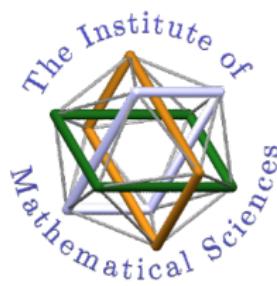


# Differential cross section for the Higgs boson production in 4 lepton channel at LHC and $k_T$ factorization approach

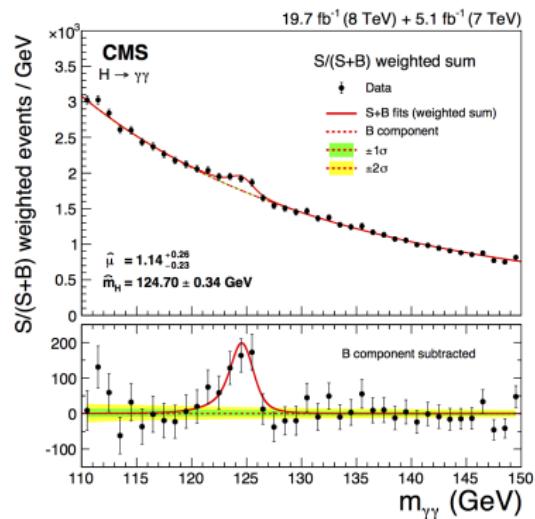
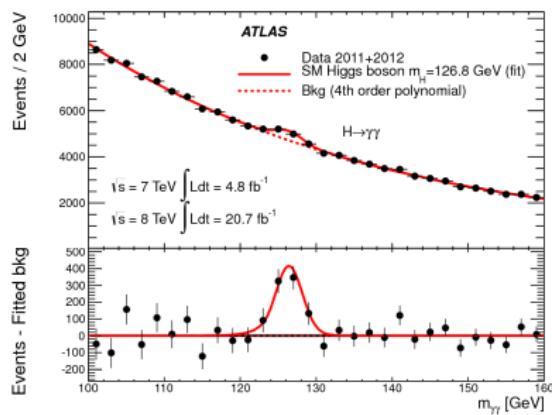
Vaibhav S. Rawoot,  
IMSc, Chennai, India



In collaboration with

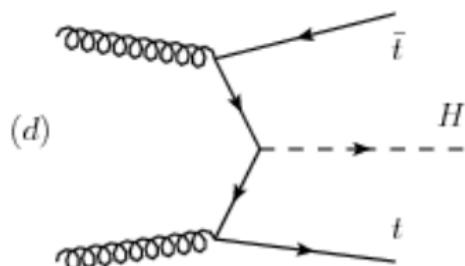
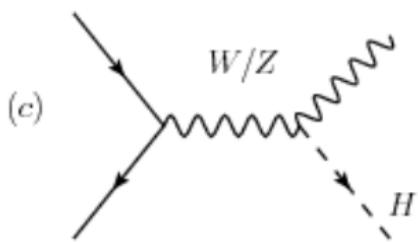
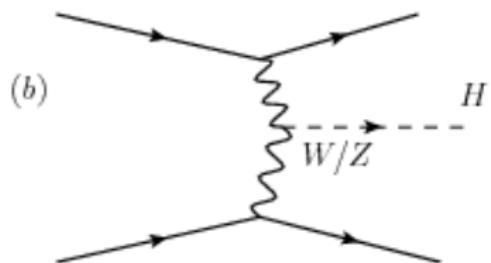
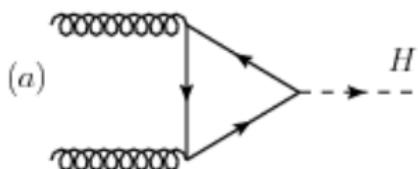
Rashidul Islam (Calcutta University, Kolkata), Mukesh Kumar (University of Witwatersrand, Johannesburg) and V. Ravindran (IMSc, Chennai)

# The Higgs Discovery at ATLAS and CMS



Plots from CMS and ATLAS collaboration.

