

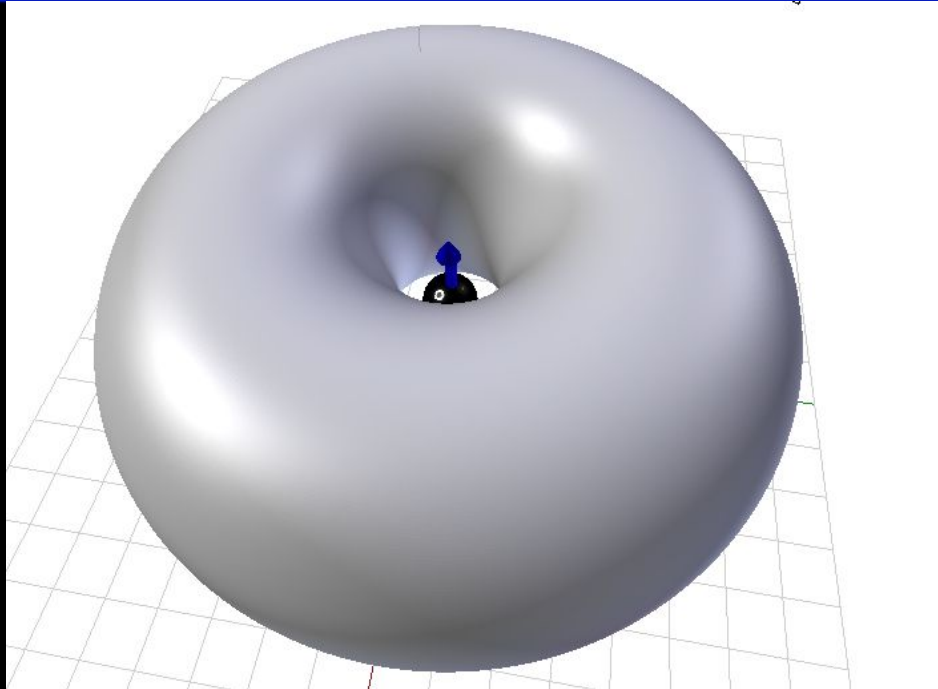
Probing ultralight bosons with gravitational waves

Nikhef seminar (26th of March, 2020)

Talk based on:

Arxiv:1804.09659

Arxiv:1908.02312

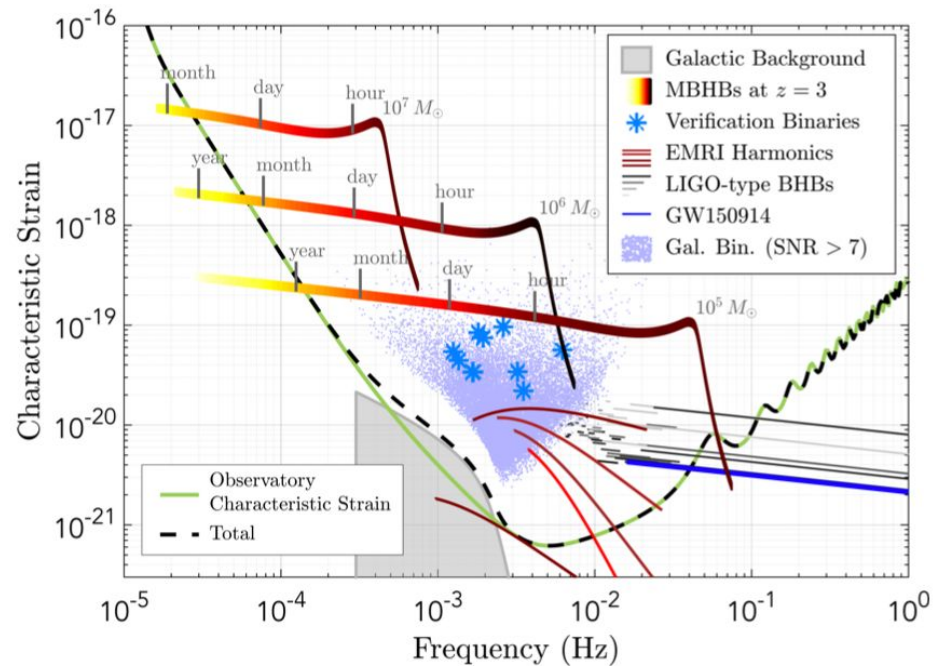
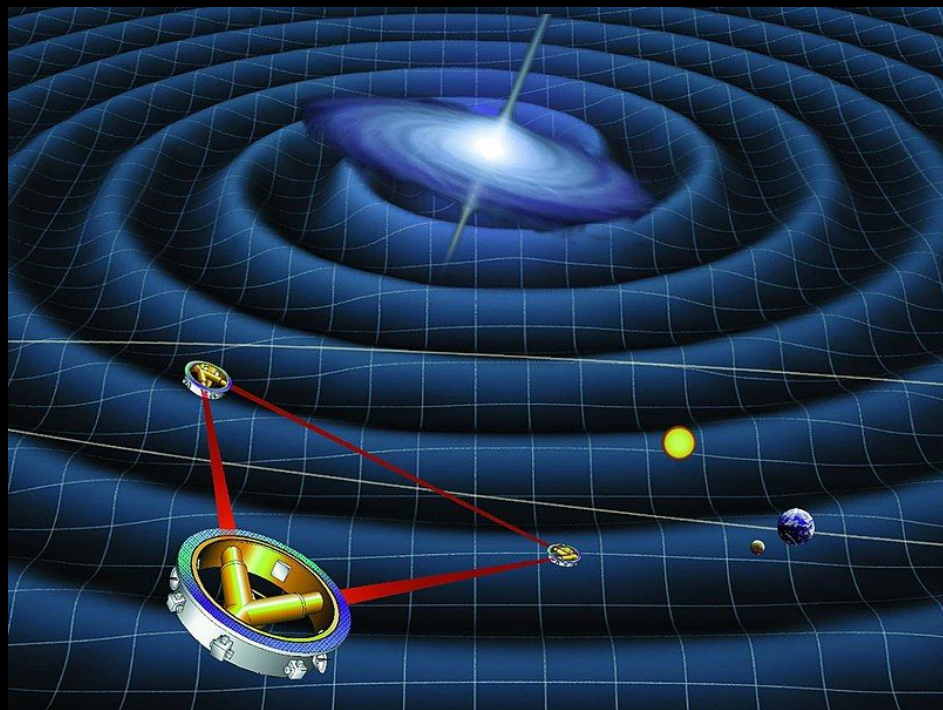


In collaboration
with:

- Kaze Wong
- Richard Brito
- Emanuele Berti
- Tjonnie Li
- Ken Ng
- Salvatore Vitale

Otto Akseli Hannuksela
Nikhef

First part of the talk: LISA EMRI Measurements



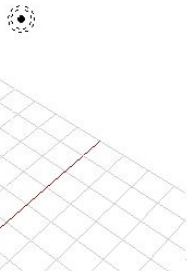
What are light bosons, what do we expect and who is interested?

- **Any** particle that is a boson and has a light mass (often $\ll 10^{-5}$ eV)
- Range of particles fall into this category:
 - Light/ultralight axions
 - QCD Axion (upper end)
 - Wave dark matter
 - Dilatons
- These are a beyond-standard-model particles and hence not proven to exist

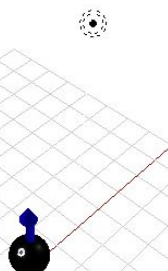
- Depending on who you ask:
- A dark matter candidate
 - Could solve cosmological and astrophysical problems, depending on its mass range
 - Would give hints about physics beyond the standard model

Simplified overview

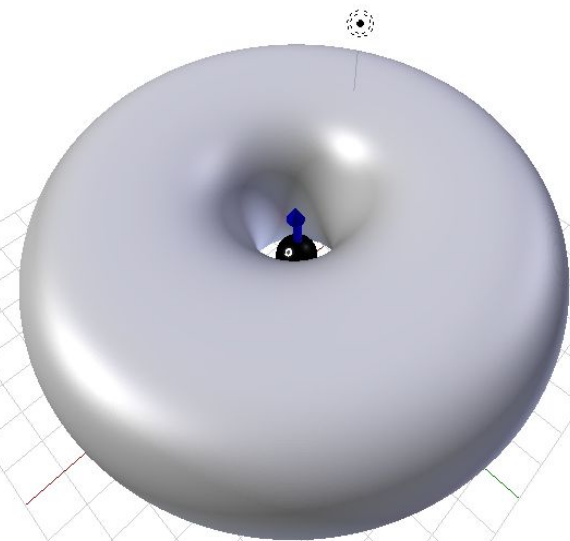
Highly spinning BH



Superradiance spins down BH



Bosons created from rotational energy

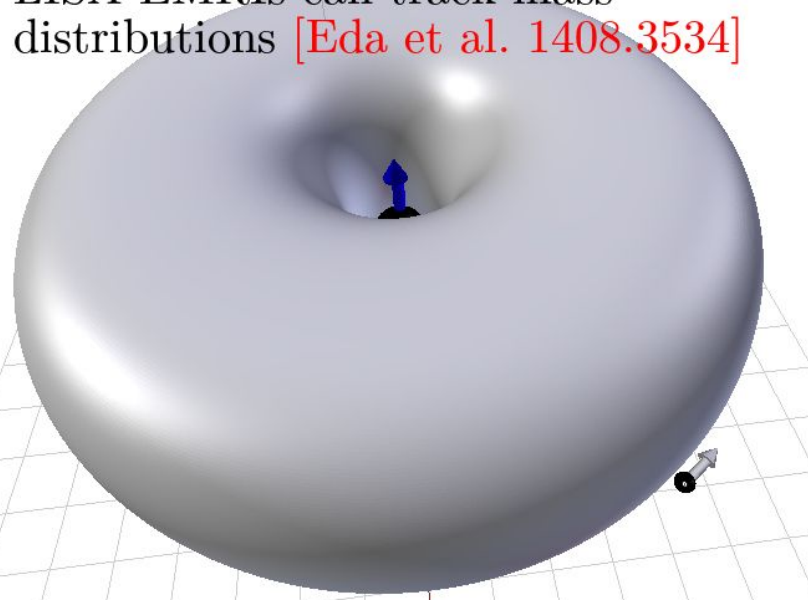


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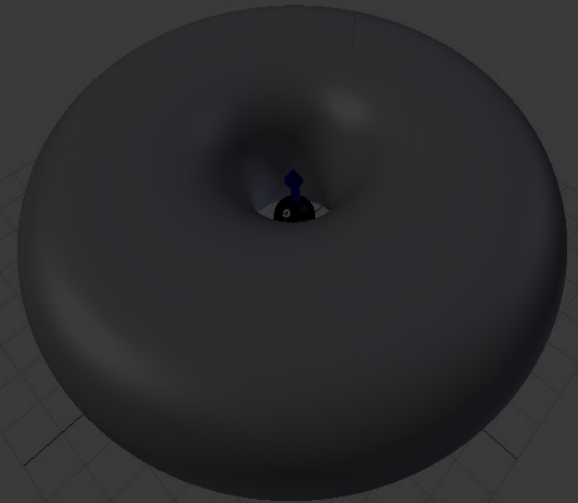
Highly spinning BH



LISA EMRIs can track mass distributions [Eda et al. 1408.3534]



is created from rotational energy



Black Hole & Boson Cloud: Theory

$$[\square - \mu_S^2]\Psi = 0$$

$$\psi(\mu_S, a, M, r) \propto \tilde{r}^l e^{-\tilde{r}/2} L_n^{2l+1}(\tilde{r})$$

$$\tilde{r} = 2rM\mu_S^2 / (l+n+1)$$

$$\Psi \sim e^{t/\tau}$$

$$\omega \sim \mu_S - \frac{\mu_S}{2} \left(\frac{M\mu_S}{l+n+1} \right)^2 + \frac{i}{\gamma_{nlm}} \left(\frac{am}{M} - 2\mu_S r_+ \right) (M\mu_S)^{4l+5}$$

