Towards a Pixel TPC: construction and test of a 32 chip GridPix detector

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9 Abstract

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A Time Projection Chamber module with 32 GridPix chips was constructed and 10 the performance was measured using data taken in a test beam at DESY in 2012. 11 The GridPix chips each consist of a Timepix3 chip with integrated amplification 12 grid and have a high efficiency to detect single ionisation electrons. In the 13 test beam setup, the module was placed in between two sets of Mimosa silicon 14 detector planes that provided external high precision tracking and the whole 15 detector setup was slided into the PCMAG magnet at DESY. The analysed 16 data were taken at electron beam energies of 5 and 6 GeV and at magnetic 17 fields of 0 and 1 $\text{Tesla}(\mathbf{T})$. 18

The result for the transverse diffusion coefficient D_T is $287 \,\mu\text{m}/\sqrt{cm}$ at B = 19 0 T and D_T is $121 \,\mu\text{m}/\sqrt{cm}$ at B = 1 T. The longitudinal diffusion coefficient 20 D_L is measured to be $268 \,\mu\text{m}/\sqrt{cm}$ at B = 0 T and $252 \,\mu\text{m}/\sqrt{cm}$ at B = 1 T. 21 Results for the tracking systematical uncertainties in xy were measured to be 22 smaller than 14 µm with and without magnetic field. The tracking systematical 23 uncertainties in z were smaller than $14 \,\mu\text{m}$ (B = 0 T) and $22 \,\mu\text{m}$ (B = 1 T). 24 Finally, the result for the dEdx resolution for a MIP particle based on a 1 meter 25 track and a realistic GridPix coverage of 60% was measured to be 4% in a 1 T 26 magnetic field. 27

28 Keywords: Micromegas, gaseous pixel detector, micro-pattern gaseous

September 28, 2023

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30 1. Introduction

Earlier publications on a single chip [1] and four chip (quad) GridPix detectors [2] showed the potential of the GridPix technology and the large range of applications for these devices [3]. In particular, it was demonstrated that single ionisation electrons can be detected with high efficiency and great precision, allowing an excellent track 3D position measurements and particle identification based on the number of electrons and clusters.

As a next step towards a Pixel Time Projection Chamber for a future collider experiment [4], [5], a module consisting of 32 GridPix chips based on the Timepix3 chip was constructed.

⁴⁰ A GridPix detector consists of a CMOS pixel Timepix3 chip [6] with in-⁴¹ tegrated amplification grid added by MEMS postprocessing techniques. The ⁴² Timepix3 chip can be operated with a low threshold of 515 e^- , and has a low ⁴³ equivalent noise charge of about 70 e^- . The GridPix single chip and quad de-⁴⁴ tectors have a very fine granularity of 55 µm × 55 µm and a high efficiency to ⁴⁵ detect single ionisation electrons.

⁴⁶ Based on the experience gained with these detectors a 32 GrixPix chip mod⁴⁷ ule - consisting of 8 quads - was built. A drift box defining the electric field
⁴⁸ and gas envelop was constructed. A readout system for up to 128 chips with 4
⁴⁹ multiplexers readout by one speedy pixel detector readout board was designed.
⁵⁰ After a series of tests using the laser setup in the laboratory at Nikhef [7], the
⁵¹ detector was taken to DESY for a two week test beam campaign.

At DESY the 32 chip detector was placed in between two sets of Mimosa silicon detector planes and mounted on a movable stage. The whole detector setup was slided into the centre of the PCMAG magnet at DESY. A trigger was provided by a scintillator counter. The data were taken at different stage positions and electron beam energies of 5 and 6 GeV and at magnetic fields of 0 and 1 Tesla(T). The performance of the 32 GrixPix chip module was measured

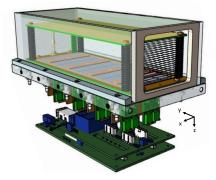


Figure 1: Schematic 3-dimensional render of the 8-quad module detector for illustration purposes.

⁵⁸ using these data sets.