# Higgs Production



# Higgs Decay Modes

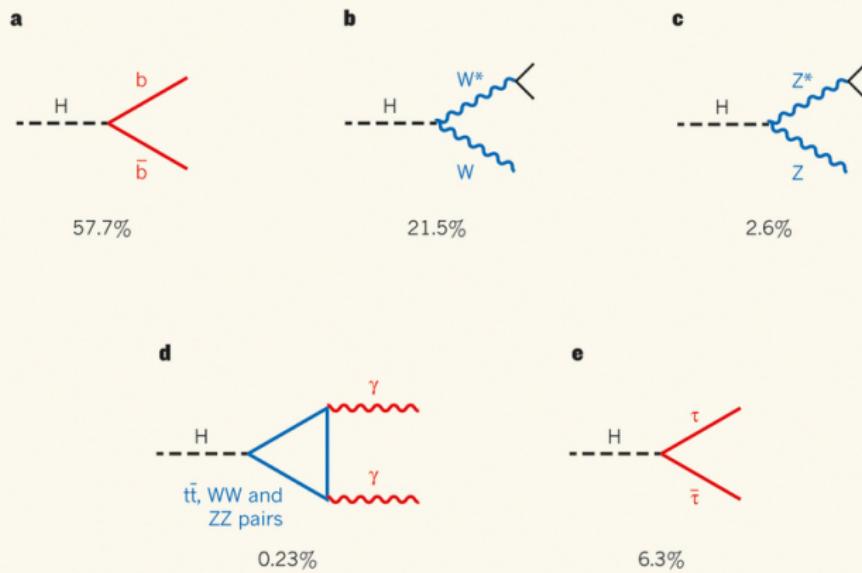
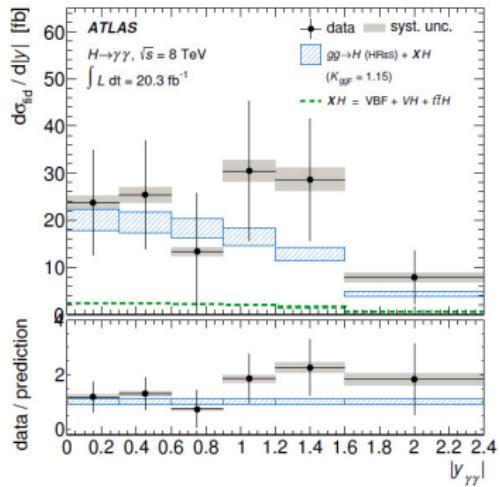
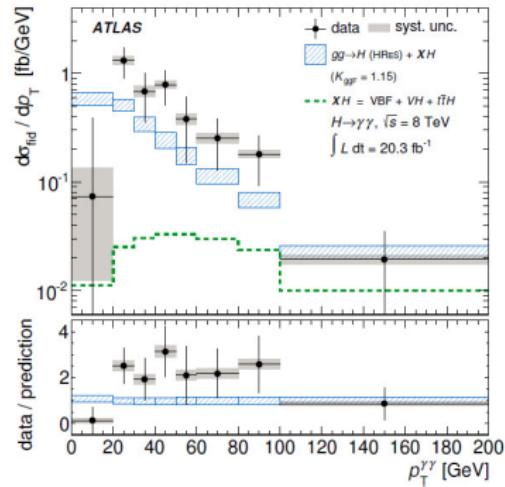


Fig taken from “Frank Wilczek, Nature 496, 439441”

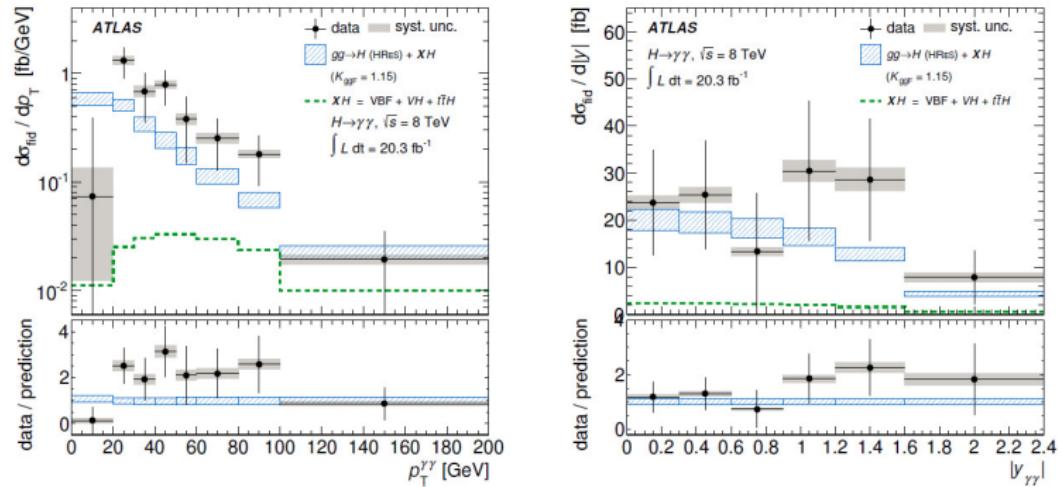
# Differential cross section measurement @ATLAS



G. Aad *et al.* [ATLAS Collaboration], JHEP 1409, 112 (2014)

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- $|\eta| < 2.37$
- $p_T/m_{\gamma\gamma} > 0.35(0.25)$