- Described by Klein-Gordon equation in Kerr metric
[Press & Teukolsky (1972)
[10.1038/238211a0](https://arxiv.org/abs/10.1038/238211a0)]
- Simplifying assumption:
Newtonian potential, small coupling
[Detweiler (1980)
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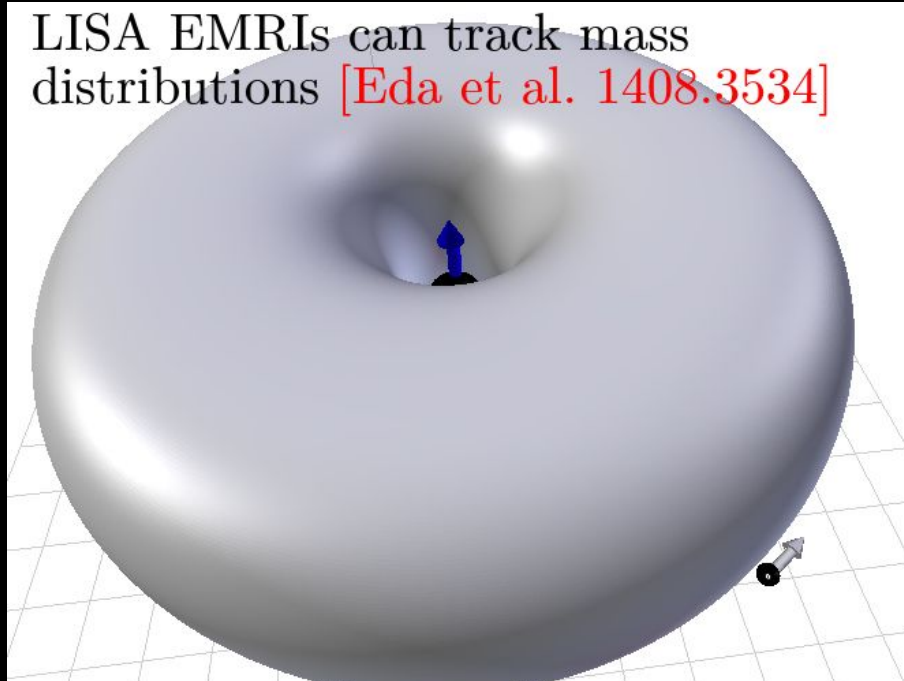
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$$\varphi(t, r, \theta, \phi) = ABre^{-Br/2} \cos(\phi - \omega_R t) \sin \theta$$

LISA EMRIs can track mass
distributions [Eda et al. 1408.3534]



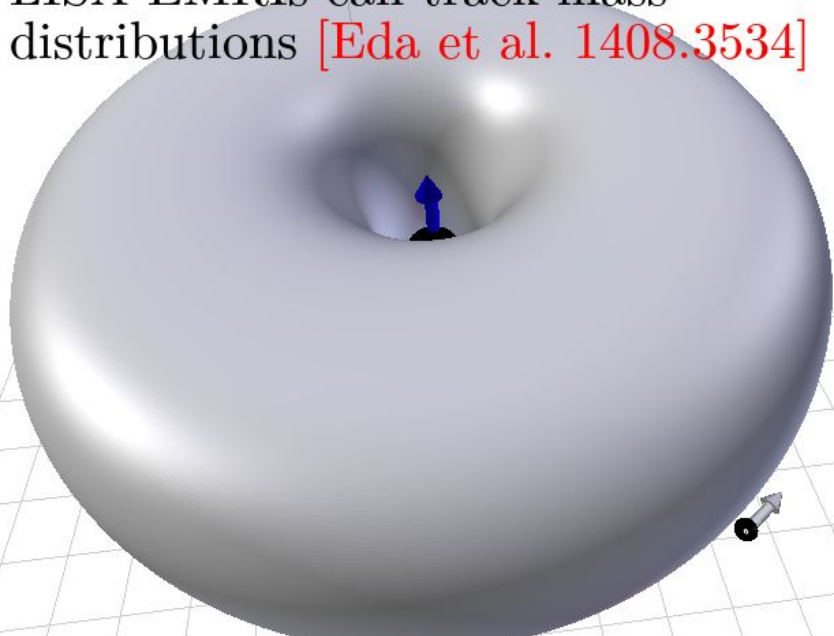
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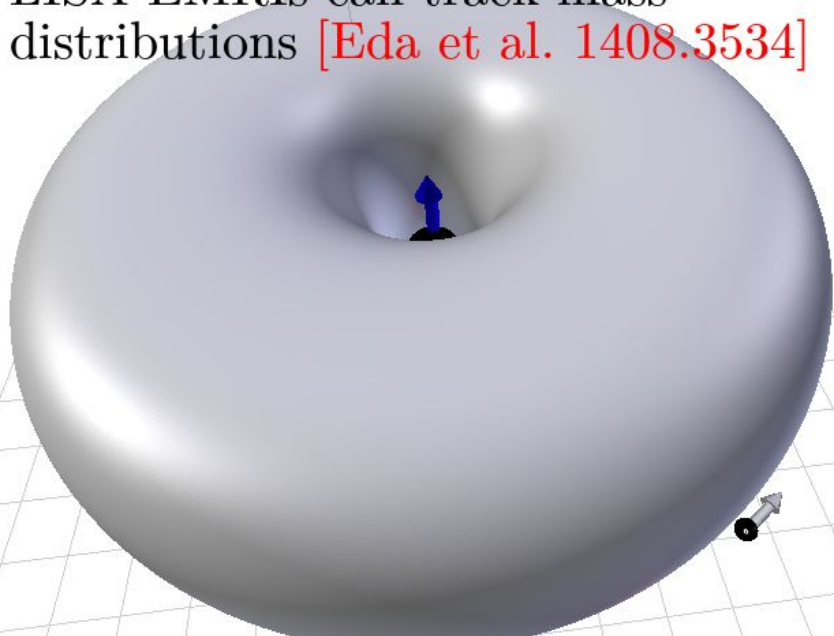
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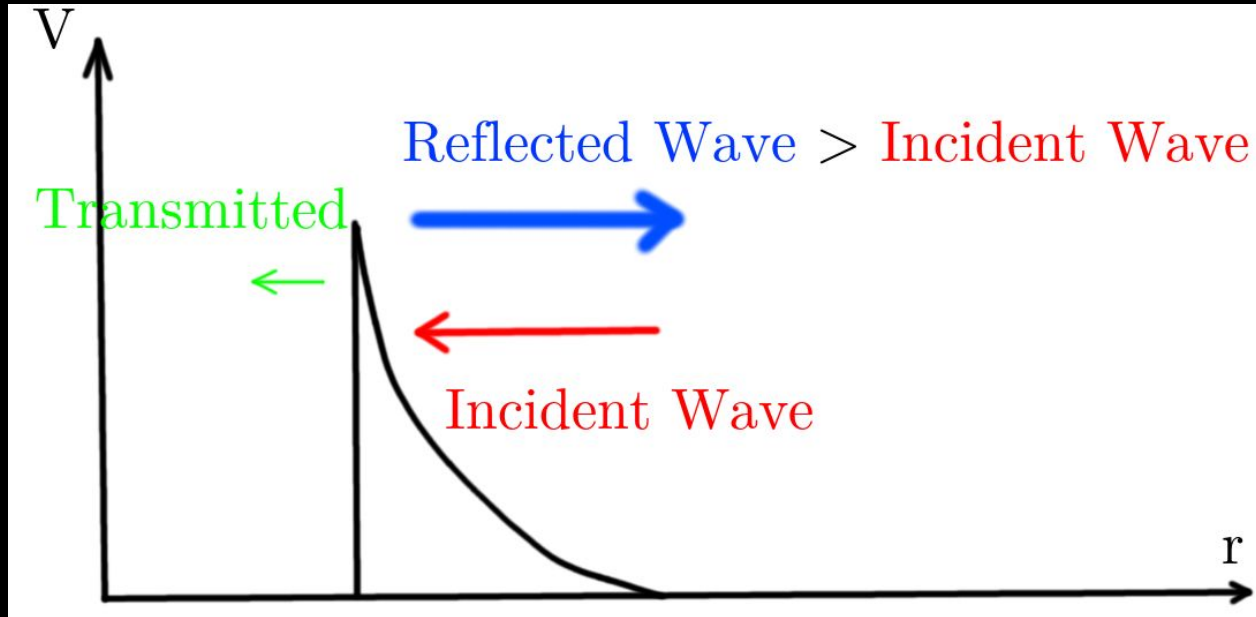
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Spontaneous Cloud Formation: Superradiant Scattering & instability

$$[\square - \mu_S^2]\Psi = 0$$

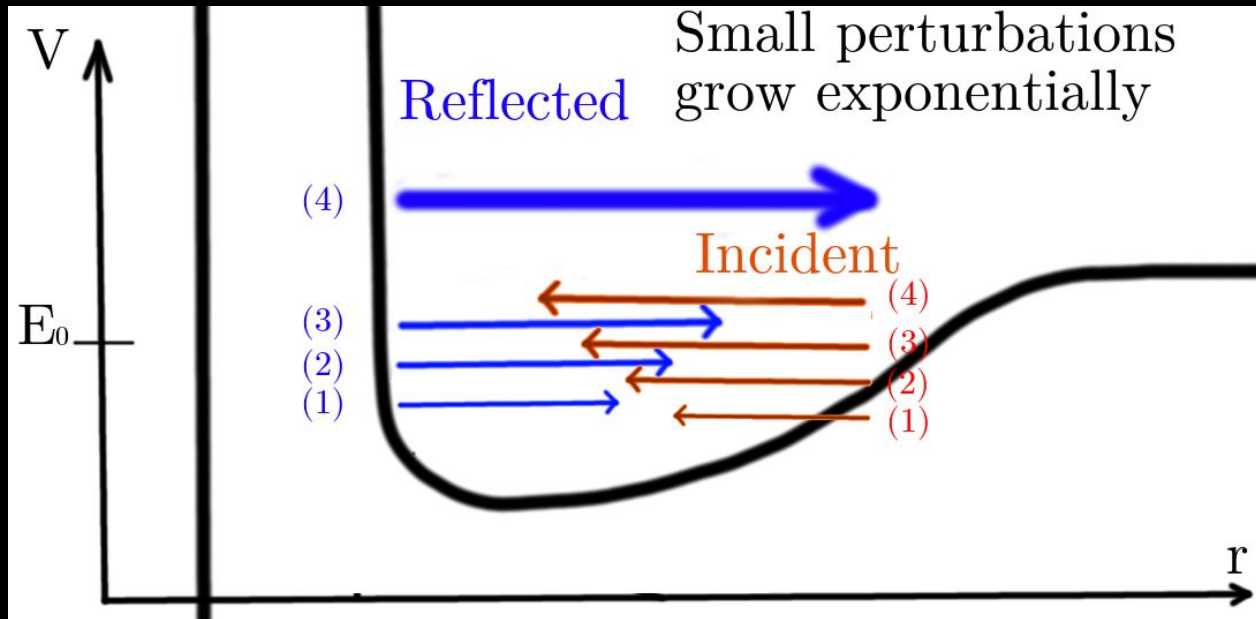
- Superradiance:
Wave analogue of Penrose process
[Zel'dovich (1971)
JETP Lett. 14, 180]



