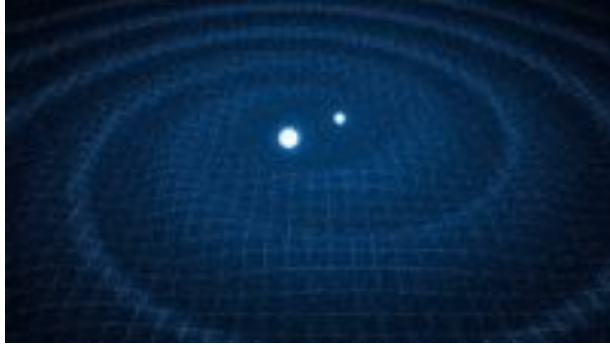


Strong gravitational lensing of gravitational waves: an upcoming new multi-messenger channel

Justin Janquart
j.janquart@uu.nl

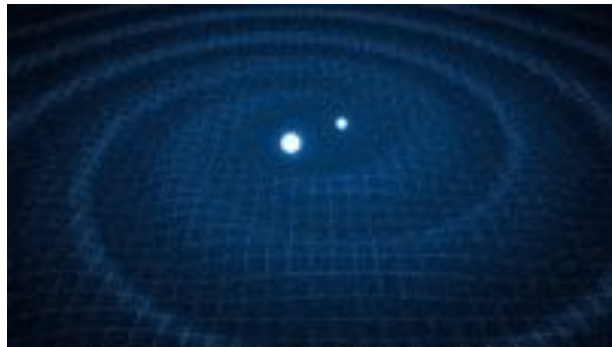
What are gravitational waves?



credits : NASA

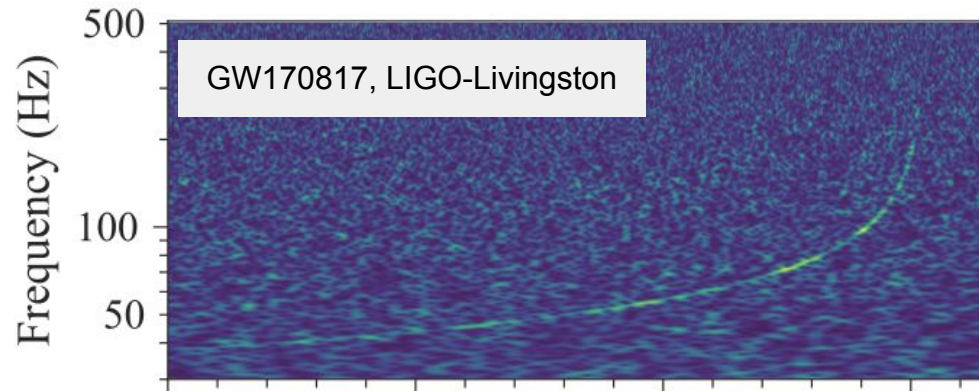
Two massive objects (Black hole, neutron star, ...) orbit each other

What are gravitational waves?