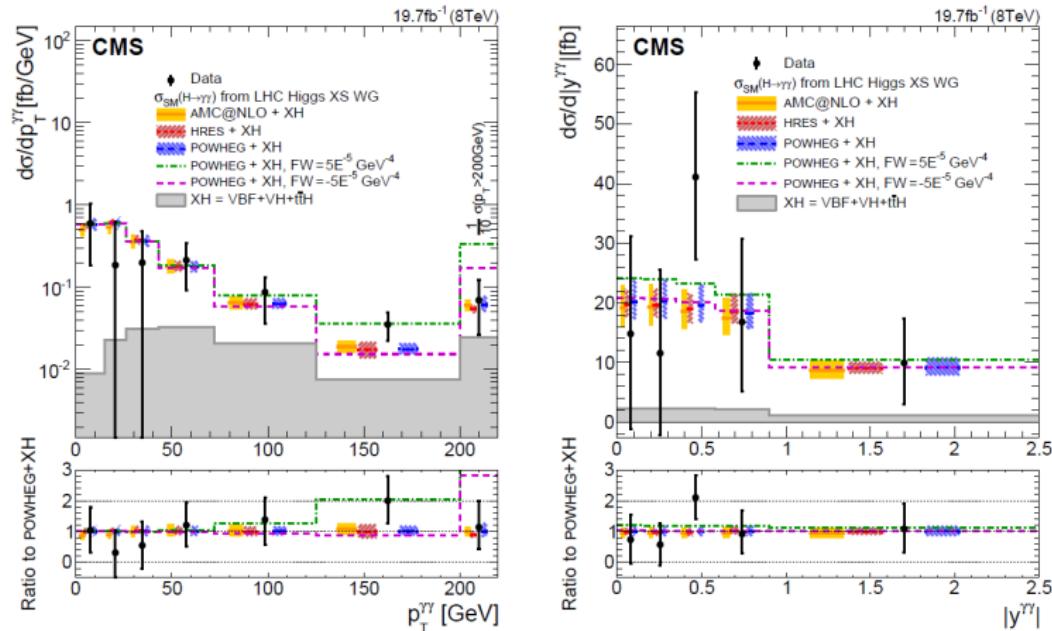
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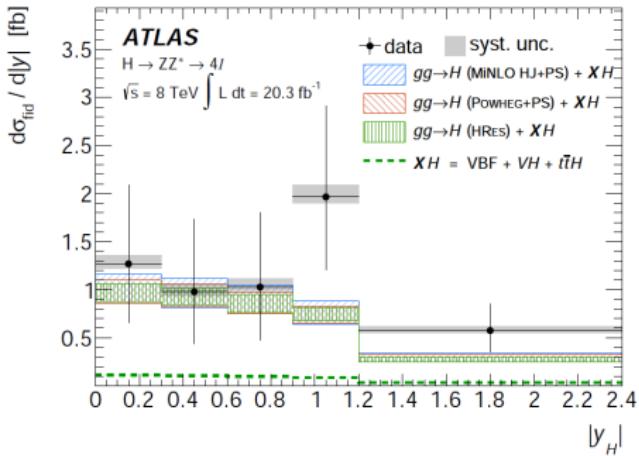
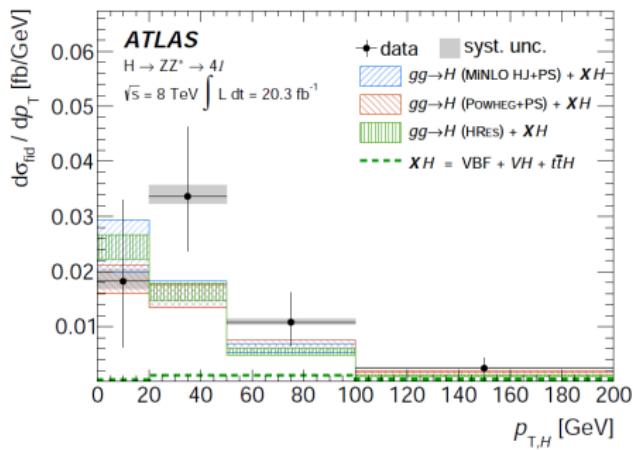
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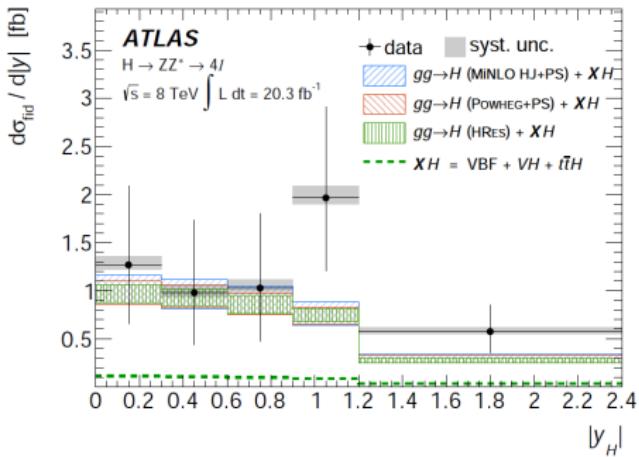
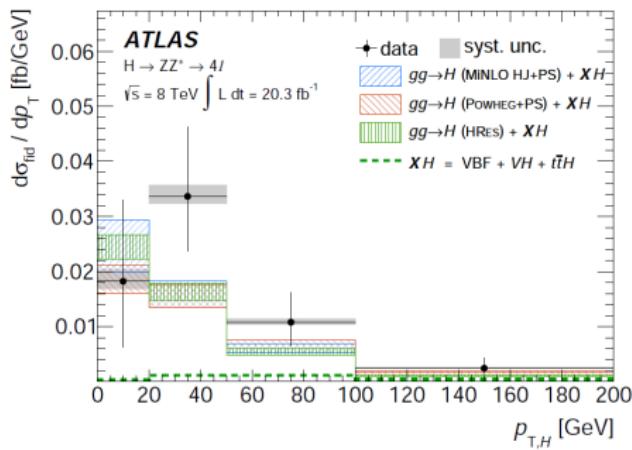


