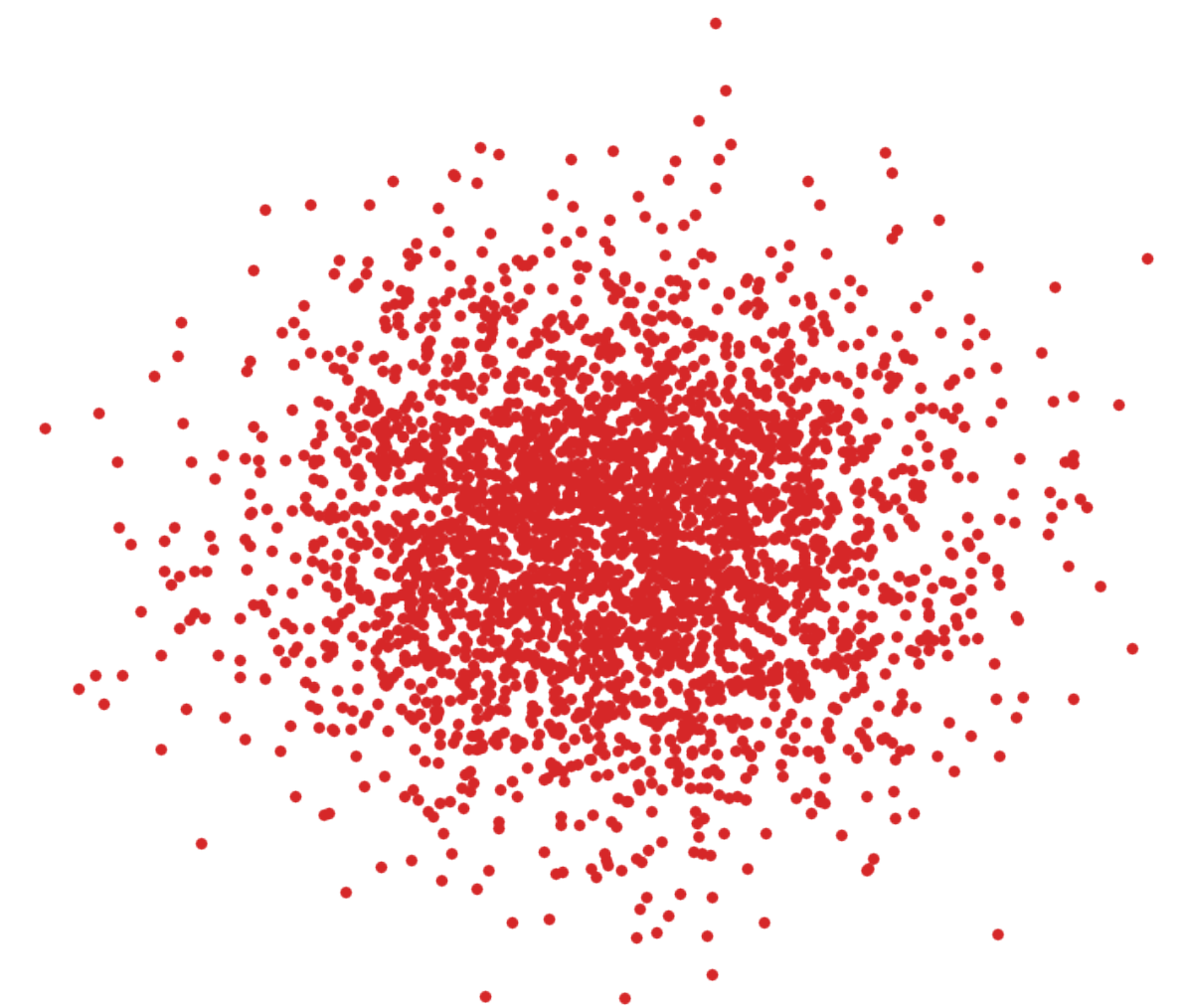
Leja et al. (2017)

What should our population model be?

A score-based diffusion model



target distribution
($t = 0$)

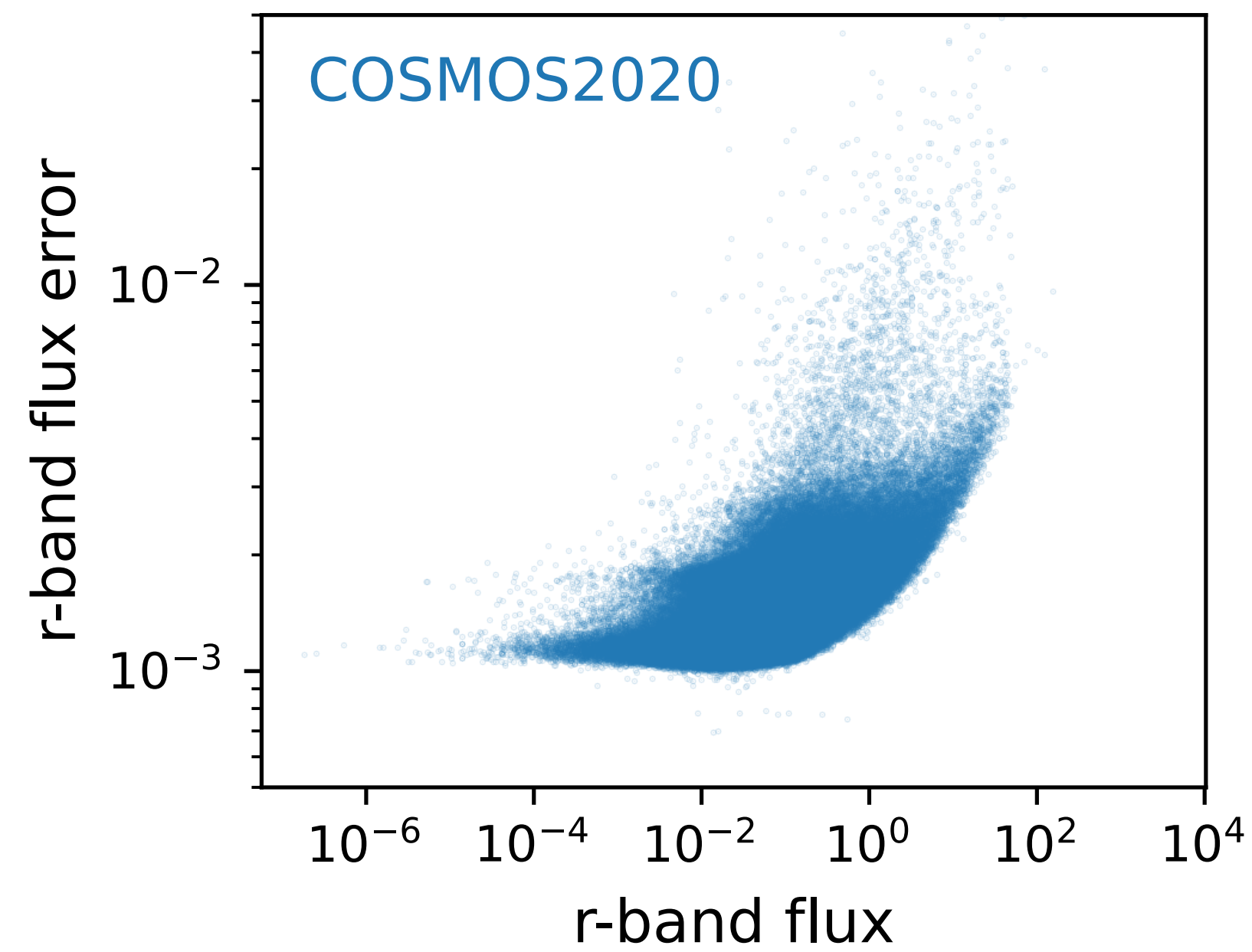


iid Gaussian noise
($t = T$)

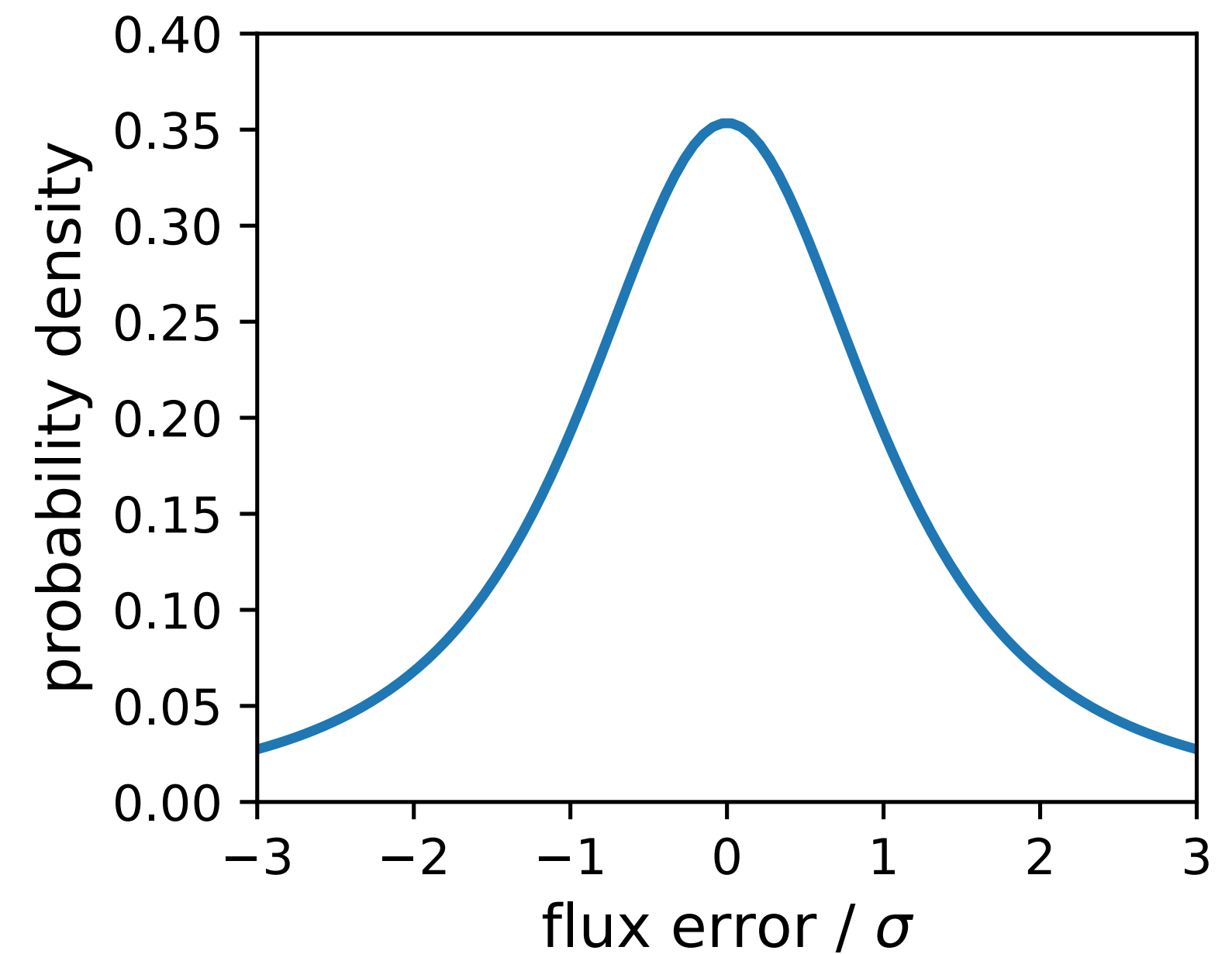
What goes into the data model?

Uncertainty, noise, and calibration

Uncertainty model
(mixture density network)

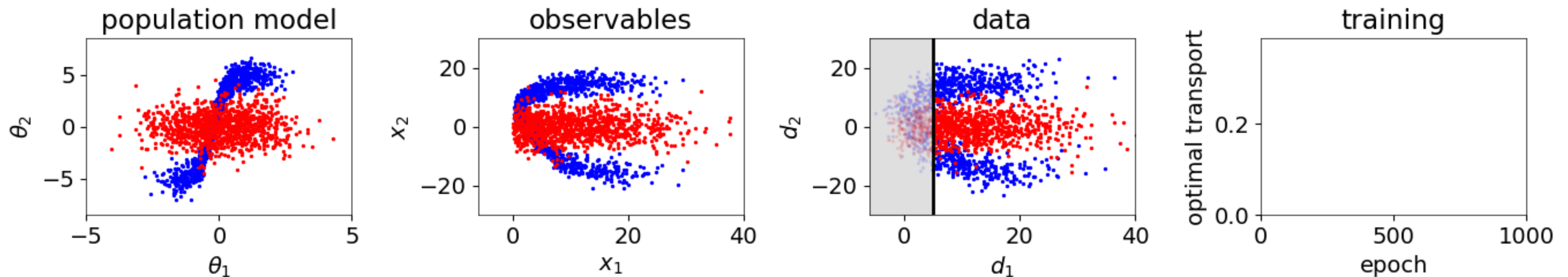


Student's- t error model



How do we fit a model like this?

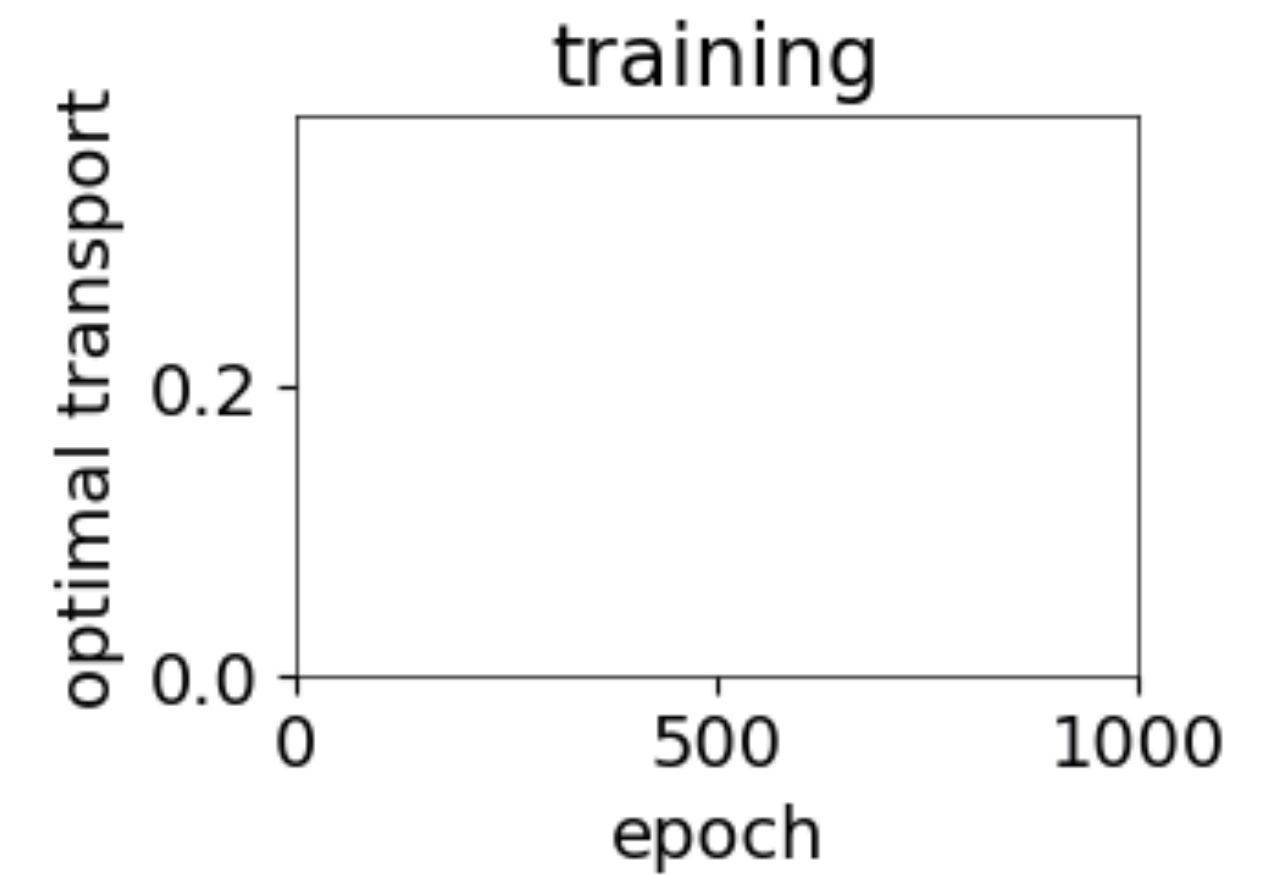
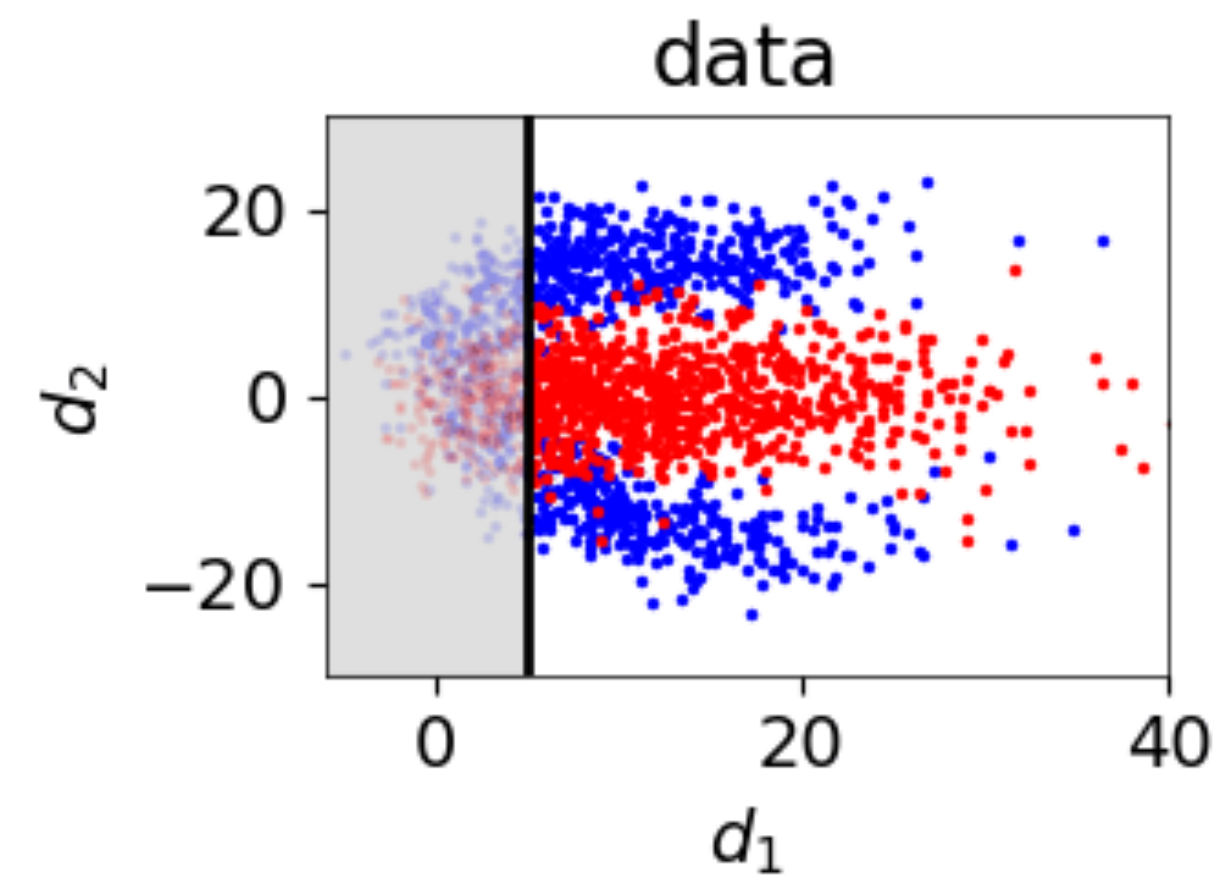
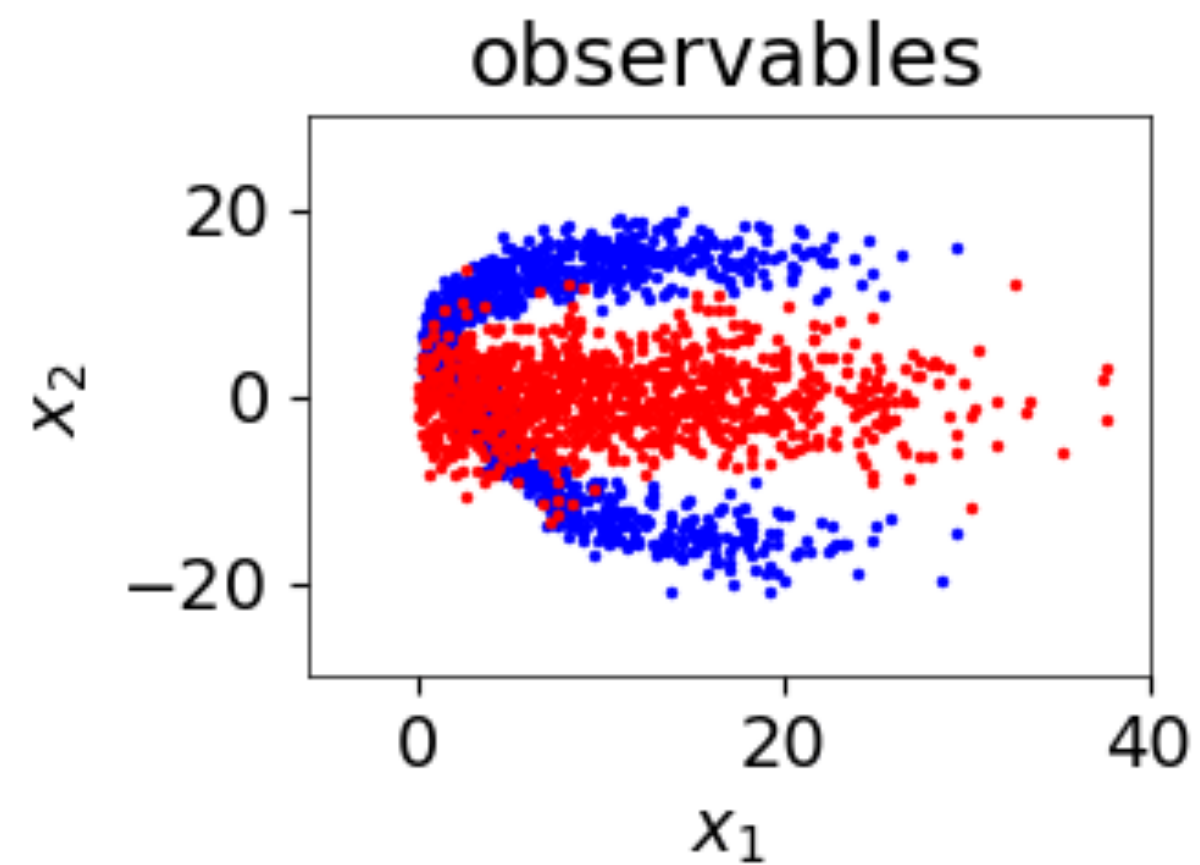
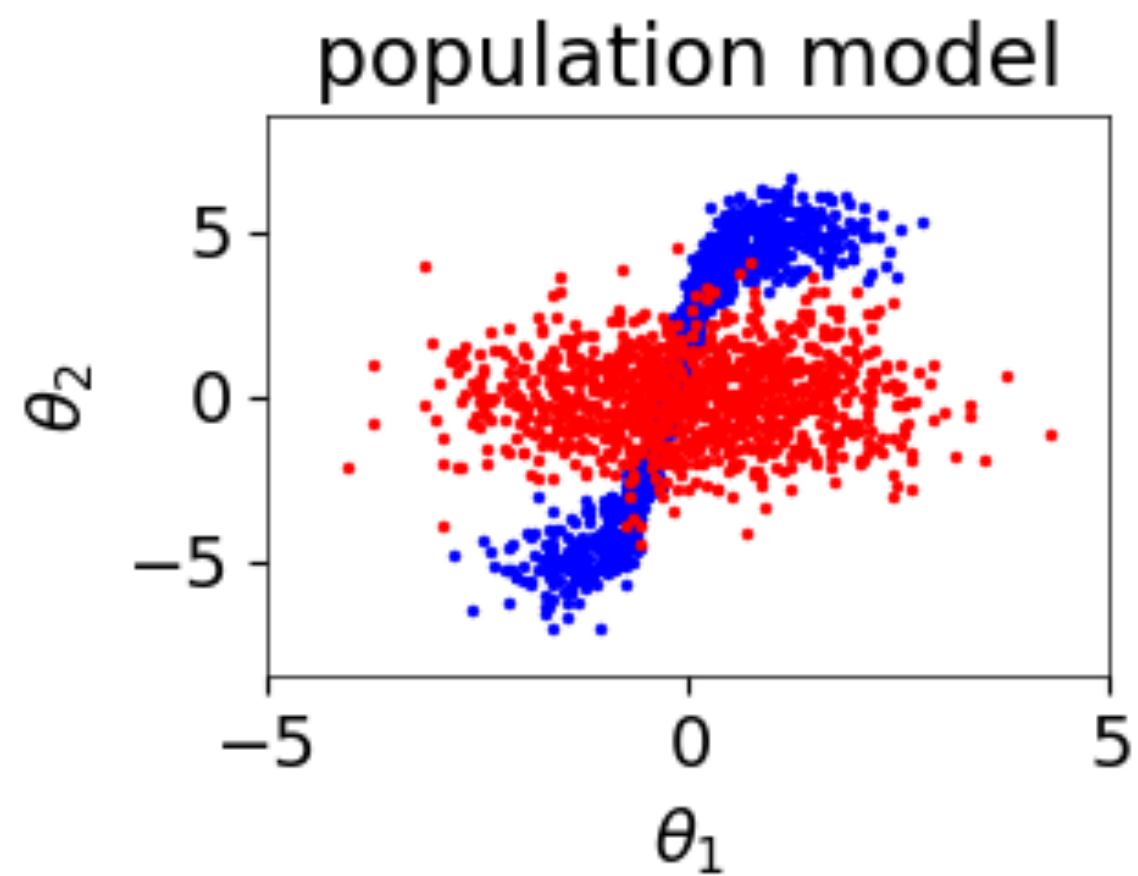
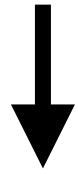
Optimal Transport (a.k.a. the Wasserstein Distance)



How do we fit a model like this?

