

Branching fraction measurement of  
 $B^0 \rightarrow D_s^+ \pi^-$

Jordy Butter



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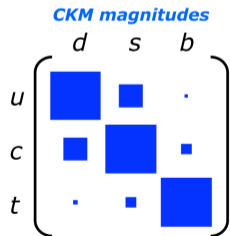
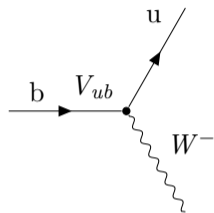


# CKM matrix

- The Cabibbo-Kobayashi-Maskawa (CKM) Matrix gives the coupling strength of quark transitions

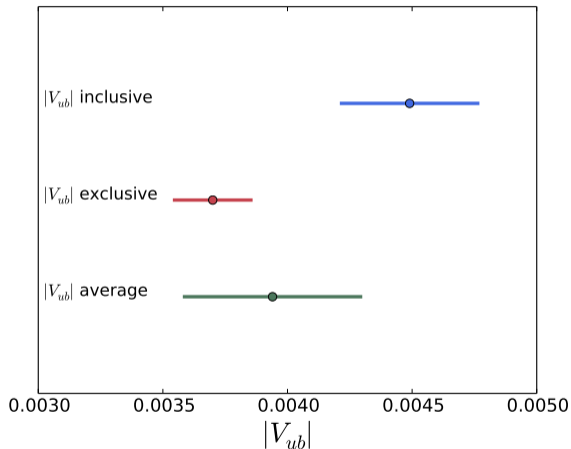
$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

- Why is this matrix close to diagonal?
- Why do we have three generations of quarks?



# CKM element $|V_{ub}|$

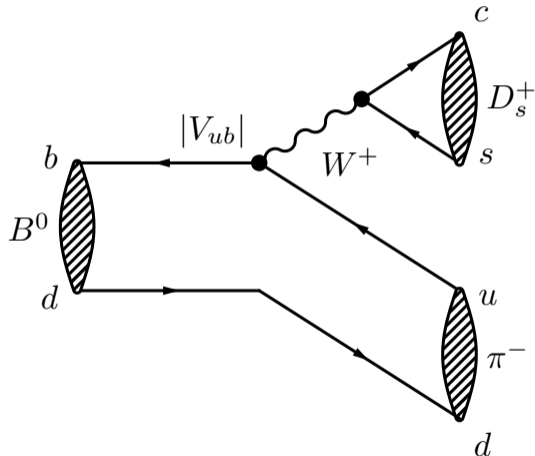
- $V_{ub}$  CKM element with largest uncertainty
- Discrepancy between inclusive and exclusive measurements
  - Inclusive  $\Rightarrow B \rightarrow X_u l \bar{\nu}_l$  decays
  - Exclusive  $\Rightarrow$  Specific decays (e.g.  $B^0 \rightarrow \pi^- l^+ \nu$ )
- More measurements help in solving this issue
  - This analysis:  $B^0 \rightarrow D_s^+ \pi^-$



# Motivation

## Probing $|V_{ub}|$

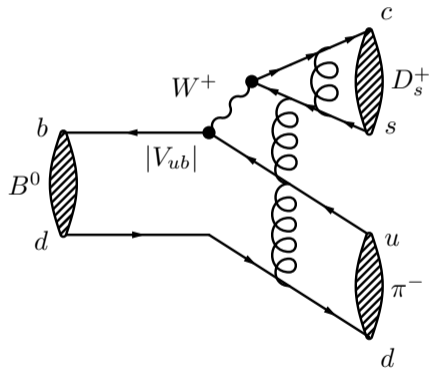
- This analysis looks at a hadronic decay probing the  $b \rightarrow u$  quark transition
- Only first order tree diagram
- $\mathcal{B}(B^0 \rightarrow D_s^+ \pi^-) \propto |V_{ub}|^2$



# Motivation

## Probing $|a_{\text{NF}}|$

- Hadronic decay  $\rightarrow$  QCD important
- Known:
  - Form factor  $F(B^0 \rightarrow \pi^-)$
  - Decay Constant:  $f_{D_s}$
- Unknown:
  - Non-factorisation constant  $|a_{\text{NF}}(D_s^+ \pi^-)|$
- $\mathcal{B}(B^0 \rightarrow D_s^+ \pi^-) \propto |V_{ub}|^2 |a_{\text{NF}}|^2 |F(B^0 \rightarrow \pi^-)|^2 f_{D_s}^2$



# Motivation

## Other motivations

### Determining $r_{D\pi}$

The parameter

$$r_{D\pi} = \left| \frac{A(B^0 \rightarrow D^+ \pi^-)}{A(B^0 \rightarrow D^- \pi^+)} \right|,$$

is necessary ingredient for  $CP$  asymmetry measurements in  $B^0 \rightarrow D^\mp \pi^\pm$  decays.