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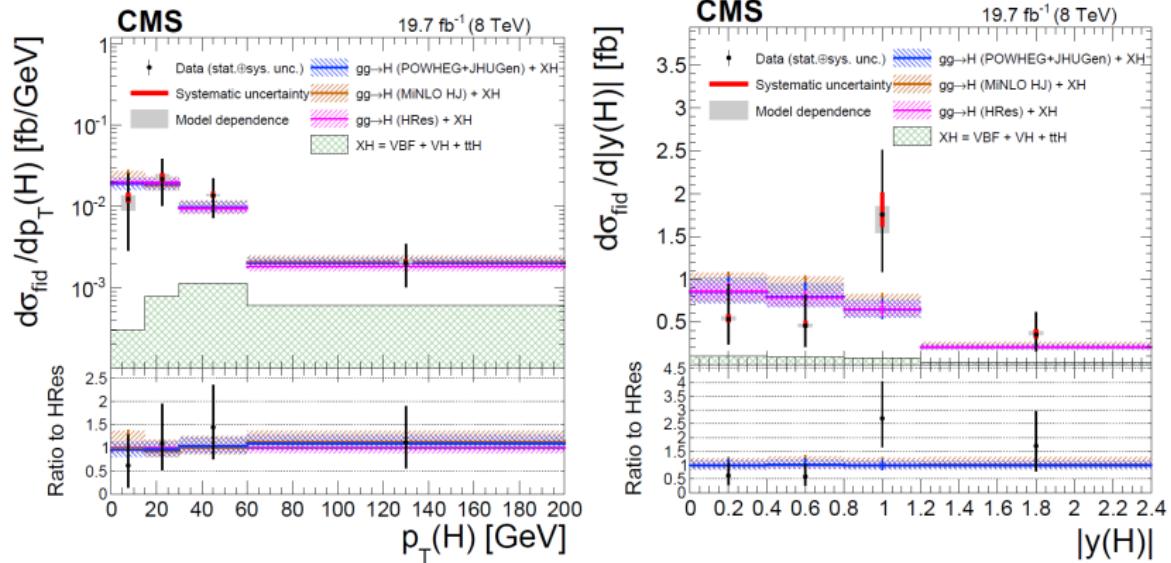
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S. Catani and M. Grazzini, Phys. Rev. Lett. **98**, 222002 (2007) [hep-ph/0703012].  
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# QCD factorization theorem

- Collinear factorization

$$\sigma(h_1 h_2 \rightarrow F) = f_{a/h_1}(x_1, Q^2) \otimes f_{b/h_2}(x_2, Q^2) \otimes \hat{\sigma}_{(ab \rightarrow F)}(Q^2) + \mathcal{O}(\Lambda/Q)$$

- Process dependent partonic cross section

$$\hat{\sigma}(Q^2) = \hat{\sigma}^{(0)} + \alpha_s(Q^2)\hat{\sigma}^{(1)} + \alpha_s^2(Q^2)\hat{\sigma}^{(2)} + \dots$$

*LO*      *NLO*      *NNLO*

- Collinear approximation in parton model and evolution of parton densities described by Dokshitzer-Gribov-Lipatov-Altarelli-Parisi (DGLAP) evolution equation.
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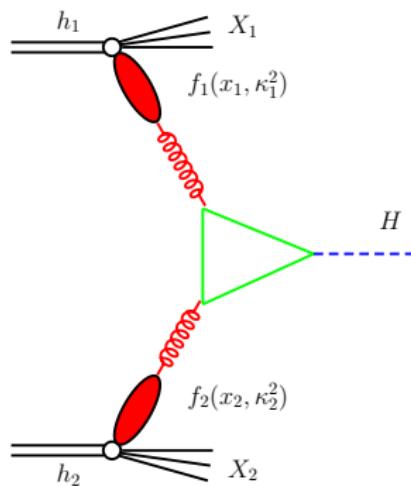
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# Higgs boson production

- $p_T$  and  $y$  distributions of differential cross section for higgs production in di-photon channel is studied recently.  
A. V. Lipatov, M. A. Malyshev and N. P. Zotov,  
*Phys. Lett. B* **735**, 79(2014) [[arXiv:1402.6481 \[hep-ph\]](https://arxiv.org/abs/1402.6481)].
- The results obtained using CCFM evolution equations within  $k_T$  factorization approach is agrees well with experimental data.
- The effect of CCFM evolution equation increases the leading order cross section by about 80-100%.
- Phenomenological study to understand the effect of CCFM evolution equation is an interesting analysis.

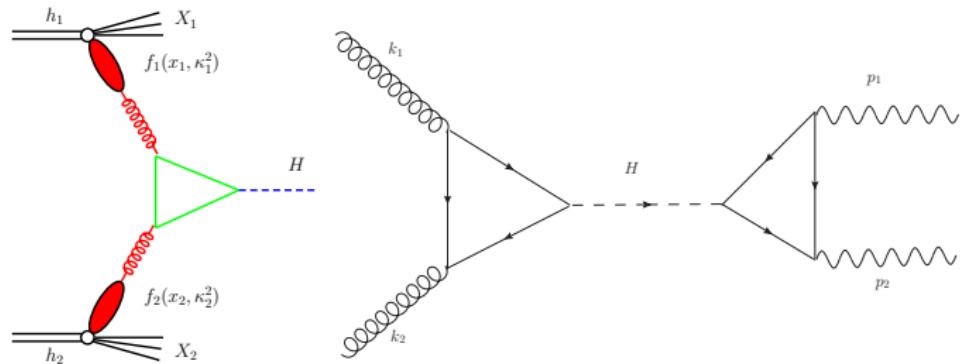
# $k_T$ factorisation for the inclusive Higgs production



$$\sigma_{pp \rightarrow H} = \int \frac{dx_1}{x_1} \frac{dx_2}{x_2} \frac{d^2 k_{1T}}{\pi} \frac{d^2 k_{2T}}{\pi} \delta((k_1 + k_2)^2 - M_H^2) \sigma_{g^* g^* \rightarrow H}(x_1, x_2, k_1, k_2) \times f_g(x_1, k_{1T}^2, \mu_F^2) f_g(x_2, k_{2T}^2, \mu_F^2)$$

