The Higgs fine-tuning problem

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Put my head here







Related to theory parameters, but how?

What do you measure?

 $\mathscr{L}_{\text{higgs}} = (D_{\mu}\Phi)^{\dagger}(D_{\mu}\Phi) + m_{\text{h}}^{2}\Phi^{\dagger}\Phi - \lambda \left(\Phi^{\dagger}\Phi\right)^{2} \qquad \left(\lambda = \frac{2m_{h}^{2}}{v^{2}}\right)$



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Beyond tree level, this potential receives corrections!







What do you measure?





"The need for scalar particles is a serious flaw"

Where the trouble began

L. Susskind - Dynamics of spontaneous symmetry breaking in the Weinberg-Salam theory (1978)

The Hierarchy problem

Proton mass 1 GeV 100 GeV W,Z, higgs mass

Planck scale 10¹⁹ GeV



Susskind's realization

• At the Planck scale our theory breaks down and gravity effects start to play an important role

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Susskind's realization

- highest mass
- become of the order of the Planck scale!



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• Therefore QM corrections on the Higgs boson mass







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Hierarchy problem = fine-tuning problem!





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The scale of new physics must **in some way couple** to the Higgs boson!



125 GeV

New insight M. Veltman - *The infrared-ultraviolet connection* (1980)

Builds on Susskind's paper, but with one small modification:

"One must compare the size of the QM *corrections* to the size of the observed quantity"



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Hierarchy problem ≠ fine-tuning problem!



Large hierarchies are allowed without introducing a fine-tuning problem!

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But in which cases does it introduce a fine-tuning problem?

Higgs is special

G. 't Hooft - Naturalness, Chiral symmetry and spontaneous chiral symmetry breaking (1979)

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We will come back to this point





It is about the Planck scale!

Higgs fine-tuning?

No, it is about the QM corrections!





And the lack of symmetries are to blame!





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And the lack of symmetries are to blame!



Fine-tuning is...

...when an observable (e.g. the Higgs mass) changes a lot as a consequence of a tiny change in other observables of the theory

The Higgs fine-tuning is **not the same as**...

- The hierarchy problem
- (Technical) naturalness, the demand that every parameter should be of O(1)
- A volume in parameter space that gives rise to the observed quantities

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Moreover, Higgs fine-tuning does not appear in the SM!

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Take home messages

- Is not directly caused by a hierarchy of scales
- has no fine-tuning problem

• Fine-tuning occurs when an observable (e.g. the Higgs mass) changes a lot as a consequence of a tiny change in the other observables of the theory

Can only occur in beyond-the-SM scenarios; the SM

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And now the fun begins...

Let's put this into formulas!




Higgs propagator at tree level:

Full Higgs propagator:



one-loop self energy







 $\frac{i(p'-k+m_f)}{(p-k)^2-m_f^2} \frac{i(-k+m_f)}{k^2-m_f^2}$



$$= -\int \frac{d^4k}{(2\pi)^4} \frac{\text{Tr}[(p-k+m_f)]}{(p-k)^2 - m_f^2}$$

 $\frac{(-k+m_f)}{k^2 - m_f^2}$



$$= -\int \frac{d^4k}{(2\pi)^4} \frac{\text{Tr}[(p - k + m_f)]}{(p - k)^2 - m_f^2}$$

 $\frac{f}{n_{f}^{2}} \frac{(-k+m_{f})}{k^{2}-m_{f}^{2}} \left(\frac{-iy_{f}}{\sqrt{2}}\right)^{2}$









$$= -\int \frac{d^4k}{(2\pi)^4} \frac{\text{Tr}[(p - k + m_f)]}{(p - k)^2 - m_f^2}$$



This diverges, so we need to regulate it!