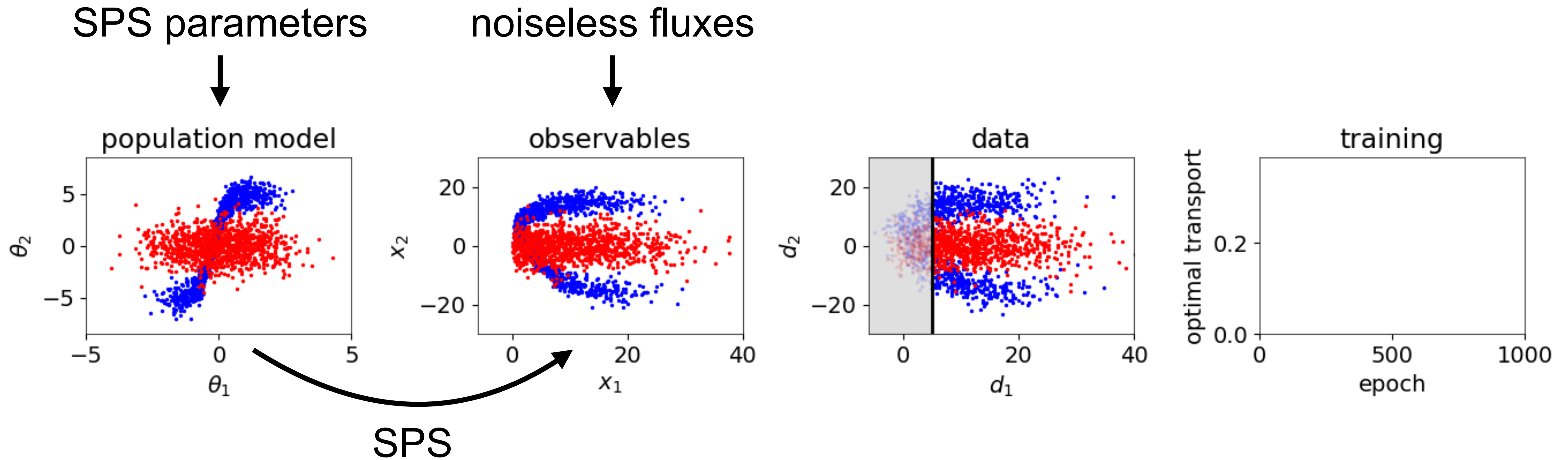
Optimal Transport (a.k.a. the Wasserstein Distance)

SPS parameters



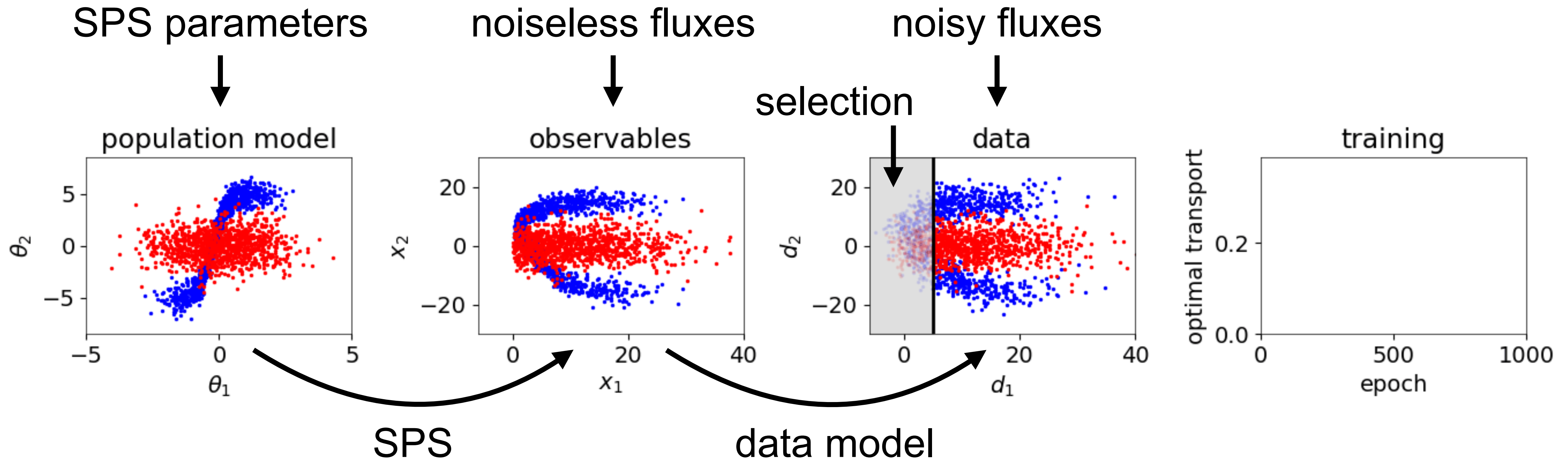
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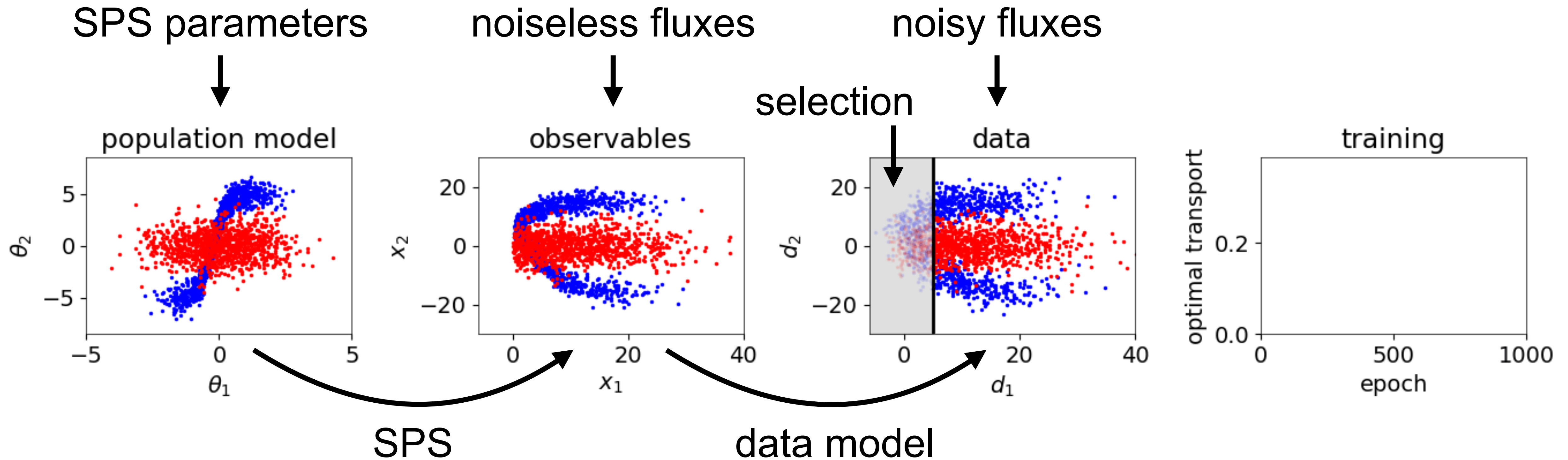
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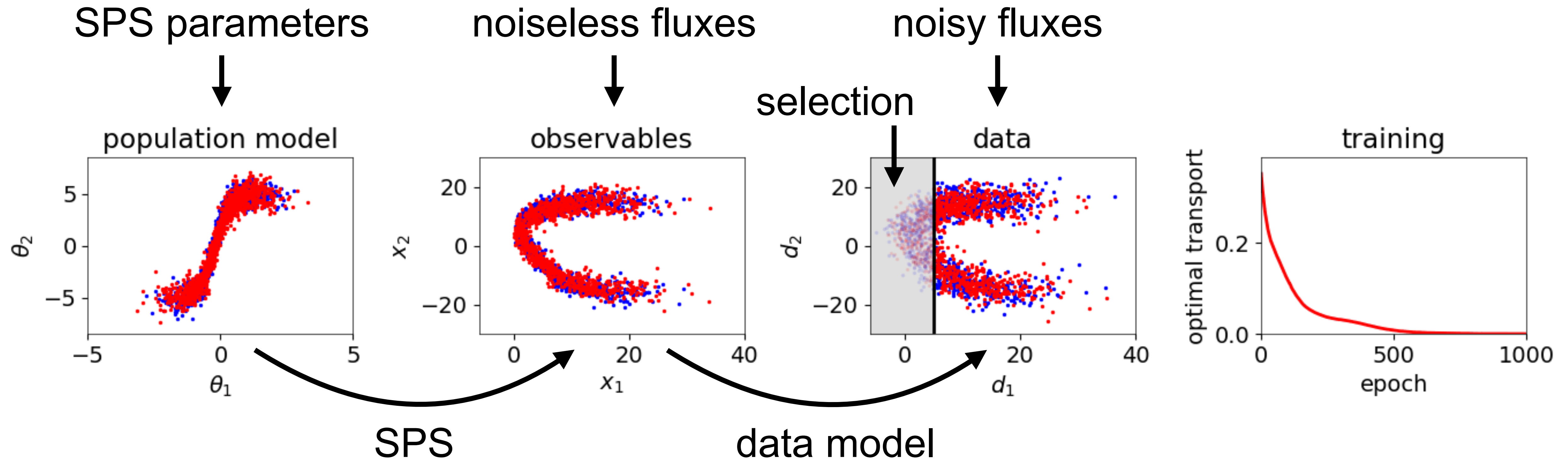
How do we fit a model like this?

Optimal Transport (a.k.a. the Wasserstein Distance)



How do we fit a model like this?

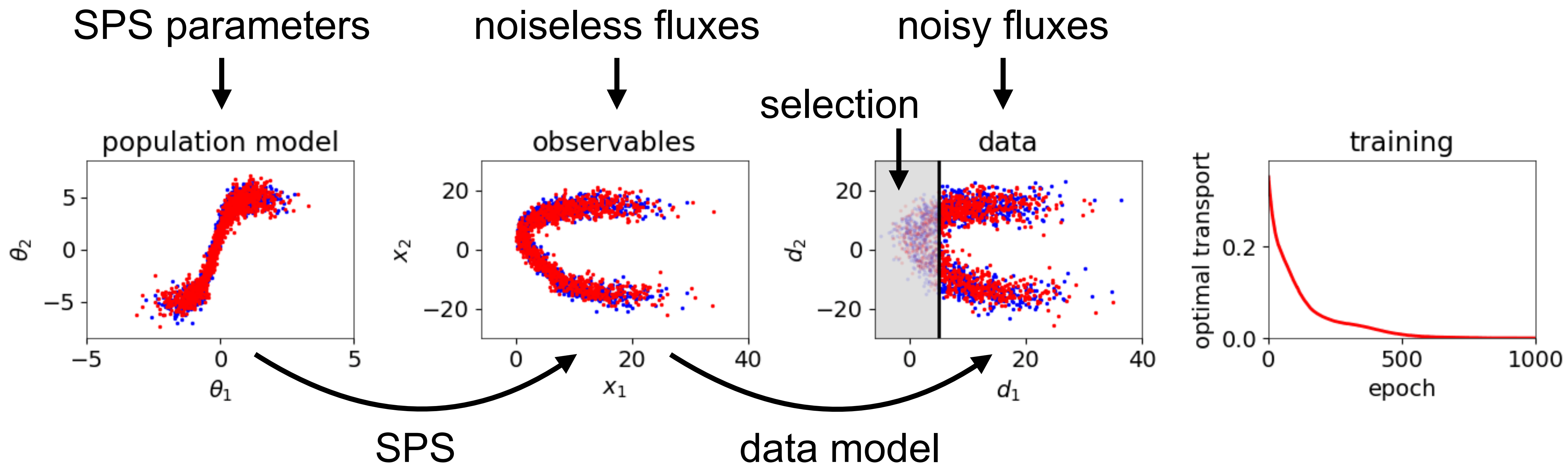
Optimal Transport (a.k.a. the Wasserstein Distance)

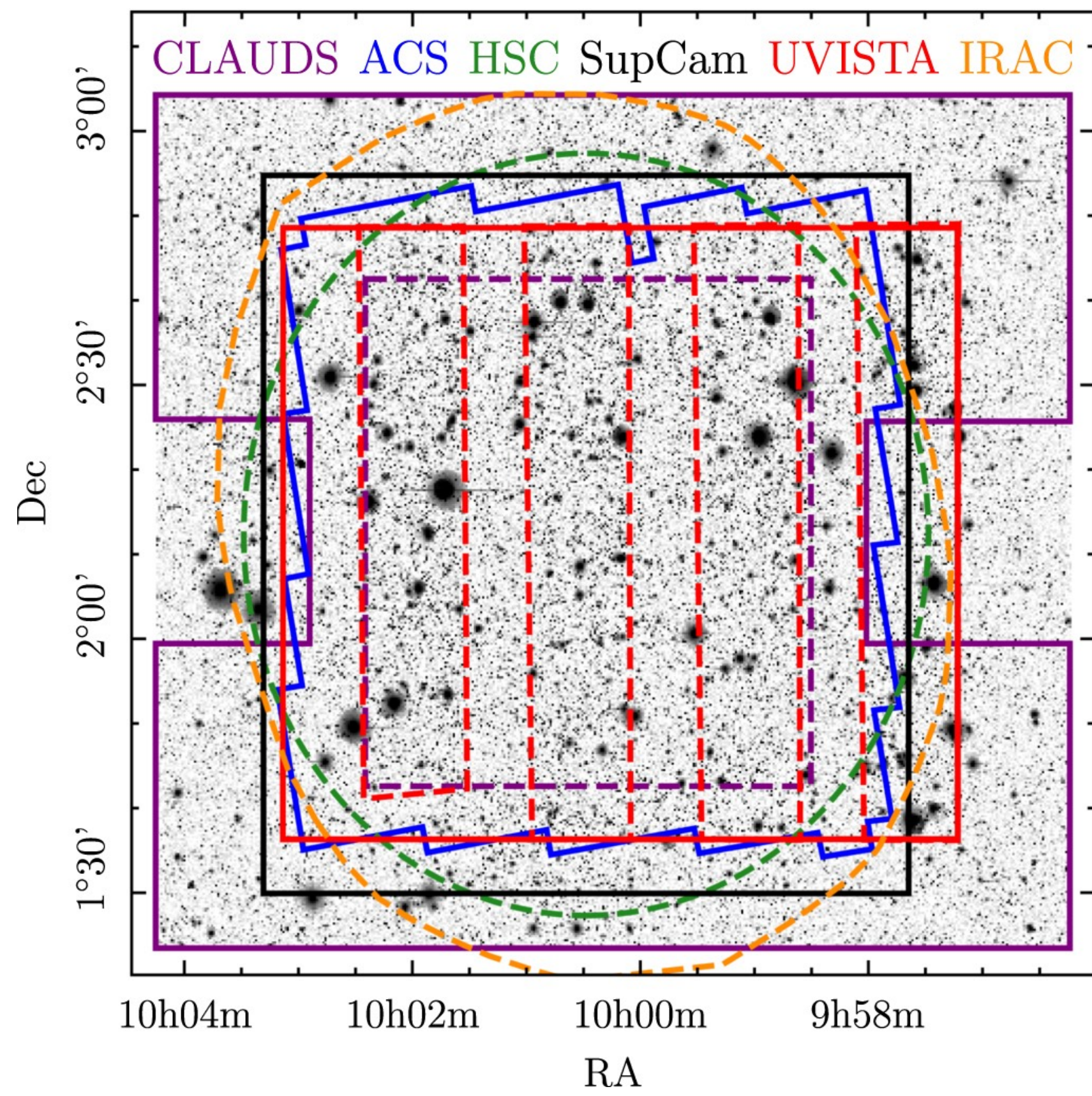


Credit: Justin Alsing

How do we fit a model like this?

Optimal Transport (a.k.a. the Wasserstein Distance)

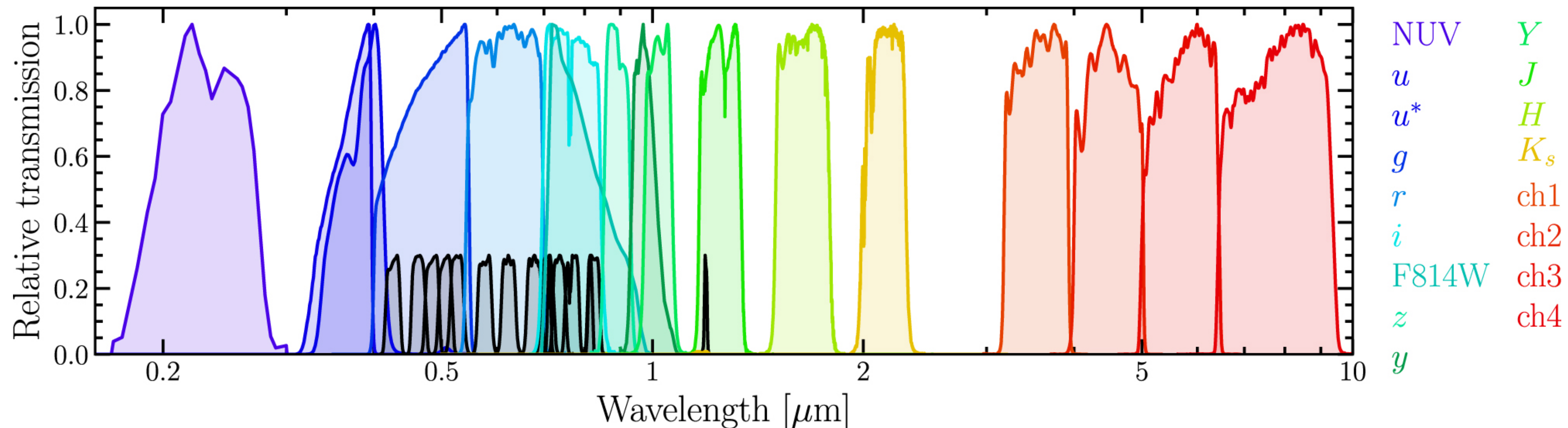




What data will we use?