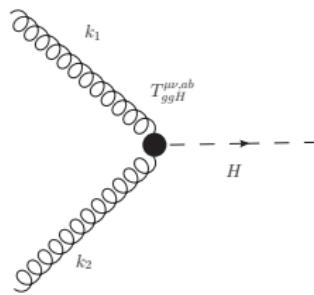
# $k_T$ factorisation for $pp \rightarrow H \rightarrow \gamma\gamma$

A. V. Lipatov, M. A. Malyshev and N. P. Zotov, Phys. Lett. B **735**, 79 (2014)



$$\begin{aligned} \frac{d\sigma(pp \rightarrow H \rightarrow \gamma\gamma)}{dy_1 dy_2 d^2 p_{1T} d^2 p_{2T}} &= \frac{1}{16\pi^2 (x_1 x_2 s)^2} \frac{1}{2} \int \frac{d^2 k_{1T}}{\pi} \frac{d^2 k_{2T}}{\pi} |\bar{\mathcal{M}}|^2 \\ &\times \delta^2(\mathbf{k}_{1T} + \mathbf{k}_{2T} - \mathbf{p}_{1T} - \mathbf{p}_{2T}) \\ &\times f_g(x_1, \mathbf{k}_{1T}^2, \mu^2) f_g(x_2, \mathbf{k}_{2T}^2, \mu^2) \end{aligned}$$

# Off-shell $g^*g^* \rightarrow H \rightarrow \gamma\gamma$ production amplitude

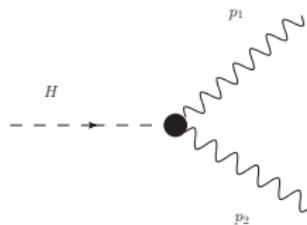


- Effective Triangle Vertex

$$T_{ggH}^{\mu\nu,ab}(k_1, k_2) = i\delta^{ab} \frac{\alpha_s}{3\pi} \left( G_F \sqrt{2} \right)^{1/2} [k_2^\mu k_1^\nu - (k_1 \cdot k_2) g^{\mu\nu}]$$

- Large top mass limit  $m_H < 2m_t \rightarrow$  Higgs boson mass  $m_H \sim 125$  GeV

# Off-shell $g^*g^* \rightarrow H \rightarrow \gamma\gamma$ production amplitude



- Effective vertex  $T_{H\gamma\gamma}^{\mu\nu}(p_1, p_2)$

$$T_{H\gamma\gamma}^{\mu\nu}(p_1, p_2) = i \frac{\alpha}{2\pi} \mathcal{A} \left( G_F \sqrt{2} \right)^{1/2} [p_2^\mu p_1^\nu - (p_1 \cdot p_2) g^{\mu\nu}]$$

# Off-shell $g^*g^* \rightarrow H \rightarrow \gamma\gamma$ production amplitude

Using  $k_1^2 = -\mathbf{k}_{1T}^2 \neq 0$  and  $k_1^2 = -\mathbf{k}_{1T}^2 \neq 0$

$$T_{H\gamma\gamma}^{\mu\nu}(p_1, p_2) = i \frac{\alpha}{2\pi} \mathcal{A} \left( G_F \sqrt{2} \right)^{1/2} [p_2^\mu p_1^\nu - (p_1 \cdot p_2) g^{\mu\nu}]$$

$$T_{ggH}^{\mu\nu, ab}(k_1, k_2) = i \delta^{ab} \frac{\alpha_s}{3\pi} \left( G_F \sqrt{2} \right)^{1/2} [k_2^\mu k_1^\nu - (k_1 \cdot k_2) g^{\mu\nu}]$$

$$\sum \epsilon^\mu \epsilon^{*\nu} = \frac{\mathbf{k}_T^\mu \mathbf{k}_T^\nu}{k_T^2}$$

- Differential cross section for di-photon production from the  $g^* g^* \rightarrow H \rightarrow \gamma\gamma$

$$\begin{aligned} \frac{d\sigma(pp \rightarrow H \rightarrow \gamma\gamma)}{dy_1 dy_2 d^2 p_{1T} d^2 p_{2T}} &= \frac{1}{16\pi^2(x_1 x_2 s)^2} \frac{1}{2} \int \frac{d^2 k_{1T}}{\pi} \frac{d^2 k_{2T}}{\pi} |\bar{\mathcal{M}}|^2 \\ &\times \delta^2(\mathbf{k}_{1T} + \mathbf{k}_{2T} - \mathbf{p}_{1T} - \mathbf{p}_{2T}) \\ &\times f_g(x_1, \mathbf{k}_{1T}^2, \mu^2) f_g(x_2, \mathbf{k}_{2T}^2, \mu^2) \end{aligned}$$



$$x_1 \sqrt{s} = |\mathbf{p}_{1T}| e^{y_1} + |\mathbf{p}_{2T}| e^{y_2}$$

$$x_2 \sqrt{s} = |\mathbf{p}_{1T}| e^{-y_1} + |\mathbf{p}_{2T}| e^{-y_2}$$

- Study for  $pp \rightarrow H \rightarrow 4 \text{ leptons}$  will be an interesting analysis.