59 1.1. 32 GridPix chip module

A 32 GrixPix chip module was built using the quad module [2] as a basic 60 building block. The quad module consists of four GridPix chips and is optimised 61 for a high fraction of sensitive area of 68.9%. The external dimensions are 62 $39.6 \,\mathrm{mm} \times 28.38 \,\mathrm{mm}$. The four chips which are mounted on a cooled base plate 63 (COCA), are connected with wire bonds to a common central 6 mm wide PCB. 64 A 10 mm wide guard electrode is placed over the wire bonds 1.1 mm above the 65 aluminium grids, in order to prevent field distortions of the electric drift field. 66 The guard is the main inactive area, and its dimensions are set by the space 67 required for the wire bonds. On the back side of the quad module, the PCB 68 is connected to a low voltage regulator. The aluminium grids of the GridPixes 69 are connected by 80 µm insulated copper wires to a high voltage (HV) filtering 70 board. The quad module consumes about 8 W of power of which 2 W is used in 71 the LV regulator. 72

Eight quad mdules were embedded in a box, resulting in a GridPix module with a total of 32 chips. A schematic 3-dimensional drawing of the detector is shown in Figure 1. A schematic drawing of the quads in the module is shown in Figure 2, where also the beam direction is indicated.

The internal dimensions of the box are 79 mm along the x-axis, 192 mm along 77 the y-axis, and $53 \,\mathrm{mm}$ along the z-axis (drift direction), and it has a maximum 78 drift length (distance between cathode and readout anode) of 40 mm. The drift 79 field is shaped by a series of parallel CuBe field wires of 50 µm diameter with a 80 wire pitch of 2 mm and guard strips are located on all of the four sides of the 81 active area. In addition, six guard wires - shown with dashed line in Figure 2 82 are suspended over the boundaries of the chips, where no guard is present, to 83 _ minimize distortions of the electric drift field. The wires are located at a distance 84 of 1.15 mm from the grid planes, and their potential is set to the potential at 85 this drift distance. The box has two Kapton 50 µm windows to allow the beam 86 to pass with minimal multiple scattering. 87

The data acquisition system of the quad module was adopted to allow for 88 multiple quads to be readout. A multiplexer card was developed that handles 89 four quads or 16 chips and combines the Timepix3 data into one data stream. 90 For the 32 GrixPix module two multiplexers are connected to a speedy pixel 91 detector readout (SPIDR) board [8] [9] that controls the chips and readout pro-92 cess. The readout speed per chip is 160 Mbps and for the multiplexer 2.56 Gbps 93 this corresponds to a maximum rate of 21 MHits/s. For each pixel the precise 94 Time of Arrival (ToA) using a 640 MHz TDC and the time over threshold (ToT) 95

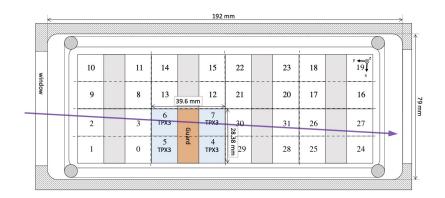


Figure 2: Schematic drawing of the 8-quad module detector with one example quad. The chips are numbered and the beam direction is shown in purple.

⁹⁶ are measured.

The gas volume of 780 ml is continuously flushed at a rate of $\sim 50 \text{ ml/min}$ with premixed T2K TPC gas. This gas is a mixture consisting of 95 % Ar, 3 % CF₄, and 2 % iC₄H₁₀ suitable for large TPCs because of the relatively high drift velocity and the low diffusion in a magnetic field.

101 1.2. Experimental setup

In preparation of the two weeks DESY test beam campaign, a support frame 102 was designed to move the 32 chip GridPix module in the transverse plane by a 103 remotely controlled stage thus that the whole detector volume could be probed. 104 The support frame also held three Mimosa 26 silicon detector planes [10] placed 105 in front of the detector and and three Mimosa planes behind the detector. 106 At DESY the Mimosa silicon detector planes that were provided by the test 107 beam coordinators were mounted. The whole detector setup was slided into 108 the centre of the PCMAG magnet at the DESY test beam facility II [11]. A 109 trigger was provided by a scintillator counter. The data were taken at different 110 stage positions to cover the whole sensitive TPC volume. Runs with electron 111 beam energies of 5 and 6 GeV and at magnetic fields of 0 and 1 Tesla(T) were 112 analysed. 113

A photograph of the detector setup in the PCMAG magnet is shown in Figure 3.

The experimental and environmental parameters such as temperature, pressure, gas flow, oxyxgen content were measured and logged by the windows operated slow control system. The experimental parameters are summarised in Table 1. The chips were cooled by circulating glycol through the cooling channels in the module carrier plate. The cooling blocks of the concentrators were further cooled by blowing pressurised air on them.

The data was produced in four main data streams: one stream produced by the Mimosa Telescope, two data streams by the two Timepix concentrators and one trigger stream. A scintillator provided a trigger signal to the Trigger Logic Unit (TLU) [12] that sends a signal to the trigger SPIDR and telescope readout.