COSMOS2020 (Weaver et al. 2022)

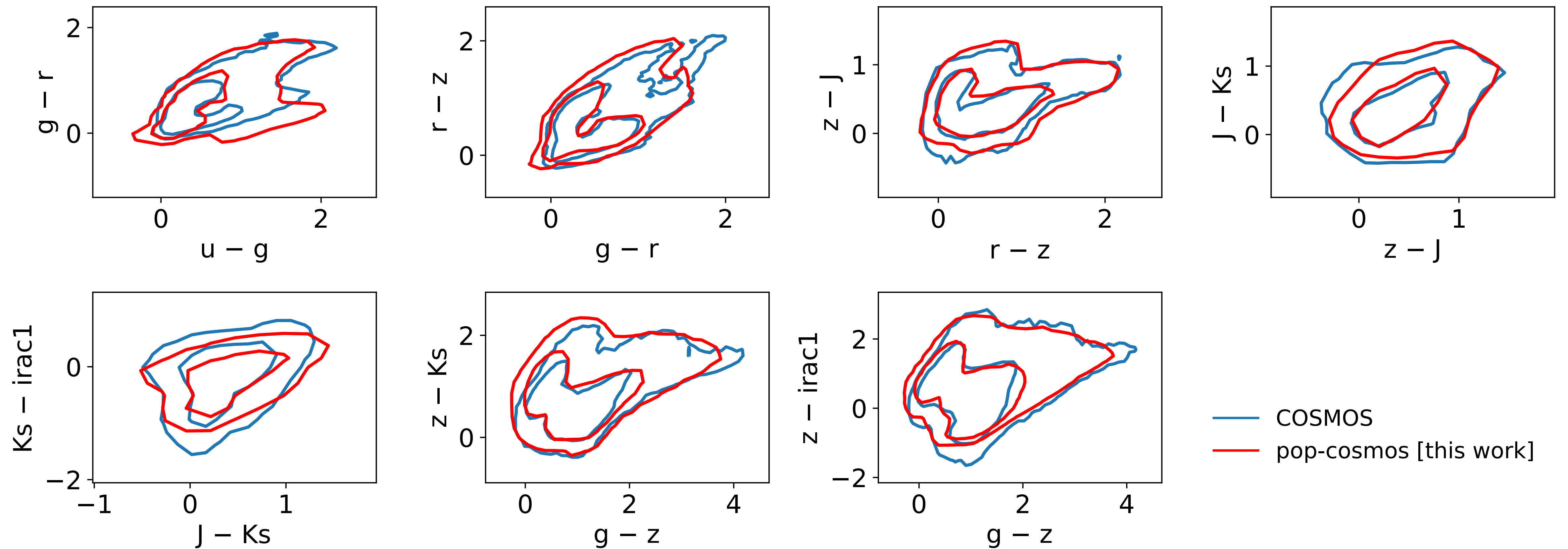
- Has $\approx 140,000$ galaxies with $r < 25$
- Wide and narrow bands
- Coverage from near-UV to mid-IR



Results

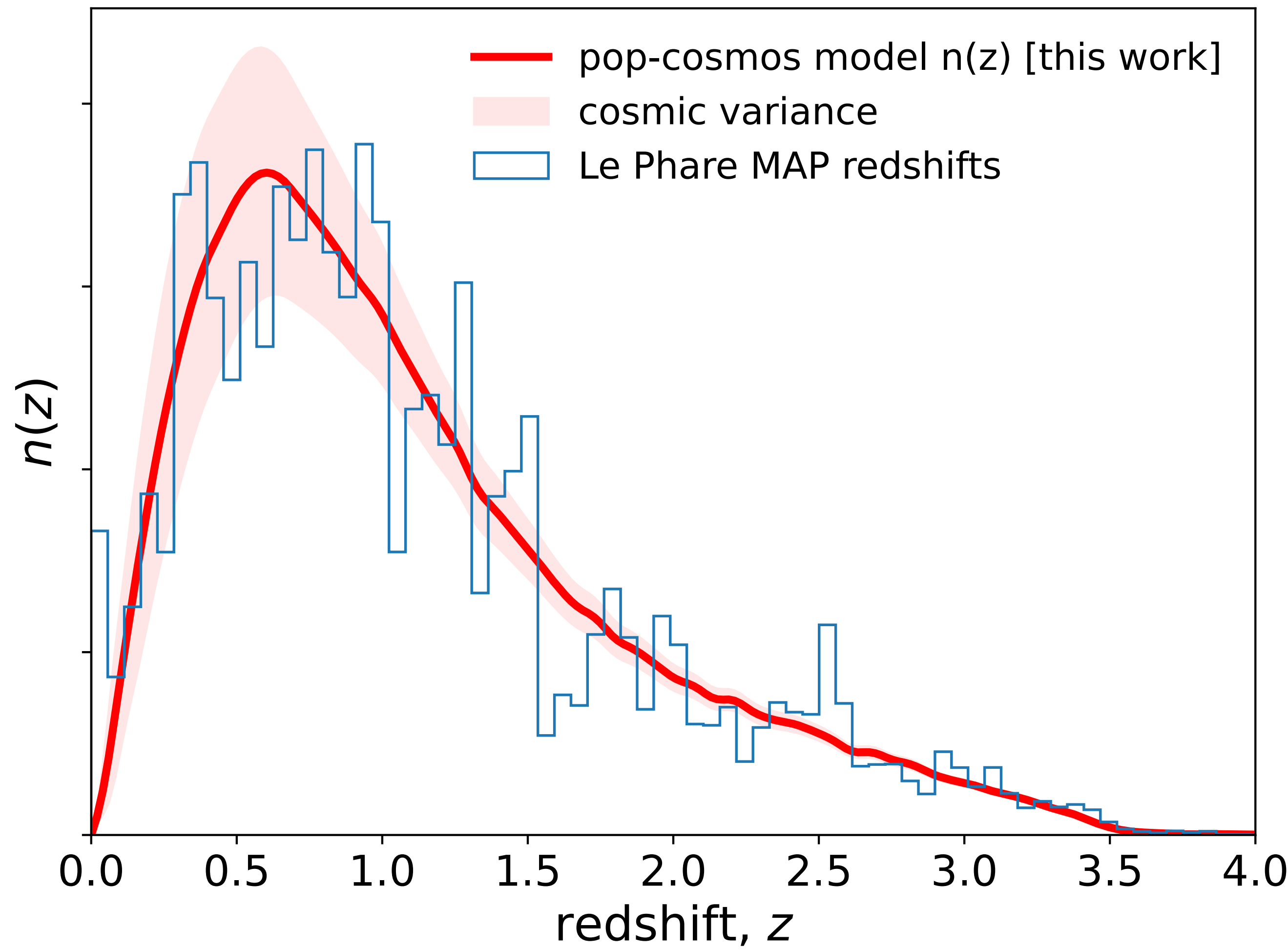
Photometric Predictions

Colour-colour plots



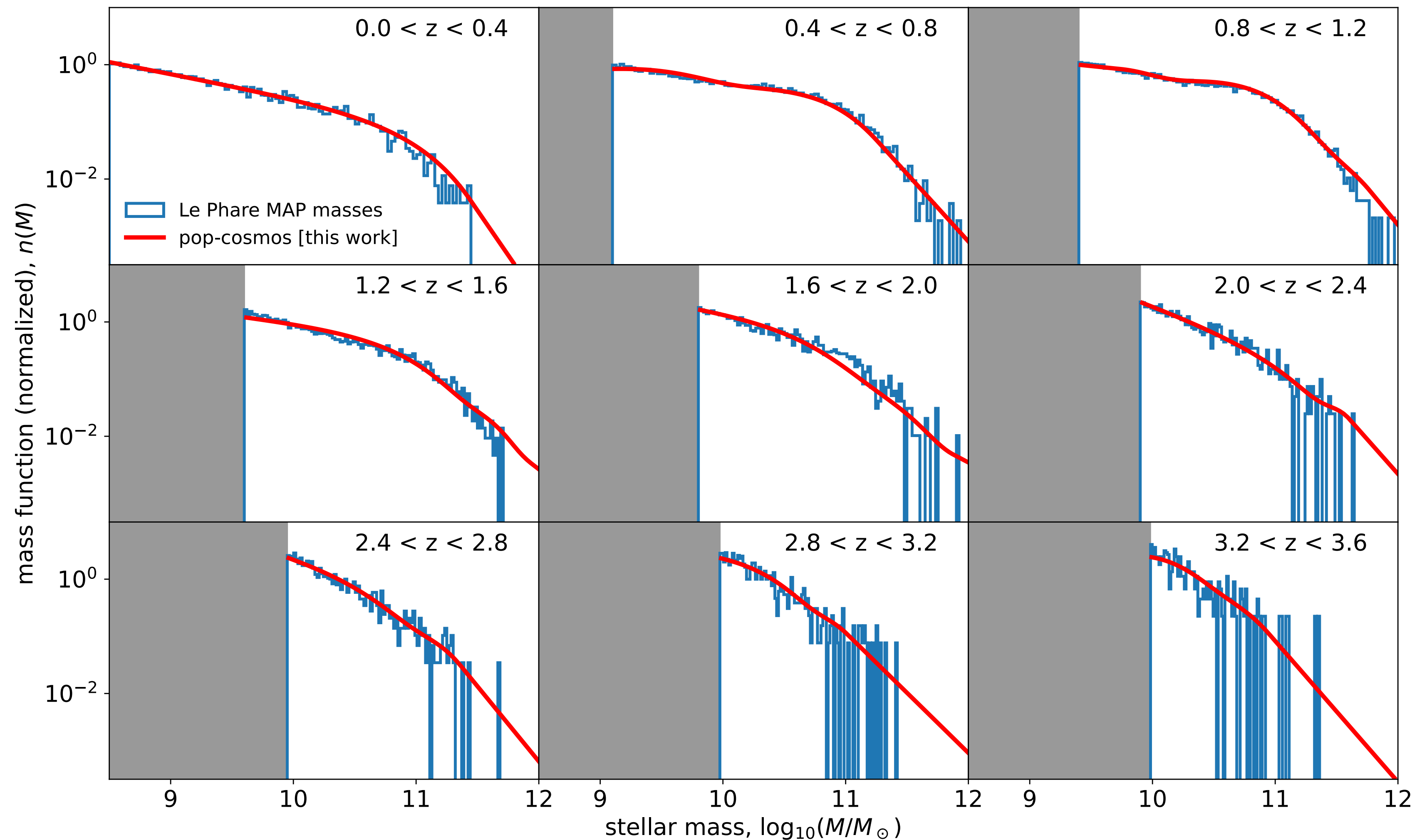
Redshift Distribution

Predicted population-level $n(z)$



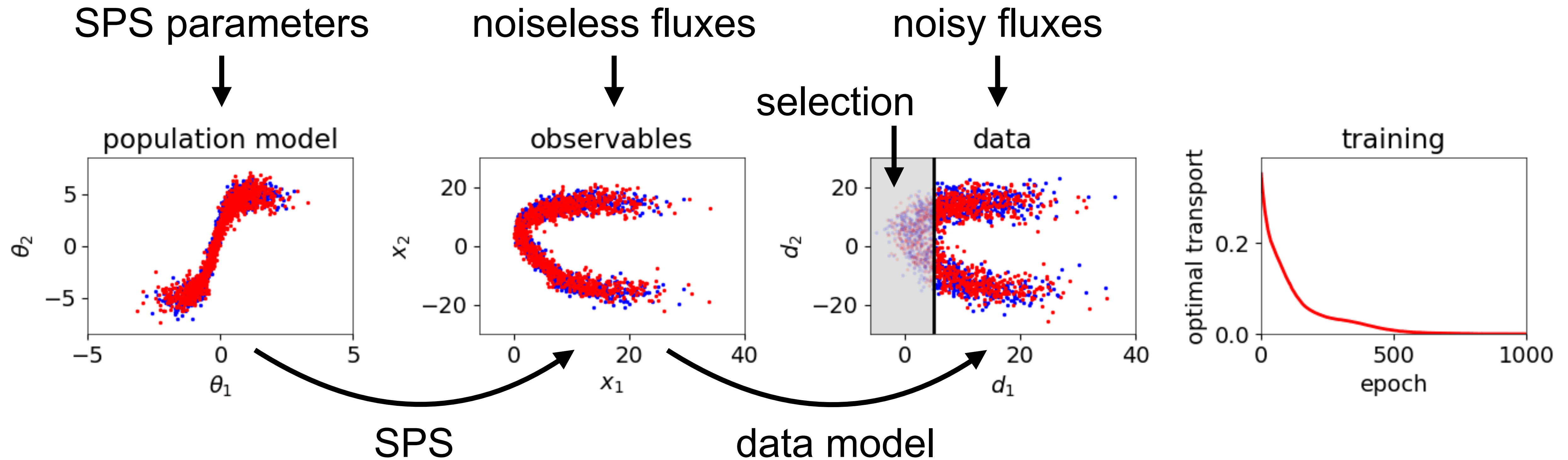
Stellar Mass Function

We get more than just redshifts!



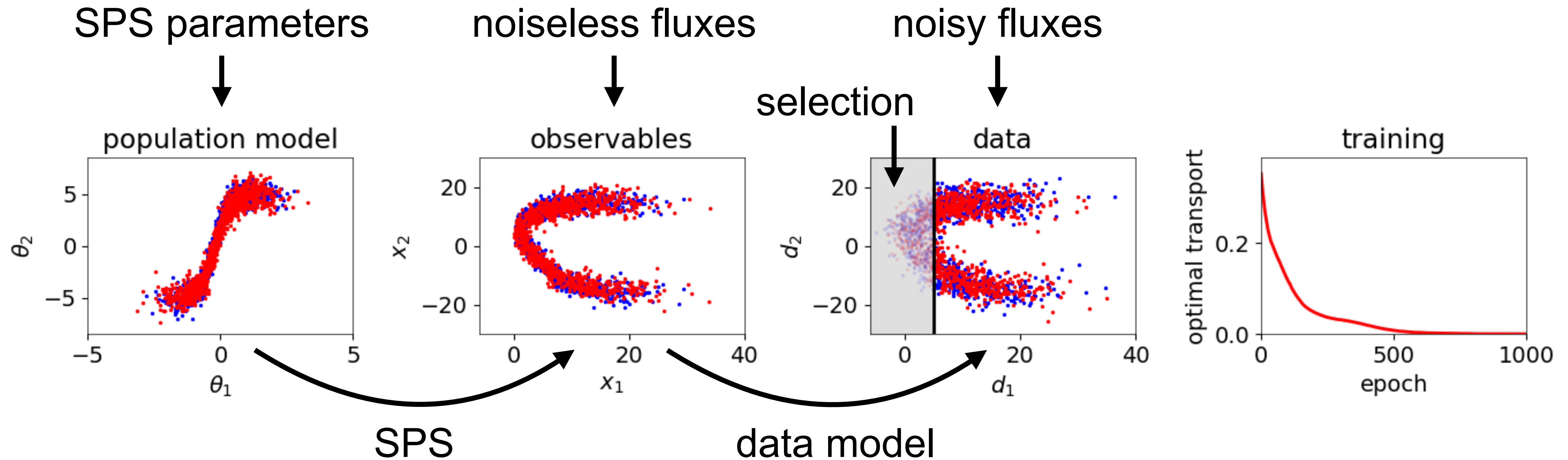
What's else can we do?

Making predictions for other surveys...



What's else can we do?

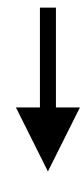
Making predictions for other surveys...



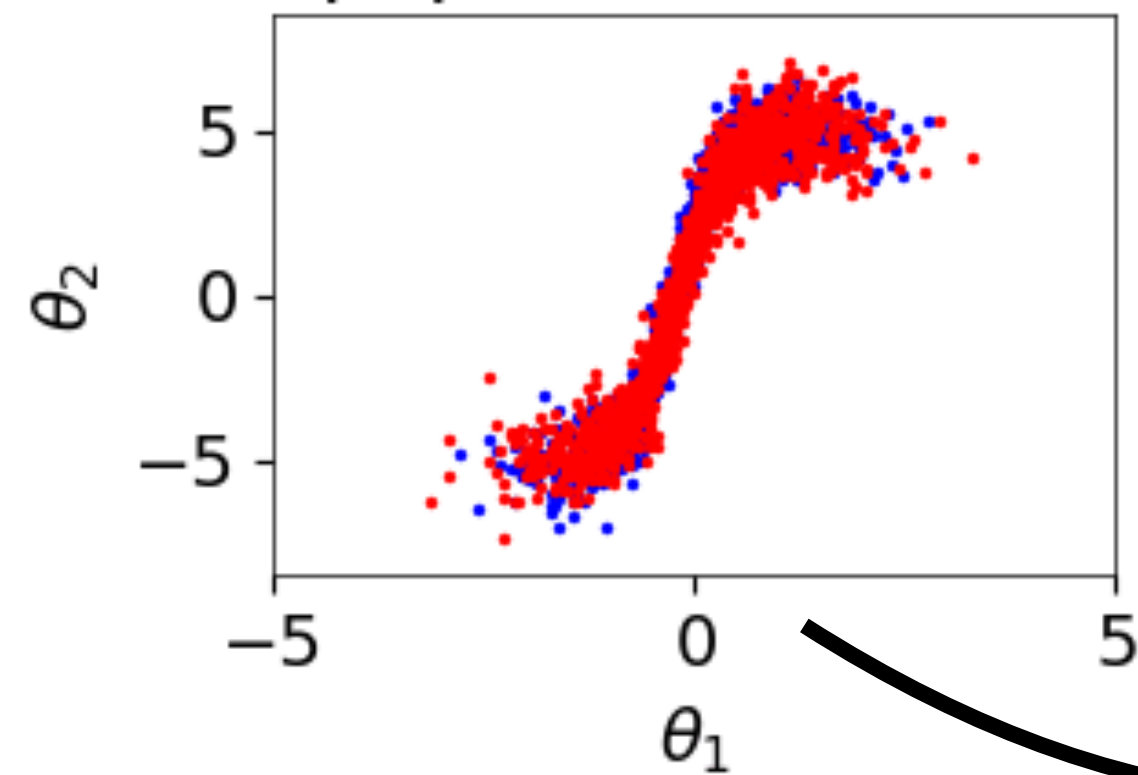
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SPS parameters