- Differential cross section for di-photon production from the  $g^* g^* \rightarrow H \rightarrow \gamma\gamma$

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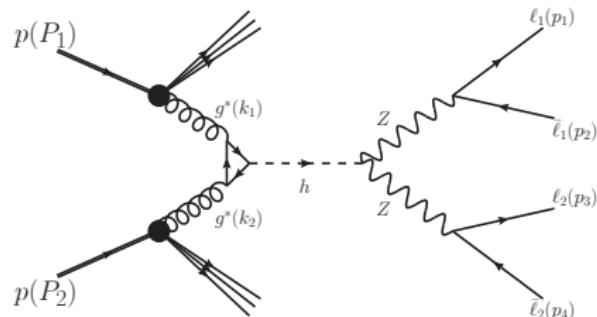


$$x_1 \sqrt{s} = |\mathbf{p}_{1T}| e^{y_1} + |\mathbf{p}_{2T}| e^{y_2}$$

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- Study for  $pp \rightarrow H \rightarrow 4 \text{ leptons}$  will be an interesting analysis.

$$pp \rightarrow H \rightarrow ZZ \rightarrow l_1 \bar{l}_1 l_2 \bar{l}_2$$



$$\sigma = \int dy_1 dy_2 dy_3 dy_4 d^2 \mathbf{p}_{1T} d^2 \mathbf{p}_{2T} d^2 \mathbf{p}_{3T} d^2 \mathbf{p}_{4T} \frac{d^2 \mathbf{k}_{1T}}{\pi} \frac{d^2 \mathbf{k}_{2T}}{\pi} \frac{1}{(2^{12})\pi^8(x_1 x_2 s)^2} |\mathcal{M}|^2 \quad (1)$$

$$\delta^2(\mathbf{k}_{1T} + \mathbf{k}_{2T} - \mathbf{p}_{1T} - \mathbf{p}_{2T} - \mathbf{p}_{3T} - \mathbf{p}_{4T}) f_g(x_1, \mathbf{k}_{1T}^2) f_g(x_2, \mathbf{k}_{2T}^2)$$

with

$$x_1 = \frac{|\mathbf{p}_{1T}|}{\sqrt{s}} e^{y_1} + \frac{|\mathbf{p}_{2T}|}{\sqrt{s}} e^{y_2} + \frac{|\mathbf{p}_{3T}|}{\sqrt{s}} e^{y_3} + \frac{|\mathbf{p}_{4T}|}{\sqrt{s}} e^{y_4}$$

and

$$x_2 = \frac{|\mathbf{p}_{1T}|}{\sqrt{s}} e^{-y_1} + \frac{|\mathbf{p}_{2T}|}{\sqrt{s}} e^{-y_2} + \frac{|\mathbf{p}_{3T}|}{\sqrt{s}} e^{-y_3} + \frac{|\mathbf{p}_{4T}|}{\sqrt{s}} e^{-y_4}$$

$$pp \rightarrow H \rightarrow ZZ \rightarrow l_1 \bar{l}_2 l_2 \bar{l}_2$$

$$\frac{d\sigma}{dy_1 dy_2 dy_3 dy_4 d\mathbf{p}_{1T}^2 d\mathbf{p}_{2T}^2 d\mathbf{p}_{3T}^2} = \int d\mathbf{k}_{1T}^2 d\mathbf{k}_{2T}^2 \frac{d\phi_1}{2\pi} \frac{d\phi_2}{2\pi} \frac{1}{(2^{12})\pi^5(x_1 x_2 s)^2} |\bar{\mathcal{M}}|^2 f_g(x_1, \mathbf{k}_{1T}^2) f_g(x_2, \mathbf{k}_{2T}^2)$$

$$\mathbf{k}_{1T} + \mathbf{k}_{2T} = \mathbf{p}_{1T} + \mathbf{p}_{2T} + \mathbf{p}_{3T} + \mathbf{p}_{4T}$$