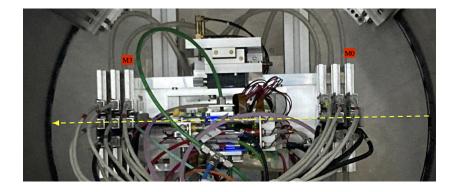


Figure 3: Photo of the detector setup at the centre of the PCMAG magnet. The Mimosa planes M0 and M3 are indidated in red as well as the beam direction (yellow). Centrally, the stager positions the TPC module thus that the beam passes through.

Table 1: Overview of the experimental parameters.	The ranges indicate the variation over the
data taking period	

Number of analysed runs at $B=0$ (1) Tesla	6(8)
Run duration	10-90 minutes
Number of triggers	3-100 k
$E_{ m drift}$	280 V/cm
$V_{ m grid}$	$340\mathrm{V}$
Threshold	$550 e^-$
Gas Temperature	$303.3-306.6~{\rm K}$
Pressure	1011 - 1023 mbar
Oxygen concentration	240 - 620 ppm
Water vapour concentration	2000 - 7000 ppm

The data acquisition system of the Telescope and trigger SPIDR injected a 126 timestamp into their respective data streams. Hits from the Mimosa planes 127 were collected with a sliding window of $-115 \,\mathrm{ms}$ to $230 \,\mathrm{ms}$ of the trigger. The 128 data acquisition of the concentrator and the trigger SPIDR were synchronized at 129 the start of the run. By comparing the time stamps in these streams, Telescope 130 tracks and TPC tracks could be matched. Unfortunately, the SPIDR trigger 131 had - due to a cabling mistake at the output of the TLU - a common 25 nsec 132 jitter. 133

In the first week of the test beam period it was found out that three HV cables had a bad connection. The cables were replaced and the module could be fully operated. Unfortunately, after a short data taking period one of the chips (nr 11) developped a short circuit and the HV on the grid of the chip was disconnected. Only after the test beam data taking period the module was repaired in the clean room in Bonn.

140 2. Analysis

¹⁴¹ 2.1. Telescope Track reconstruction procedure

The data of the Telescope is decoded and analysed using the Corryvreckan 142 software package [13]. The track model used for fitting was the general broken 143 lines (GBL) software [14]. The code was extended and optimzed to fit curved 144 broken lines for the data with a magnetic field. The telescope planes were iter-145 atively aligned using the standard alignment software provided by the package. 146 The single point Mimosa resolution is 4 µm in x and 6 µm in z (drift direction). 147 Telesope tracks were selected with at least 5 out of the 6 plane on the track 148 and a total χ^2 of better than 25 per degree of freedom. The uncertainties on the 149 Telescope track prediction in the middle of the GridPix module are dominated 150 by multiple scattering. For a 6 GeV track with no magnetic field they can be 151 measured comparing the predictions from the two telescope arms. The expected 152 uncertainty in x and z is 26 µm on average. 153

¹⁵⁴ 2.2. TPC Track reconstruction procedure

GridPx hits are selected requiring a minimum time over threshold ToT of 0.15 µs. The drift time is defined as the measured time of arrival minus the trigger time recorded in the trigger SPIDR data stream. The drift time was corrected for time slewing [2] using the measured time over threshold (ToT) and the formula 1:

$$\delta t = \frac{18.6(ns)}{\text{ToT} + 0.1577(\mu s)}.$$
(1)

Furthermore, small time shifts corrections - with an odd-even and a 16×2 pixels structure - coming from the TPX3 clock distribution were extracted from the data and applied.

The z-coordinate - i.e. the drift length - was calculated from the drift time 163 and the drift velocity. GridPix hits outside a Telescope acceptance window in 164 $x (\pm 15 \text{ mm})$ and $z (\pm 7.5 \text{ mm})$ were not used in the track finding and recon-165 struction. Based on a Hough transform an estimate of the TPC track position 166 and angles in the middle of the module (at y = 1436 pixels) was obtained. This 167 estimate was used to collect the hits around the TPC track and fit the track 168 parameters. For this fit a straight line (B=0 Tesla) or a quadratic track (B=1 169 Tesla) model was used. In the fit, the expected uncertainties per hit σ_x and 170 σ_z were used. The fit was iterated three times to perform outlier removal at 171 respectively 10, 5 and 2.5 sigma level. A TPC track was required to have a least 172 100 hits in each concentrator. At least 25% of the total number of hits should 173 be on track and the χ^2 per degree of freedom has to be less than 3 in xy and z. 174 All track parameters were expressed at a plane the middle of the TPC. 175