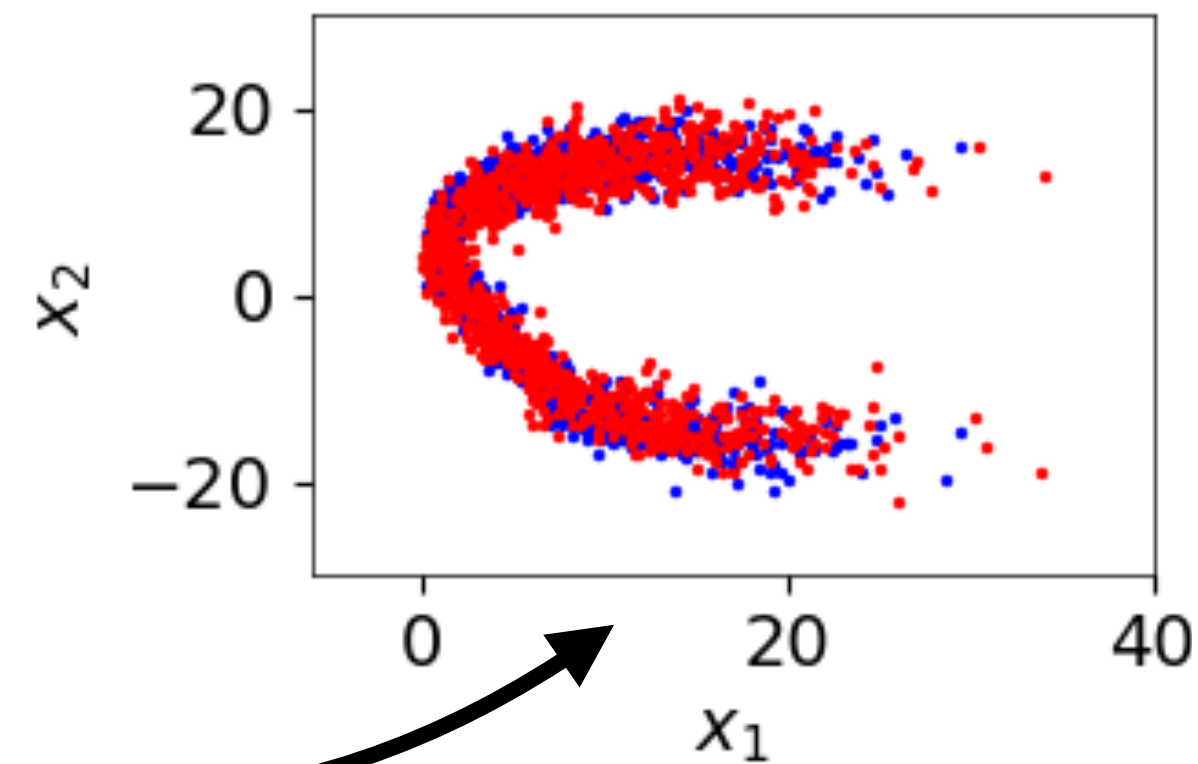
population model



noiseless fluxes



observables

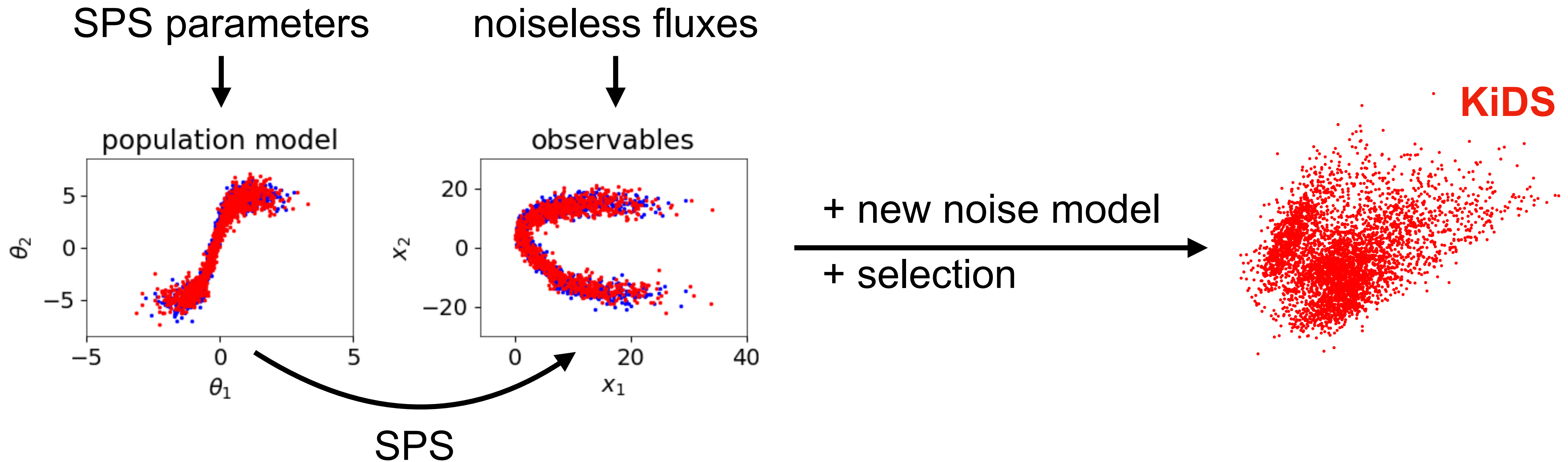


SPS



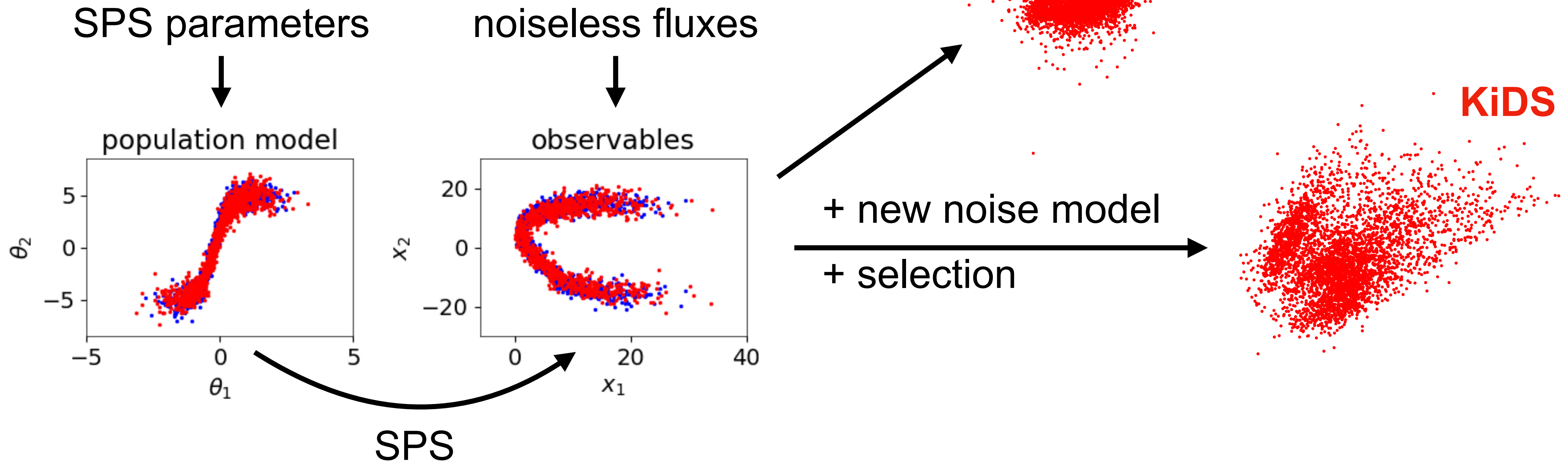
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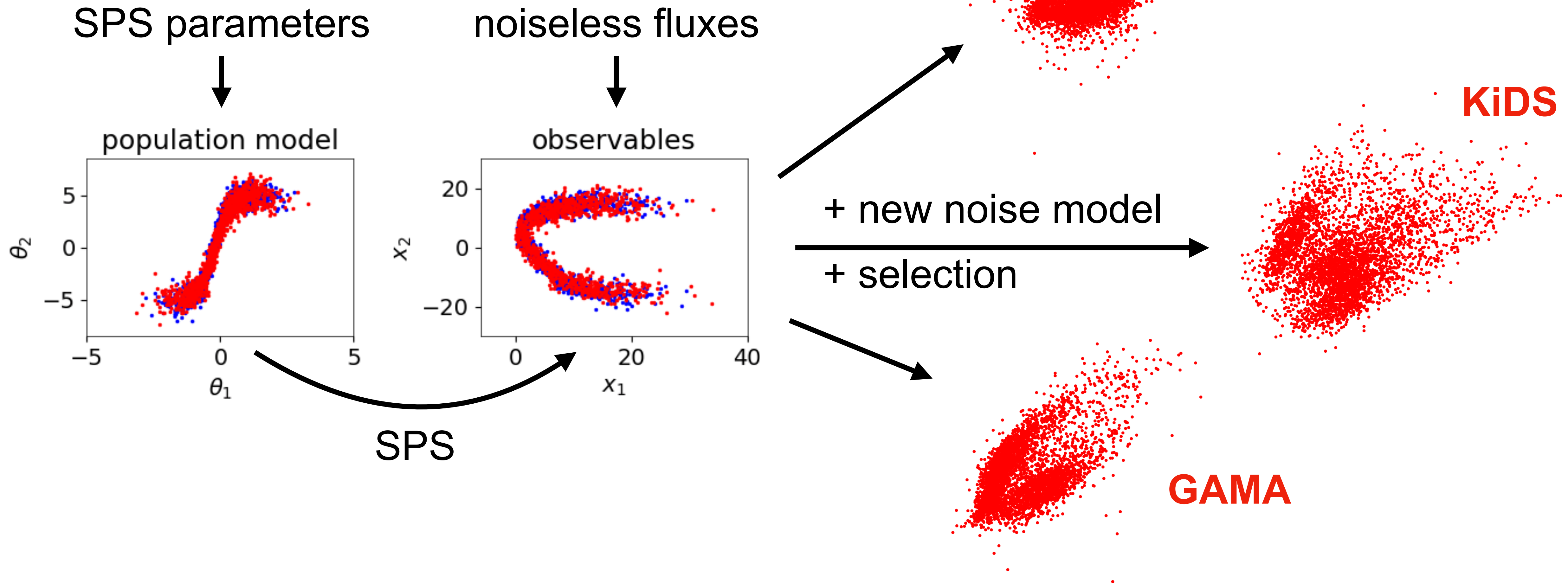
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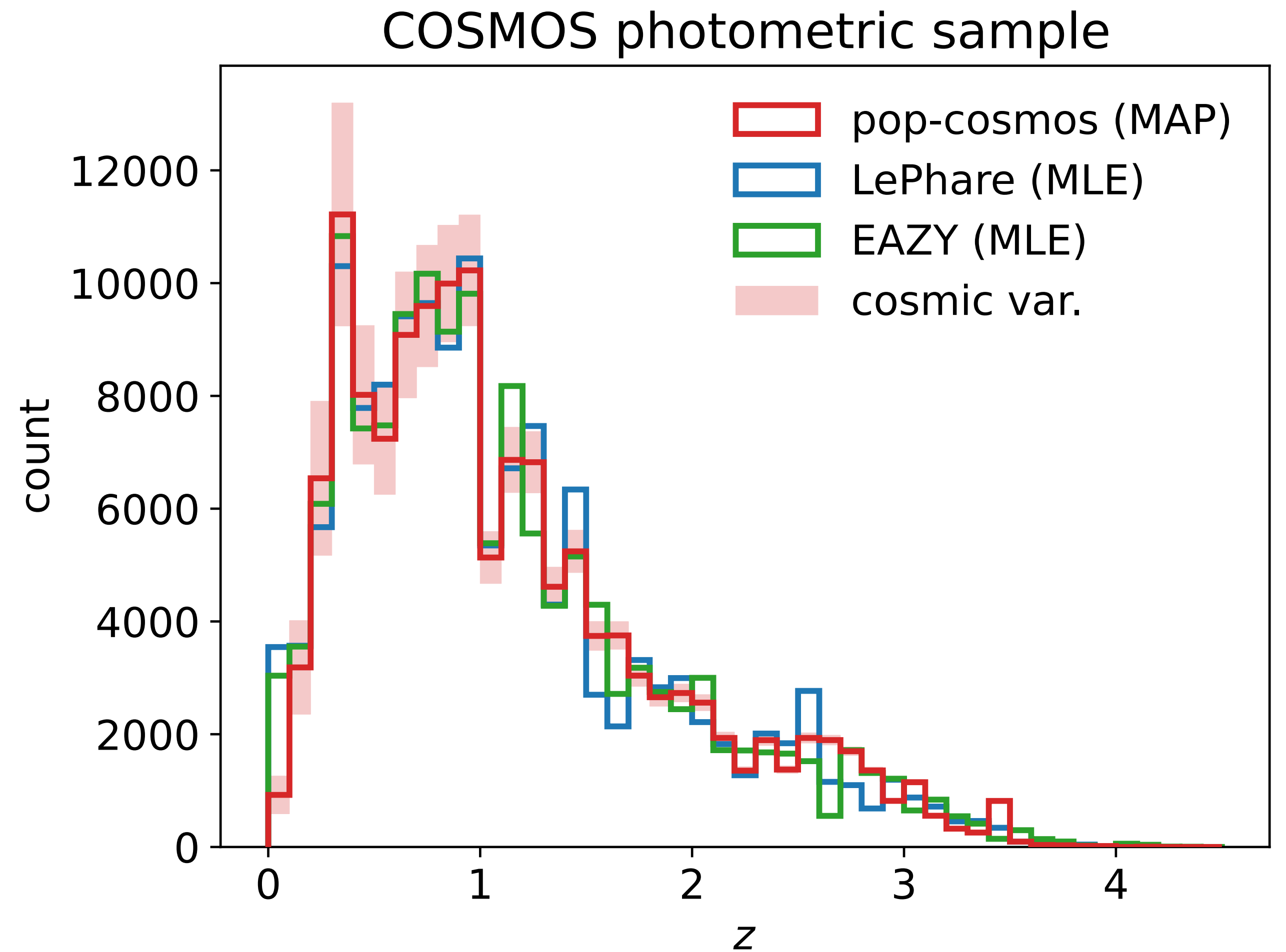
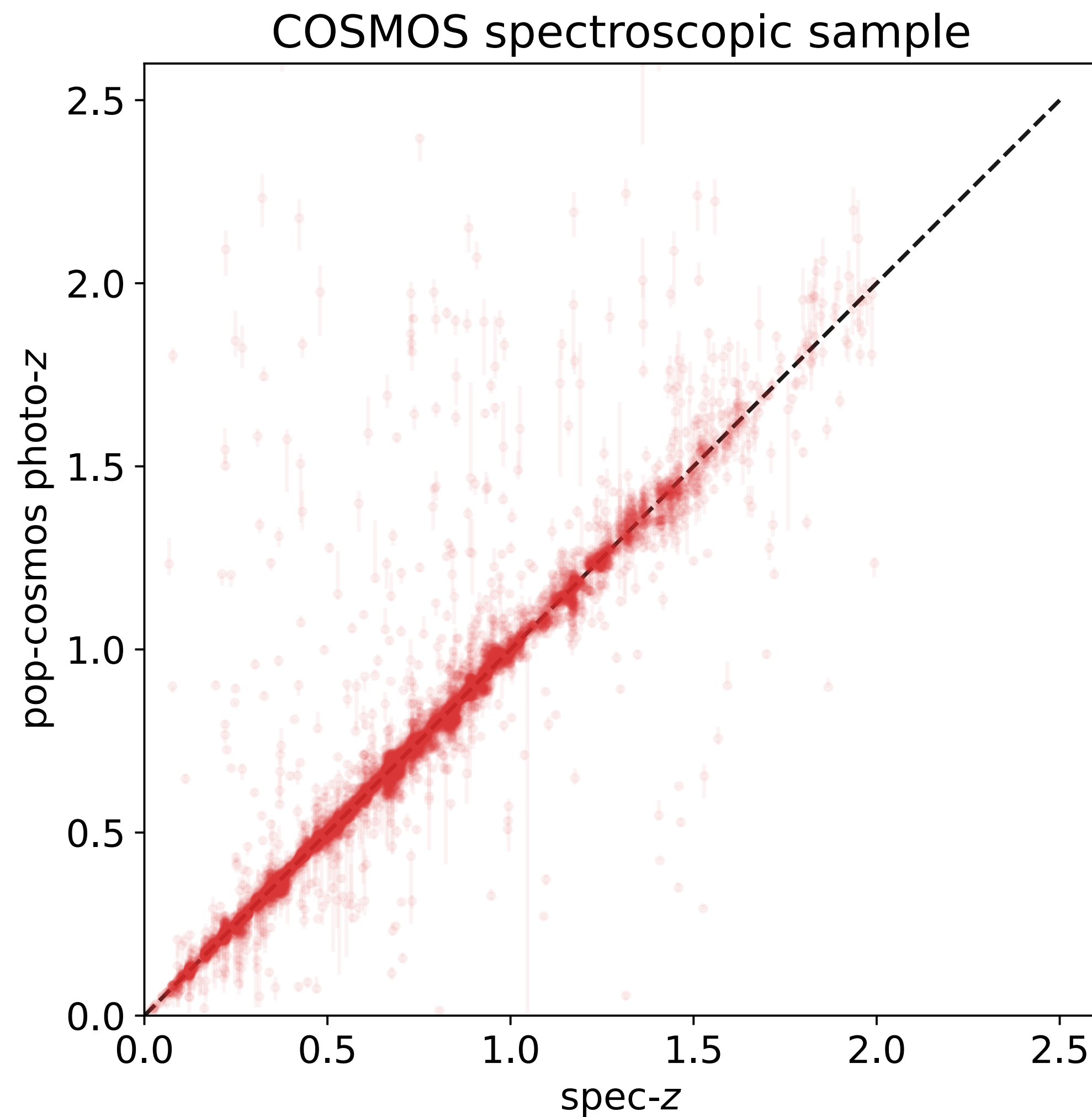
What's else can we do?

Making predictions for other surveys...



What's else can we do?

Using pop-cosmos as a prior for Bayesian photo- z estimation...



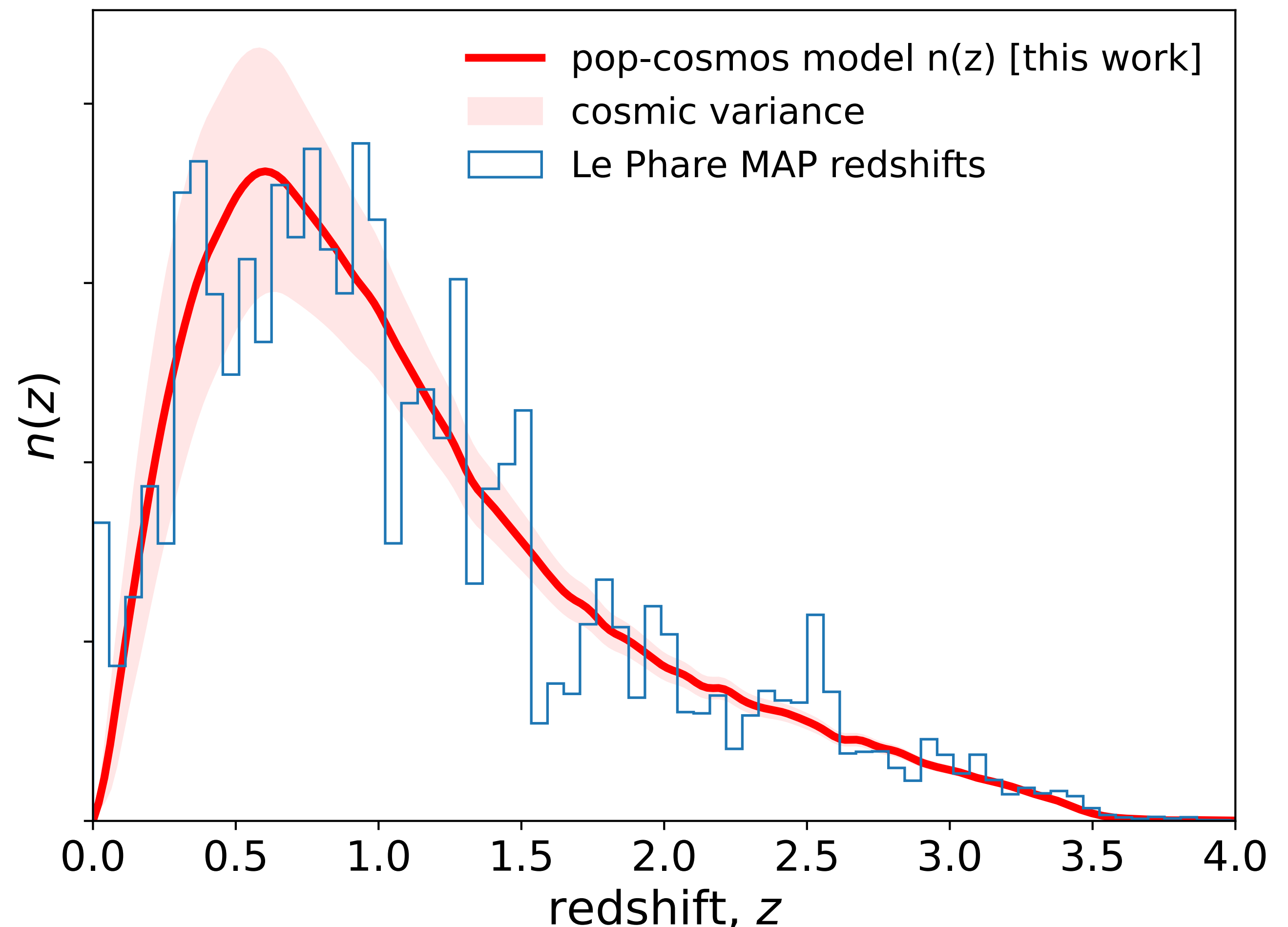
Summary

pop-cosmos



2402.00935

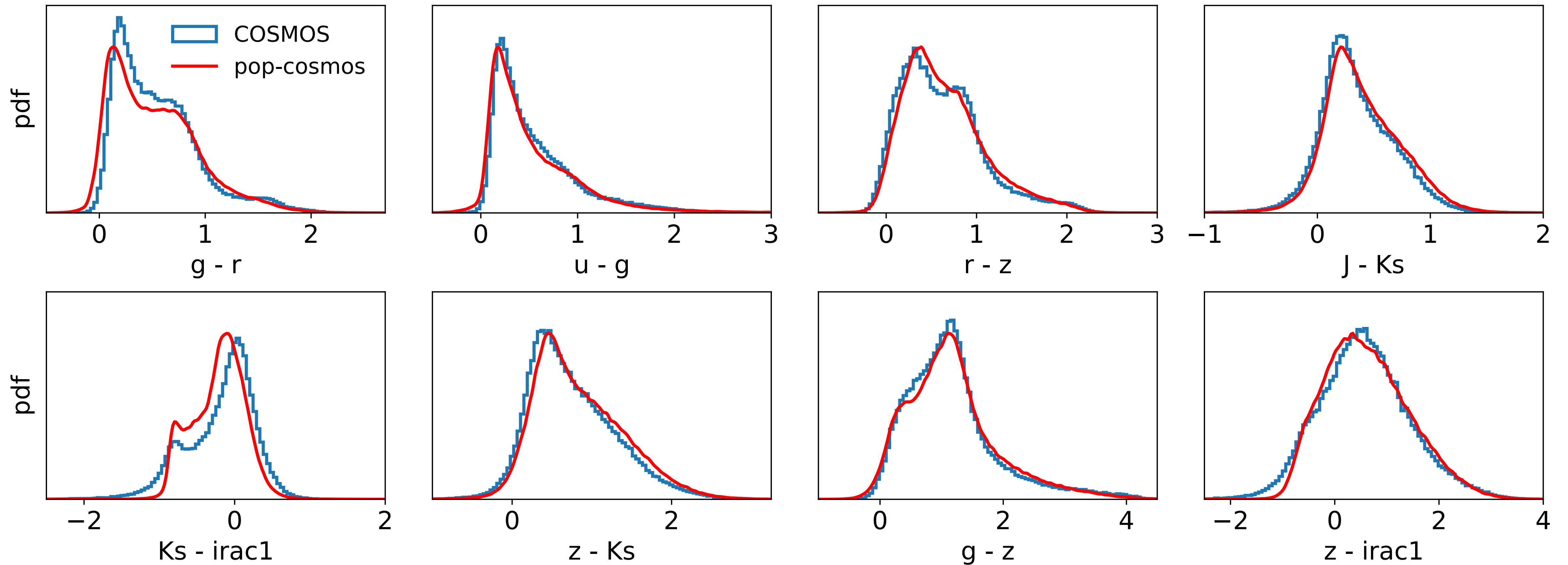
- Comprehensive forward model for galaxy photometry
- Flexible non-parametric population model
- Gives us redshift distribution, and can be used to make predictions for other surveys
- Tons of information about galaxy demographics on a huge sample with minimal selection (**see the talk + poster by Sinan Deger!**)