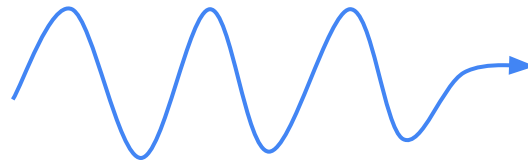


credits : NASA

Two massive objects (Black hole, neutron star, ...) orbit each other



Adapted from: LIGO-Virgo, Phys. Rev. Lett. 119.161101



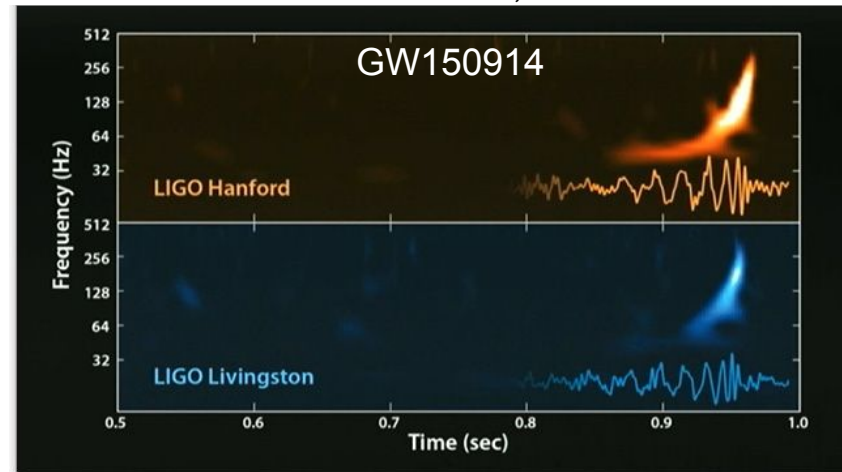
Long travel in space



Scale of Effect Vastly Exaggerated

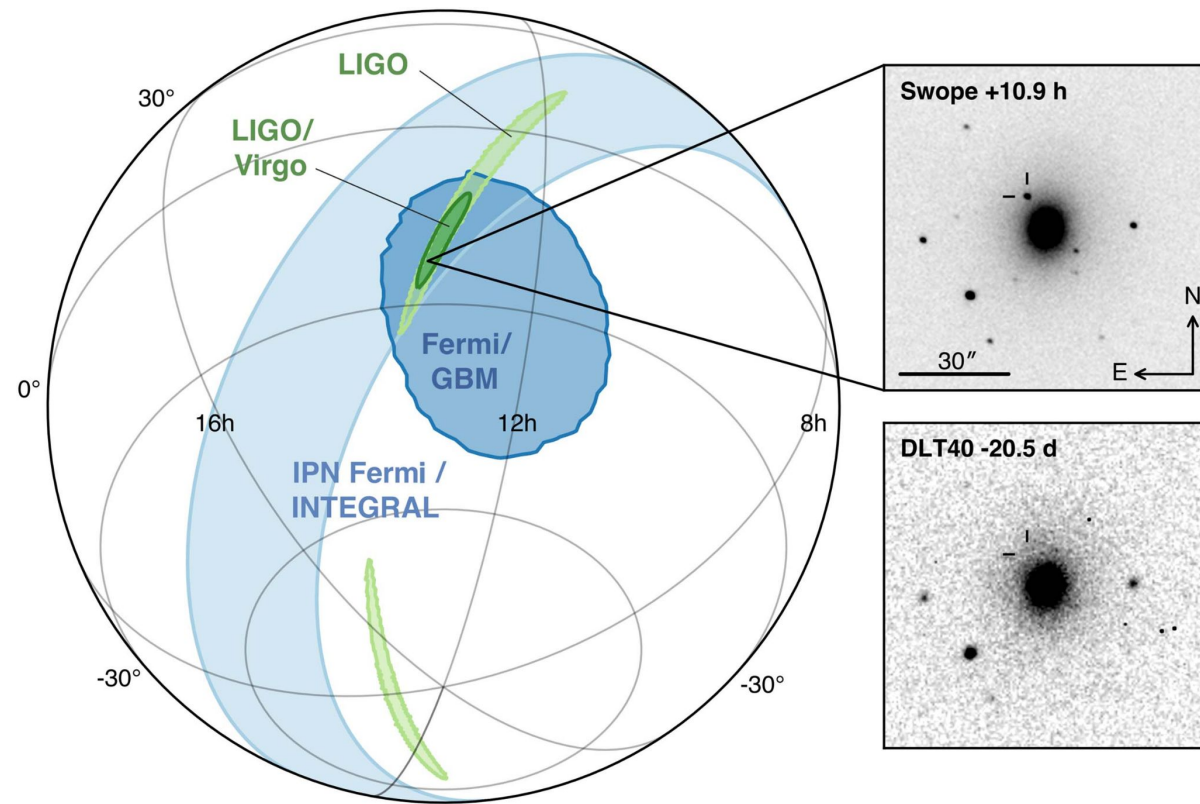
Credits: MIT

Reaches Earth, can be detected



Source: LIGO, Rev. Lett. 116 061102

GW170817, an example of a multi-messenger observation

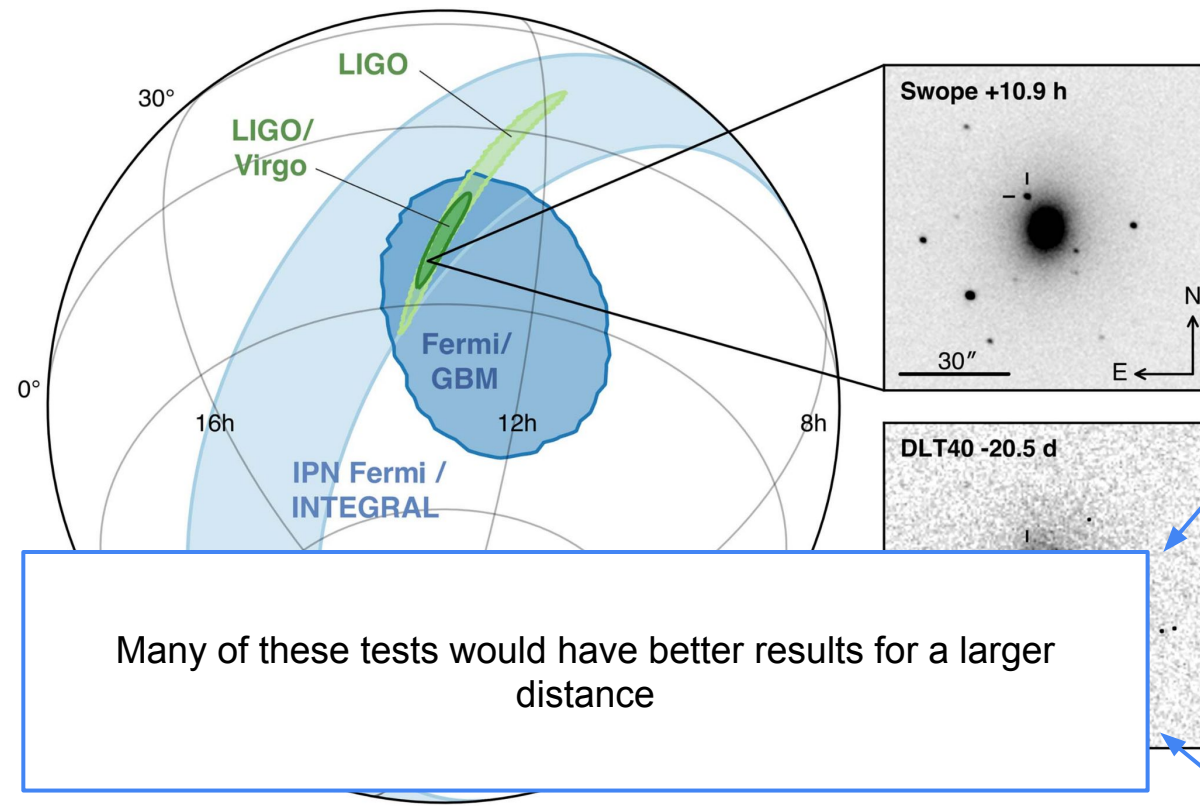


Lead to ([LIGO-Virgo. Phys. Rev. Lett. 161101](#)):

- Study of neutron stars properties (masses, tidal deformability, ...)
- Constraint on the equation of state for neutron star matter
- Using the **difference in time of travel between the photons and the gravitational wave signal**:
 - Test speed of gravity
 - Test for dispersive effects in gravitational waves
 - Test the equivalence principle
- Make **link between the GRBs and the object at their origin**
- Independent **measure of the Hubble constant**

Source: LIGO-Virgo-Fermi et al, *Astroph. J. Letters*, 848:L12

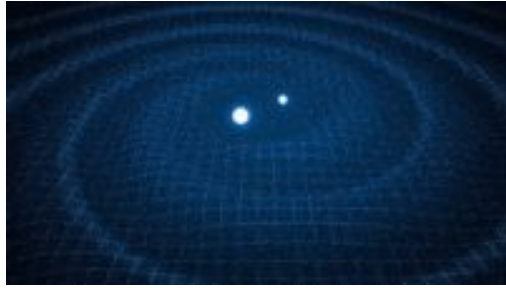
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What is strong lensing?



credits : NASA



Credits: Dick Locke

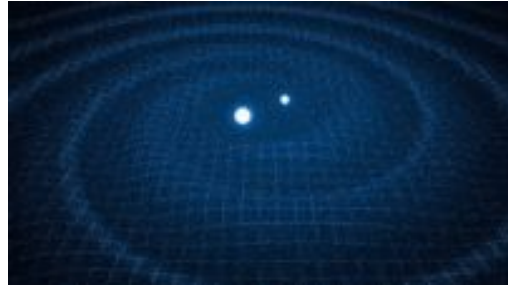
t_1



t_2



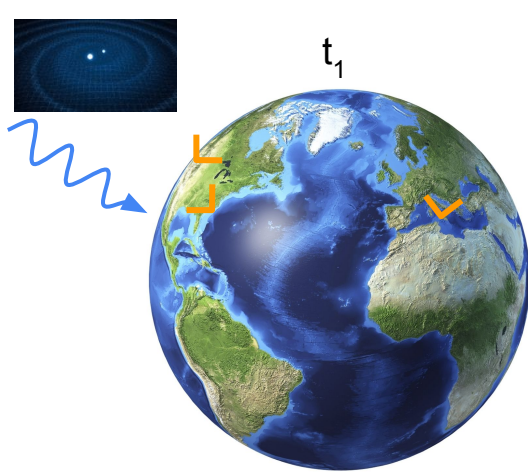
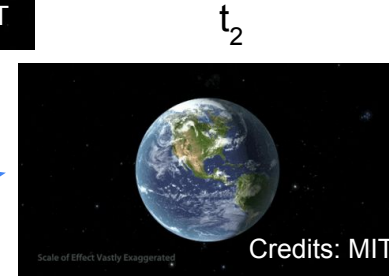
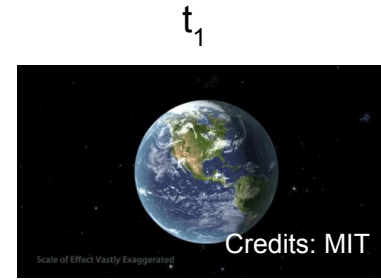
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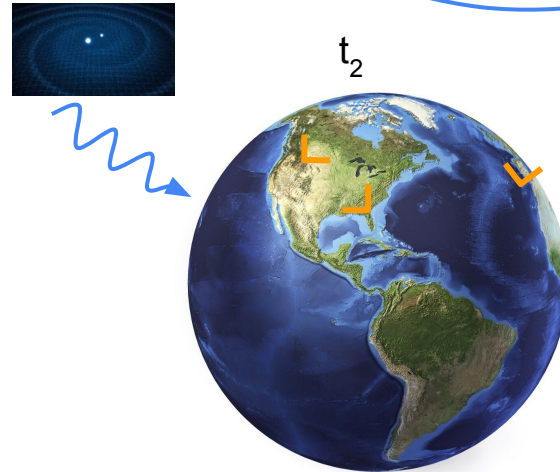
credits : NASA