The drift velocity was calibrated per run comparing the Telescope tracks to the TPC hits. For the B=0 field runs it varies between 0.0616 and 0.0630 mm/ns. For the B=1 Tesla runs between 0.0572 and 0.0591 mm/ns. The variation comes mainly from the changes in the relative humidity of the gas volume due to small leaks. The individual TPX3 chips were aligned fitting a shift in x (z) and two slopes dx(z)/d row(column). The alignment was done per run, because the

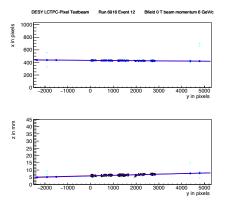


Figure 4: An event display for run 6913 without B field, with 1293 TPC hits (black dots) in the precision plane (xy) and driftplane (zy). The fitted TPC track (red line) with 1130 hits on is and the telescope track (blue line) with 5 Mimosa planes (blue hits) on track are shown. In green the off track Mimosa hits are shown.

detector was moved in and x and or z for each run. The fitted slopes also corrected for small shifts and rotations (3D) in the nominal chip position.

An example event run 6913 without B field with a TPC and a telescope track is shown in figure 4. The TPC is located between y = 0 and 2872 pixels. Three Mimosa planes are located at y ; -1000 and three at y ; 4000 pixels.

187 2.3. Track selections

In order to study the single electron resolution for the data with and without 188 magnetic field, additional selections on the Telescope and TPC tracks were 189 applied to select high quality tracks. Due to the trigger time jitter of 25 nsec, 190 the prediction of the telescope track in z must be used as the reference for z. 191 Secondly, the z hits of the TPC track were fitted to correct for the common 192 time shift and the z residuals were calculated with respect to the fitted TPC 193 track. In the xy plane the residuals of TPC hits with respect to the telescope 194 track were used to extract the single electron resolution in xy. For the resolution 195 studies runs at three different z stage positions of the TPC were selected where 196 the beam gave hits in the central chips. The data of 14 central chips (9, 12, 21, 197 21, 20, 17, 16, 2, 3, 6, 7, 30, 21, 26 and 27) was used. Two chips (8 and 13) 198

Table 2: Table with track selection cuts	
Event Selection	
$ x_{\rm TPC} - x_{\rm Telescope} < 0.3{\rm mm}$	
$ z_{\rm TPC} - z_{\rm Telescope} < 2.0{\rm mm}$	
$ dx/dy_{\rm TPC} - dx/dy_{\rm Telescope} < 4 \mathrm{mrad}$	
$ dz/dy_{\rm TPC} - dz/dy_{\rm Telescope} < 2 {\rm mrad}$	

were left out because of the E field deformations caused by the short circuit inchip 11.

²⁰¹ The track selections are summarized in table 2.

202 3. Results

203 3.1. Number of hits

The distribution of the number of TPC track hits per chip - without requiring a matched Telescope track - are shown in figure 5 for the data without magnetic field and for the B = 1 Tesla data.

The mean number of hits is measured to be 124 and 89 in the B=0 and 1 207 Tesla data sets. The most probable values are respectively 87 and 64. Note that 208 the B=0 data has a much larger Landau-like tail than the 1 Tesla data. Also 209 the fluctuations in the core of the distribution are larger. The mean time over 210 threshold for the B=0 T is $0.68 \,\mu s$ and $0.86 \,\mu s$ at a 1 Tesla field. This means 211 that the deposited charge per hit is smaller for the 0 T data. The most probable 212 value for the total deposited charge is similar for both data sets. These numbers 213 are in agreement with the predictions of [15] 106 electron-ion pairs for an 6 GeV 214 electron at B=0, crossing 236 pixels or $12.98 \,\mathrm{mm}$ and a detector running at 215 85% single electron efficiency. 216

217 3.2. Hit resolution in the pixel plane

The resolution of the hits in the transverse plane (xy) was measured as a function of the predicted drift position (z). Only hits are used crossing the

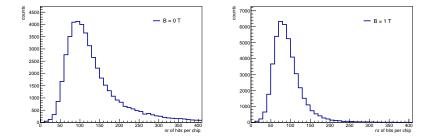


Figure 5: Distribution of the number of hits per per chip for B=0 (left) B=1 Tesla data.