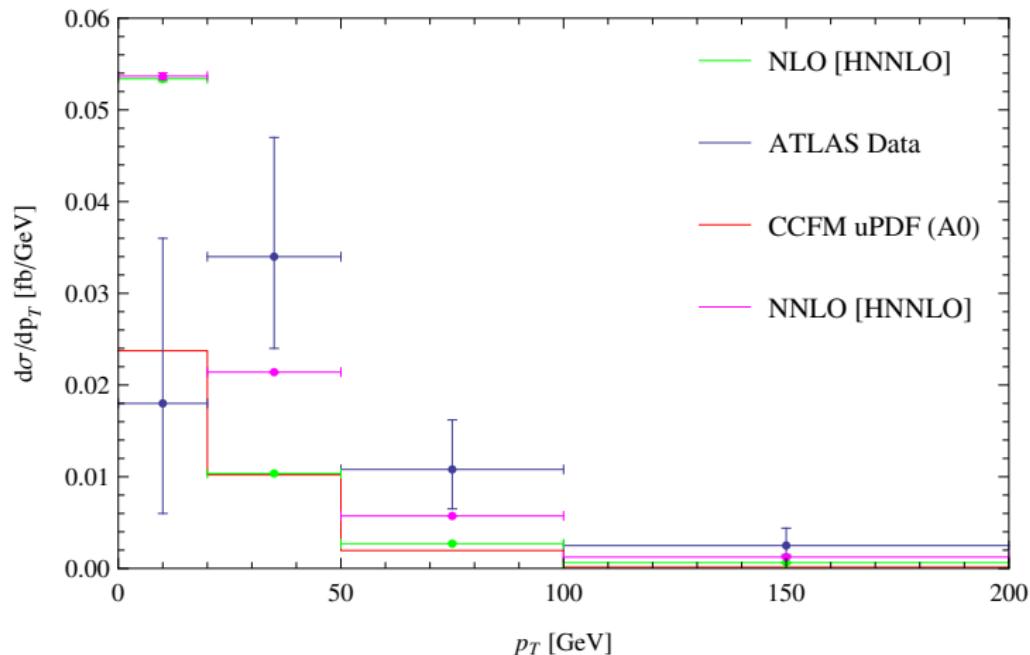
$$\mathcal{M}(g * g * \rightarrow H \rightarrow ZZ \rightarrow 4l)$$

$$\mathcal{M}(g * g * \rightarrow H \rightarrow ZZ \rightarrow 4l) = \mathcal{M}(g * g * \rightarrow H) \frac{1}{\hat{s} - m_H^2 + i\Gamma_H m_H} \mathcal{M}(H \rightarrow ZZ \rightarrow l_1 \bar{l}_1 l_2 \bar{l}_2)$$

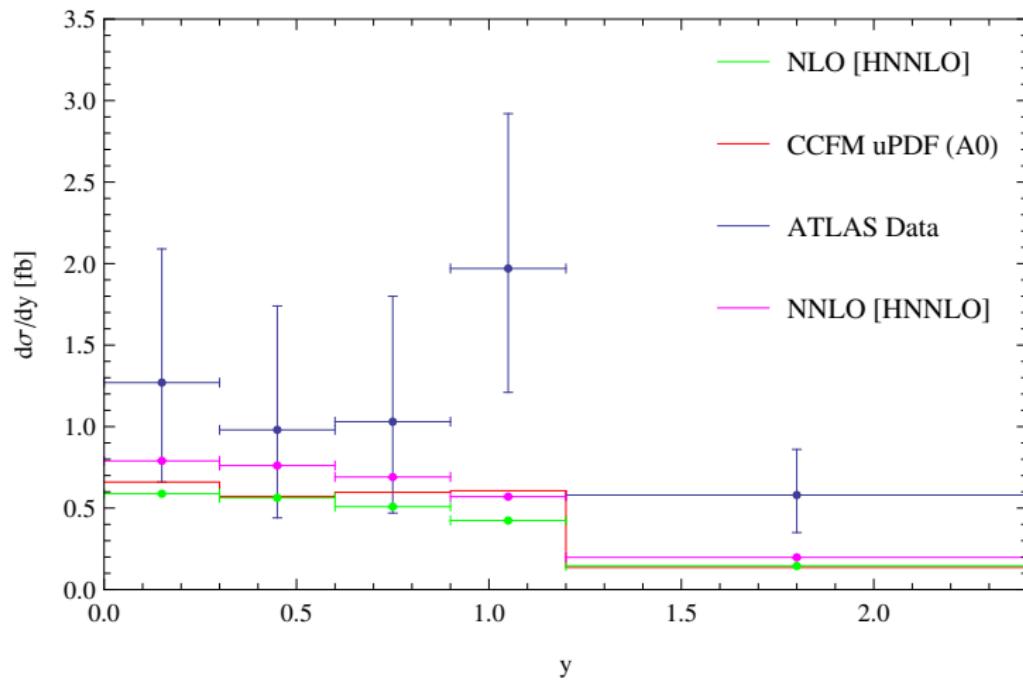
$$\begin{aligned} |\mathcal{M}|^2 &= \frac{2}{9} \frac{\alpha_s^2}{\pi^2} \frac{m_Z^4}{v^4} \frac{[(\mathbf{k}_{\perp 1} + \mathbf{k}_{\perp 2})^2 + \hat{s}]^2 \cos^2 \phi}{(\hat{s} - m_H^2)^2 + \Gamma_H^2 m_H^2} \\ &\quad \frac{[(p_1 \cdot p_4)(p_2 \cdot p_3)\{2g_L^2 g_R^2\} + (p_1 \cdot p_3)(p_2 \cdot p_4)\{g_L^4 + g_R^4\}]}{[(2p_1 \cdot p_2 - m_Z^2)^2 + \Gamma_Z^2 m_Z^2][(2p_3 \cdot p_4 - m_Z^2)^2 + \Gamma_Z^2 m_Z^2]} \end{aligned}$$

$$g_L = \frac{g_W}{\cos \theta_W} \left( -\frac{1}{2} + \sin^2 \theta_W \right), \quad g_R = \frac{g_W}{\cos \theta_W} \sin^2 \theta_W, \quad \text{and} \quad v = (\sqrt{2} G_F)^{-1/2}$$