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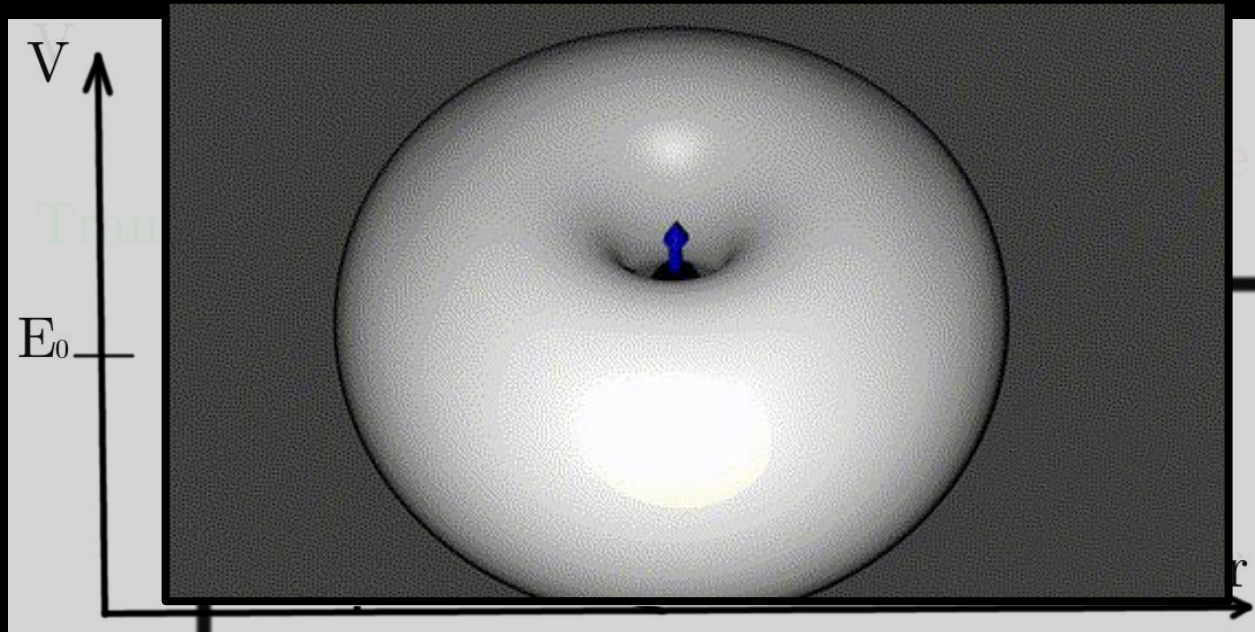
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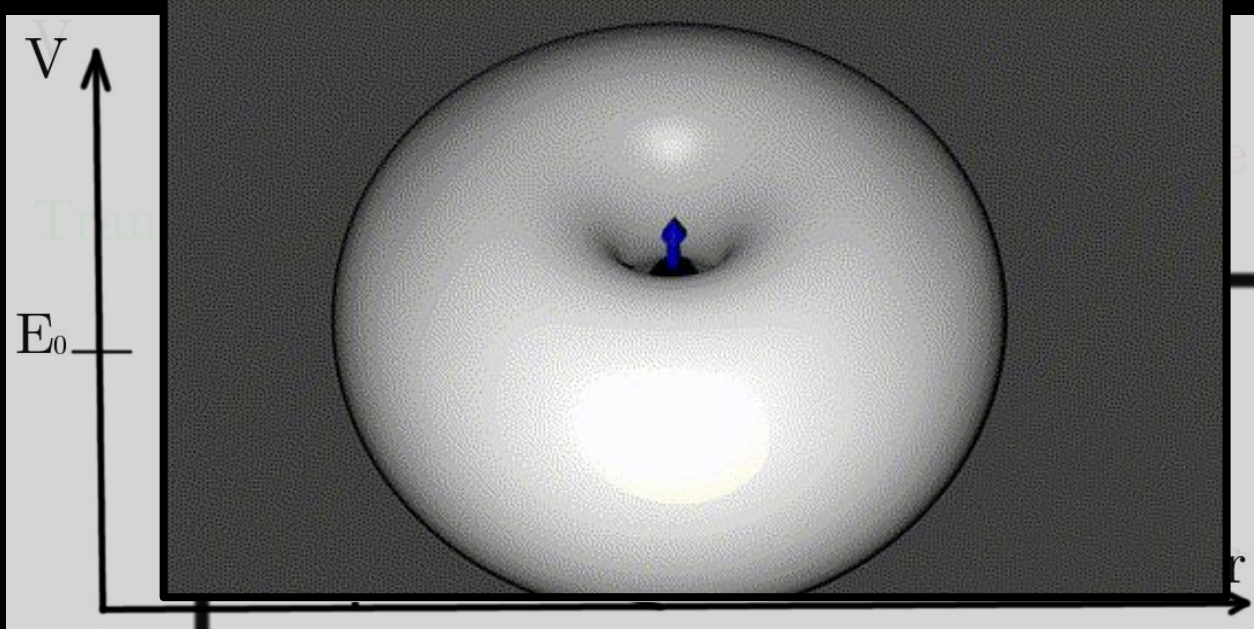
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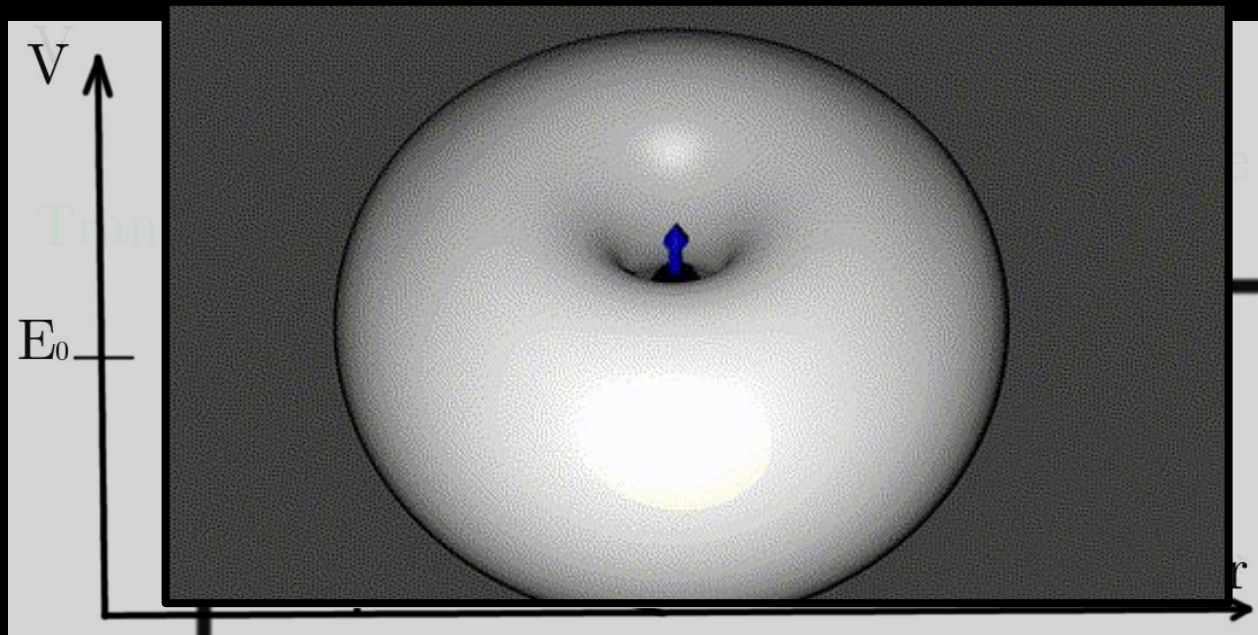
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- Spontaneous generation until critical spin
[Brito et al. (2015) 1411.0686]

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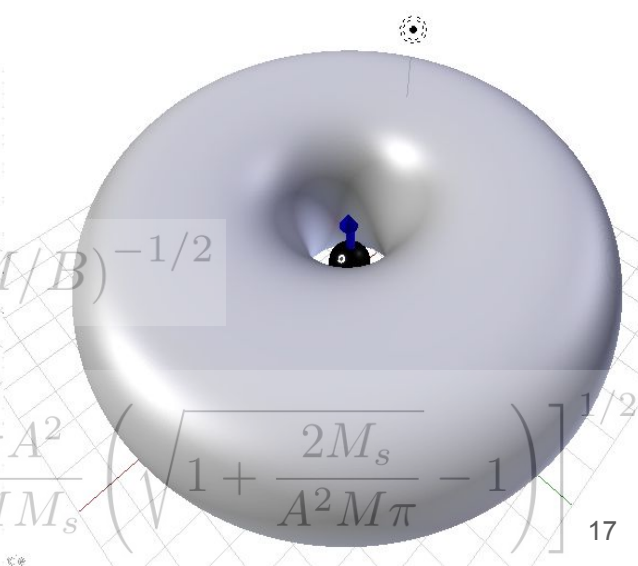
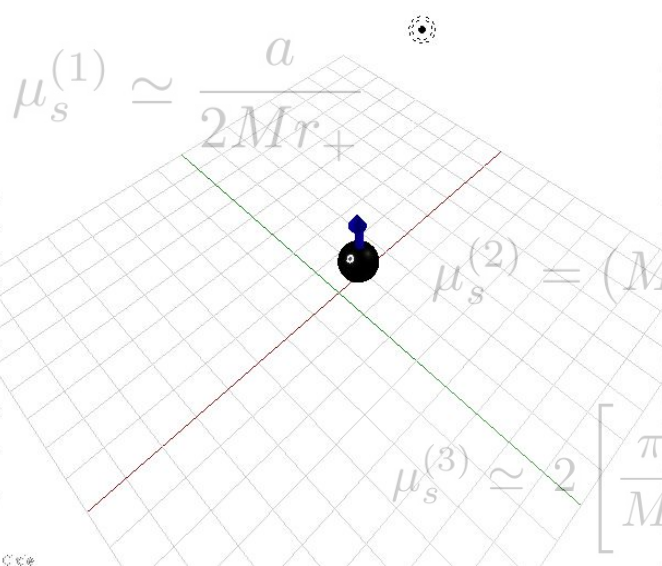
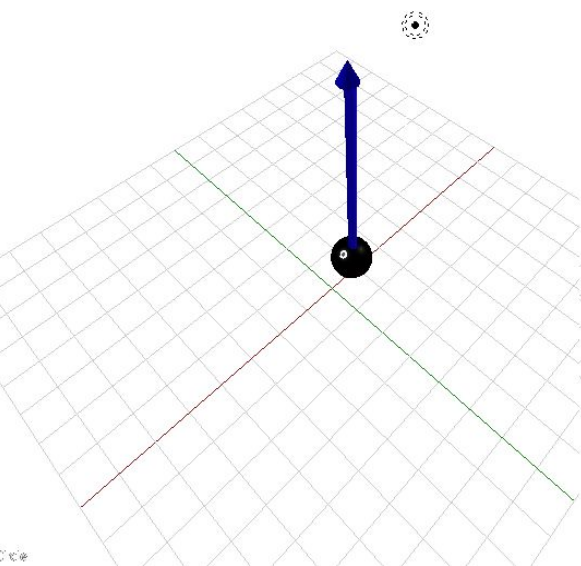
$$\mu_s^{(1)} \simeq \frac{a}{2Mr_+}$$

Superradiance Summary

Highly spinning BH

Superradiance spins down BH

Bosons created from rotational energy

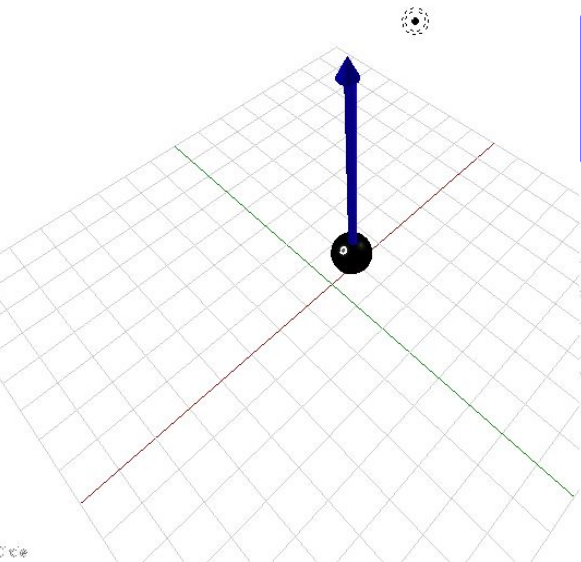


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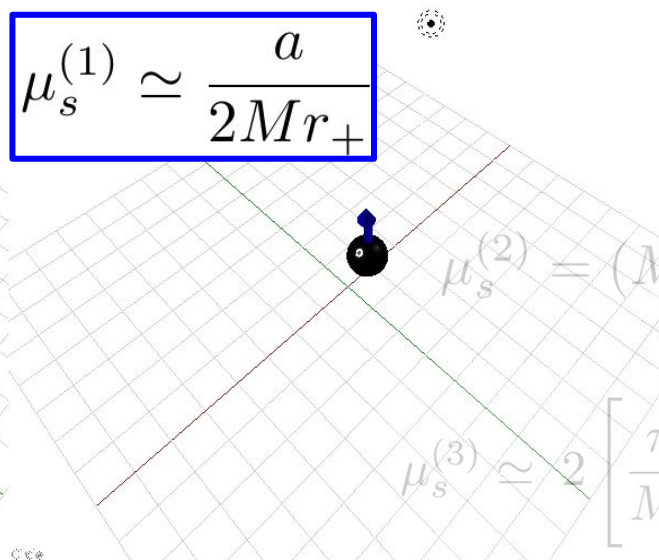
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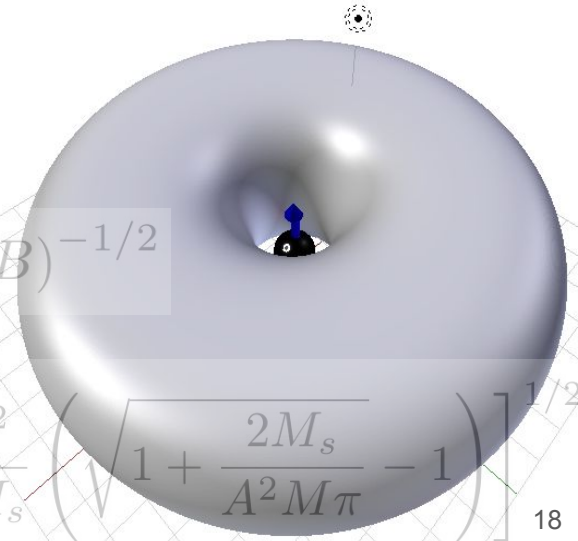


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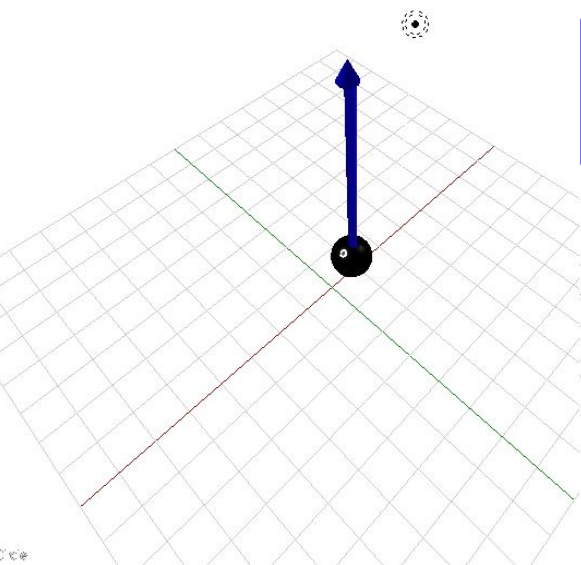
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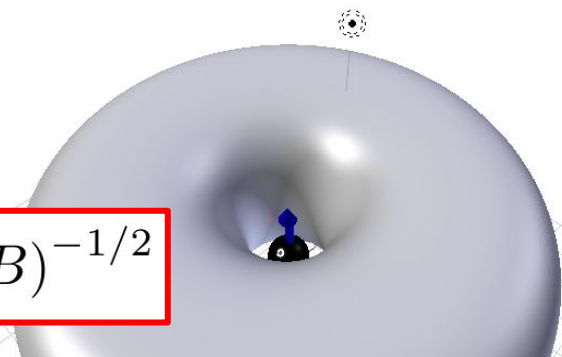