Credits: Dick Locke

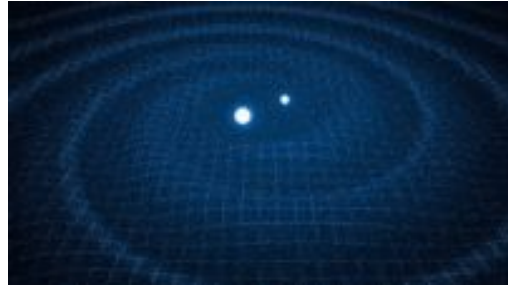


3 detectors



3 detectors

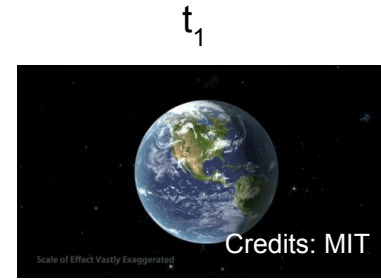
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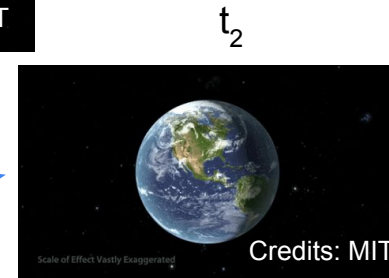
credits : NASA



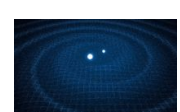
Credits: Dick Locke



Credits: MIT



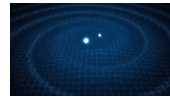
Credits: MIT



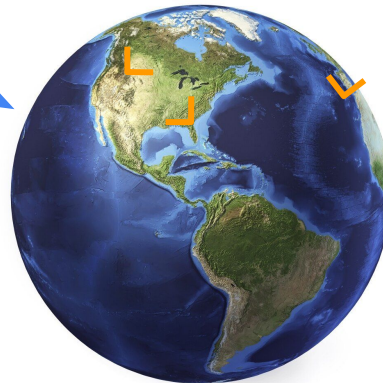
t_1



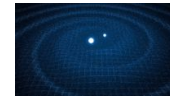
3 detectors



t_2



3 detectors

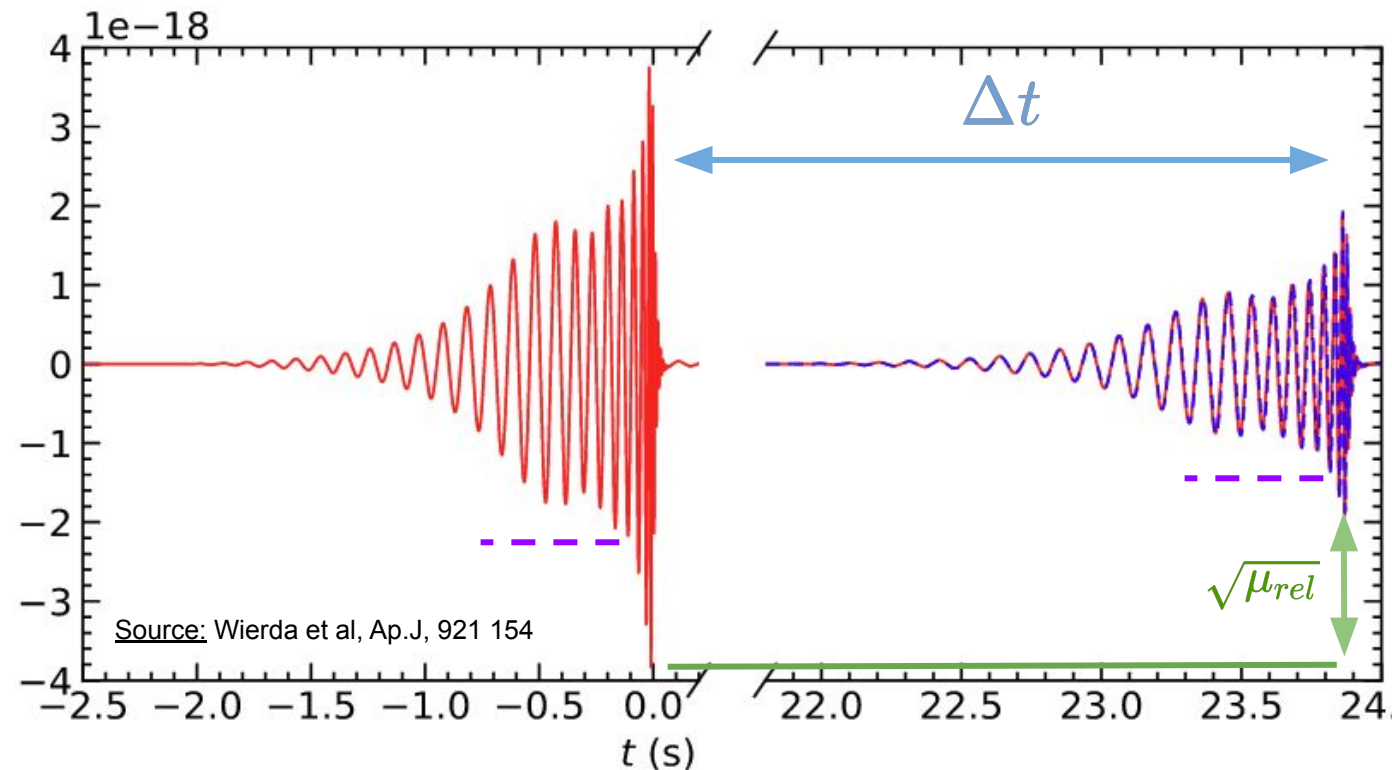


6 detectors

What is strong lensing?

Geometric optics limit ($\lambda_{GW} \ll R_{lens}$): the frequency evolution of the wave is unchanged.

→ **Several images** with the same frequency evolution.



Time delay: different paths lead to different arrival time at the detectors.

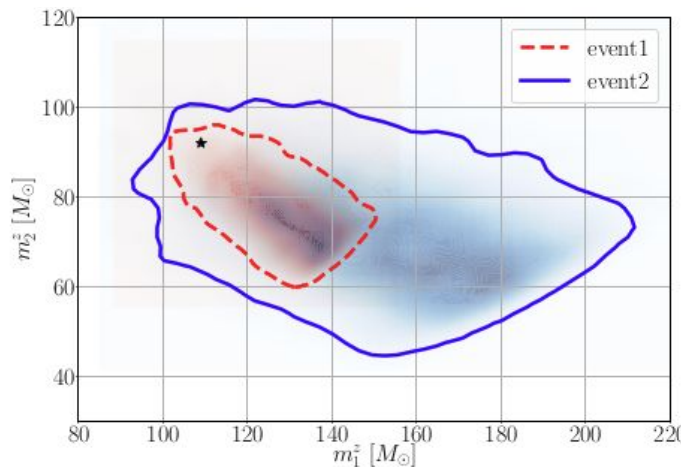
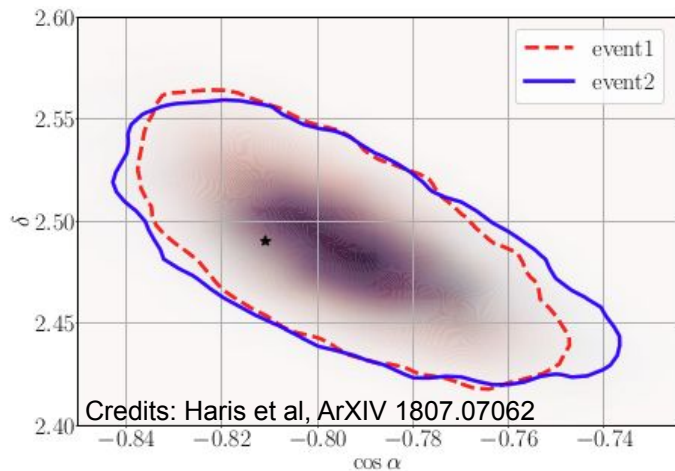
Relative magnification: links the change in amplitude for each wave