Extra Slides

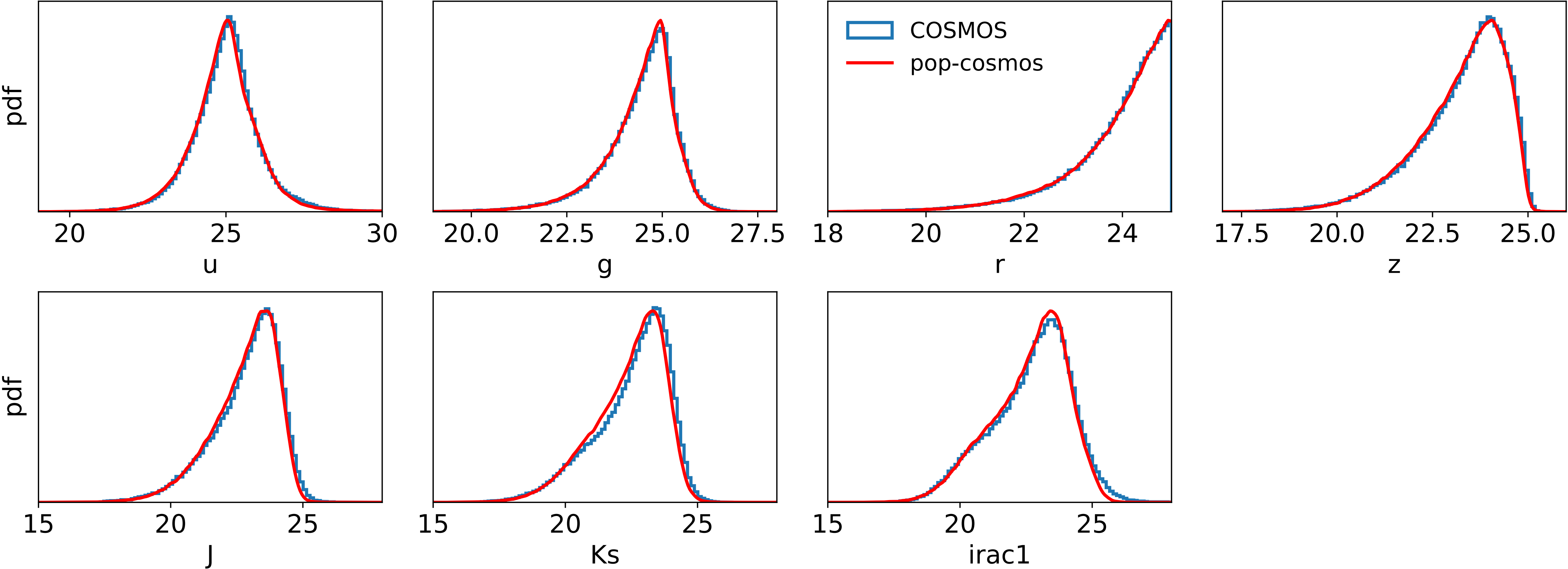
Photometric Predictions

Colour marginals



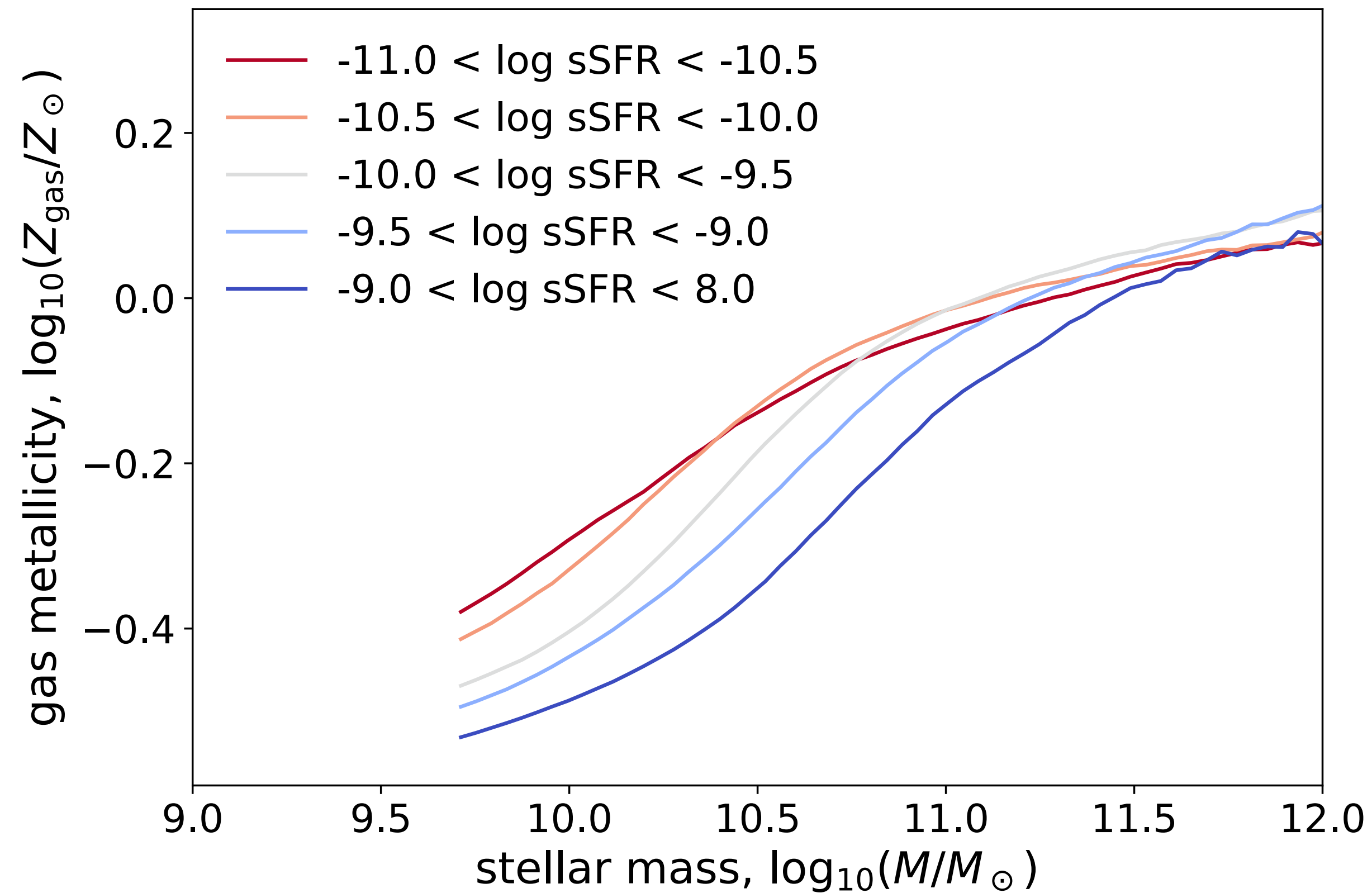
Photometric Predictions

Magnitude marginals



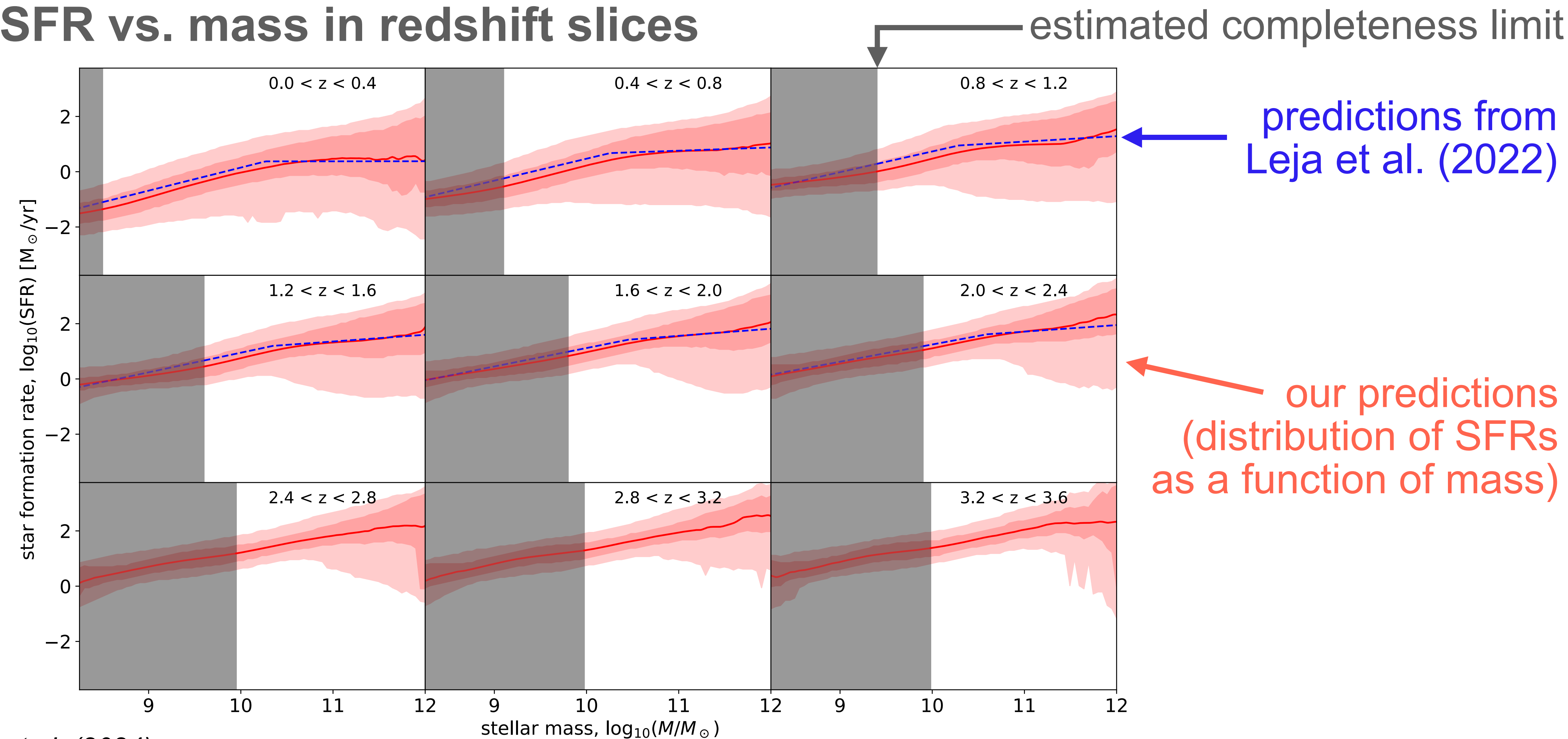
Fundamental Metallicity Relation

Gas metallicity vs. mass vs. SFR



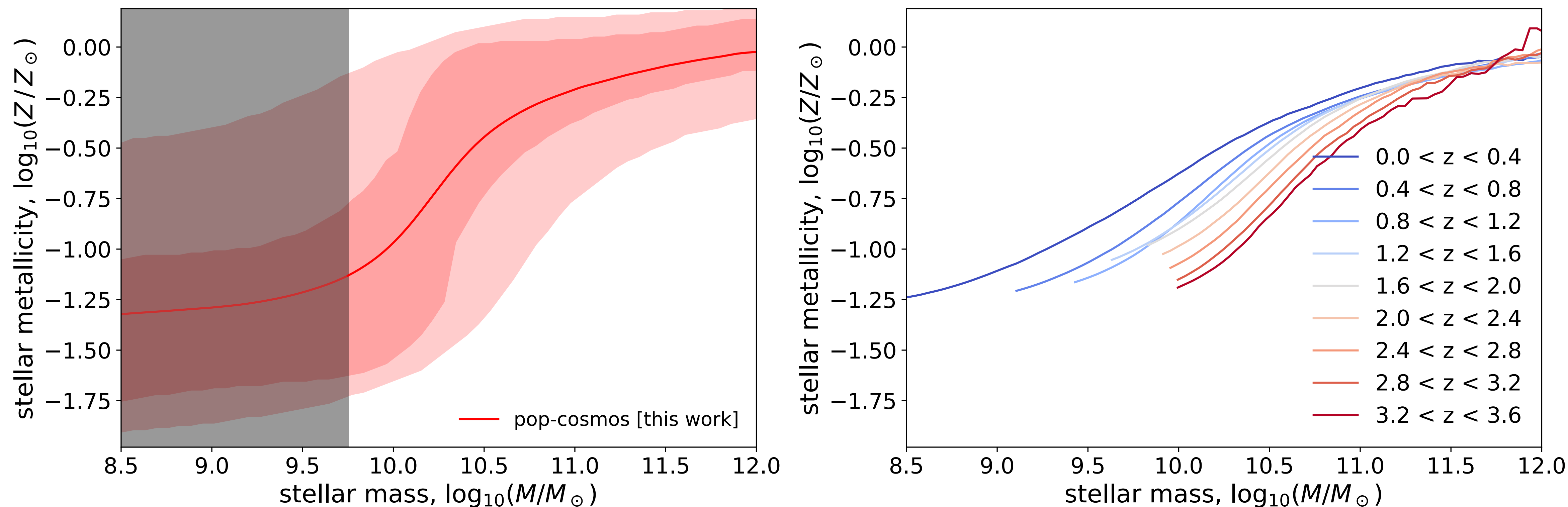
Star Forming Sequence

SFR vs. mass in redshift slices



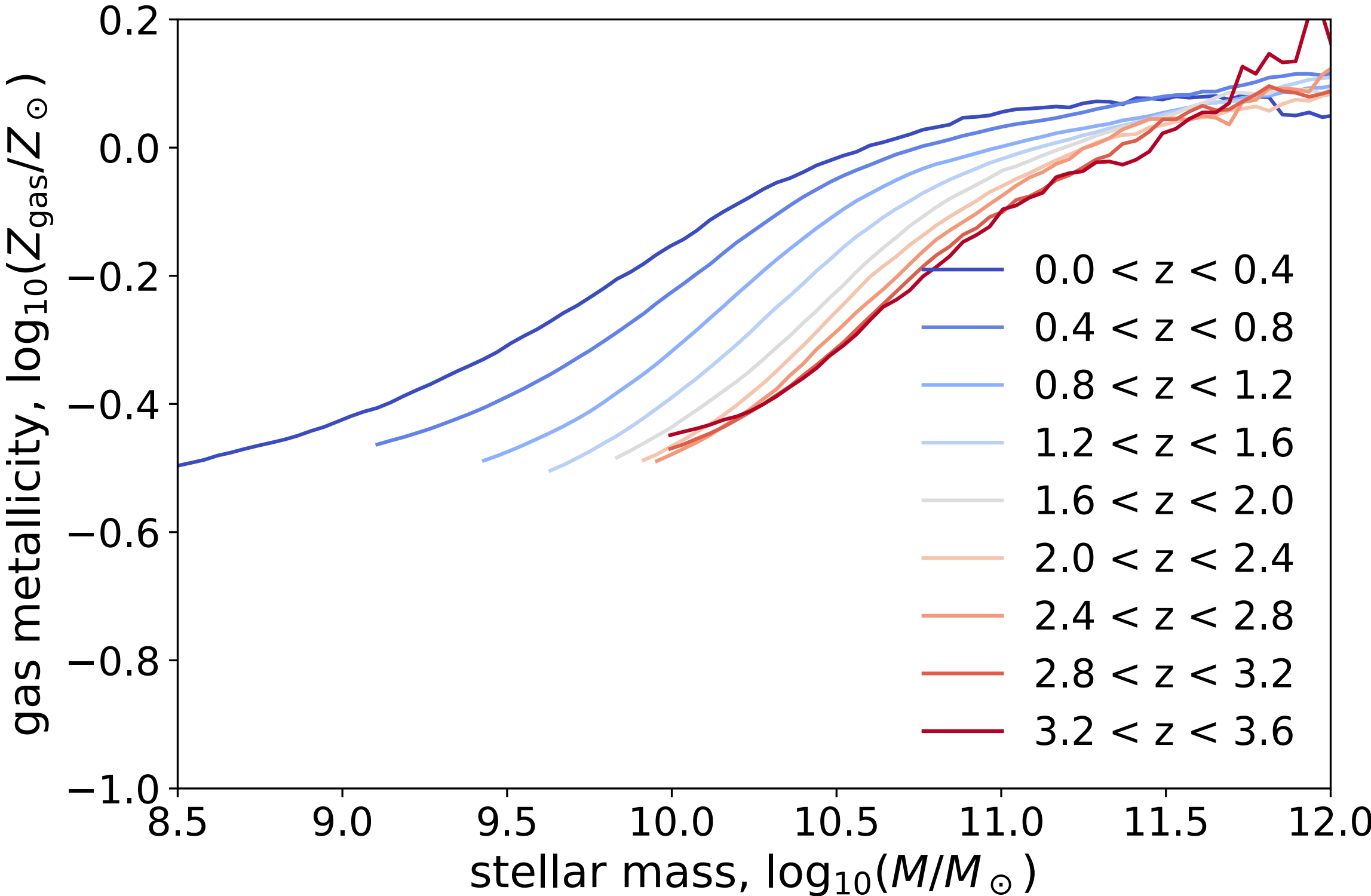
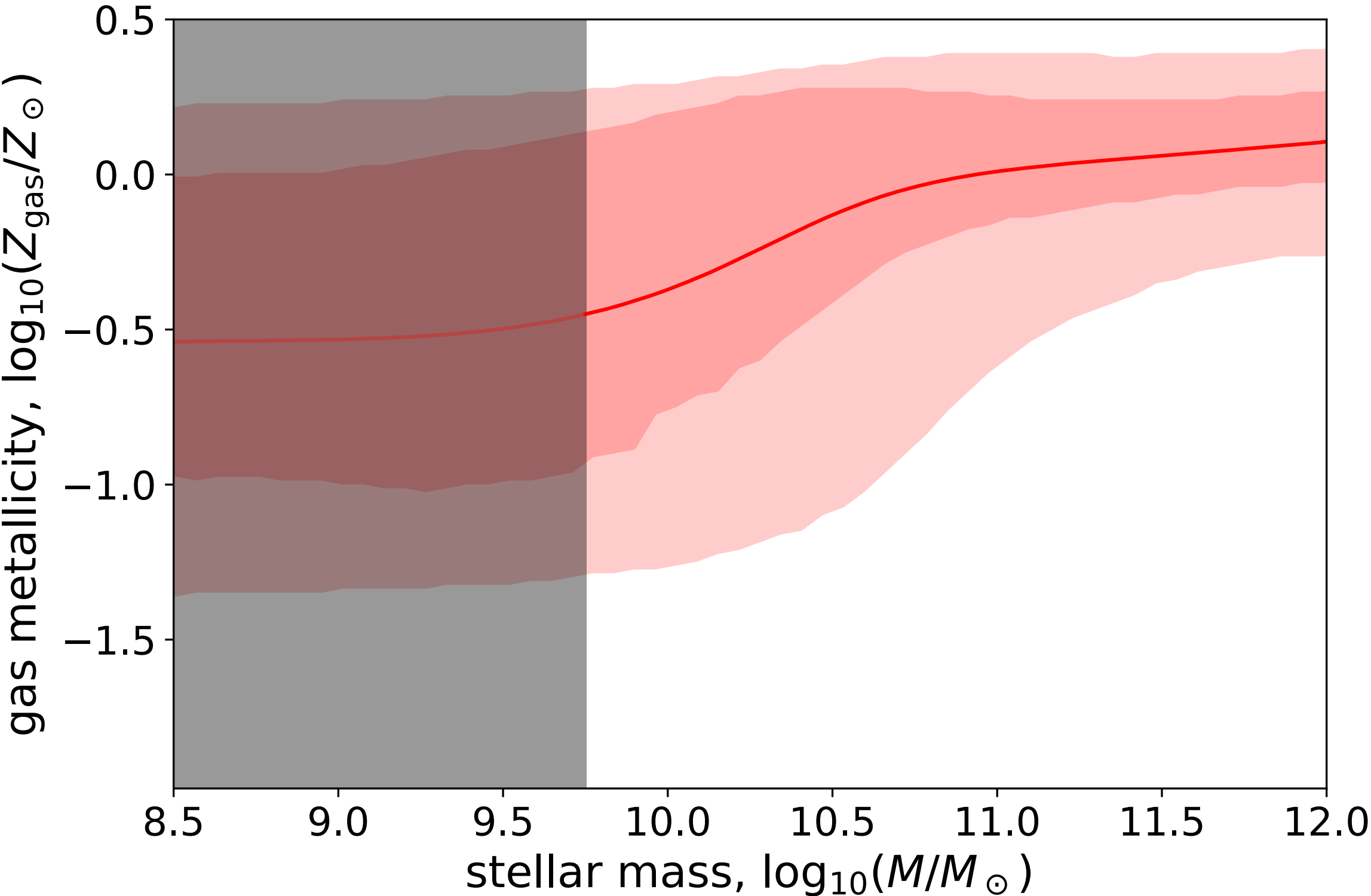
Mass-Metallicity Relation

Stellar metallicity vs. mass

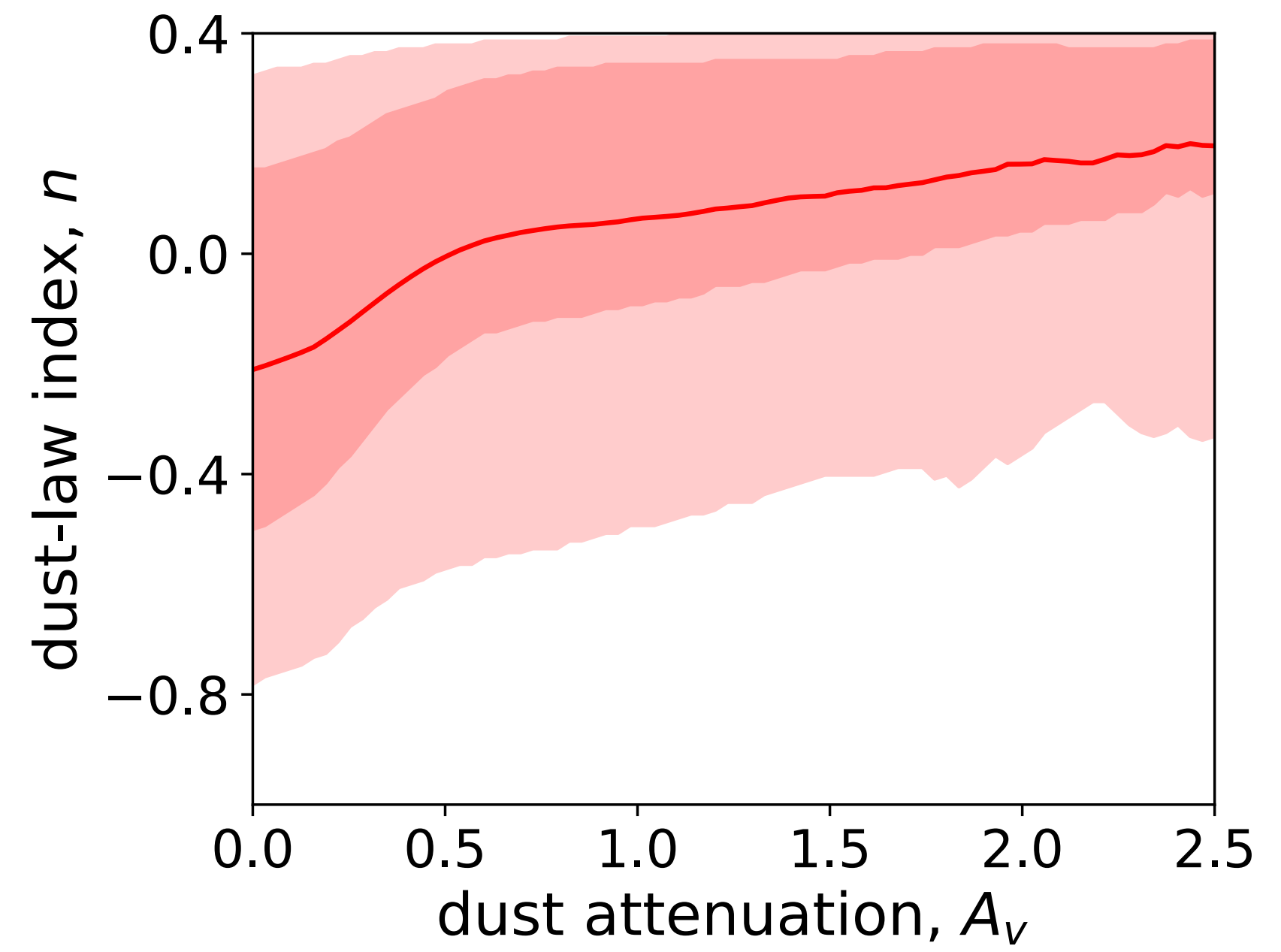
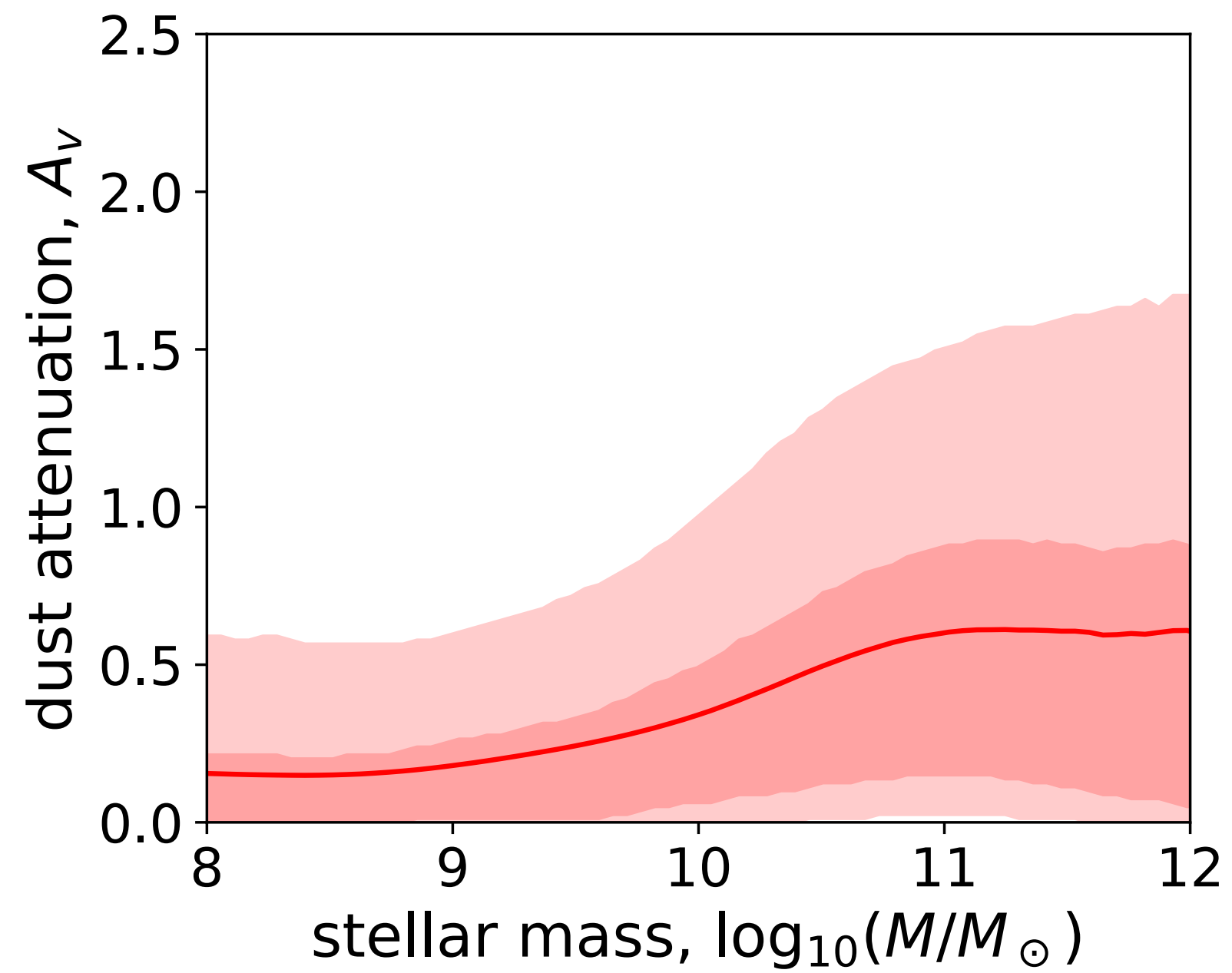
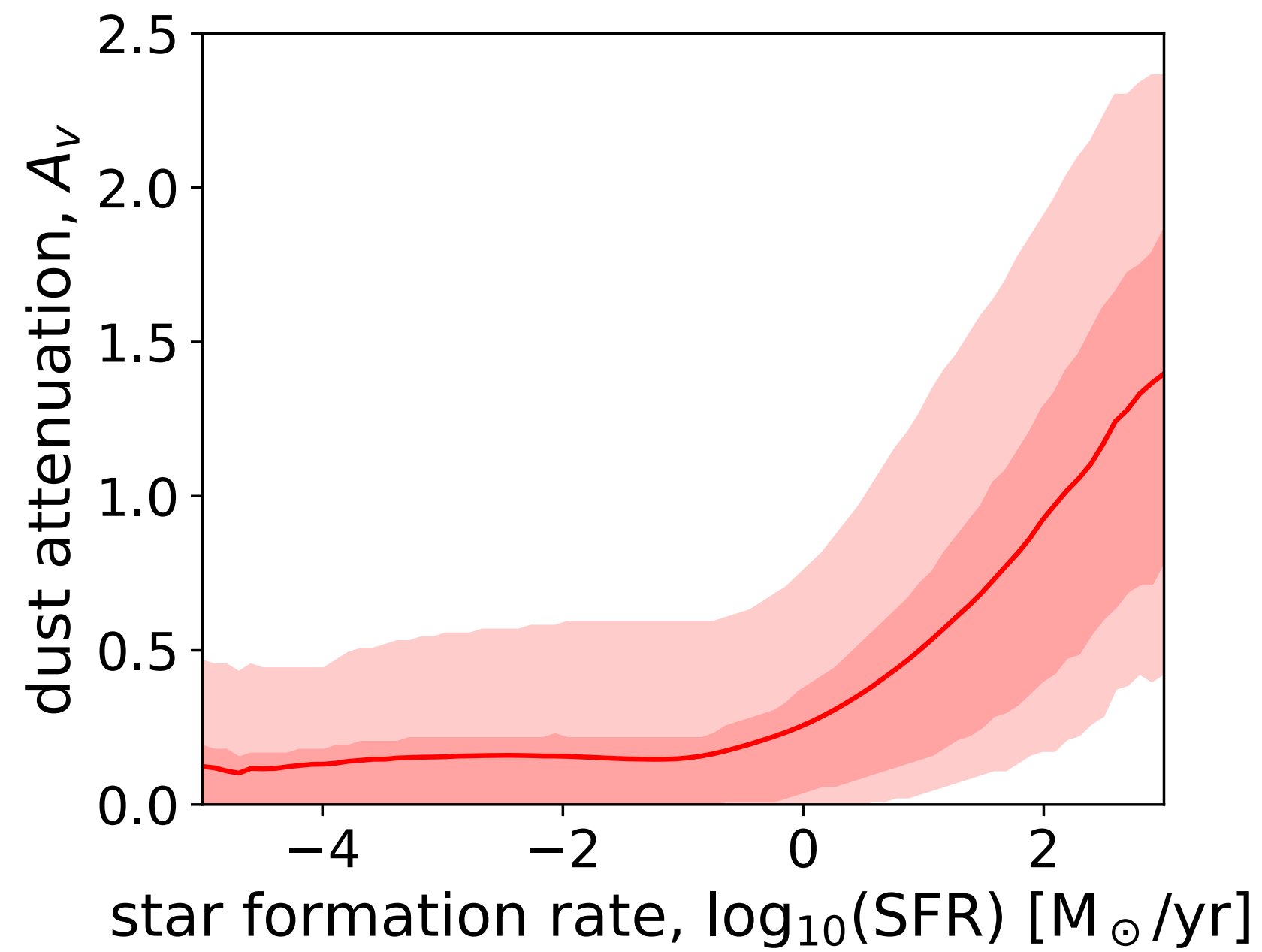