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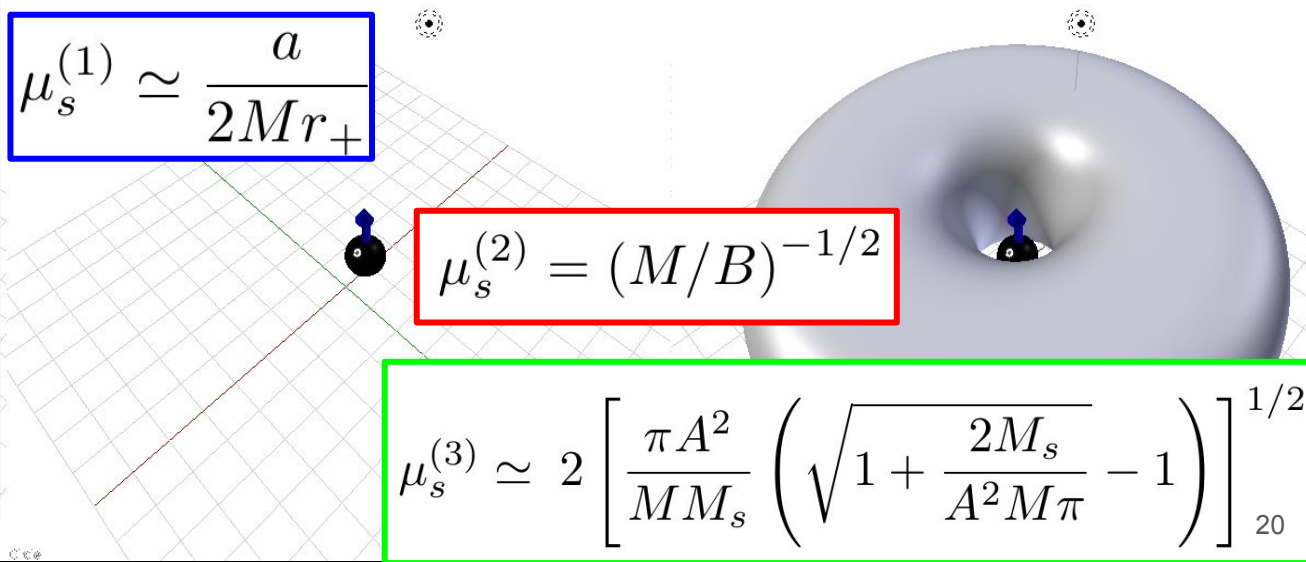
- Mass and spin measured to better than **1%** accuracy with **LISA**
- Matter effects resolvable even at lower than boson cloud densities
[Eda et al. (2014) 1408.3534]

Superradiance spins down BH Bosons created from rotational energy

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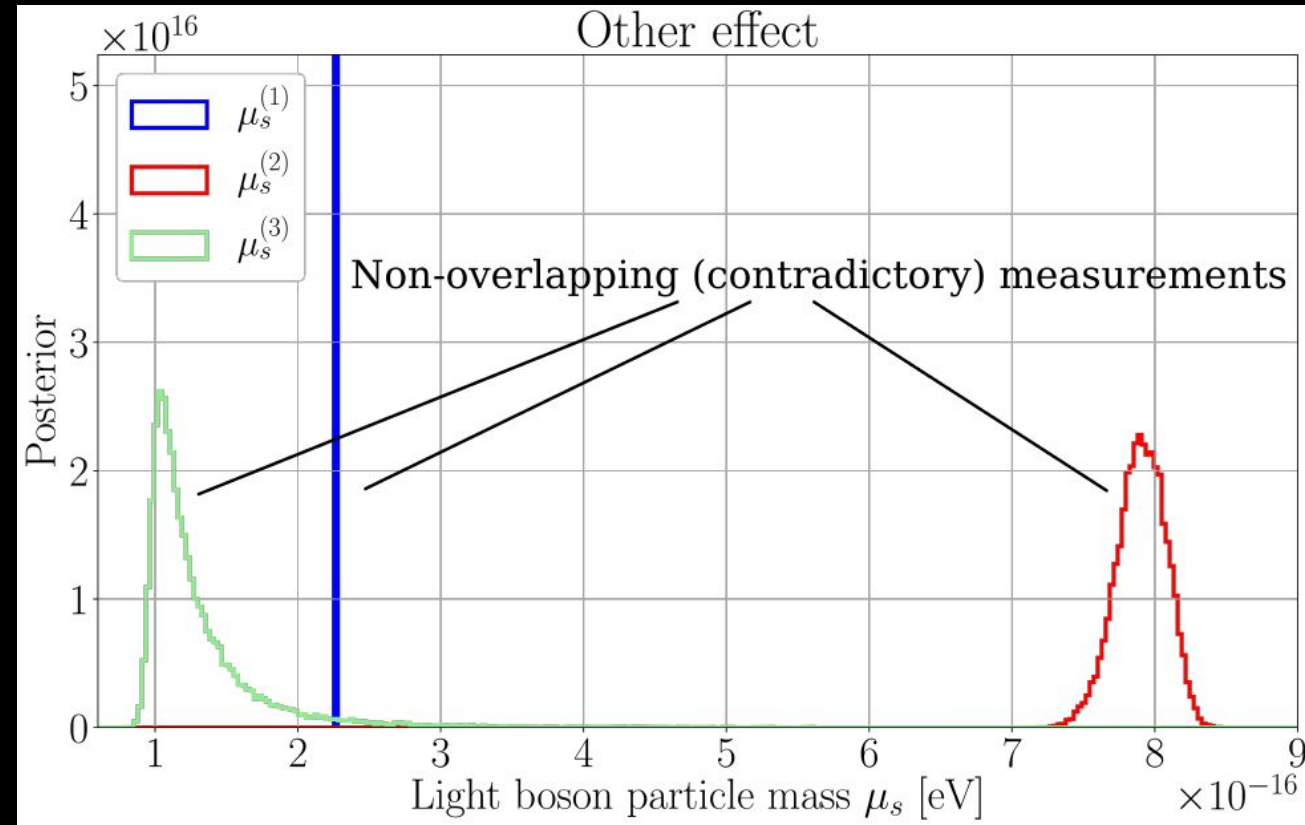
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- Critical spin: Spin-down by superradiance
- Characteristic scale of cloud: BH geometry
- Amplitude: Accretion and BH geometry

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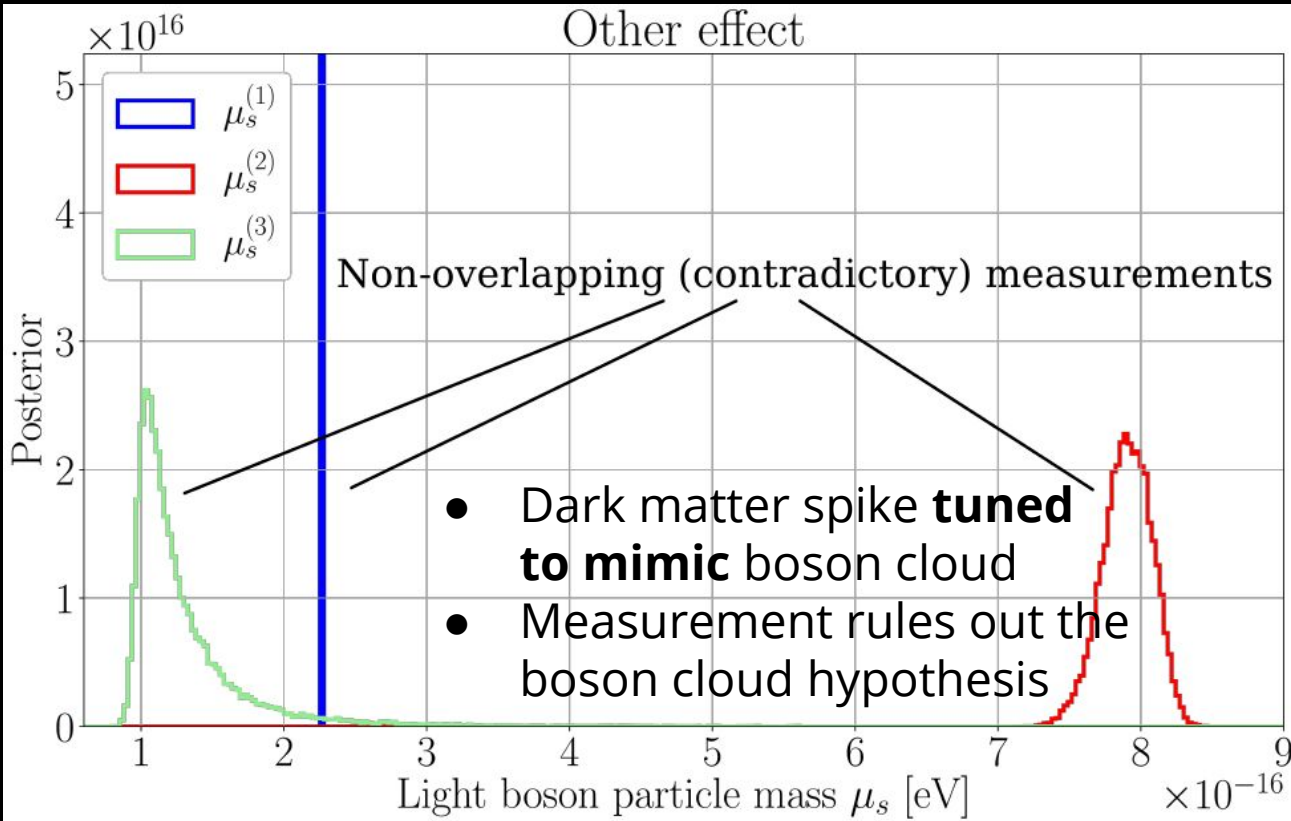
Verifying ultralight bosons



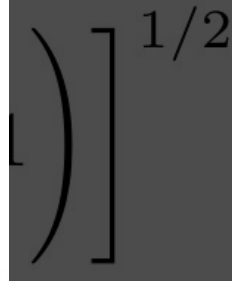
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)] ^{1/2}