fiducial region defined by central core of the beam and staying 20 pixels away from the chip edges. The resolution for the detection of ionisation electrons σ_x is given by:

$$\sigma_x^2 = \frac{d_{\text{pixel}}^2}{12} + d_{\text{track}}^2 + D_T^2(z - z_0), \qquad (2)$$

where d_{pixel} is the pixel pitch size, d_{track} the uncertainty from the track prediction, z_0 is the position of the grid, and D_T is the transverse diffusion coefficient. The resolution at zero drift distance $d_{\text{pixel}}/\sqrt{12}$ was fixed to 15.9 µm and d_{track} to 30 µm for B=0 and 42 µm for B = 1 Tesla data.

The expression (2) - leaving z_0 and the D_T as free parameters - is fitted to 227 the B=0 T data shown in Figure 6. The fit gives a transverse diffusion coefficient 228 D_T of 287 µm/ \sqrt{cm} with negligible statistical uncertainty. The measured value 229 is in agreement with value of $287\,\mu\mathrm{m}/\sqrt{cm}\pm4\%$ predicted by the gas simulation 230 software Magboltz [16]. The values of the diffusion coefficients depend on the 231 humidity that was not precisely measured during the testbeam. The humidity 232 strongly affects the drift velocity. Therefore the drift velocity prediction from 233 Magboltz was used to determine the water content per run and predictions for 234 the diffusion coefficients could be obtained. 235

A fit to the B=1 T data shown in Figure 6 gives a transverse diffusion coefficient D_T of $121 \,\mu\text{m}/\sqrt{cm}$ with negligible statistical uncertainty. The measured value is in agreement with the value of $119 \,\mu\text{m}/\sqrt{cm} \pm 2\%$ predicted by Magboltz.

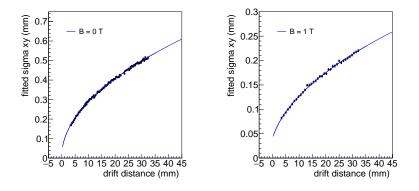


Figure 6: Measured hit resolution in the pixel plane (back points) fitted with the resolution function according to equation (2) (blue line).

240 4. Conclusion and outlook

A Time Projection Chamber module with 32 GridPix chips was constructed and the performance was measured using data taken in a test beam at DESY in 243 2012. The analysed data were taken at electron beam energies of 5 and 6 GeV 244 and at magnetic fields of 0 and 1 Tesla(T).

The result for the transverse diffusion coefficient D_T is $287 \,\mu\text{m}/\sqrt{cm}$ at B = 0 T and D_T is $121 \,\mu\text{m}/\sqrt{cm}$ at B = 1 T. The longitudinal diffusion coefficient D_L is measured to be $268 \,\mu\text{m}/\sqrt{cm}$ at B = 0 T and $252 \,\mu\text{m}/\sqrt{cm}$ at B = 1 T. Results for the tracking systematical uncertainties in xy were measured to be smaller than 14 μ m with and without magnetic field. The tracking systematical uncertainties in z were smaller than 14 μ m (B = 0 T) and 22 μ m (B = 1 T).

251 Acknowledgements

The 32 Gridpix module could not be constructed without the enormous effort and creative energy that Fred Hartjes has invested in it over several years. This research was funded by the Netherlands Organisation for Scientific Research NWO. The authors want to thank the support of the mechanical and electronics departments at Nikhef and the detector laboratory in Bonn. The measurements

- $_{\rm 257}$ $\,$ leading to these results have been performed at the Test Beam Facility at DESY $\,$
- ²⁵⁸ Hamburg (Germany), a member of the Helmholtz Association (HGF).