Mass-Metallicity Relation

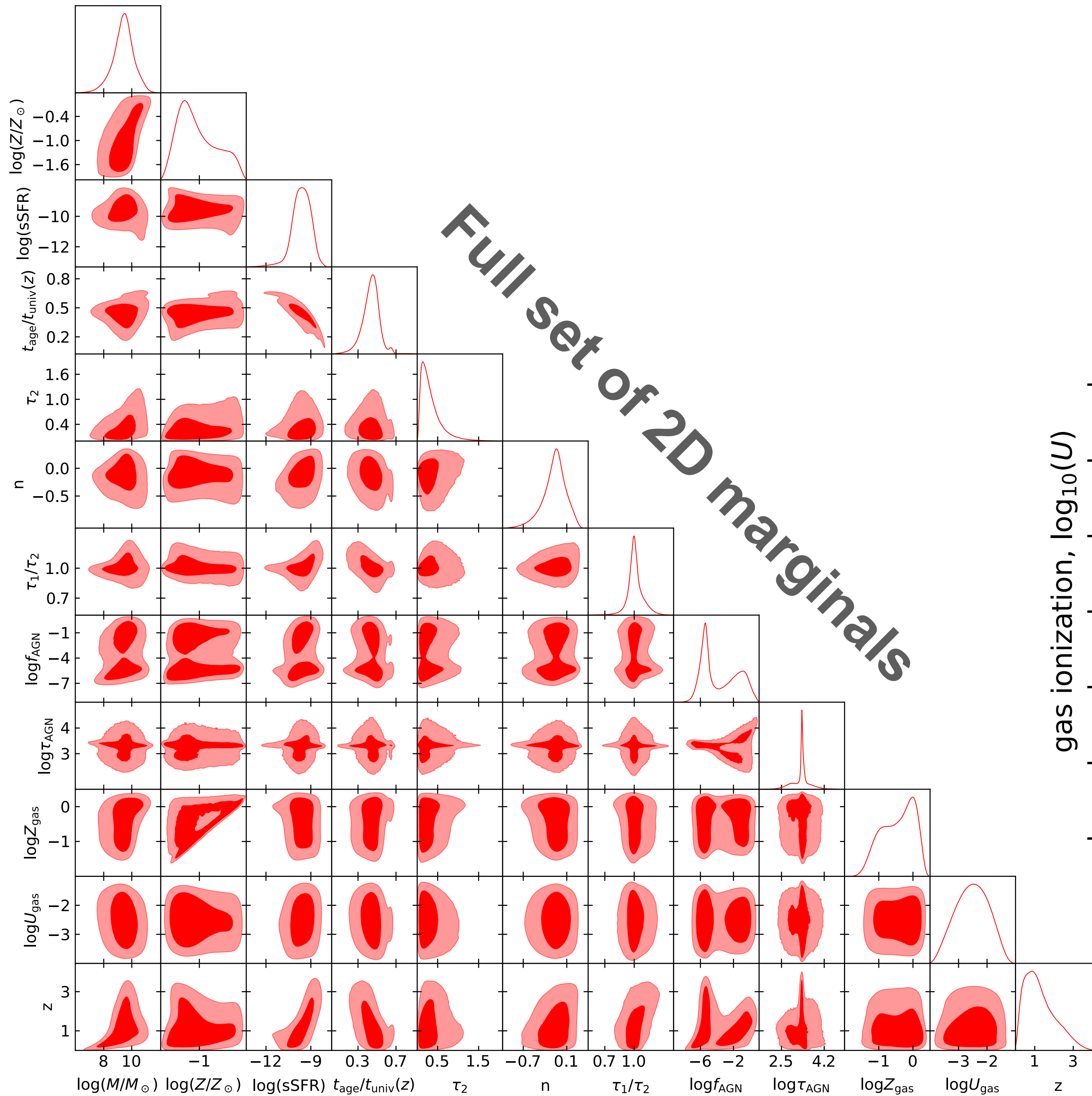
Gas metallicity vs. mass



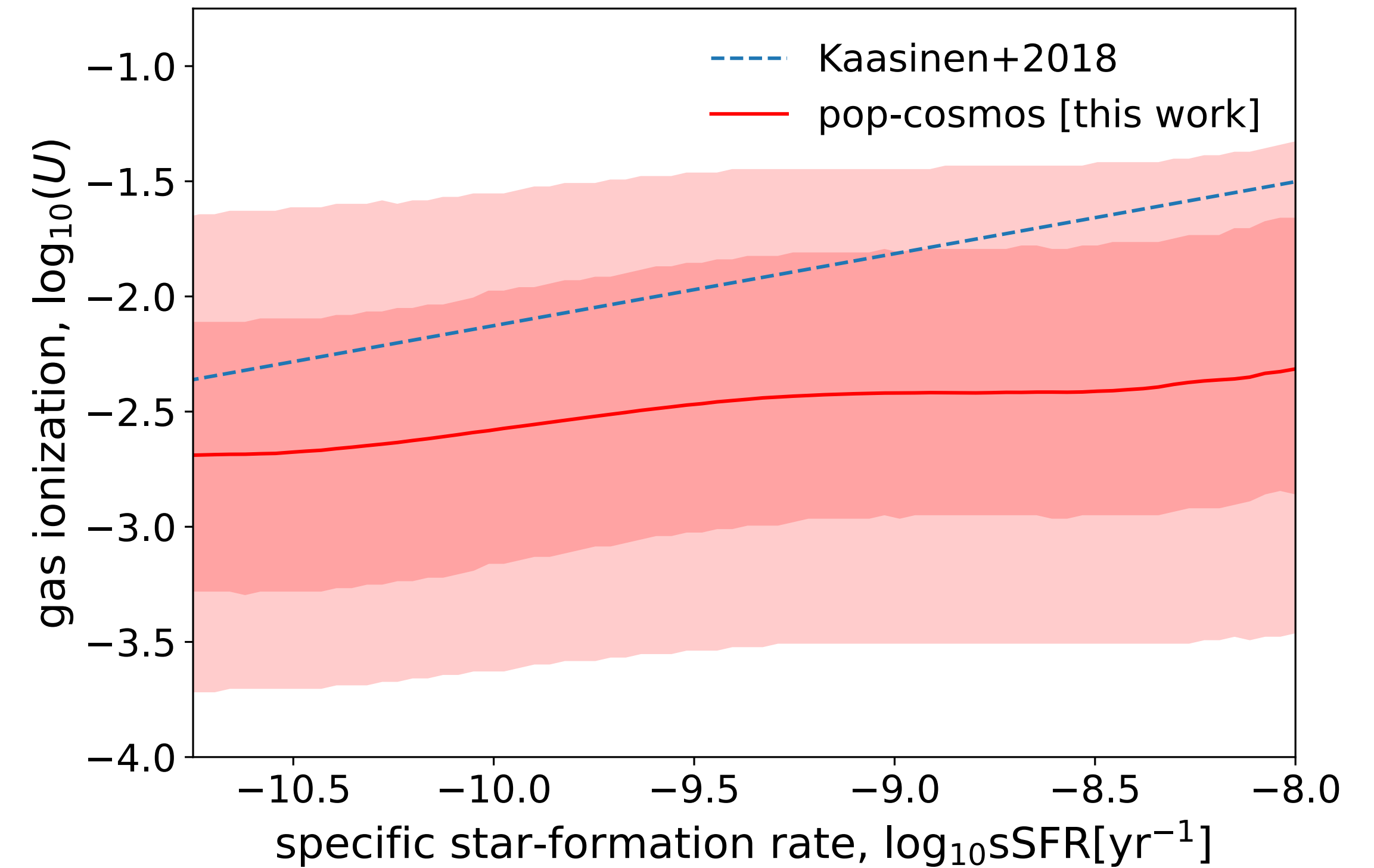
Dust



Even More Plots!