Overall phase shift: depends on the position relative to the source, one can have $\{0, \frac{\pi}{2}, \pi\}$

Finding the needle in the haystack

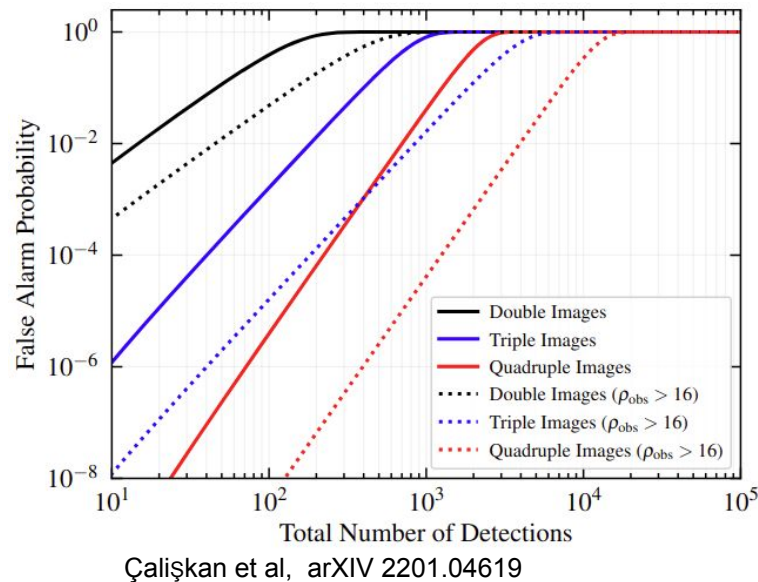
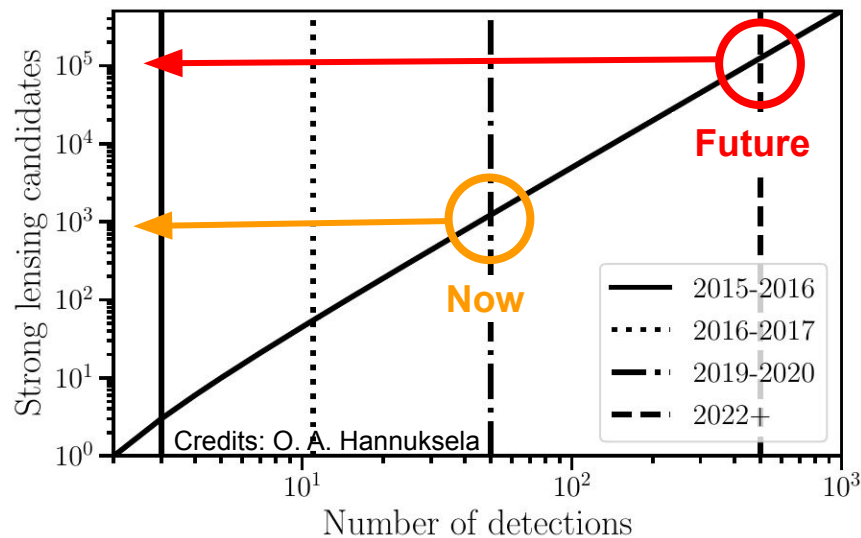
- How do we identify strong lensing?

→ By looking to event pairs with similar intrinsic parameters and sky location



Finding the needle in the haystack

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- What is the needle, what is the haystack?
 - Need to analyze all the pairs of events in the data, matching posteriors can happen by chance



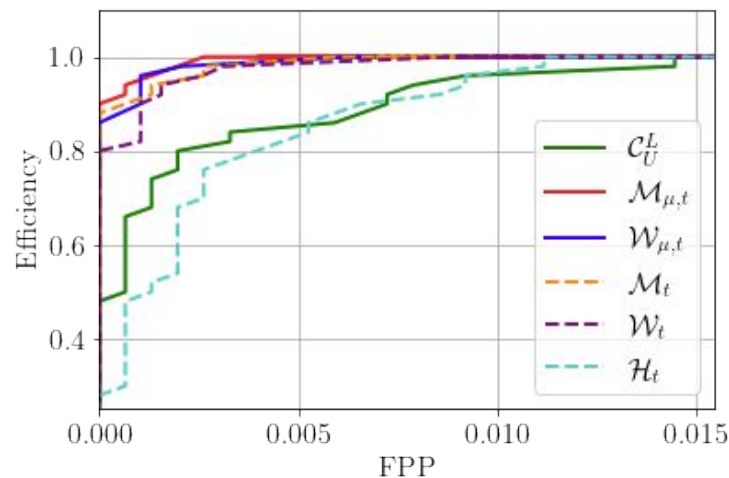
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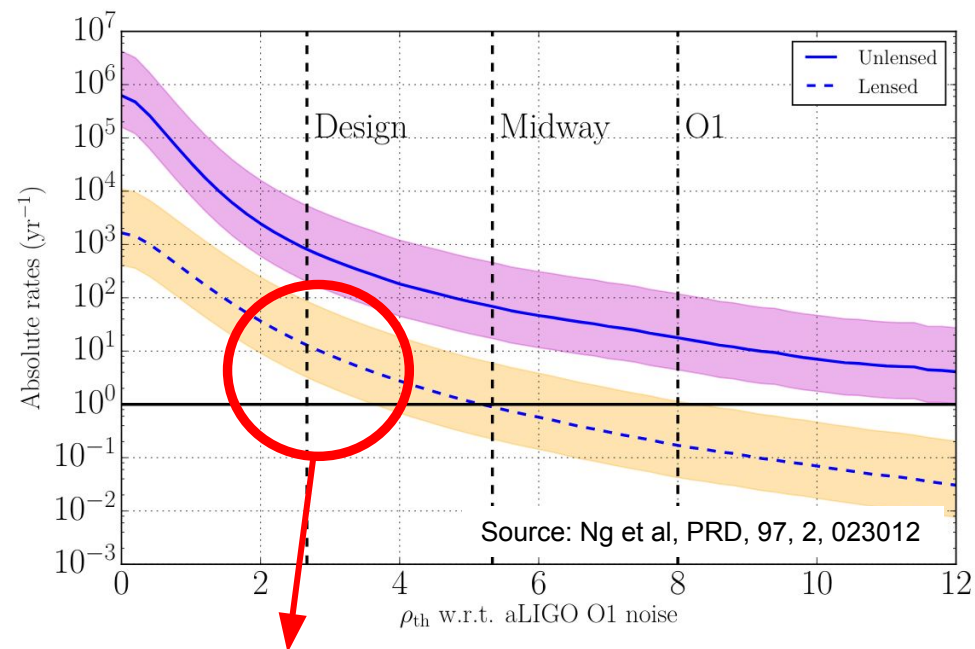
Several methods developed over the years:

- Fast but not very precise:
 - Posterior overlap ([Haris et al, ArXIV 1807.07062](#))
 - Machine learning based ([Goyal et al, PRD, 104, 12](#))
- Very precise but slow:
 - Full joint parameter estimation ([Liu et al, ApJ, 908, 1](#); [Lo & Hernandez, arXIV 2104.09339](#))
- Fast and precise:
 - GOLUM ([Janquart et al, MNRAS, 506, 4](#))

Possibility to constrain more the similarities based on the expected lenses ([Janquart et al, ArXIV 2205.11499](#)):

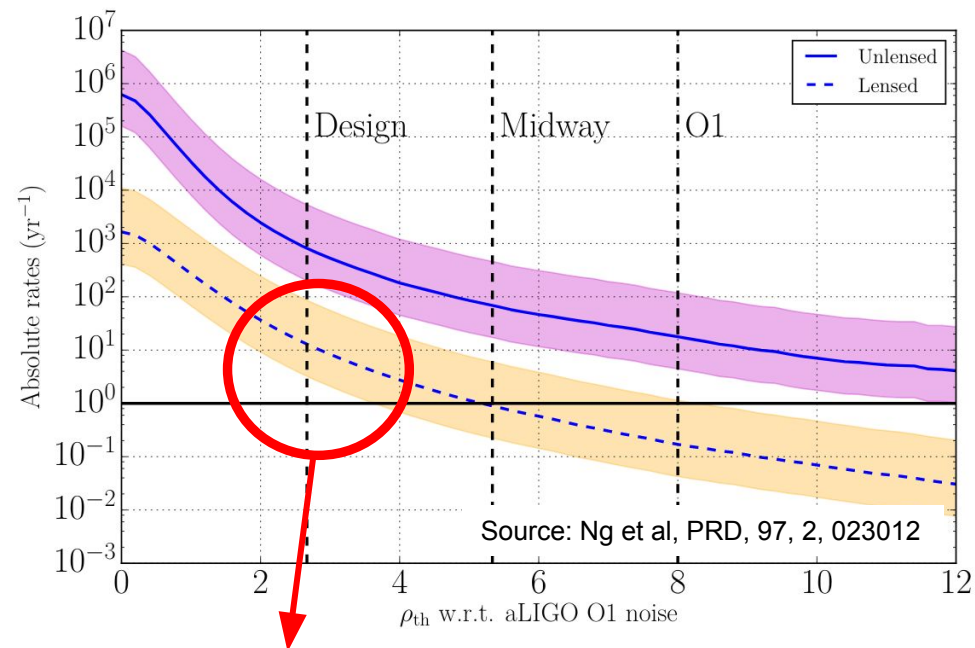


Why is this interesting?



Could be detected soon!

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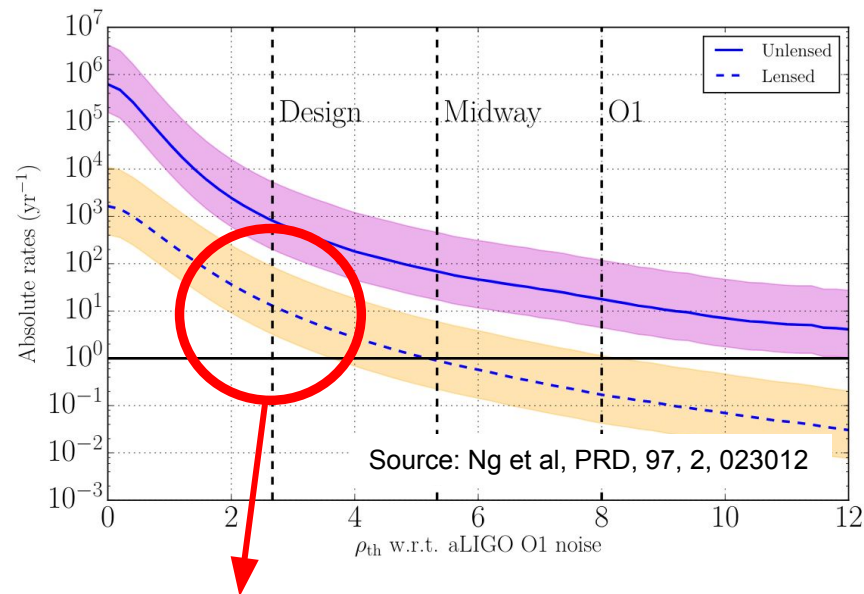


Could be detected soon!

Searches are already ongoing:

- In GWTC-2: [Hannuksela et al, 2019](#)
 - In GWTC-3.1: [LIGO & Virgo, 2021](#)
- } No signs of lensing yet

Why is this interesting?



Could be detected soon!

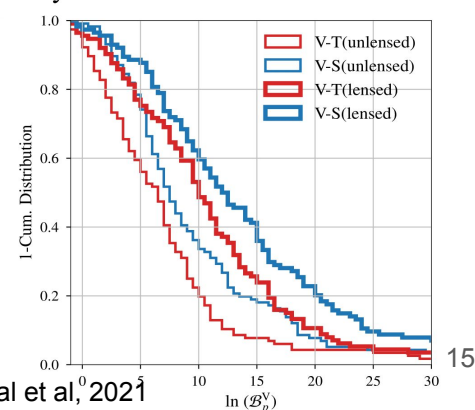
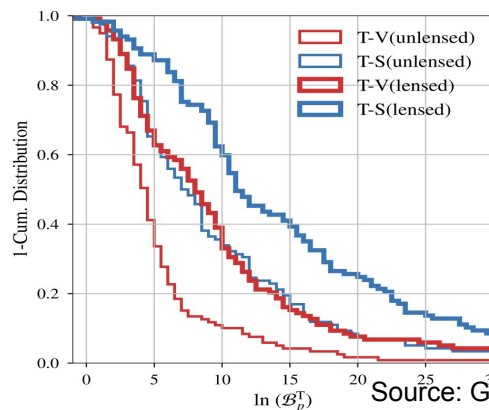
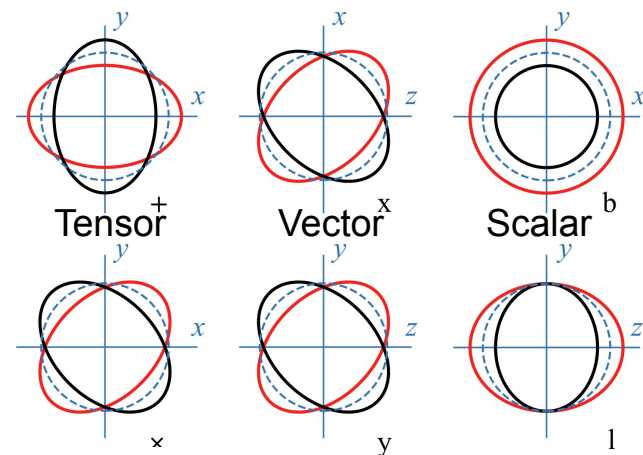
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Some interesting science cases:

For example:

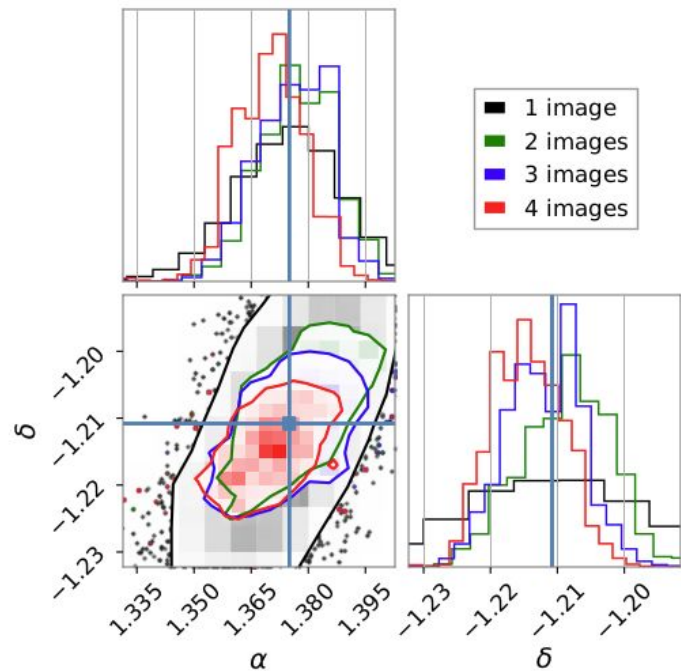
- Test GW polarizations ([Goyal et al. 2021](#))
- Probing of higher-order modes ([Janquart et al. 2021](#))



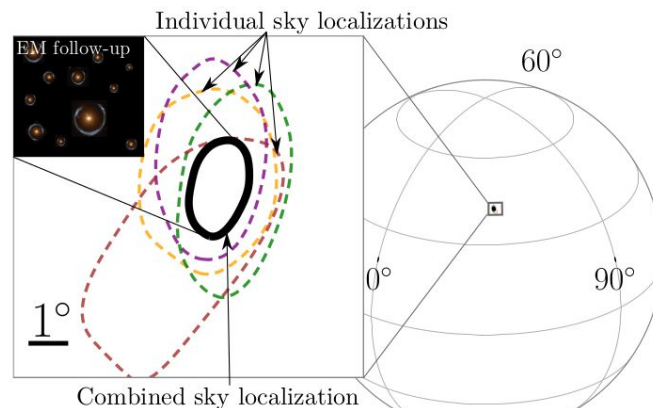
Source: Goyal et al, 2021

Where is the multi-messenger?

→ The increase in effective number of detectors lead to an improved sky location!



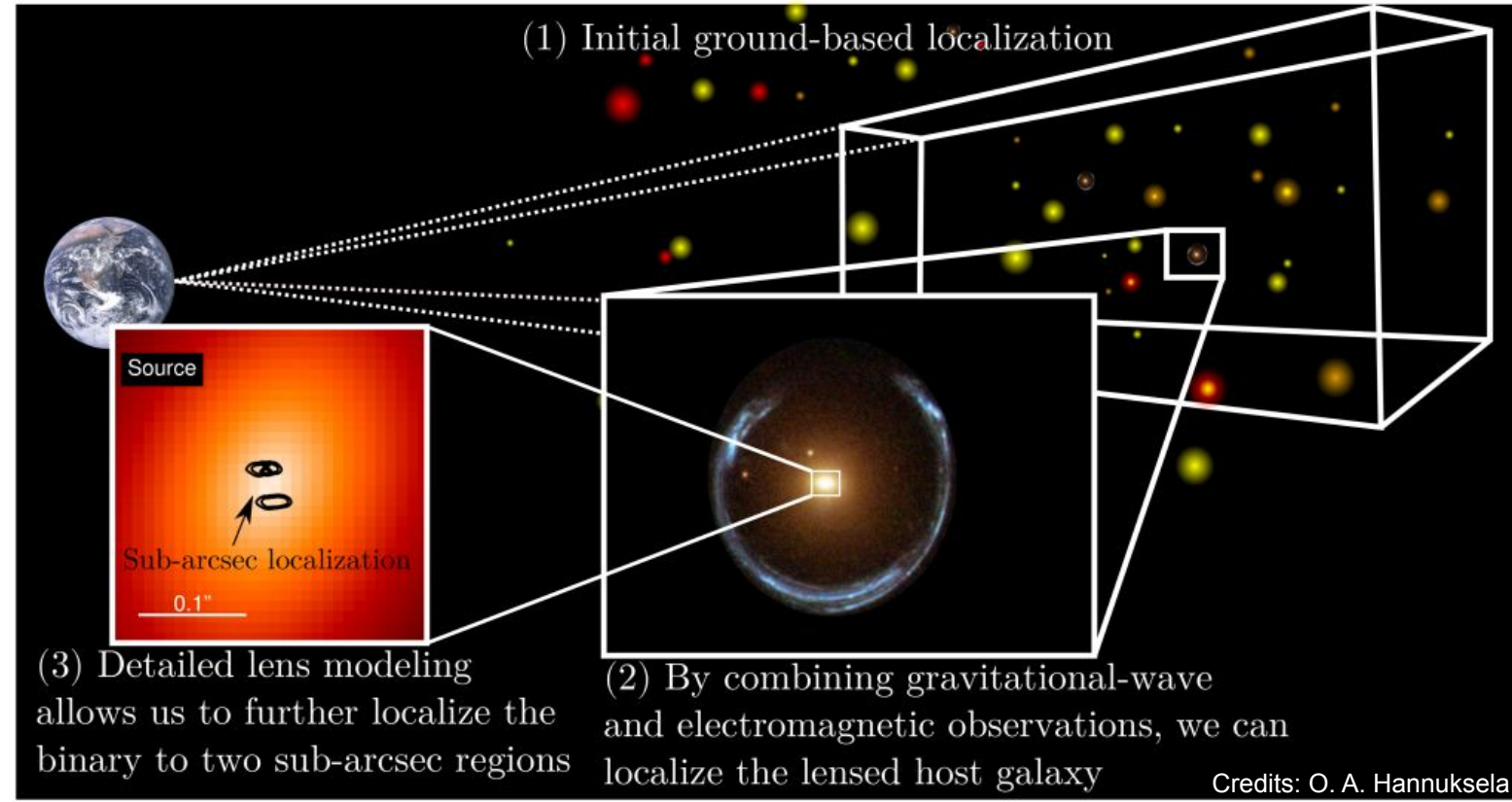
Source: Janquart et al, MNRAS, 506, 4



Source: Hannuksela et al, MNRAS, 498, 3

Where is the multi-messenger?