1. Use a 'UV cut-off' regulator Λ

$$\int d(k^2) \quad \rightarrow \quad \int_0^{\Lambda^2} d(k^2)$$

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It carries no physical meaning

1. Use a 'UV cut-off' regulator Λ

$$\int d(k^2) \longrightarrow \int_0^{\Lambda^2} d(k^2)$$

One has to absorb Λ in the bare (unmeasurable!) parameters of the theory

$$m_{\rm h}^2 \to m_{\rm h, phys}^2 - \Lambda^2$$

$= \Lambda^2 \quad \longrightarrow \quad i\Pi(p^2) \propto \Lambda^2$

$$m_{\rm h}^2 + i\Pi \rightarrow m_{\rm h, phys}^2$$



$$\int \frac{\mathrm{d}^4 \mathrm{k}}{(2\pi)^4} \to \int \frac{\mathrm{d}^{4-\epsilon} \mathrm{k}}{(2\pi)^{4-\epsilon}}$$

 $y_f \rightarrow y_f \, \mu^{-\frac{c}{2}}$



 $= -\int \frac{\mathrm{d}^4 k}{(2\pi)^4} \frac{\mathrm{Tr}[(p - k + m_f)]}{(p - k)^2 - m_f^2} \frac{(-k + m_f)}{k^2 - m_f^2} \left(\frac{-iy_f}{\sqrt{2}}\right)^2$



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$$= -\int \frac{d^{4-\epsilon}k}{(2\pi)^{4-\epsilon}} \frac{\text{Tr}[(p-k+m_f)]}{(p-k)^2 - m_f^2} \frac{(-k+m_f)}{k^2 - m_f^2}$$

$$\stackrel{p^2 = m_h^2 \to 0}{=} \frac{3iy_f^2}{4\pi^2} m_f^2 \left[-\frac{1}{\epsilon} + \ln\left(\frac{m_f^2}{\mu^2}\right) + \dots \right]$$

 $\frac{-m_f)}{m_f^2} \left(\frac{-iy_f\mu^{-\frac{\epsilon}{2}}}{\sqrt{2}}\right)^2$



$$= -\int \frac{d^{4-\epsilon_{k}}}{(2\pi)^{4-\epsilon}} \frac{\operatorname{Tr}[(p-k+m_{f})]}{(p-k)^{2}-m_{f}^{2}} \frac{(-k+m_{f})]}{k^{2}-m_{f}^{2}} \left(\frac{-iy_{f}\mu^{-\frac{\epsilon}{2}}}{\sqrt{2}}\right)^{2}$$

$$\stackrel{m_{h}^{2} \to 0}{=} \frac{3iy_{f}^{2}}{4\pi^{2}}m_{f}^{2} \left[\frac{1}{-\epsilon} + \ln\left(\frac{m_{f}^{2}}{\mu^{2}}\right) + \ldots\right]$$
The regulator can be absorbed in a redefinition of the bare parameters
$$\frac{1}{p^{2}-m_{h}^{2}-i\Pi(p^{2})} \longrightarrow \frac{1}{p^{2}-m_{h,\text{finite}}^{2}-i\Pi_{\text{finite}}(p^{2})}{\frac{1}{p^{2}-m_{h,\text{finite}}^{2}-i\Pi_{\text{finite}}(p^{2})}$$

$$= -\int \frac{d^{4-\epsilon_{k}}}{(2\pi)^{4-\epsilon}} \frac{\operatorname{Tr}[(p-k+m_{f})]}{(p-k)^{2}-m_{f}^{2}} \frac{(-k+m_{f})]}{k^{2}-m_{f}^{2}} \left(\frac{-iy_{f}\mu^{-\frac{k}{2}}}{\sqrt{2}}\right)^{2}$$

$$p^{2} = m_{h}^{2} \rightarrow 0 \frac{3iy_{f}^{2}}{4\pi^{2}} m_{f}^{2} \left[\frac{1}{-\epsilon} + \ln\left(\frac{m_{f}^{2}}{\mu^{2}}\right) + \dots\right]$$
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$$= -\int \frac{d^{4-\epsilon}k}{(2\pi)^{4-\epsilon}} \frac{\text{Tr}[(p-k+m_f)]}{(p-k)^2 - m_f^2} \frac{(-k+m_f)}{k^2 - m_f^2}$$

$$p^{2} = m_{h}^{2} \rightarrow 0 \frac{3iy_{f}^{2}}{4\pi^{2}}m_{f}^{2} \left[-\frac{1}{\epsilon} + \ln\left(\frac{m_{f}^{2}}{\mu^{2}}\right) + \frac{1}{\epsilon} + \ln\left(\frac{m_{f}^{2}}{\mu^{2}}\right) + \frac{1}{\epsilon} + \ln\left(\frac{m_{f}^{2}}{\mu^{2}}\right) \right]$$