Gas ionisation



Validation

Data-space validation using Q-Q and P-P plots

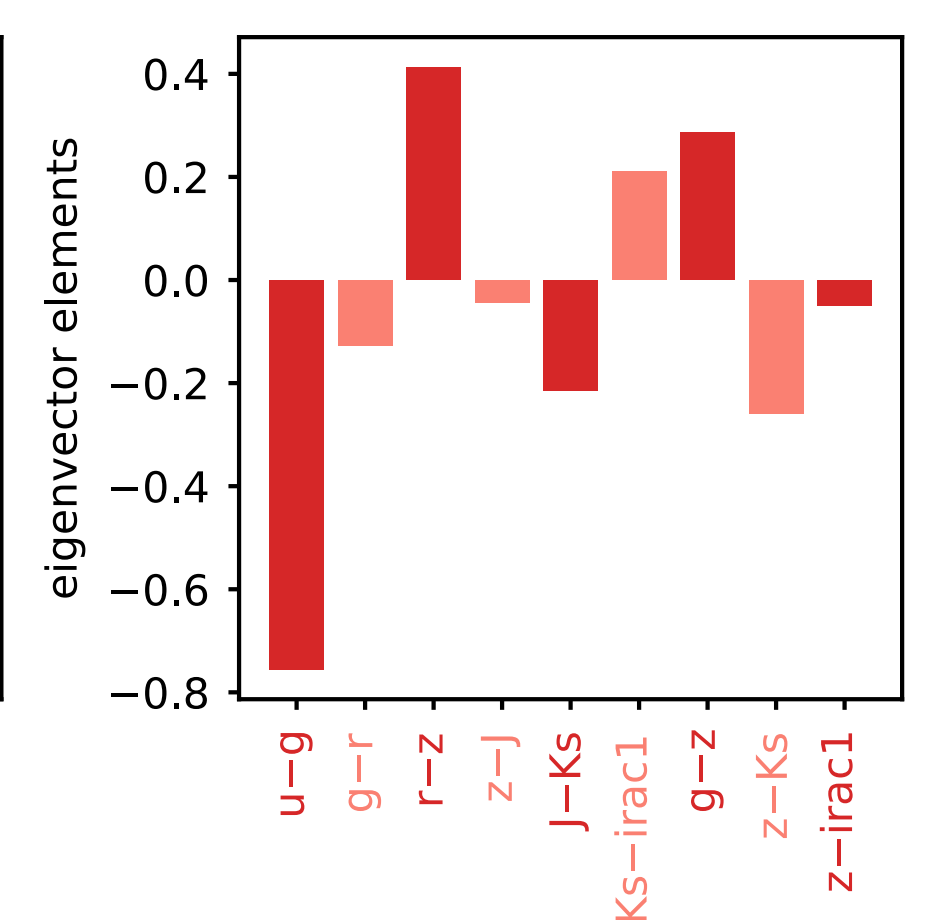
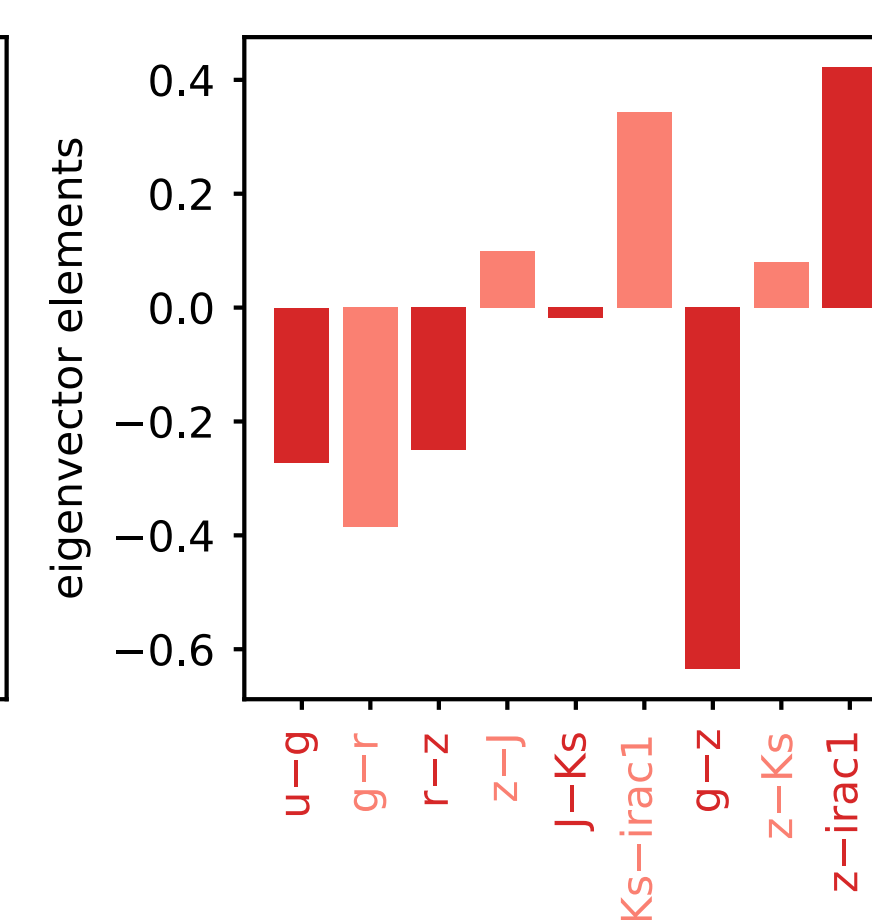
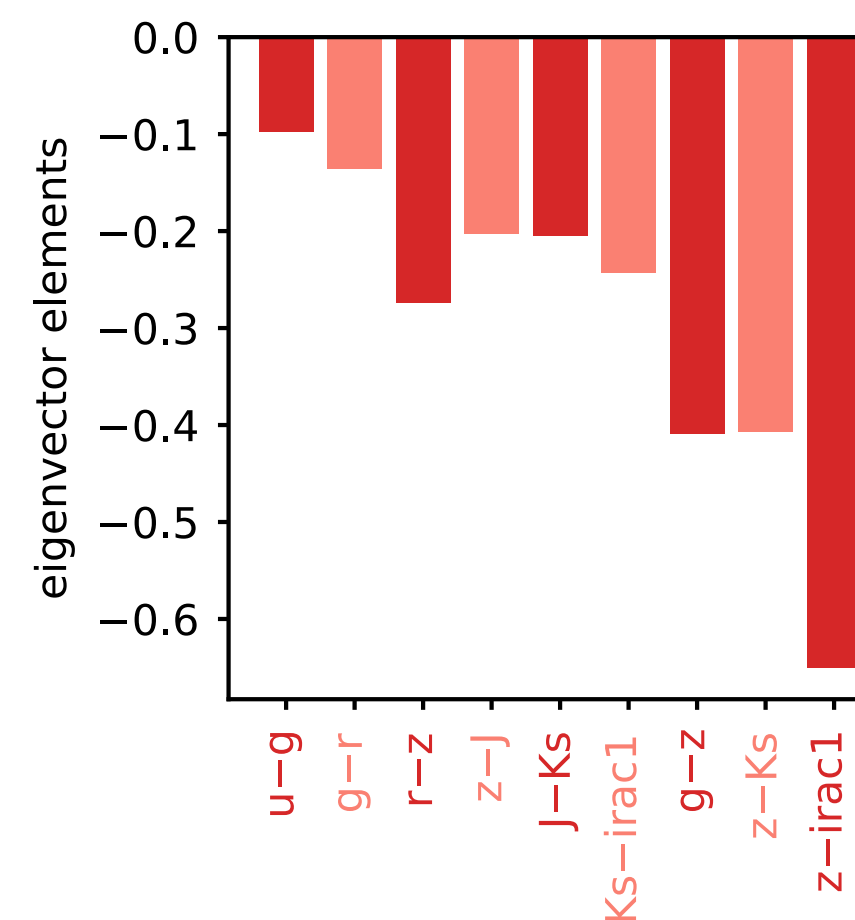
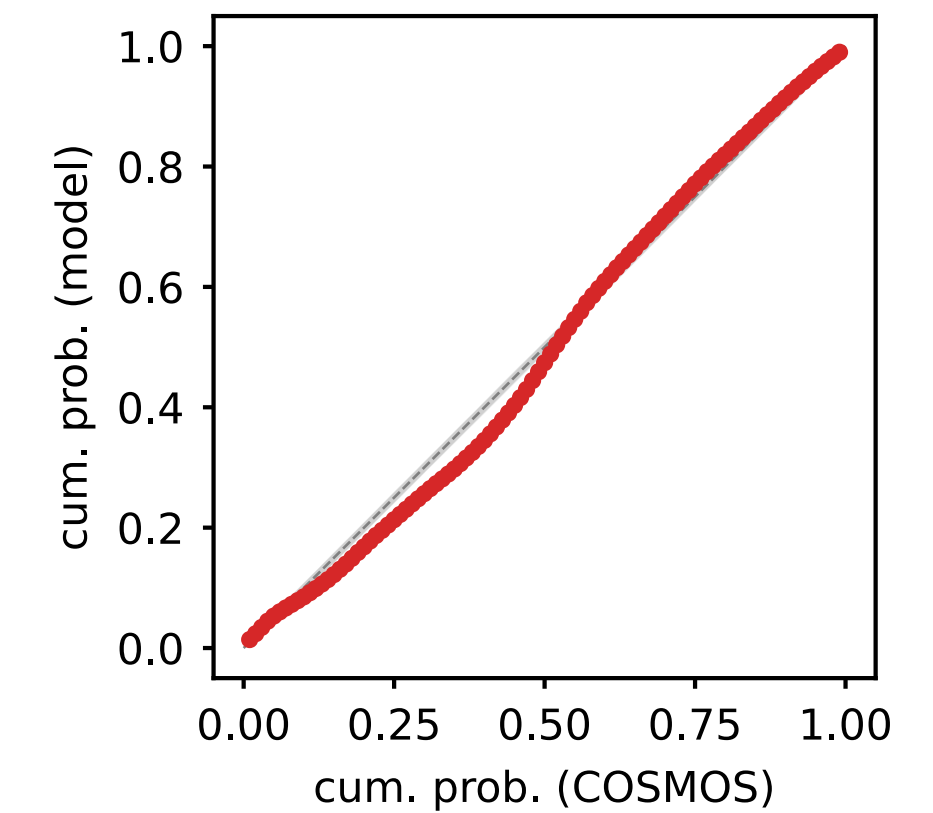
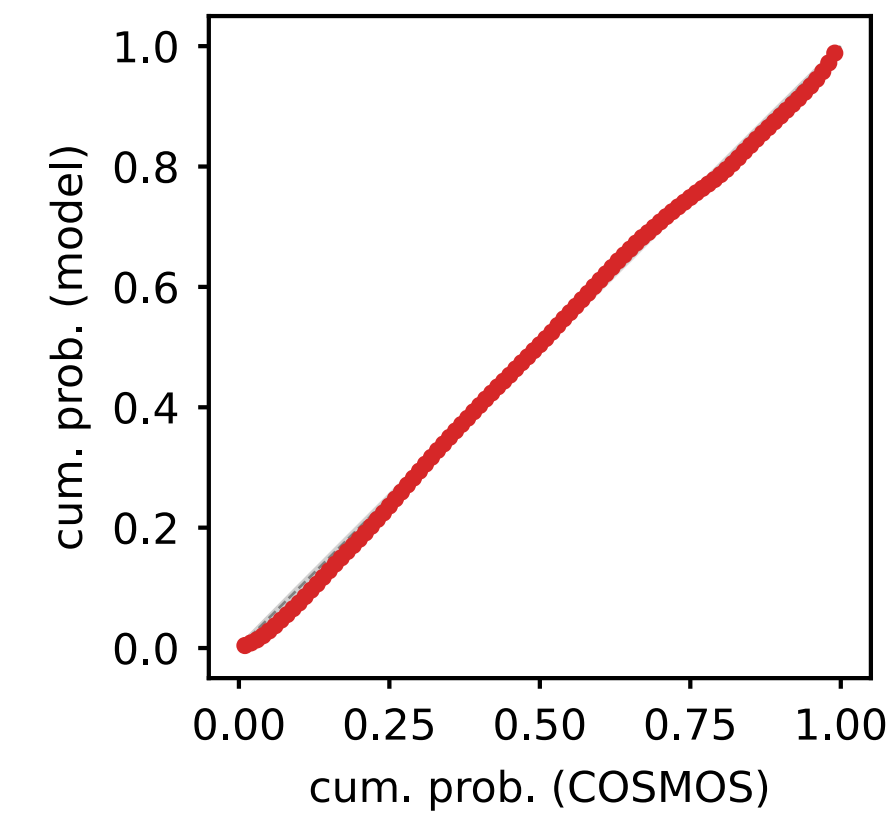
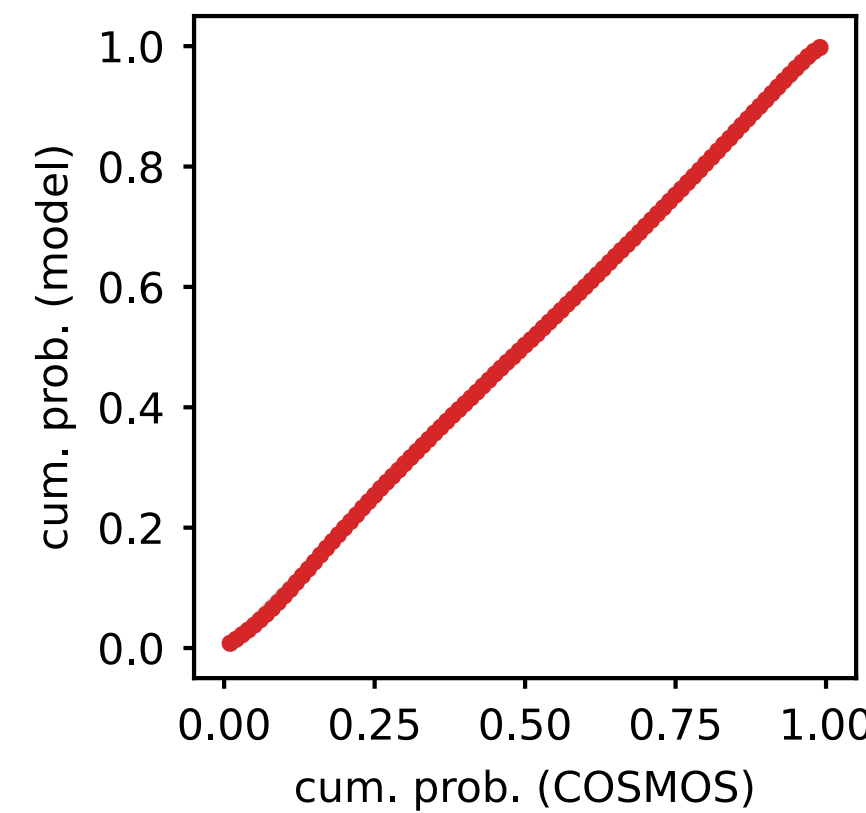
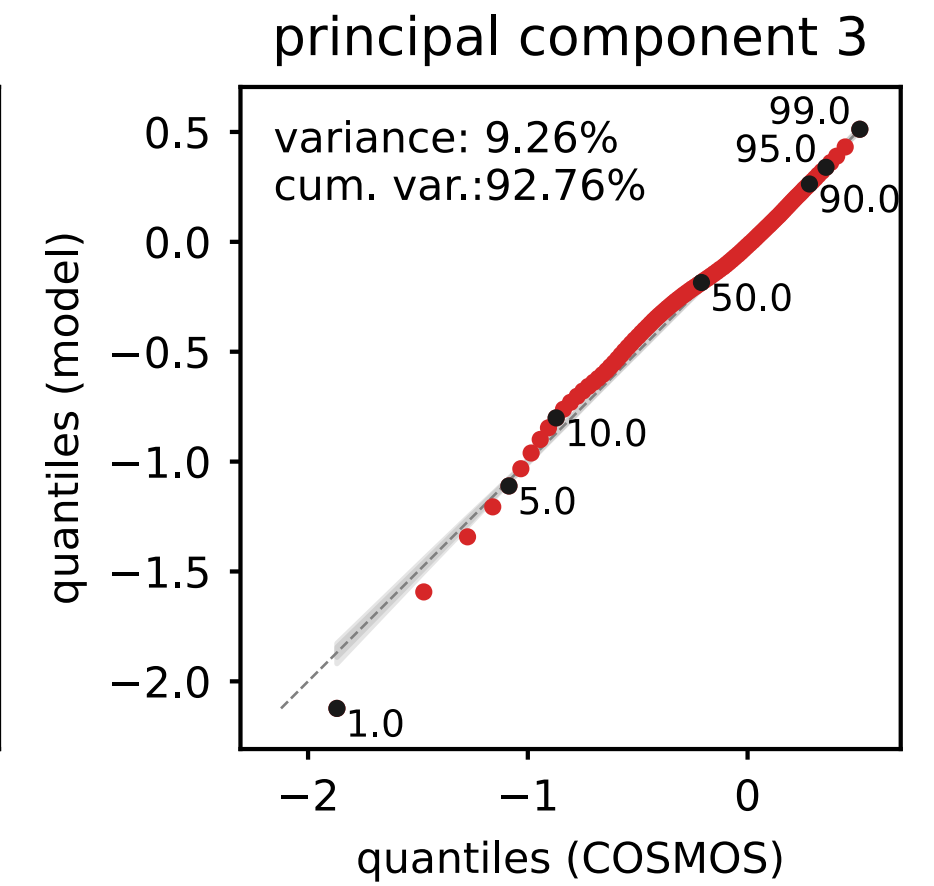
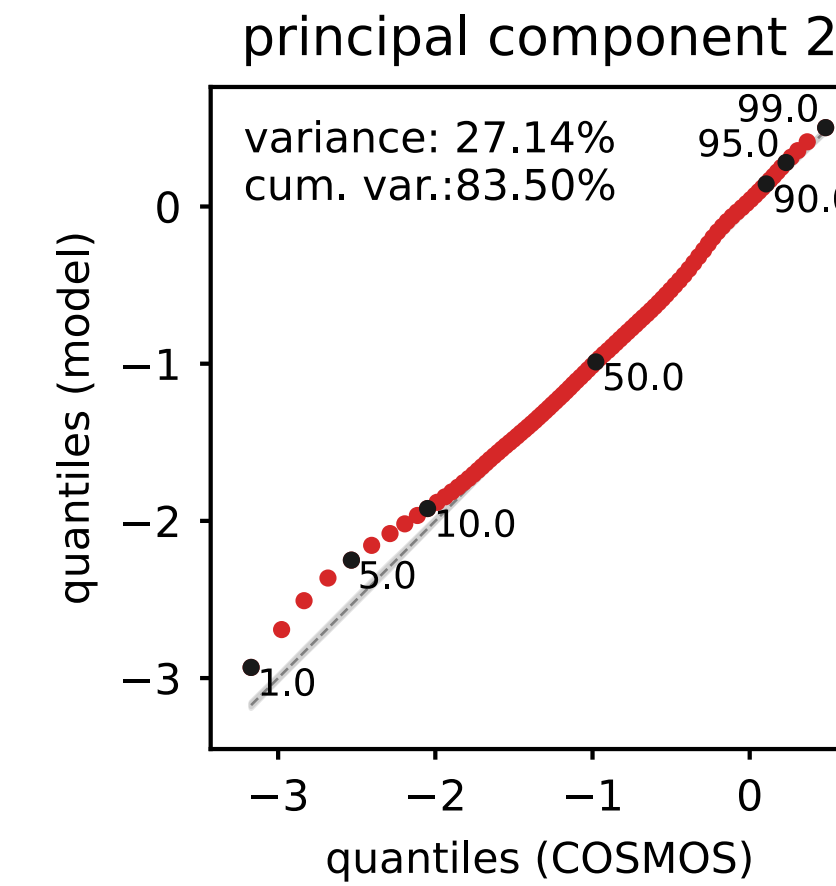
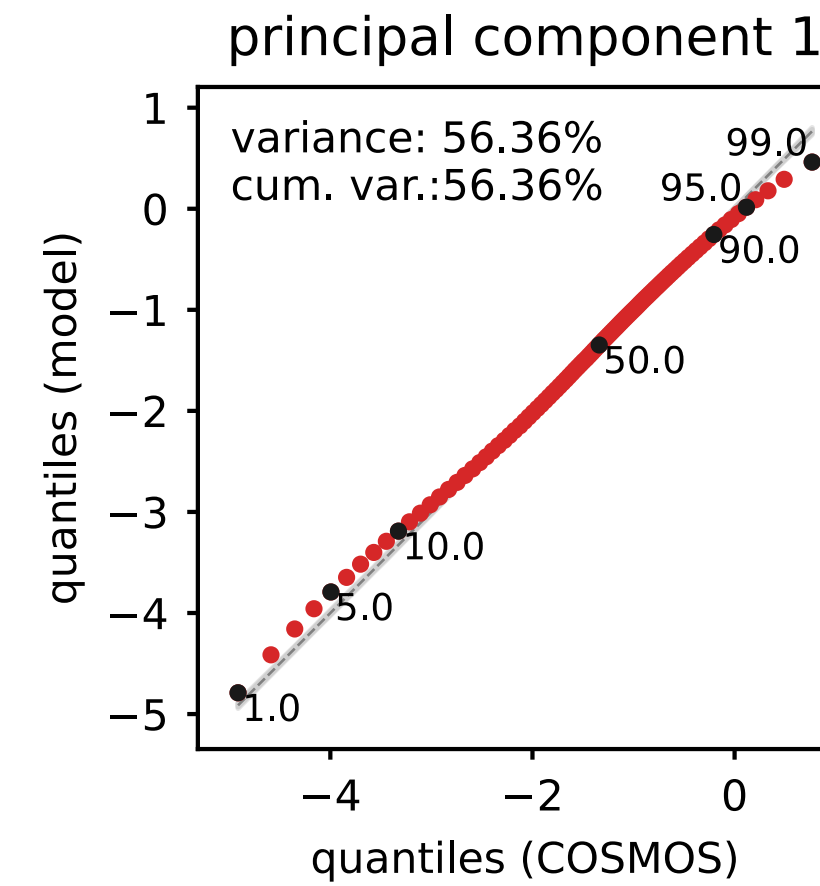
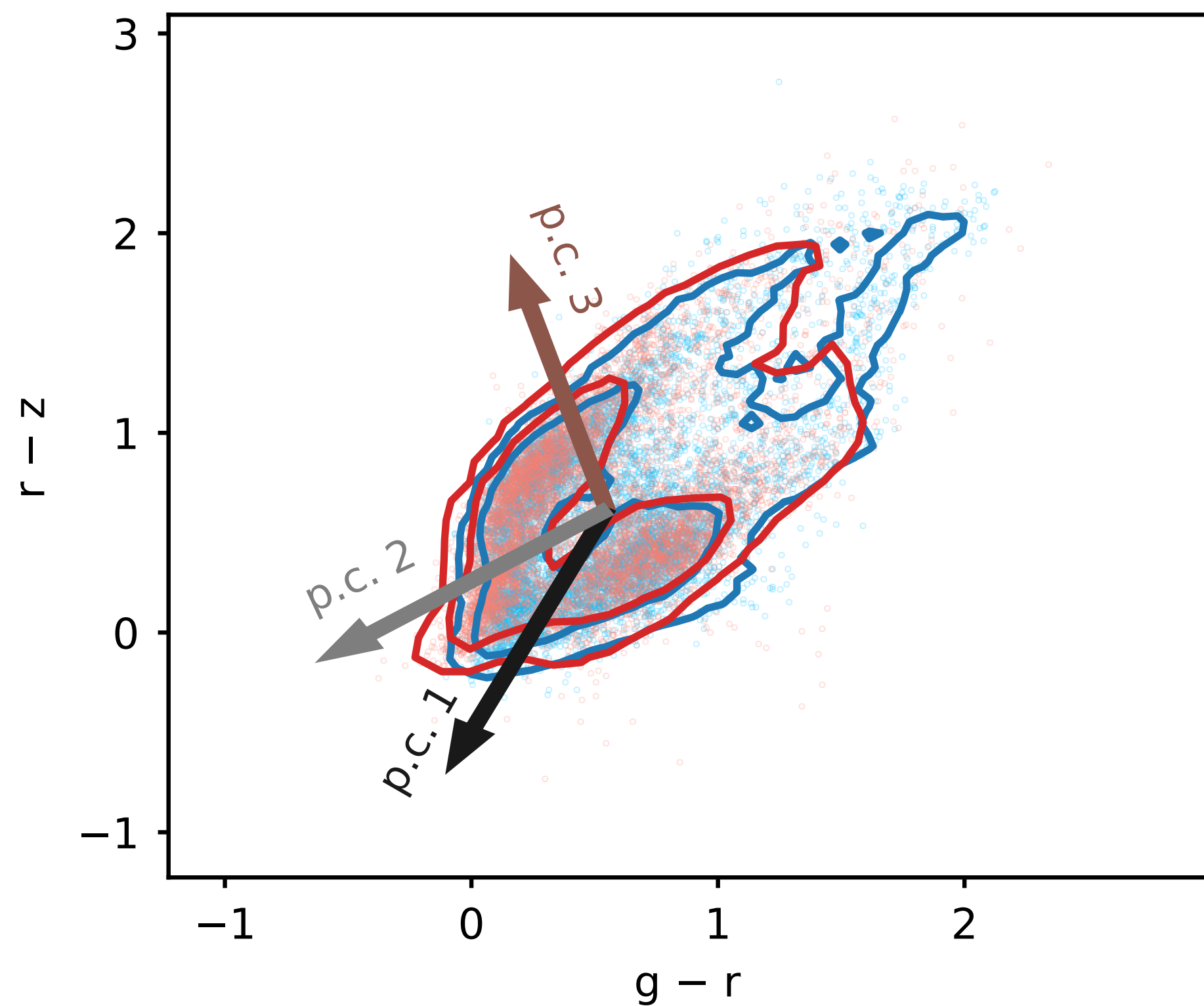
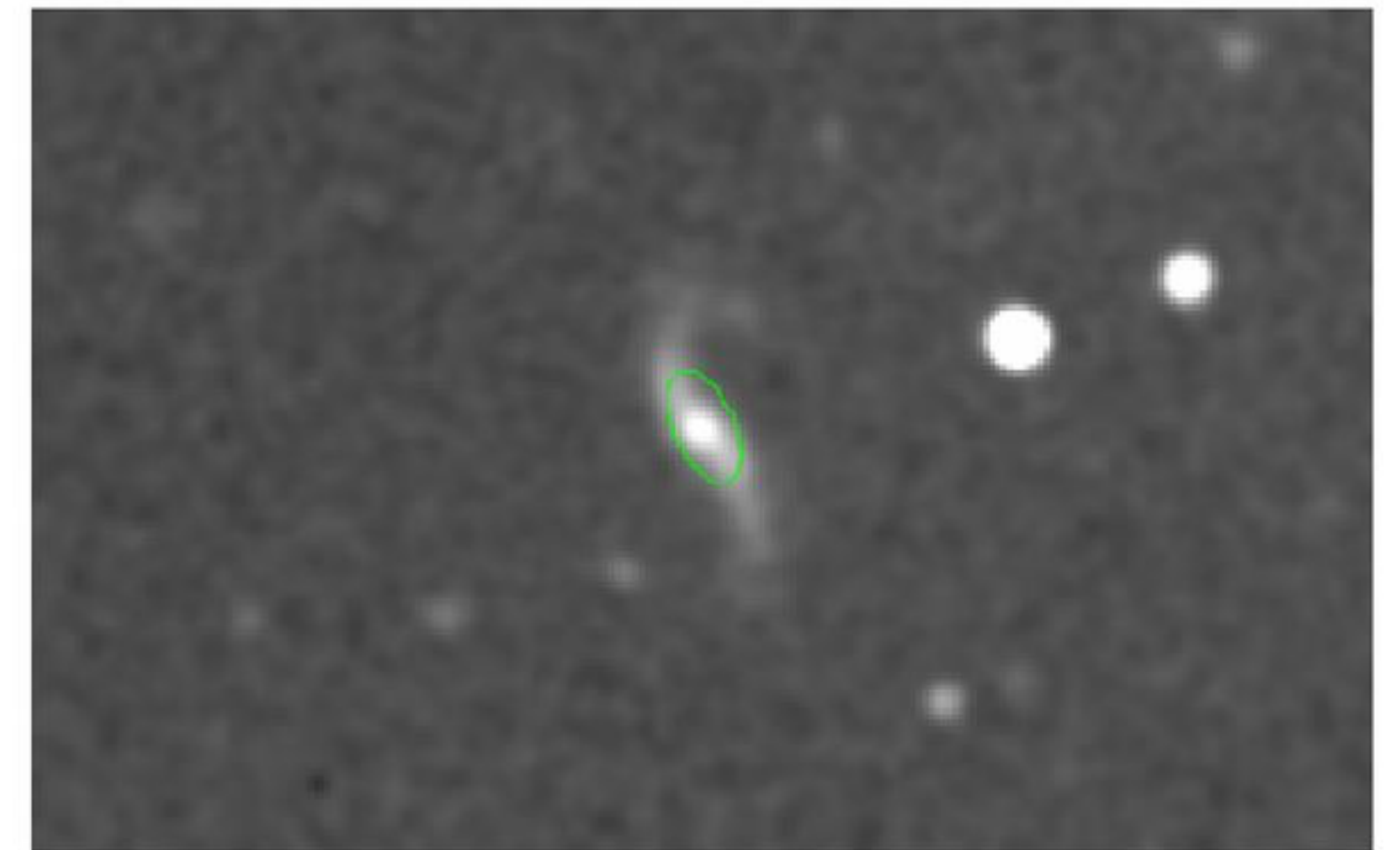


Image Based Selection

- Some galaxy surveys have image-level selection (e.g. based on shape, PSF)
- We can train a conditional density estimator $P(\text{image property} \mid \varphi)$ to learn a model for the relevant image-level summary statistics given SPS parameters
- Allows us to forward model these catalogs without simulating full images



KiDS: Kuijken et al. (2015)

Our stellar population synthesis parameters

\approx Prospector- α

$\varphi = [\log_{10}(M/M_{\odot}),$ stellar mass

$\Delta \log_{10}(\text{SFR}),$ star forming history ($\times 7$)