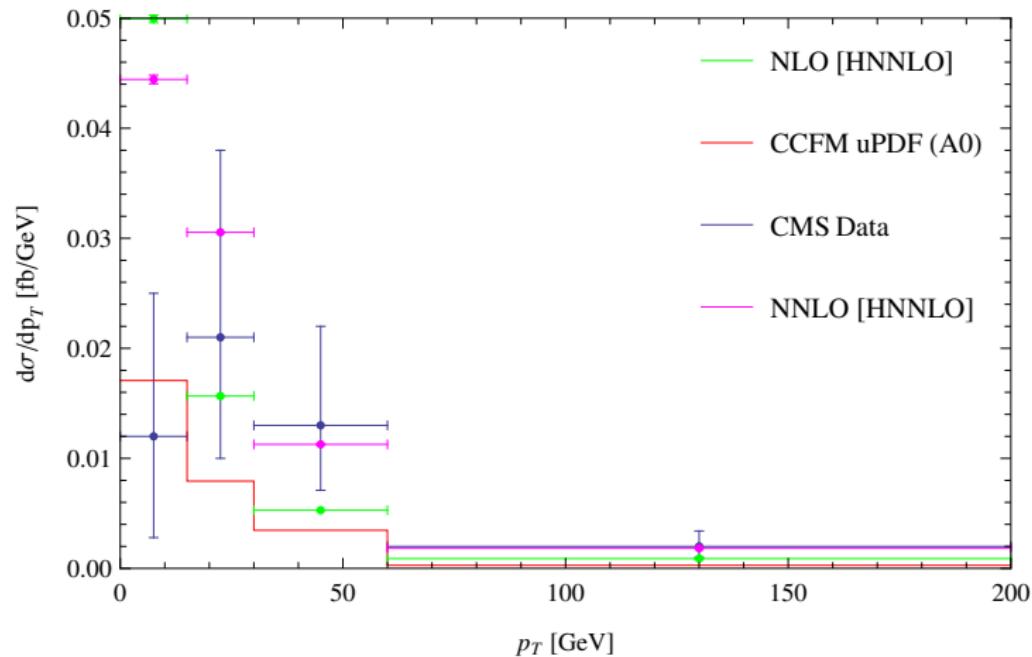
# ATLAS data for $pp \rightarrow H \rightarrow 4\text{leptons}$ and $k_T$ factorization approach



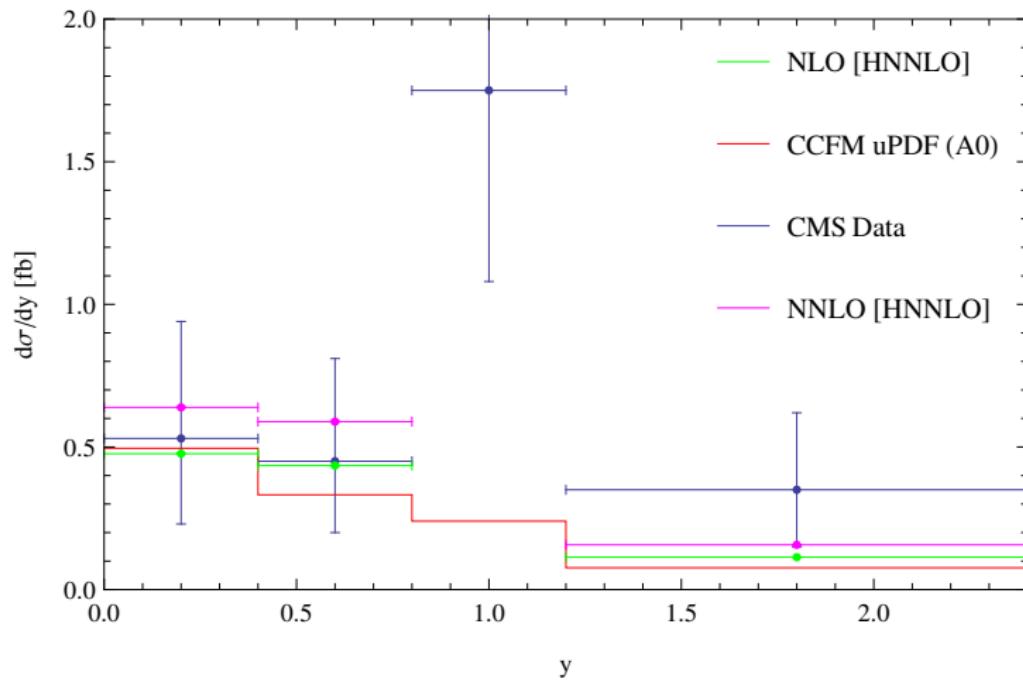
# ATLAS data for $pp \rightarrow H \rightarrow 4\text{leptons}$ and $k_T$ factorization approach



# CMS data for $pp \rightarrow H \rightarrow 4 \text{ leptons}$ and $k_T$ factorization approach



# CMS data for $pp \rightarrow H \rightarrow 4 \text{ leptons}$ and $k_T$ factorization approach



# Conclusions

- We have estimated differential cross section for higgs production in four lepton channel.
- Recent data from ATLAS and CMS collaboration for differential cross section in fiducial region are important in this study.
- The results obtained using CCFM evolution equations are close to NLO results obtained using collinear factorization.
- Calculating higher order corrections withing  $k_T$  factorization is a challenge and it would be an interesting analysis for Phenomenological study.

# Thank You