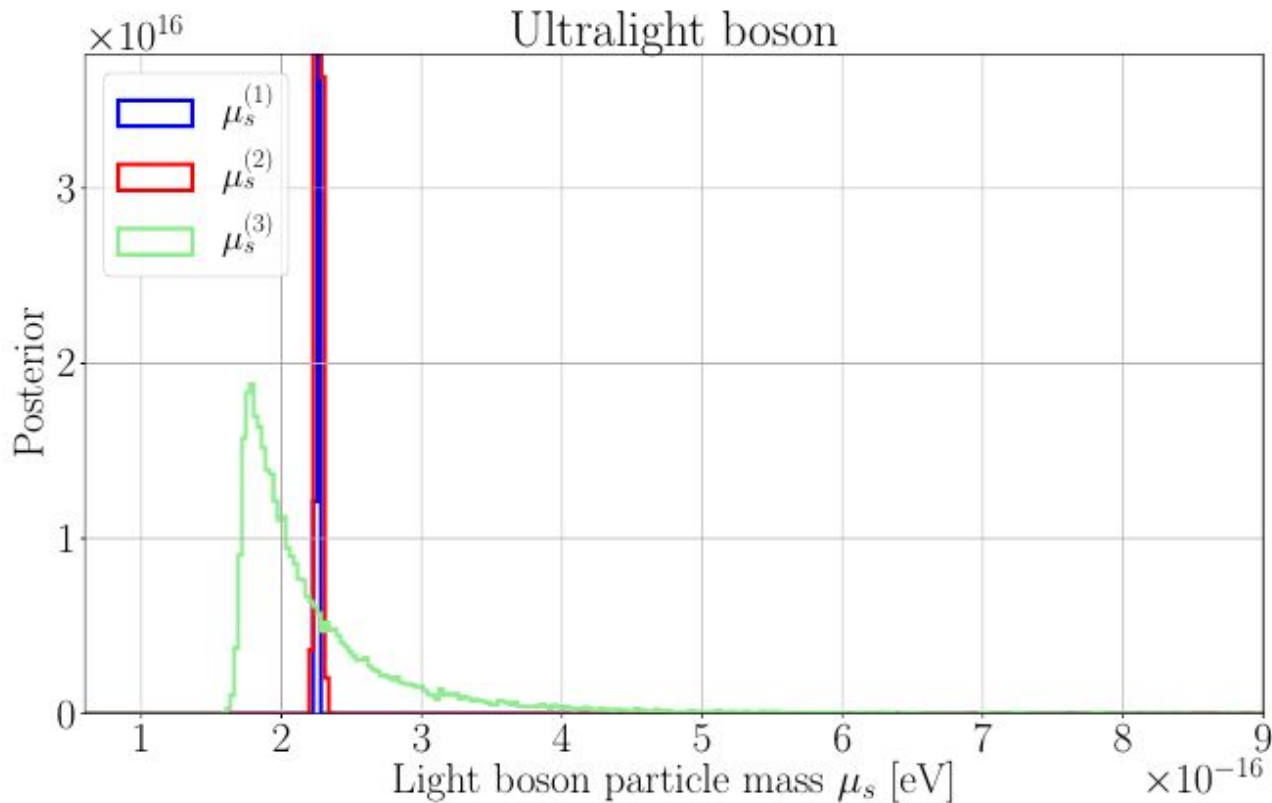
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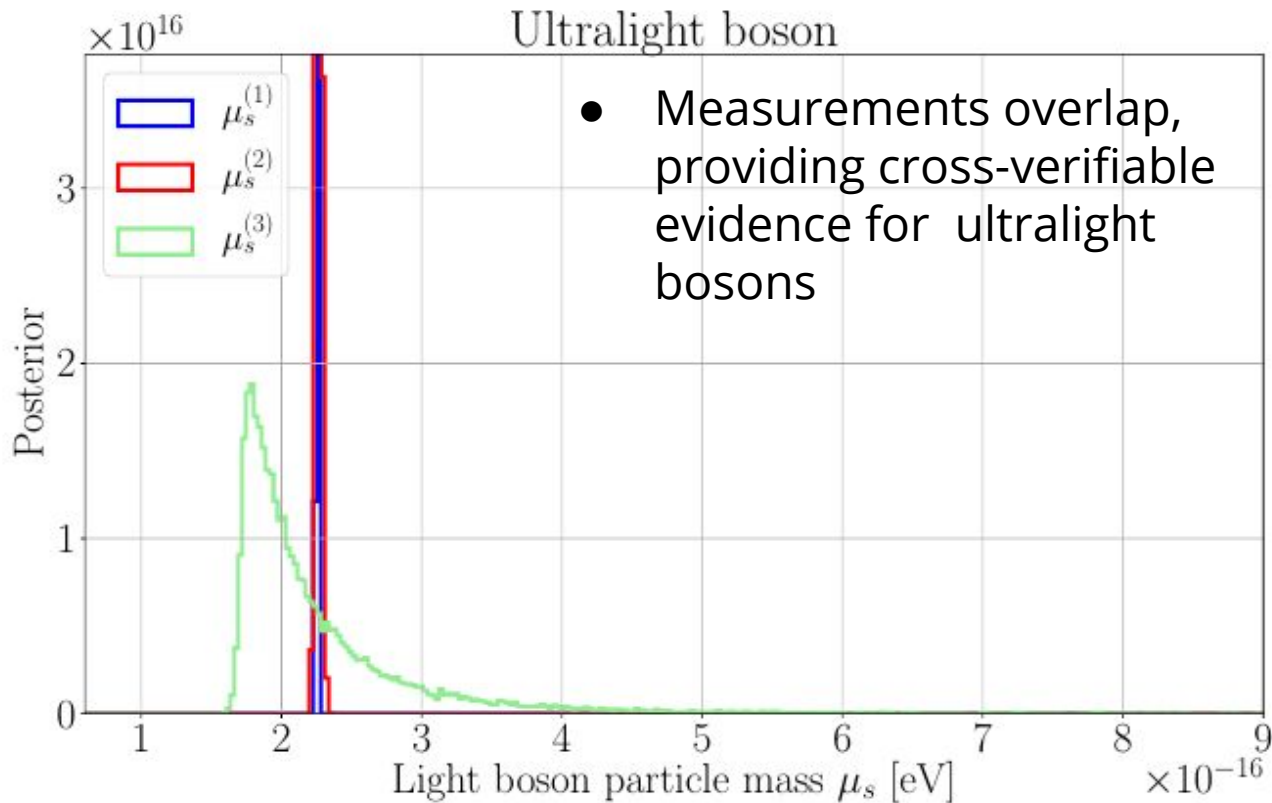
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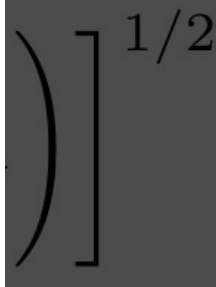
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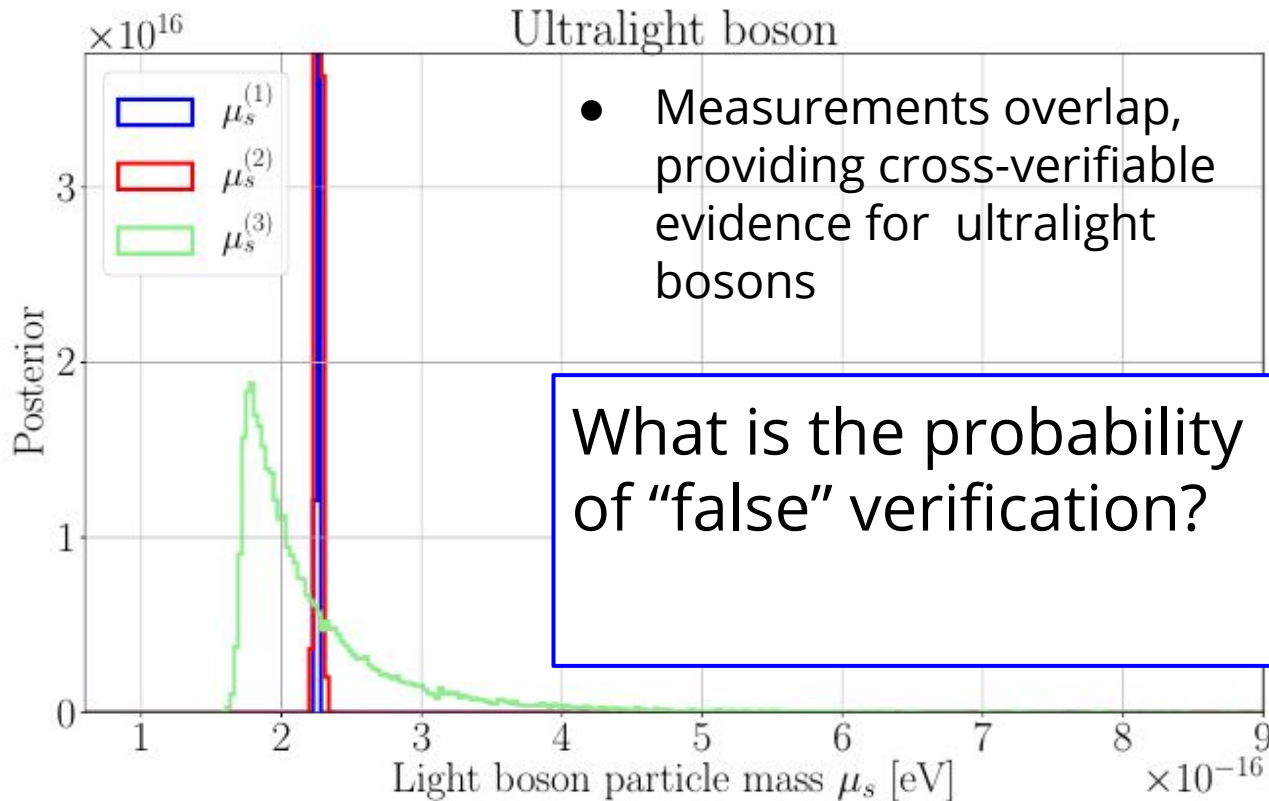
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)] $1/2$

Detections Across LISA Range

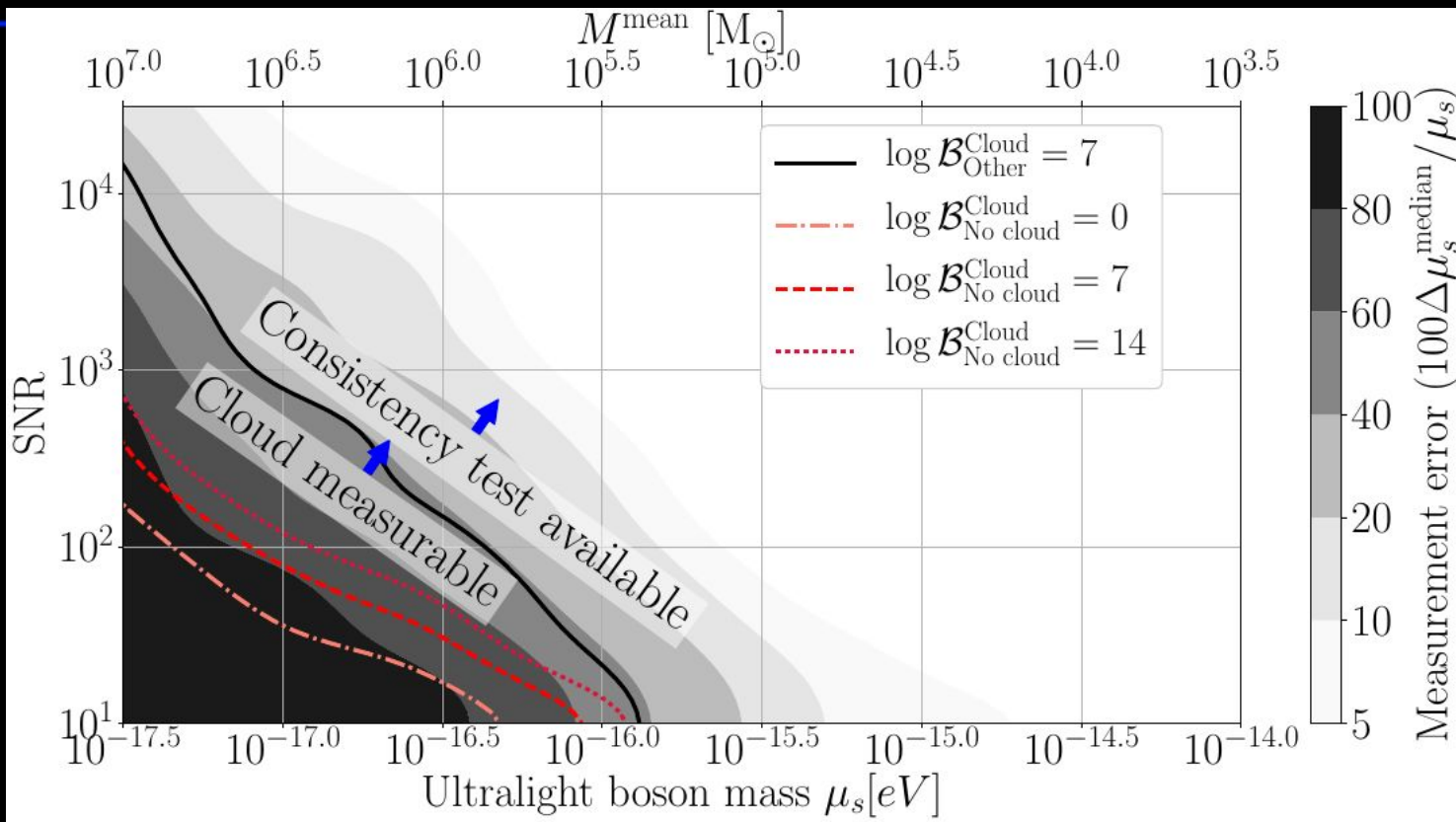
- Inject several GWs from various black hole/cloud systems
- Distribute spin linearly
- Distribute mass & mass ratio logarithmically