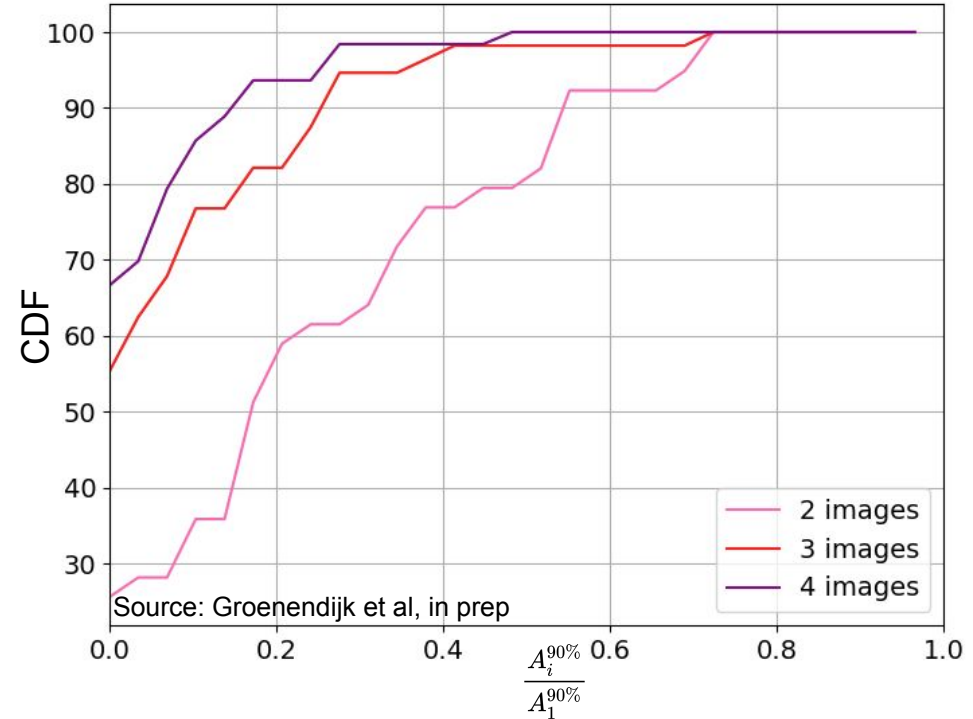
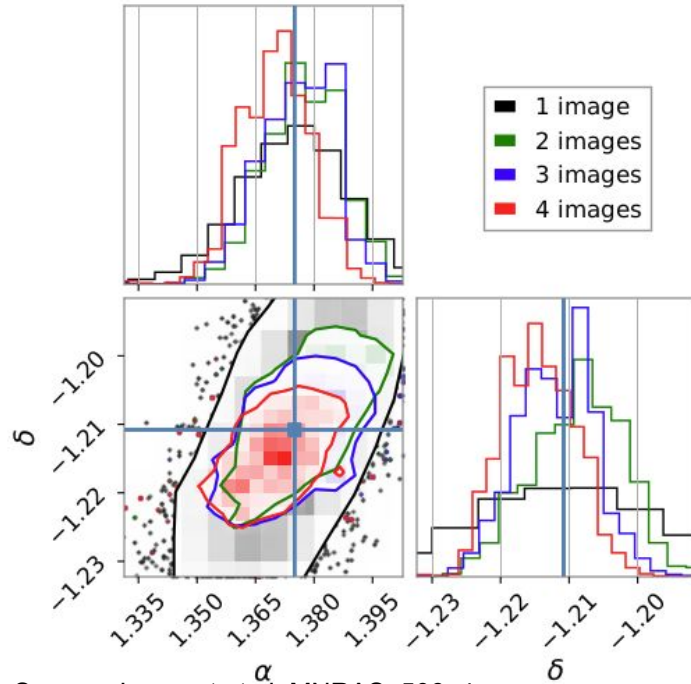
Assuming the merger happens in a Galaxy, the electromagnetic signal should also be lensed → Using this and gravitational wave information, one can identify the lens and the host galaxy in the reduced sky area.



→ We have our counterpart!

How much does lensing actually help?

For the **sky location** itself: Depends on the number of images but can be significant depending on the individual images

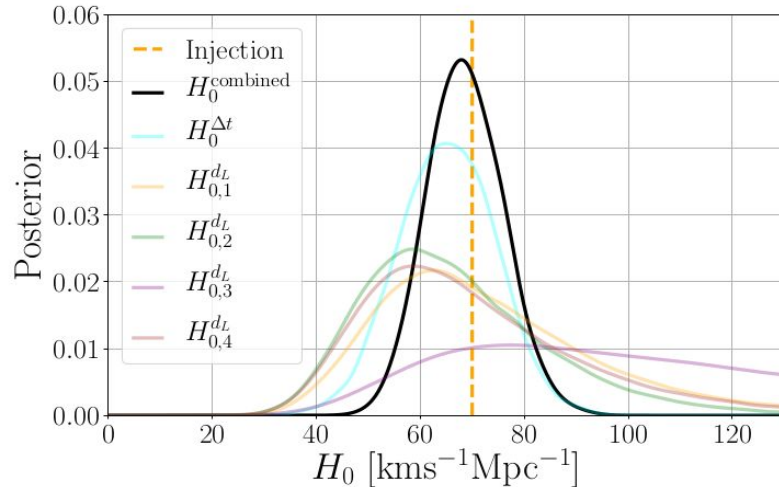


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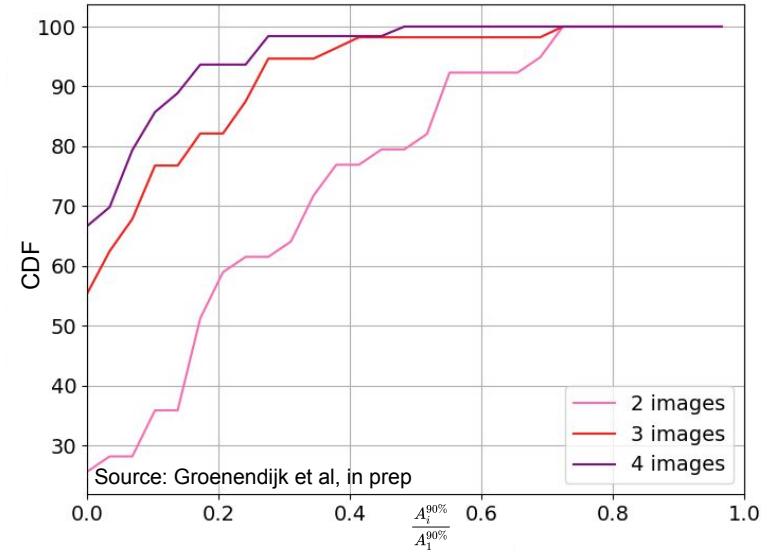
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For **science cases**:

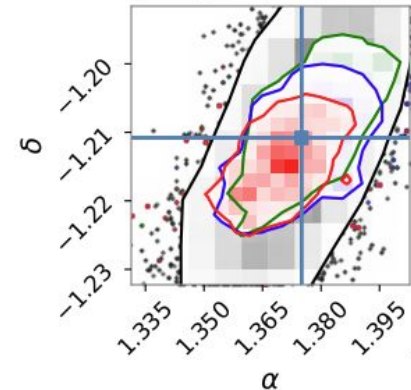
- Since black hole mergers can be seen further than neutron star mergers, any cumulative effect (speed of gravity, dispersion, ...) can accumulate more and lead to a stronger effect
- The multiple images can lead to several measure of the same information, leading to a better measurement