But this is a real physical effect!





$$= -\int \frac{d^{4-\epsilon}k}{(2\pi)^{4-\epsilon}} \frac{\operatorname{Tr}[(\not - k + m_f)}{(p-k)^2 - m_f^2} \frac{(-k + m_f)]}{k^2 - m_f^2} \left(\frac{-iy_f \mu^{-\frac{\epsilon}{2}}}{\sqrt{2}}\right)^2$$

$$= \frac{m_h^2 \to 0}{4\pi^2} \frac{3iy_f^2}{4\pi^2} m_f^2 \left[-\frac{1}{\epsilon} + \ln\left(\frac{m_f^2}{\mu^2}\right) + \dots \right]$$

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The shift is p

— The shift is proportional to the mass of the fermion







In the SM, $m_f \simeq 175 \text{ GeV} \simeq m_{h,\text{phys}}$

The SM has no FT problem

125 GeV



In BSM, who knows what value m_f might become...

... and what happens if you shift the value of this observable by a small amount

What about the other particles?

$$\begin{array}{ll} \text{Higgs} \\ \text{boson} \end{array} \quad i\Pi_{\text{Higgs}} \propto m_f^2 \end{array}$$

Gauge $i\Pi_V \propto m_V^2$

 $\begin{array}{ll} \text{Chiral} \\ \text{fermions} \end{array} \quad i\Pi_f \propto m_f^2 \end{array}$

What about the other particles?

$$\begin{array}{ll} \mbox{Higgs} & i\Pi_{\rm Higgs} \propto m_f^2 \\ \mbox{Gauge} & i\Pi_V \propto m_V^2 \\ \mbox{Chiral} & i\Pi_f \propto m_f^2 \end{array}$$

The key issue is that the Higgs is renormalized additively, while vector bosons and chiral fermions are renormalized multiplicatively

The issue is not that the Higgs mass suffers from the presence of a quadratic divergence...

What about the other particles?



This, in turn, is caused by the absence of a protecting symmetry for the Higgs boson

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The key issue is that the Higgs is renormalized additively, while vector bosons and chiral fermions are renormalized multiplicatively



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• Fine-tuning occurs when an observable (e.g. the Higgs mass) changes a lot as a consequence of a tiny change in the other observables of the theory

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But why is there so much discussion about it?

The LHC did not show conclusive evidence of NP at the TeV scale

Is FT a good guiding principle to search for NP?

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Is FT a good guiding principle to search for NP?

It is not a theoretical requirement: a theory is internally consistent with FT But it is also not merely an aesthetic requirement

We describe our world using effective theories



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e.g. We do not need a quantum mechanical description of gravity to explain how apples fall from trees

nor knowledge of the Planck scale to understand the physics of the LHC



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But of course, this does not mean that nature is required to be free of FT!


- BSM that does not couple to the SM
- Composite Higgs particle
- A new symmetry that protects the Higgs boson
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Accept a fine-tuned BSM

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Experimentalists are needed to settle the issue, and every outcome is possible

> This is the scientific method at work!

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Understanding fine-tuning

- How to quantify FT?
- What levels of FT are allowed?
- How should 'FT' be interpreted?
- What is the role of renormalization?

Accept a fine-tuned BSM

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- Fine-tuning occurs when an observable (e.g. the Higgs) mass) changes a lot as a consequence of a tiny change in the other observables of the theory
- Fine-tuning is not directly caused by a hierarchy of scales
- The SM has no Higgs fine-tuning problem (!!!)
- Fine-tuning is not merely an aesthetic problem, and whatever outcome of the experiment will be, it needs an explanation

Conclusions