$$j \in [0.4, 0.98]$$

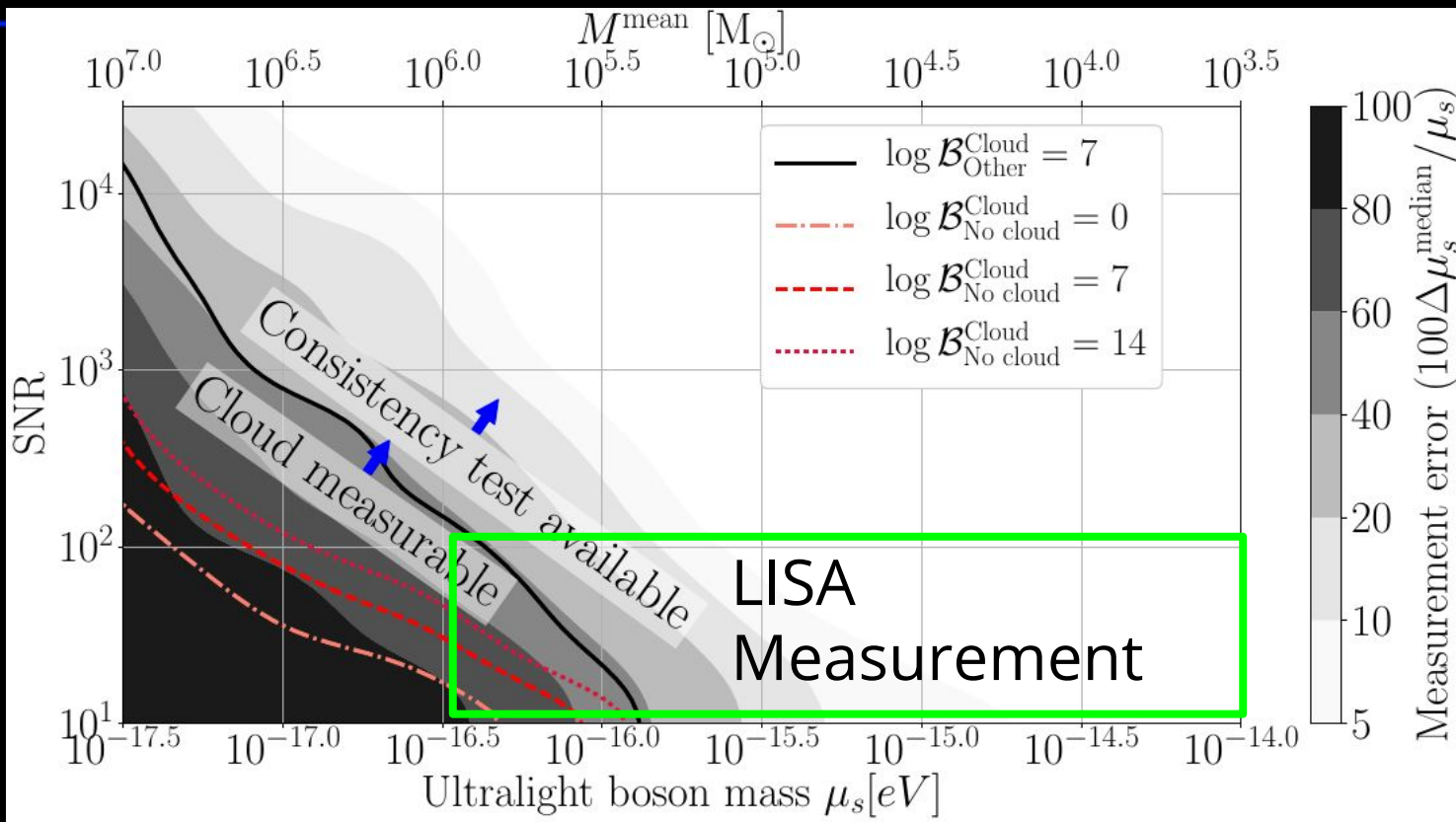
$$M \in [10^3, 10^7] M_{\odot}$$

$$q \in [10^{-3}, 10^{-2}]$$

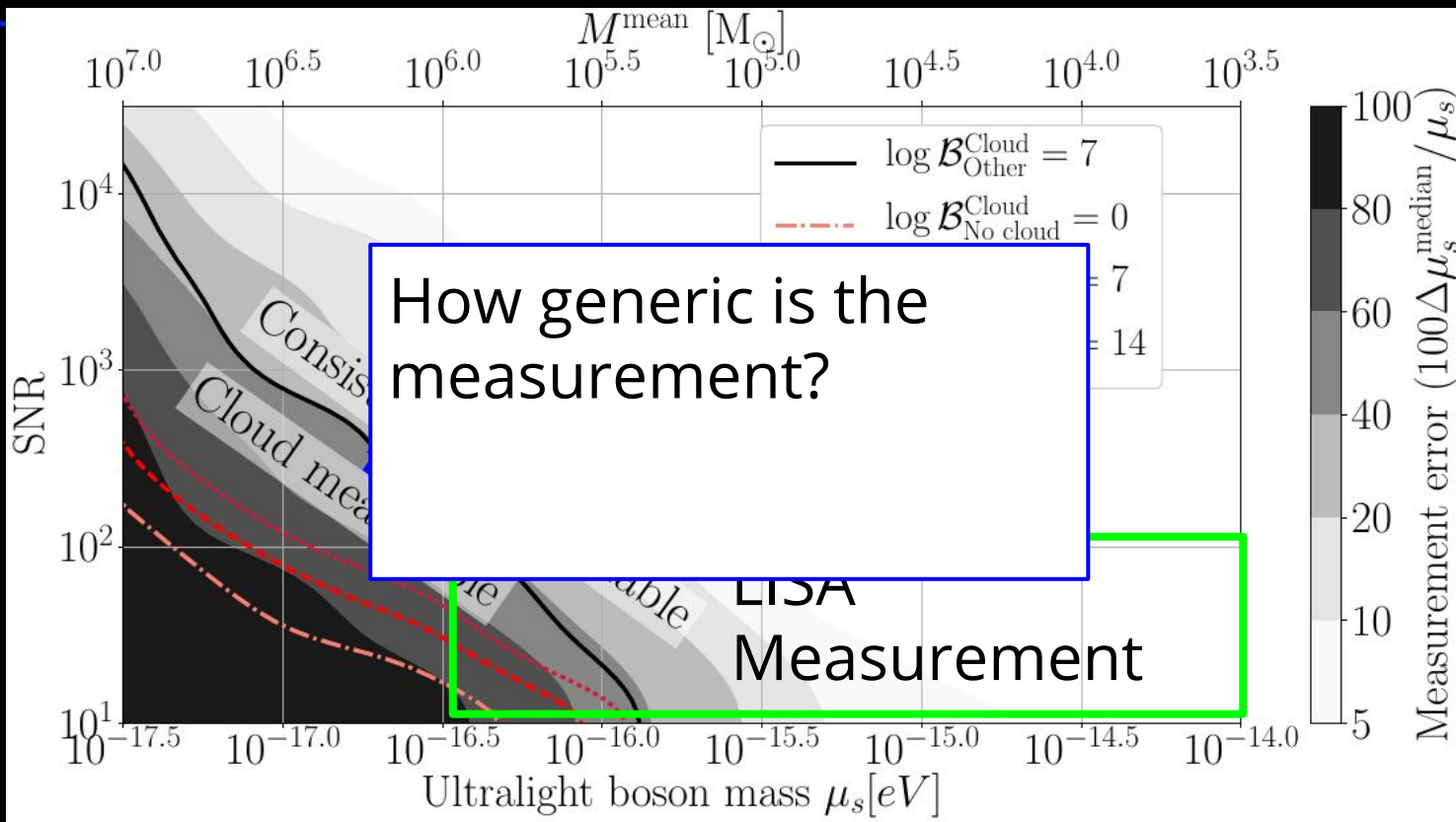
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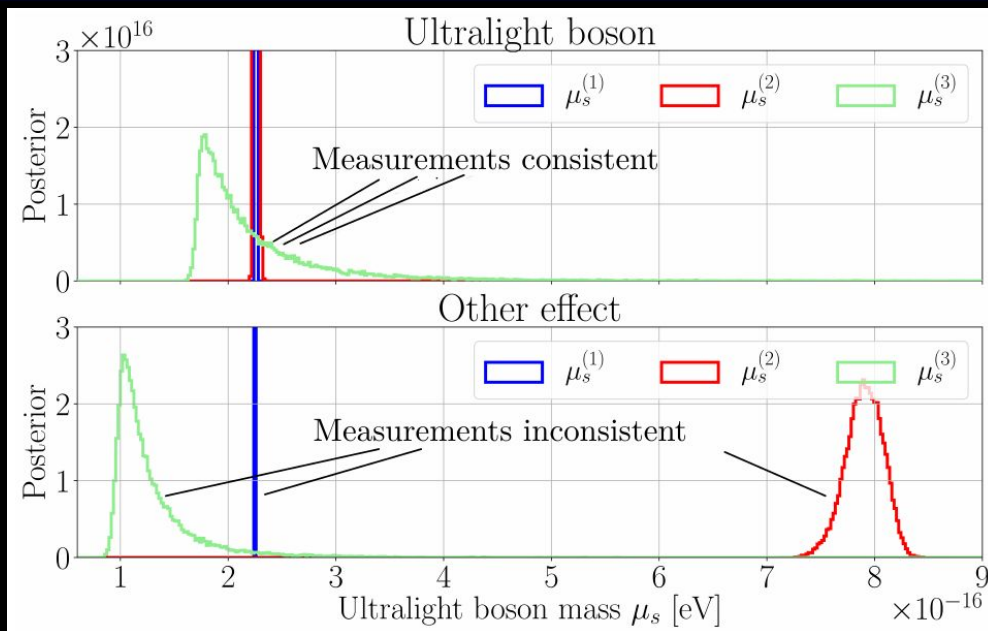


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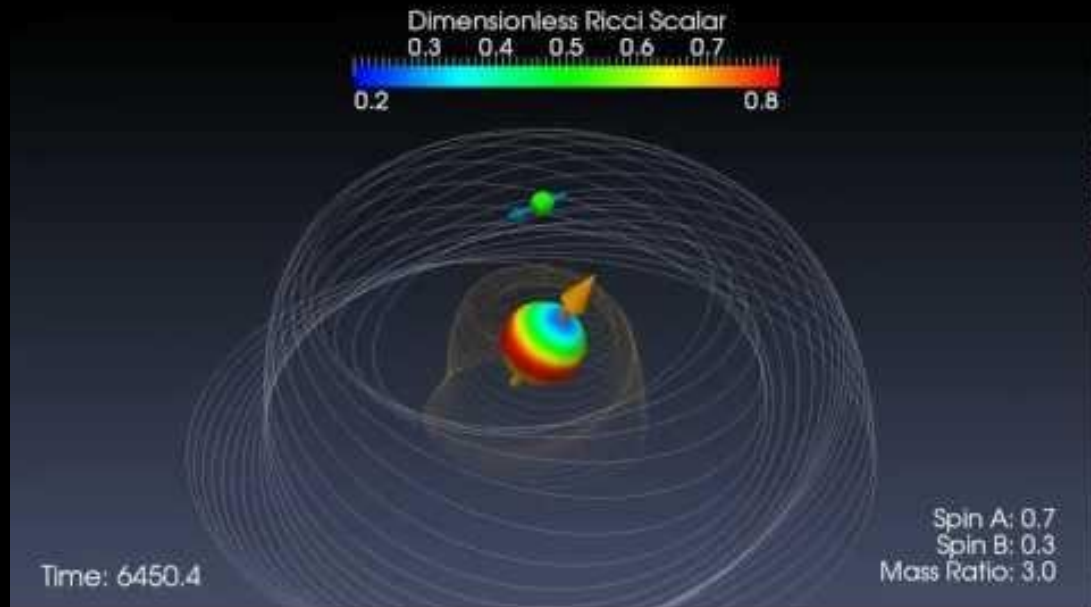
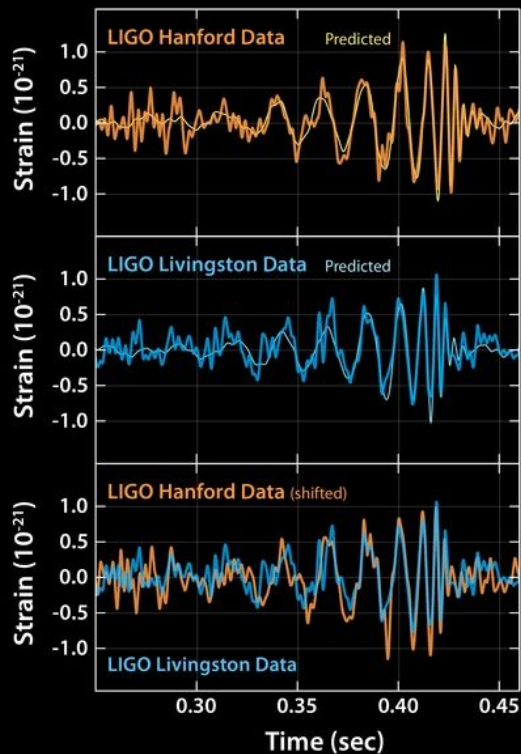
With continued progress:

- Ultralight bosons could be tested for across a wide mass range with LISA EMRIs using “consistency tests” that make use of the fact that black hole/cloud systems are over-determined



$$\mu_s \in [10^{-17}, 10^{-14}] \text{ eV}$$

Second part of the talk: LIGO/Virgo spin measurements



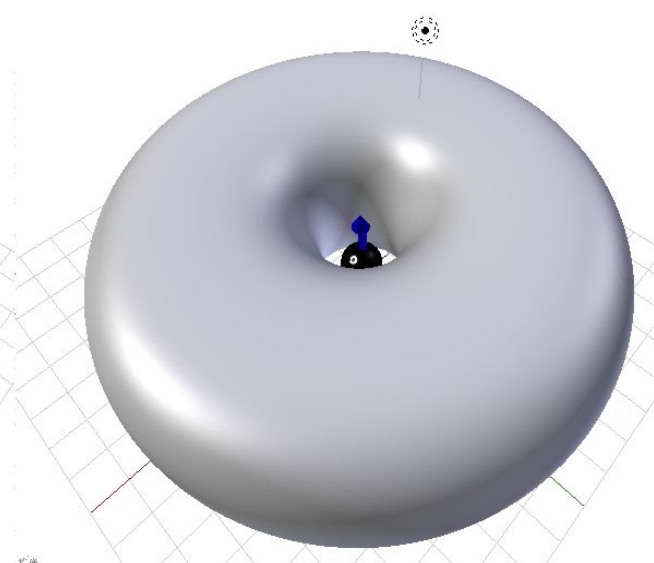
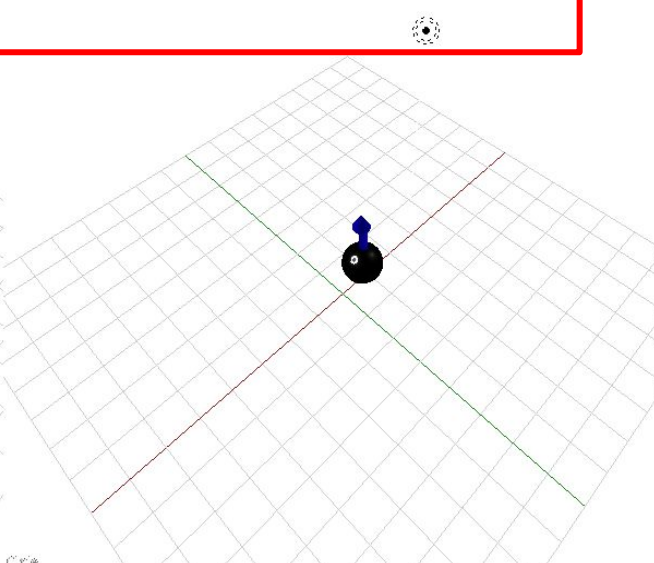
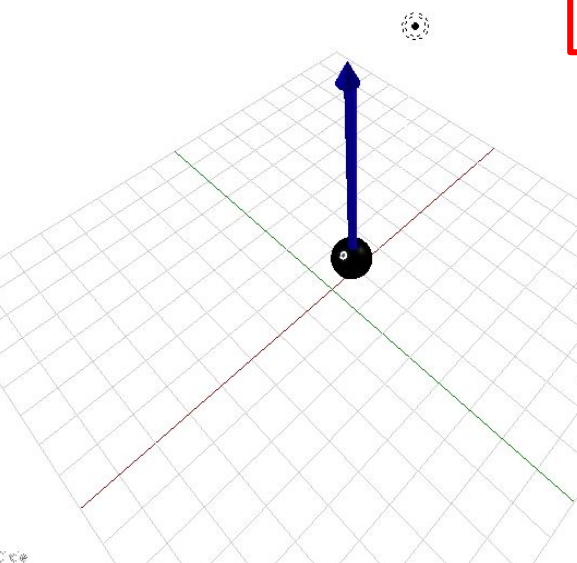
Credits: SXS collaboration

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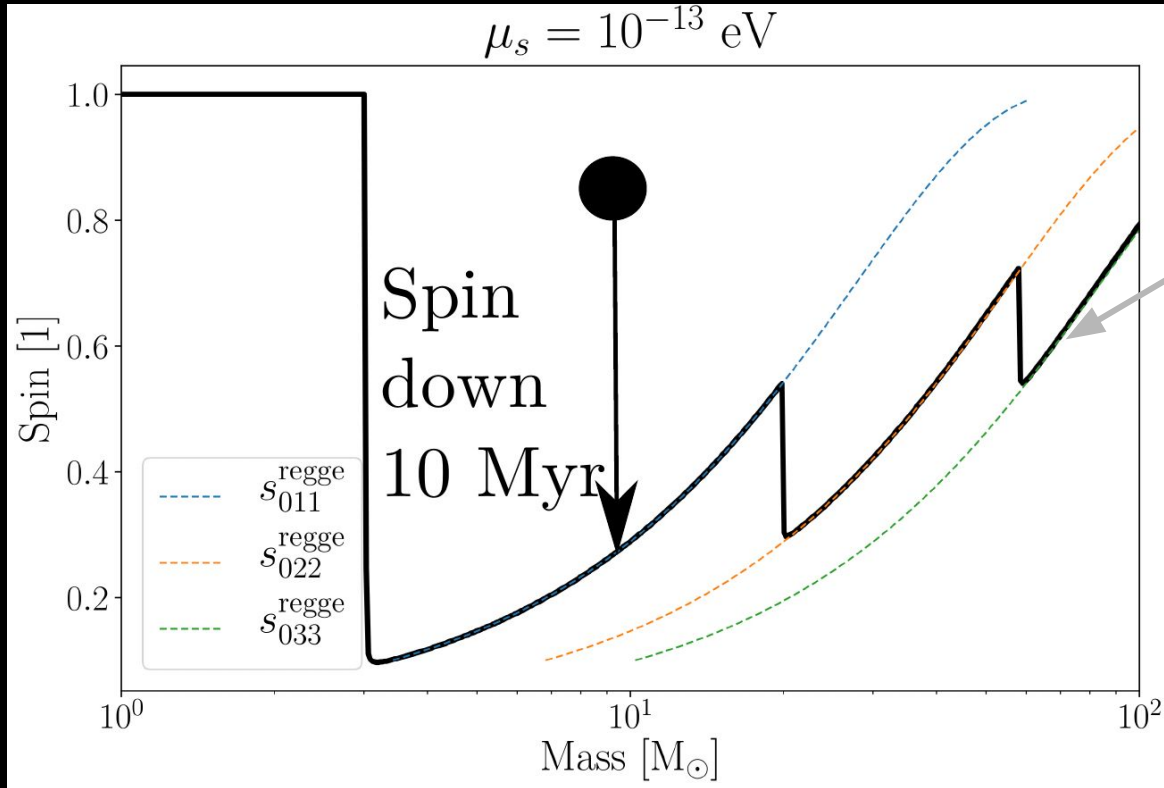
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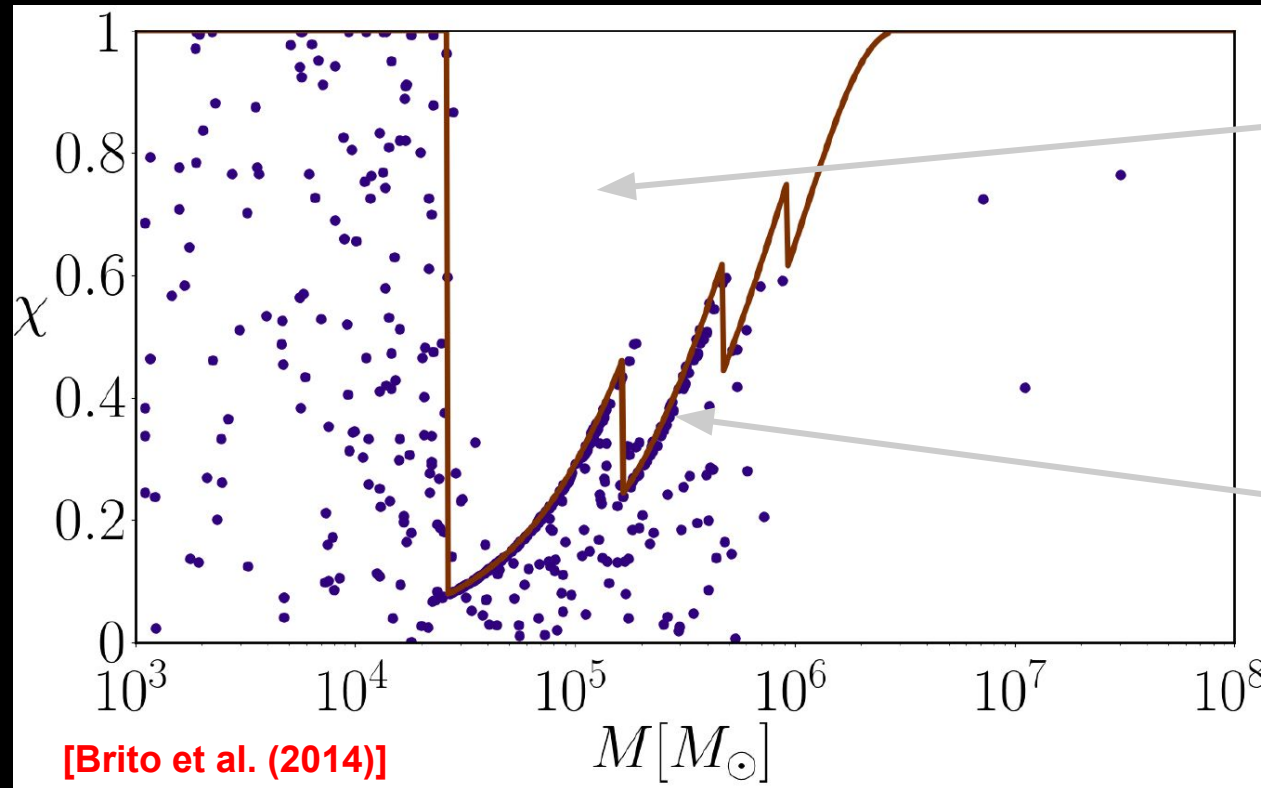


Regge trajectory



Regge trajectory

Regge trajectory



Regge gap (void of black holes at high spin)

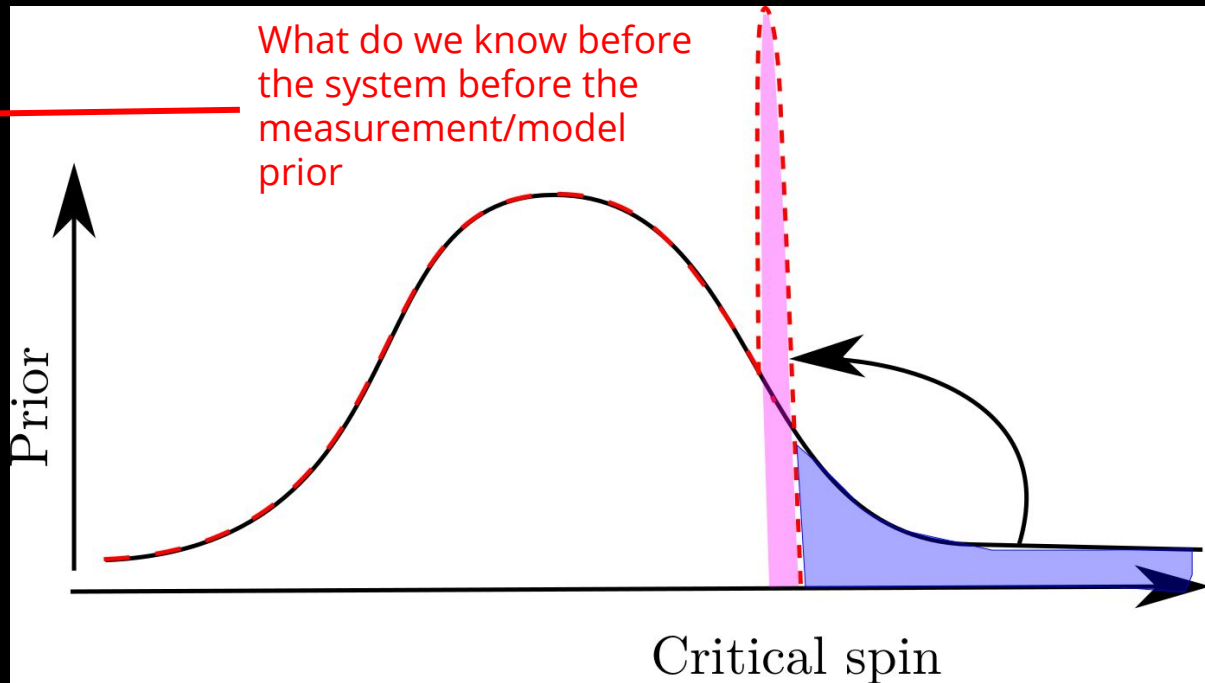
Black holes accumulate around the Regge trajectory