Source: Hannuksela et al, MNRAS, 498, 3



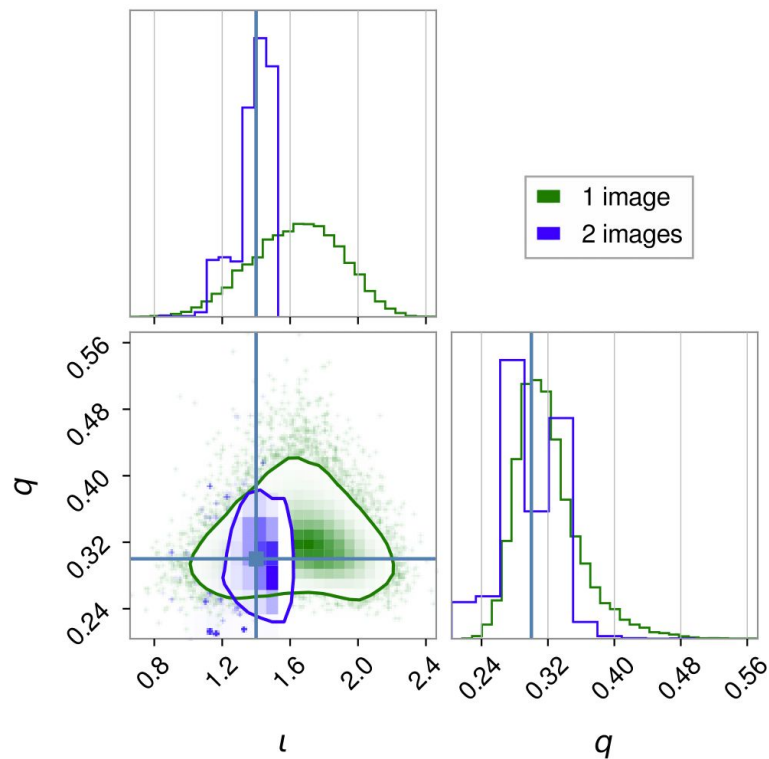
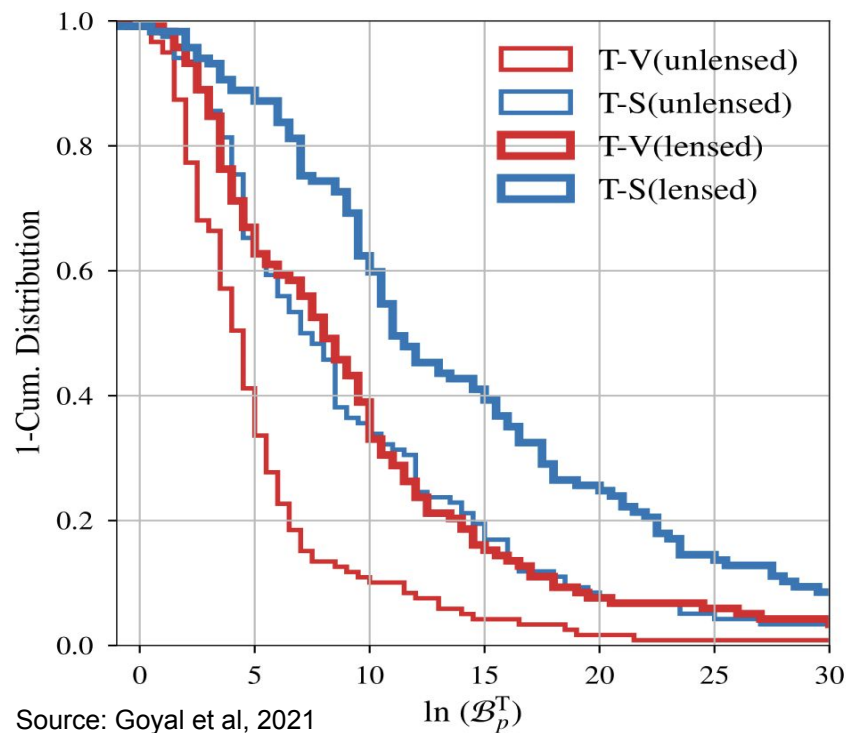
Source: Groenendijk et al, in prep



Source: Janquart et al, MNRAS, 506, 4

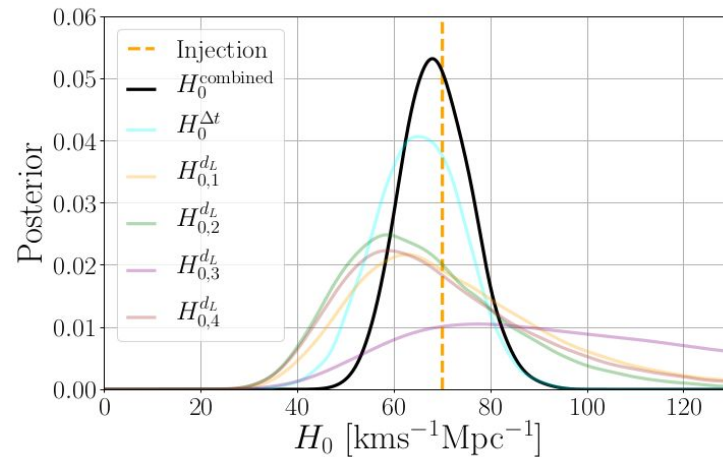
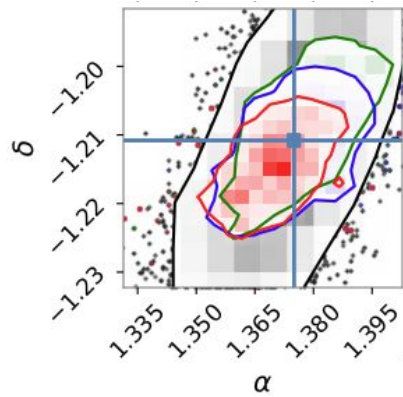
What can we do in the end?

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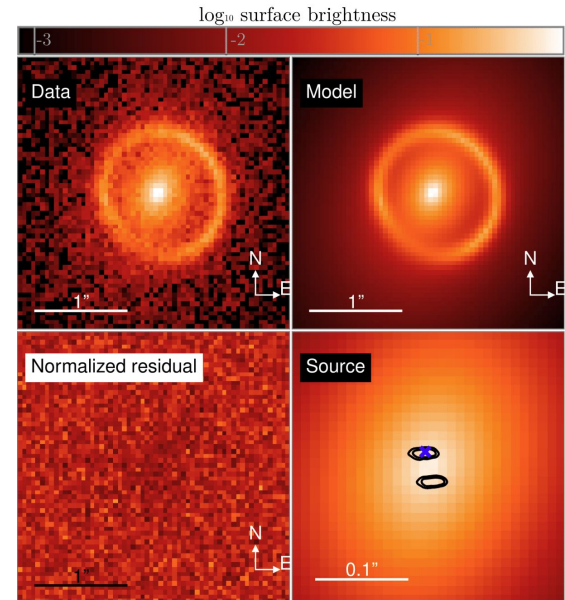


What can we do in the end?

- Test GW polarizations ([Goyal et al, 2021](#))
- Probing of higher-order modes ([Janquart et al, 2021](#))
- Origin of black holes ([Hannuksela et. al, 2020](#))
- Expansion of the Universe ([Liao et. al 2017](#), [Hannuksela et. al 2020](#))
- Probe fundamental physics ([Collett & Bacon 2017](#), [Fan et al 2017](#))



Source: Hannuksela et al, 2020



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And in the end?

- Gravitational waves **can be lensed**
- Gravitational wave lensing is an **active field** of research
- Strong lensing of gravitational waves **is upon us** and they would manifest themselves as **repeated events with the same frequency evolution**
- There are **still some challenges to confidently identify** strongly-lensed gravitational wave events
- If identified, strong lensing would open the door to **many interesting science cases** such as a better study of the events themselves based on their higher-order mode content, investigation of the gravitational wave polarization content, ... without electromagnetic counterpart
- If, in addition, there is an **electromagnetic counterpart identified, even more tests would be possible**, such as the study of the origin of binary black holes, tests for cosmology, tests of general relativity.

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Thank you for your attention!