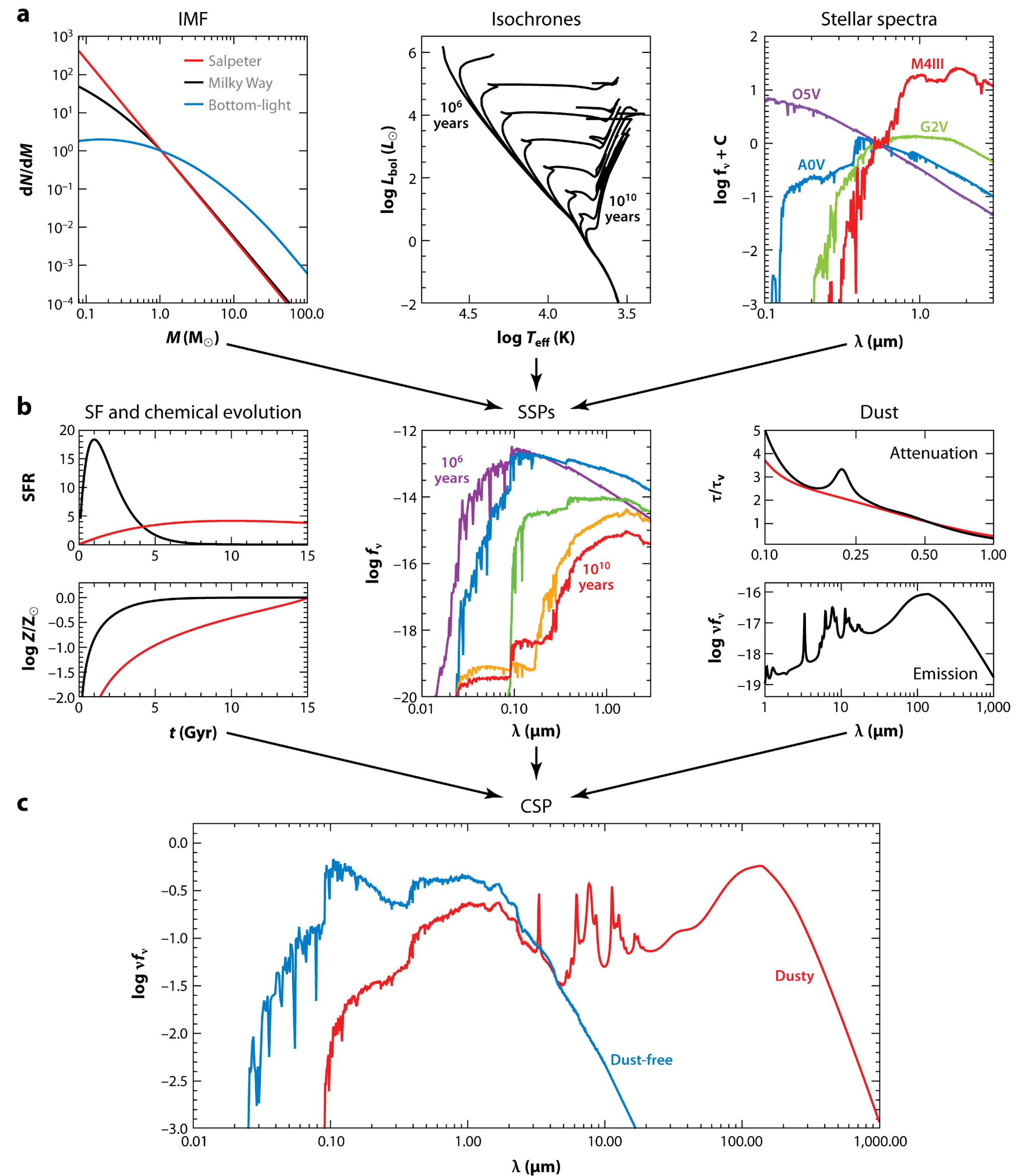
$\tau_1, \tau_2, n,$ dust attenuation

$\ln(f_{\text{AGN}}), \ln(\tau_{\text{AGN}}),$ active galactic nuclei

$\log_{10}(Z/Z_{\odot}),$ stellar metallicity

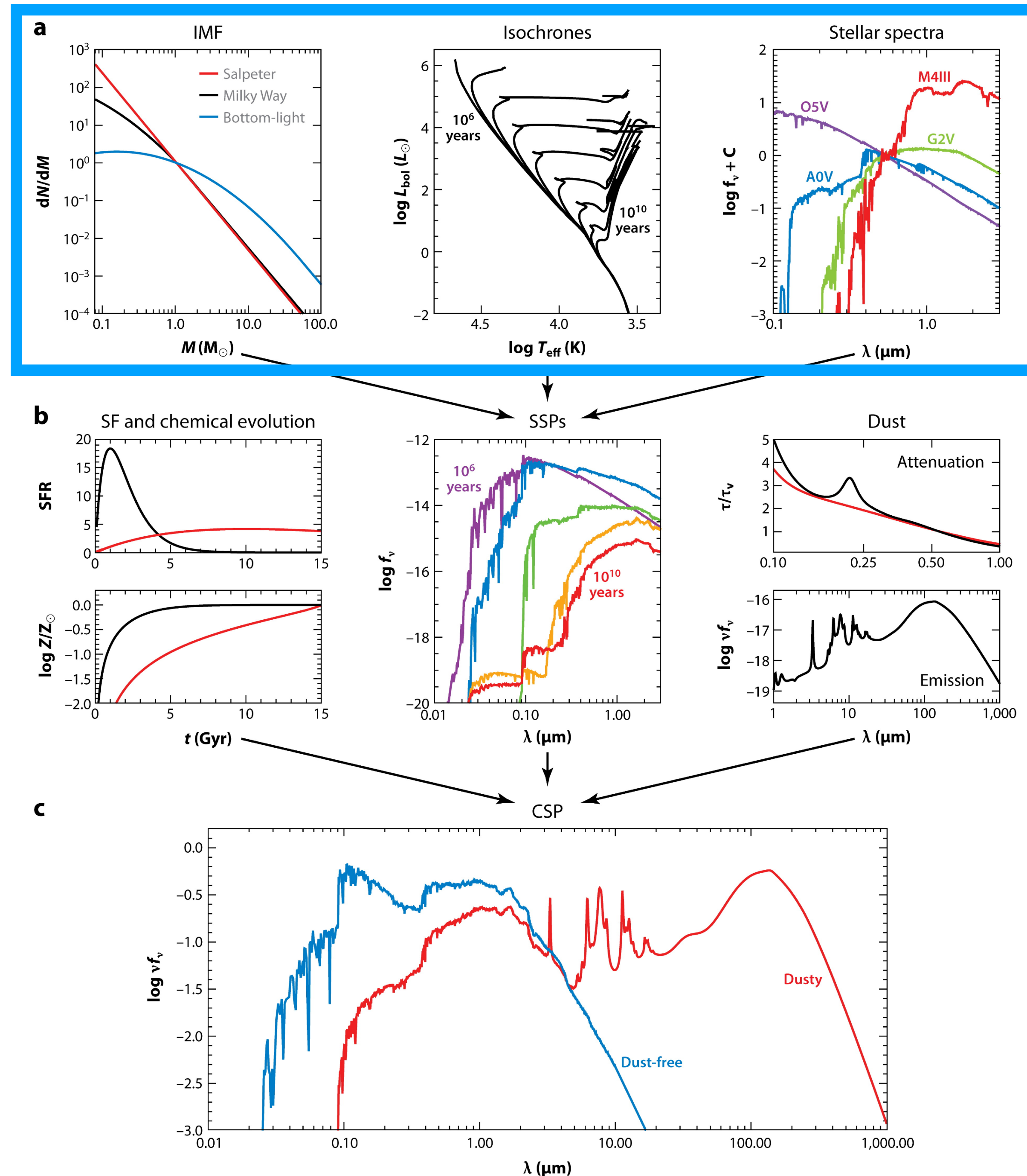
$\log_{10}(Z_{\text{gas}}/Z_{\odot}), \log_{10}(U_{\text{gas}})]$ gas metallicity + ionisation

What goes into stellar population synthesis?



What goes into stellar population synthesis?

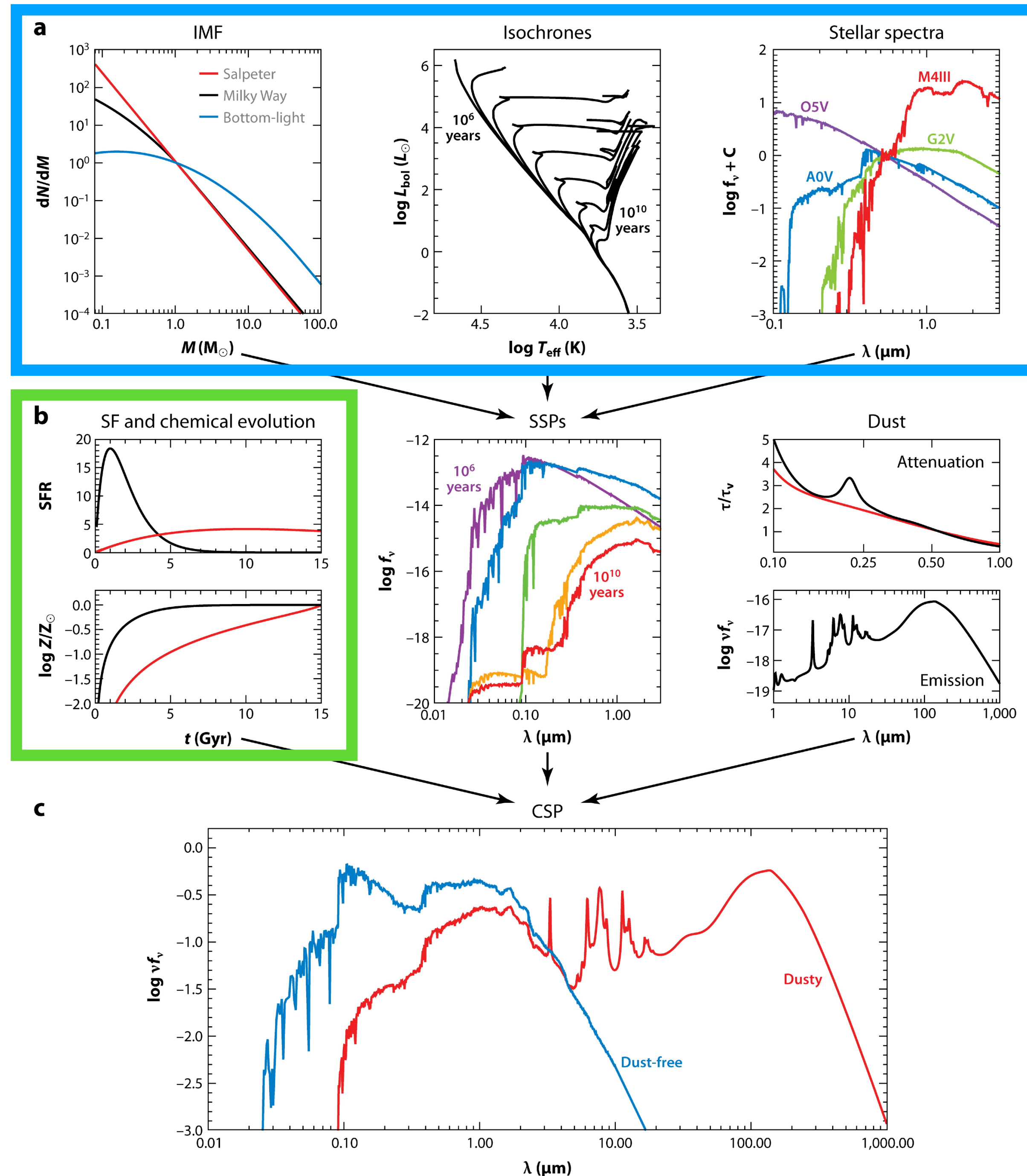
Assembly of simple stellar populations from initial mass function, isochrones, and stellar spectra



What goes into stellar population synthesis?

Assembly of simple stellar populations from initial mass function, isochrones, and stellar spectra

Star formation history / evolution

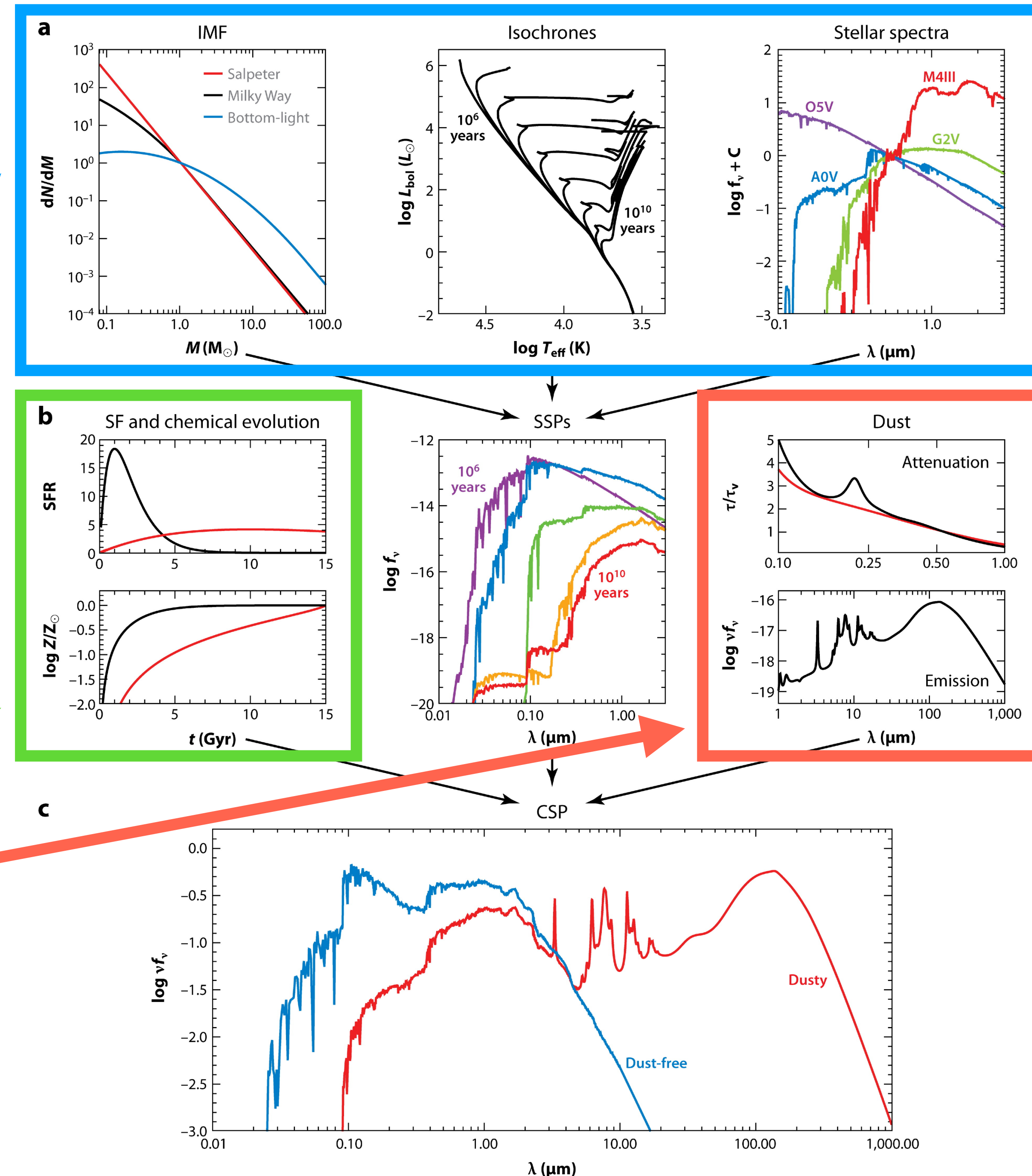


What goes into stellar population synthesis?

Assembly of simple stellar populations from initial mass function, isochrones, and stellar spectra

Star formation history / evolution

Dust attenuation and emission



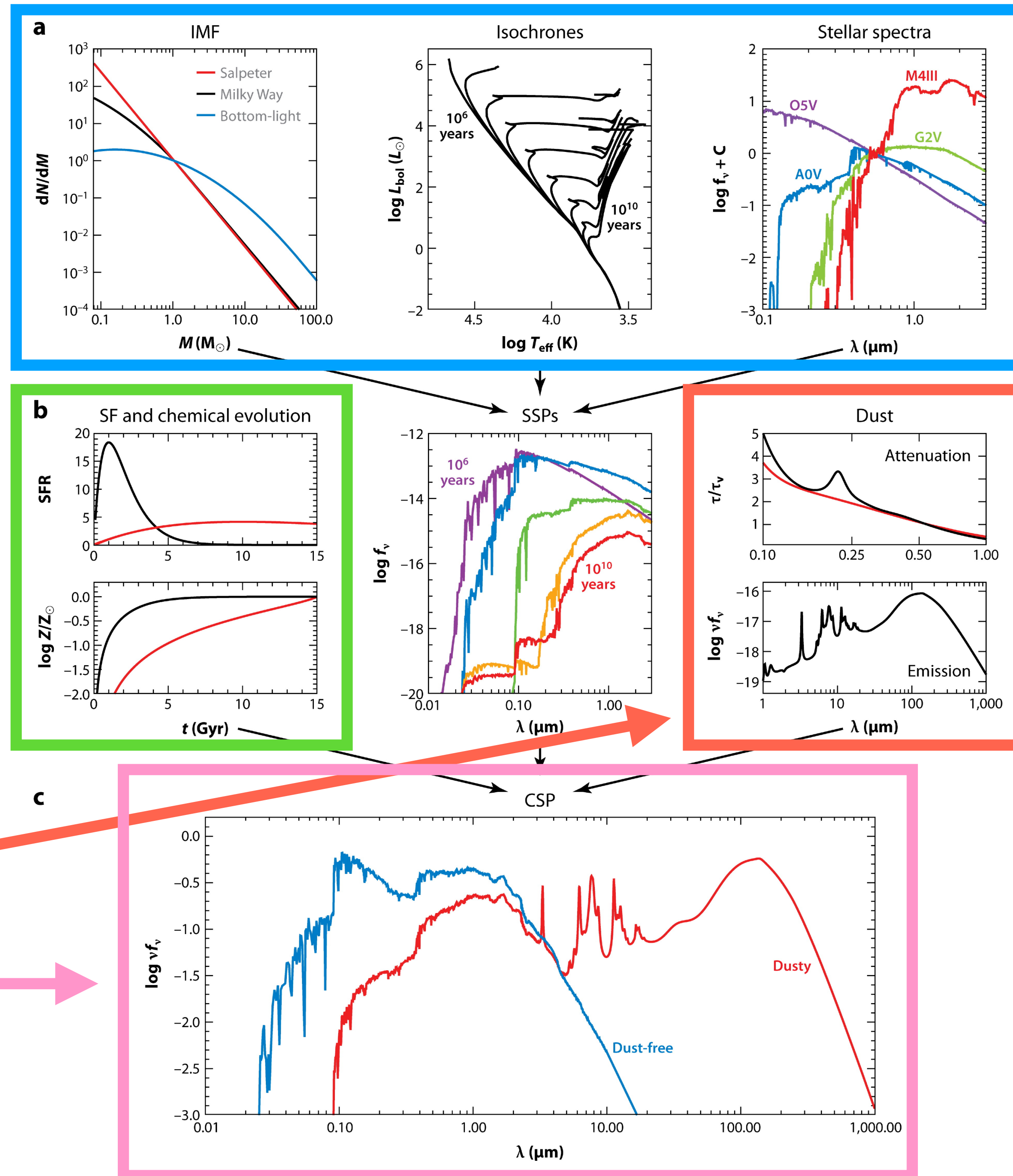
What goes into stellar population synthesis?

Assembly of simple stellar populations from initial mass function, isochrones, and stellar spectra

Star formation history / evolution

Dust attenuation and emission

Assembly of composite stellar populations



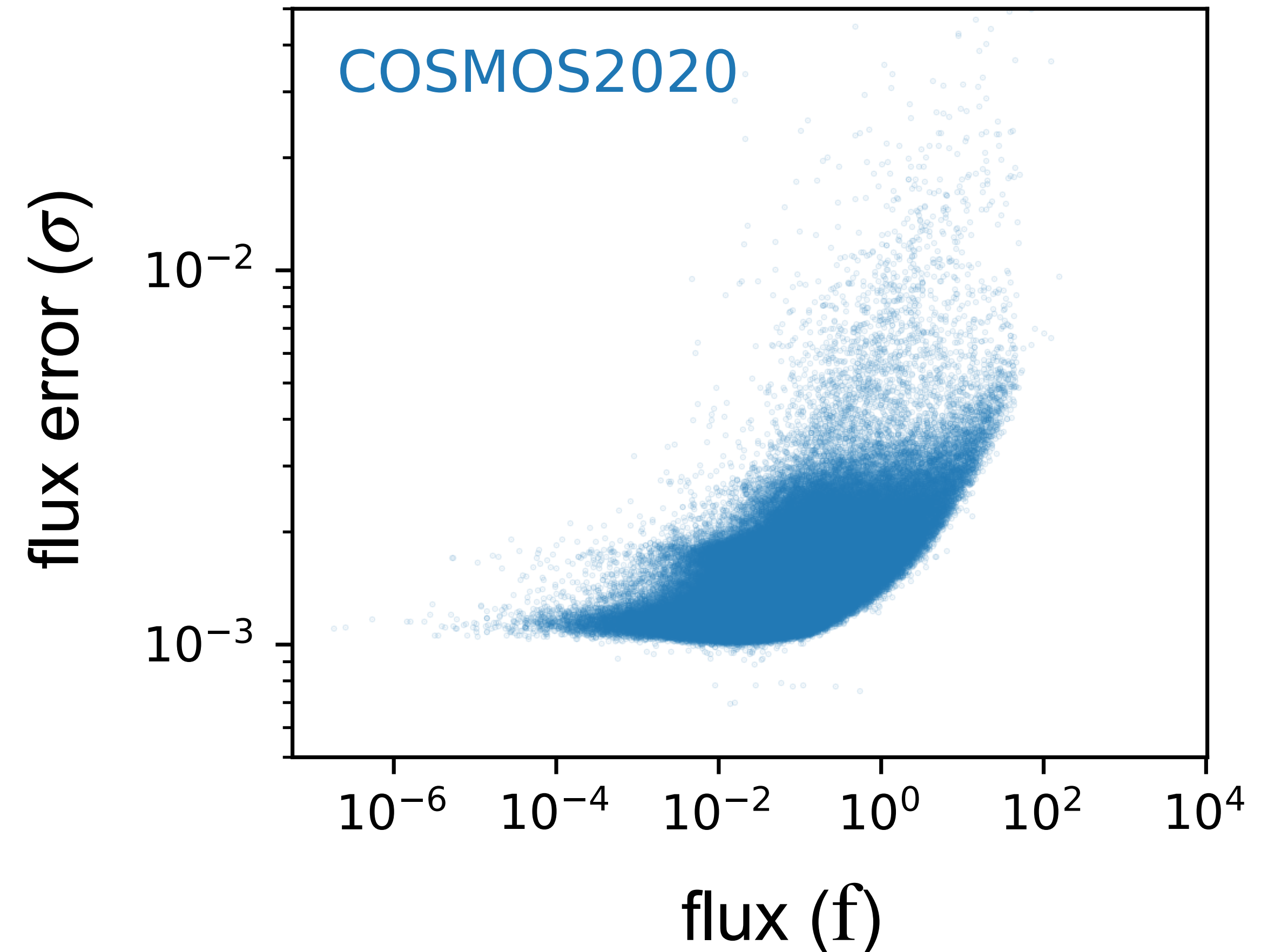
Our uncertainty model

Mixture density network (see Bishop 2006)

$$\mathbf{s} \sim N(0,1)$$

$$\sigma = \mu(\mathbf{f}) + \Sigma(\mathbf{f}) \odot \mathbf{s}$$

↑
dense neural network
(2 layers, 128 hidden
units, tanh activation)



More on diffusion models

Variance-exploding SDE

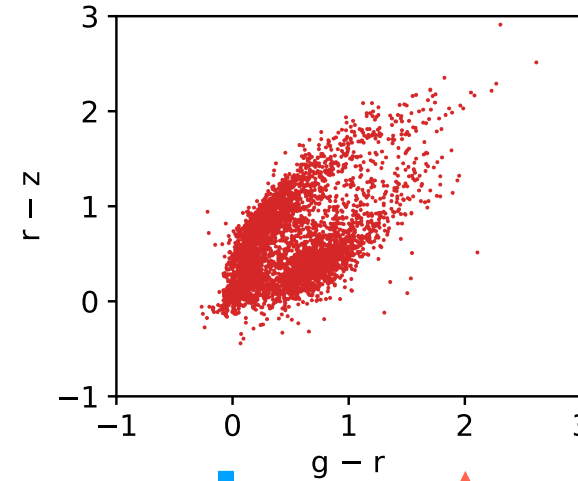
$$\mathbf{x}(t = 0) \sim P_0(\mathbf{x}) \equiv P(\varphi, z)$$

$$\downarrow \text{forward}$$
$$d\mathbf{x} = g(t) d\mathbf{w}$$

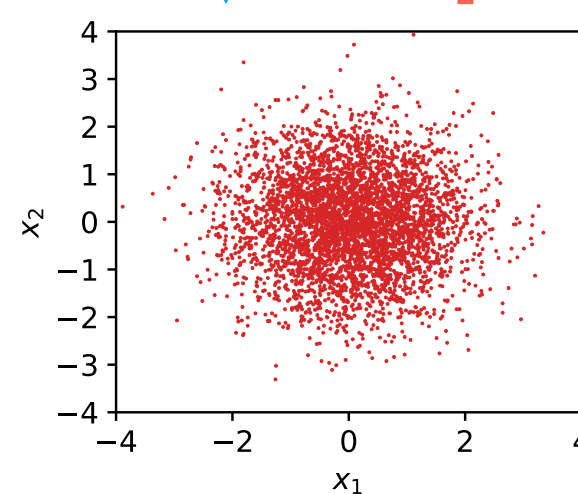
$$\mathbf{x}(t = T) \sim P_T(\mathbf{x}) \equiv N(0, 1)$$

reverse

$$d\mathbf{x} = -\frac{1}{2}g^2(t) \nabla_{\mathbf{x}} P_t(\mathbf{x}) dt$$



$$\downarrow$$



$$s(\mathbf{x}, t) = \nabla_{\mathbf{x}} P_t(\mathbf{x}) \quad \text{score function}$$

$$d\mathbf{x} = g(t) d\mathbf{w} \quad \text{Brownian motion } (\mathbf{w})$$

$$d\mathbf{x} = -\frac{1}{2}g^2(t) \nabla_{\mathbf{x}} P_t(\mathbf{x}) dt$$

$$g^2(t) = \frac{d\sigma^2(t)}{dt}$$

$$\sigma(t) = \sigma_0(\sigma_T/\sigma_0)^{t/T}$$

$$\sigma_0 = 0.01, \sigma_T = 6, T = 1$$