259 References

- [1] C. Ligtenberg, et al., Performance of a GridPix detector based on the
 Timepix3 chip, Nucl. Instrum. Meth. A 908 (2018) 18-23. arXiv:1808.
 04565, doi:10.1016/j.nima.2018.08.012.
- [2] C. Ligtenberg, et al., Performance of the GridPix detector quad, Nucl.
 Instrum. Meth. A 956 (2020) 163331. arXiv:2001.01540, doi:10.1016/
 j.nima.2019.163331.
- [3] J. Kaminski, Y. Bilevych, K. Desch, C. Krieger, M. Lupberger, GridPix de tectors introduction and applications, Nucl. Instrum. Meth. A845 (2017)
 233–235. doi:10.1016/j.nima.2016.05.134.
- [4] C. Ligtenberg, A GridPix TPC readout for the ILD experiment at the future International Linear Collider, Ph.D. thesis, University of Amsterdam (2021).
- URL https://www.nikhef.nl/pub/services/biblio/theses_pdf/ thesis_C_Ligtenberg
- [5] M. Lupberger, Y. Bilevych, H. Blank, D. Danilov, K. Desch, A. Hamann,
 J. Kaminski, W. Ockenfels, J. Tomtschak, S. Zigann-Wack, Toward the
 Pixel-TPC: Construction and Operation of a Large Area GridPix Detector,
 IEEE Trans. Nucl. Sci. 64 (5) (2017) 1159–1167. doi:10.1109/TNS.2017.
 2689244.
- [6] T. Poikela, J. Plosila, T. Westerlund, M. Campbell, M. De Gaspari,
 X. Llopart, V. Gromov, R. Kluit, M. van Beuzekom, F. Zappon,
 V. Zivkovic, C. Brezina, K. Desch, Y. Fu, A. Kruth, Timepix3: a 65K
 channel hybrid pixel readout chip with simultaneous ToA/ToT and sparse
 readout, JINST 9 (05) (2014) C05013.

- [7] F. Hartjes, A diffraction limited nitrogen laser for detector calibration in
 high energy physics, Ph.D. thesis, University of Amsterdam (1990).
- 286 URL https://www.nikhef.nl/pub/services/biblio/theses_pdf/ 287 thesis_F_Hartjes.pdf
- [8] J. Visser, M. van Beuzekom, H. Boterenbrood, B. van der Heijden, J. I.
 Muñoz, S. Kulis, B. Munneke, F. Schreuder, SPIDR: a read-out system for
 Medipix3 & Timepix3, Journal of Instrumentation 10 (12) (2015) C12028.
 doi:10.1088/1748-0221/10/12/C12028.
- [9] B. van der Heijden, J. Visser, M. van Beuzekom, H. Boterenbrood, S. Kulis,
 B. Munneke, F. Schreuder, SPIDR, a general-purpose readout system for
 pixel ASICs, JINST 12 (02) (2017) C02040. doi:10.1088/1748-0221/12/
 02/C02040.
- [10] H. Jansen, S. Spannagel, J. Behr, A. Bulgheroni, G. Claus, E. Corrin,
 D. Cussans, J. Dreyling-Eschweiler, D. Eckstein, T. Eichhorn, M. Goffe,
 I. M. Gregor, D. Haas, C. Muhl, H. Perrey, R. Peschke, P. Roloff, I. Rubinskiy, M. Winter, Performance of the eudet-type beam telescopes, EPJ
 Techniques and Instrumentation 3 (1) (2016) 7. doi:10.1140/epjti/
 s40485-016-0033-2.
- ³⁰² [11] J. D.-E. e. a. R. Diener, The desy ii test beam facility', Nuclear Instruments ³⁰³ and Methods in Physics Research. Section A: Accelerators, Spectrometers,
- Detectors and Associated Equipment 922 (2019) 265–286. arXiv:1807.
 09328, doi:10.1016/j.nima.2018.11.133.
- ³⁰⁶ [12] D. Cussans, Description of the JRA1 Trigger Logic Unit (TLU), v0.2c,
 ³⁰⁷ EUDET Collaboration (2009).
- JOB
 URL
 https://www.eudet.org/e26/e28/e42441/e57298/
- 309 EUDET-MEMO-2009-04.pdf
- [13] J. Kröger, S. Spannagel, M. Williams, User manual for the corryvreckan
 test beam data reconstruction framework, version 1.0 (2019). arXiv:1912.
 00856.

- [14] C. Kleinwort, General broken lines as advanced track fitting method, Nuclear Instruments and Methods in Physics Research Section A: Accelerators, Spectrometers, Detectors and Associated Equipment 673 (2012) 107–
 110. doi:10.1016/j.nima.2012.01.024.
- ³¹⁷ [15] R. Veenhof, Garfield simulation of gaseous detectors, version 9, Reference
 ³¹⁸ W5050 (1984-2010).
- 319 URL https://garfield.web.cern.ch
- ³²⁰ [16] S. F. Biagi, Monte Carlo simulation of electron drift and diffusion in count-
- ing gases under the influence of electric and magnetic fields, Nucl. Instrum.
- Meth. A421 (1-2) (1999) 234-240. doi:10.1016/S0168-9002(98)01233-9.