Incorporating the Regge trajectory to the GW analysis

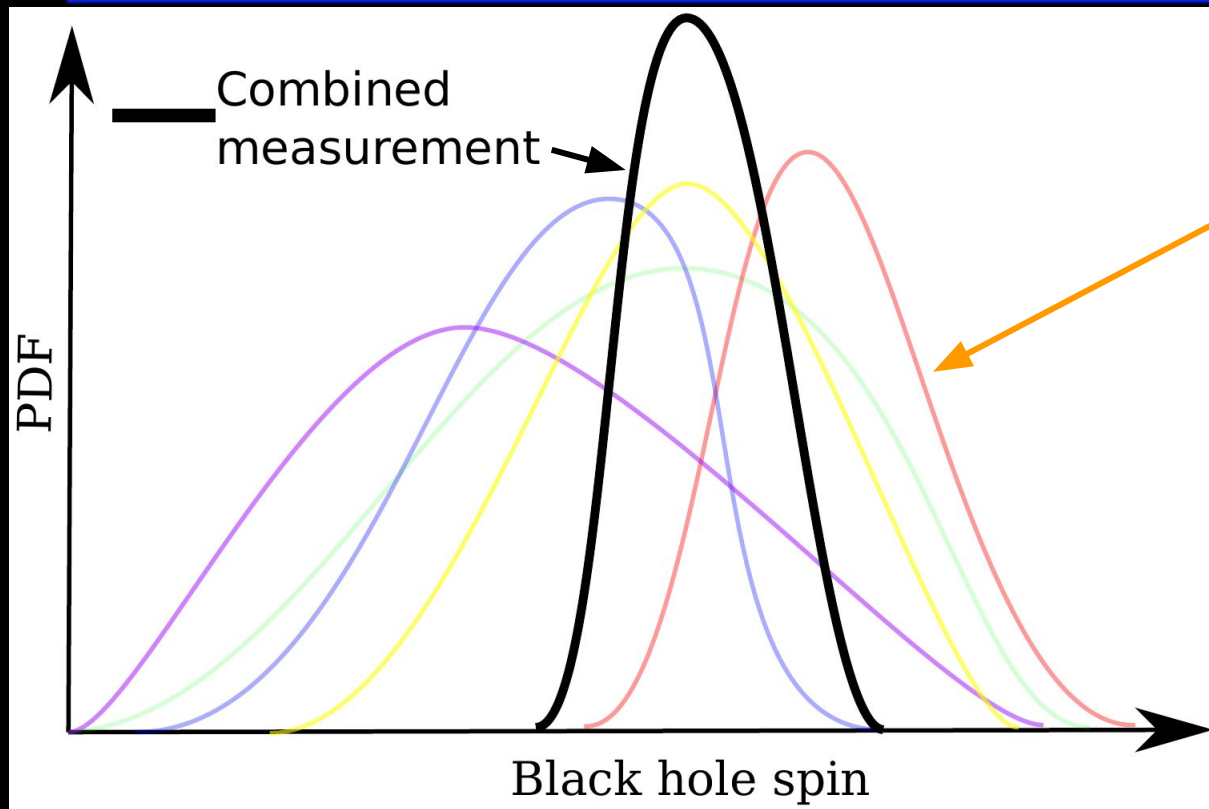
$$\mathcal{Z} = \int \mathcal{L}(\vec{\theta}) p(\vec{\theta}) d\vec{\theta}$$

How likely the model is correct / model evidence

How the GW and detector noise look like

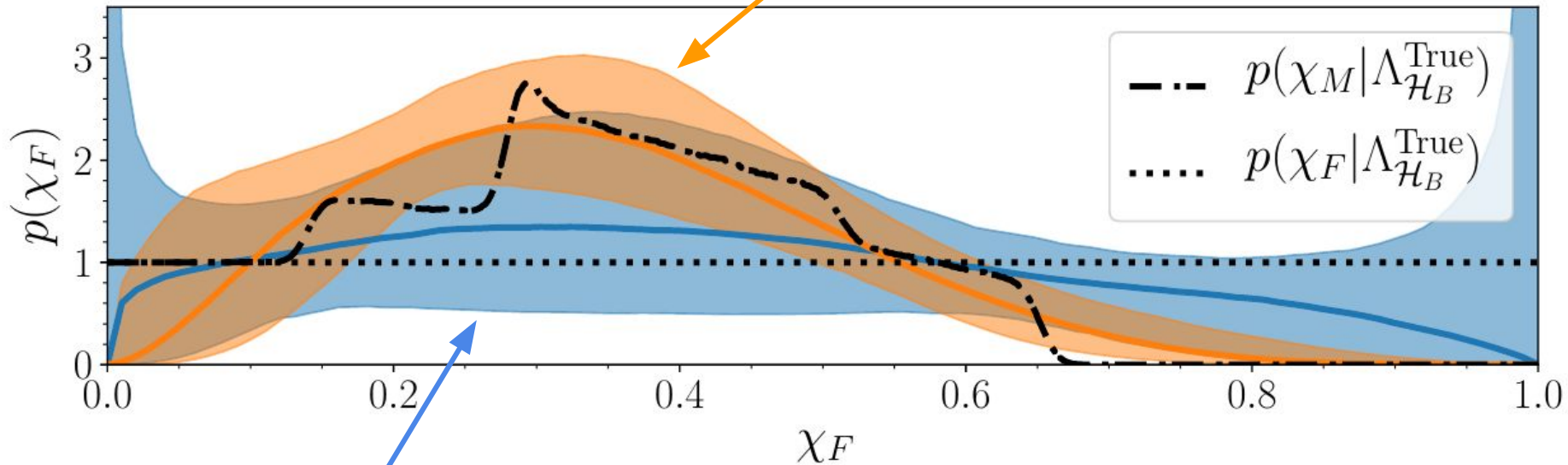


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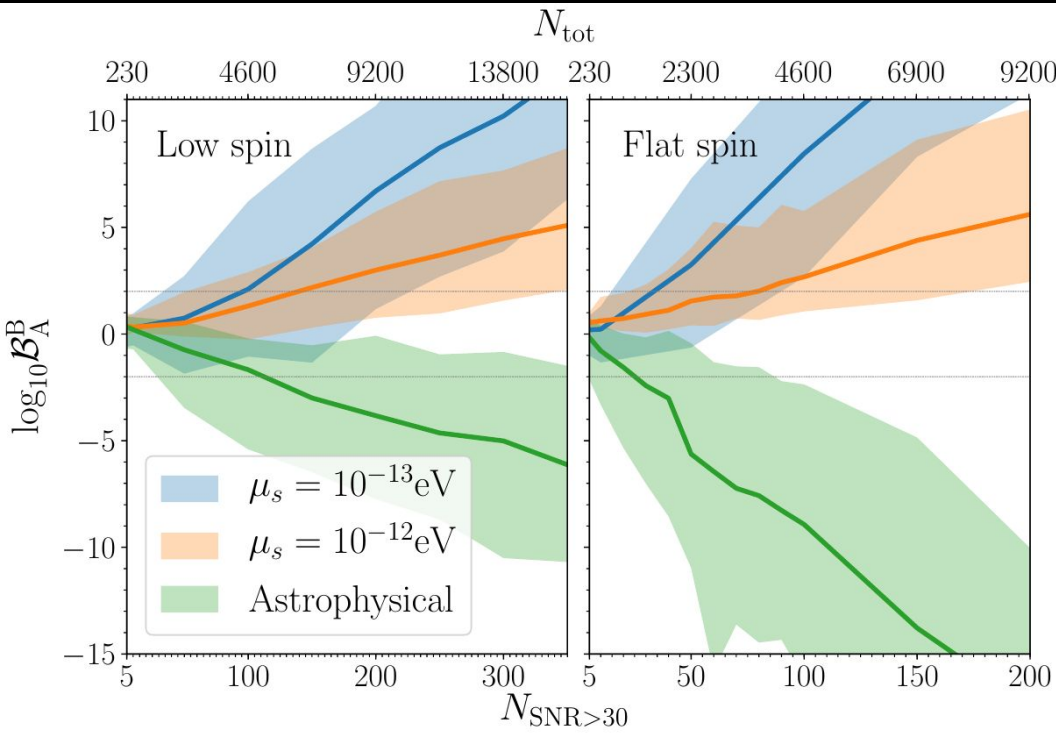
LIGO/Virgo spin measurements

Boson model tracks the Regge trajectory
(in this case dot-dashed black line)



Non-boson model consistent with the flat spin distribution
(dotted line) and doesn't capture the Regge trajectory with good precision

Model selection results



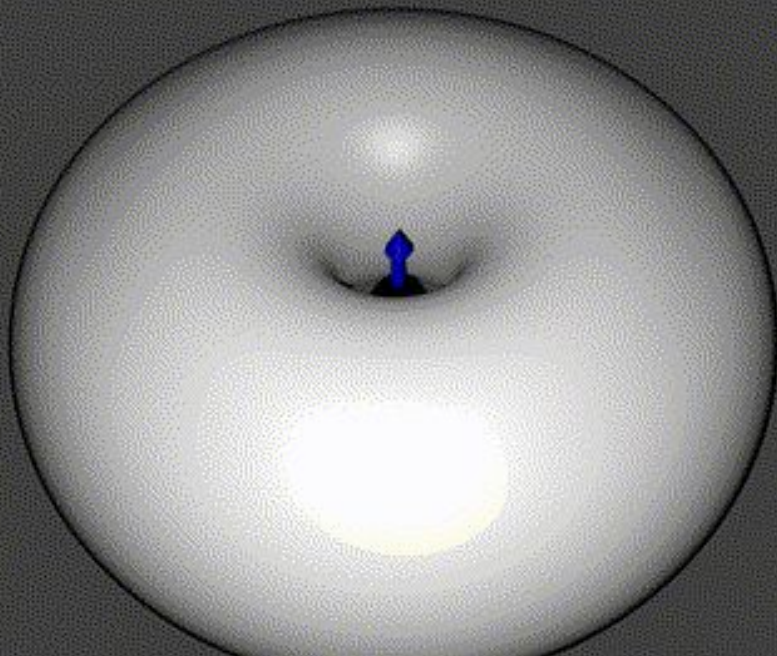
Population models Flat spin Low spin

Astrophysical	25^{+60}_{-20}	110^{+270}_{-80}
$\mu_s = 10^{-13} \text{ eV}$	35^{+55}_{-20}	95^{+130}_{-60}
$\mu_s = 10^{-12} \text{ eV}$	80^{+95}_{-55}	140^{+95}_{-85}

Forecast:

- LIGO/Virgo at design sensitivity: May rule out light bosons
- Einstein telescope: Might confirm the light bosons if they exist.
- Better models including selection effects and binary inspiral modeling could yield more stringent results

Summary

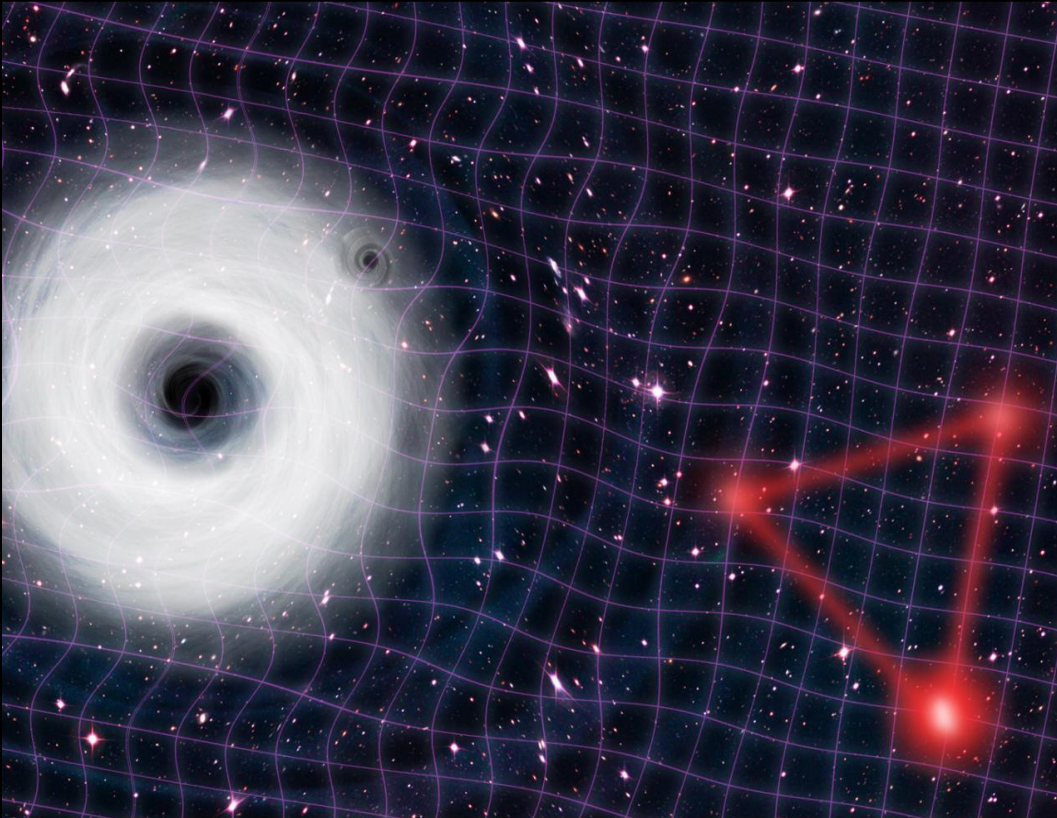


- Light bosons couple to black holes, spinning them down, and forming massive 'clouds'.
- The clouds could be tested for across a wide mass range with LISA EMRIs using "consistency tests"
- LIGO/Virgo and future ground-based detectors might allow us to probe the bosons through black hole spins

Thank you

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