Assuming  $SU(3)$  flavour symmetry,

$$r_{D\pi} = \tan \theta_c \frac{f_{D^+}}{f_{D_s}} \sqrt{\frac{\mathcal{B}(B^0 \rightarrow D_s^+ \pi^-)}{\mathcal{B}(B^0 \rightarrow D^- \pi^+)}}.$$

### $f_s/f_d$ dependence on collision energy

- Side result: relative event yield  $B^0/B_s^0$
- Use data with collision energies of 7/8 TeV and 13 TeV to find out

$$\frac{f_s/f_d|_{\sqrt{s}=13 \text{ TeV}}}{f_s/f_d|_{\sqrt{s}=7/8 \text{ TeV}}}$$

- $f_s/f_d$  is crucial for **all**  $B_s^0$  branching fraction measurements at LHCb, most notably the famous  $B_s^0 \rightarrow \mu^- \mu^+$

# Strategy

How to calculate  $\mathcal{B}(B^0 \rightarrow D_s^+ \pi^-)$

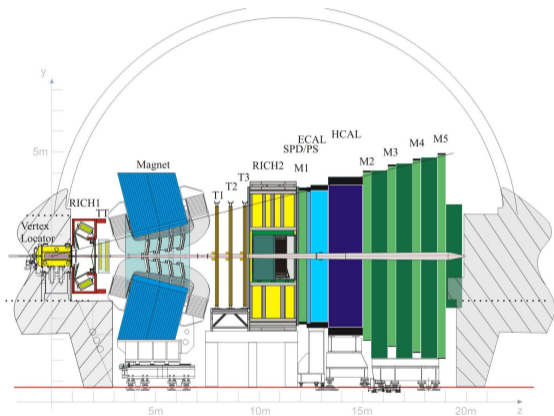
- Branching fraction  $\propto$  yield
- Normalisation channel  $B^0 \rightarrow D^- \pi^+$  used
  - Unknown  $B^0$  production
  - Topological similar to  $B^0 \rightarrow D_s^+ \pi^-$
  - Small uncertainty

$$\mathcal{B}(B^0 \rightarrow D_s^+ \pi^-) = \frac{N_{B^0 \rightarrow D_s^+ \pi^-}}{N_{B^0 \rightarrow D^- \pi^+}} \frac{\epsilon_{B^0 \rightarrow D^- \pi^+}}{\epsilon_{B^0 \rightarrow D_s^+ \pi^-}} \mathcal{B}(B^0 \rightarrow D^- \pi^+) \frac{\mathcal{B}(D^- \rightarrow K^+ \pi^- \pi^-)}{\mathcal{B}(D_s^+ \rightarrow K^- K^+ \pi^-)}$$

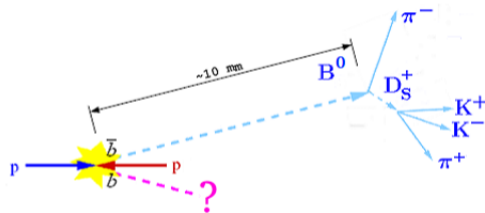
- My job:
  - $\Rightarrow$  Fit yields  $\rightarrow$  Invariant mass fits
  - $\Rightarrow$  Determine efficiencies  $\rightarrow$  Obtain from simulation

# Detector

## LHCb detector



Cross-section of the LHCb detector



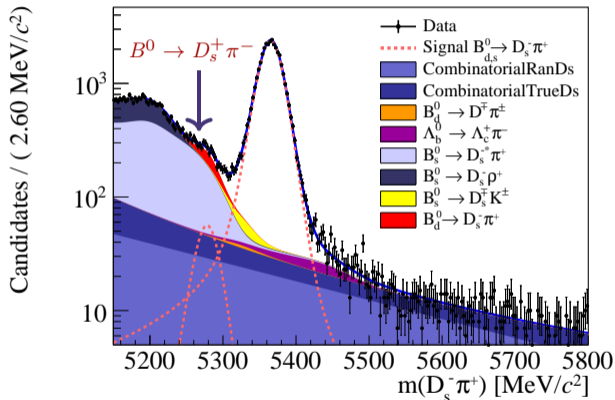
Decay signature  $B^0 \rightarrow D_s^+ \pi^-$



# Strategy

The  $B^0 \rightarrow D_s^+ \pi^-$  signal

- $B^0 \rightarrow D_s^+ \pi^-$  signal is relatively small
- Need to control:
  - $B_s^0 \rightarrow D_s^- \pi^+$  shape
  - Partially reconstructed backgrounds
  - Misidentified backgrounds
  - Combinatorial background

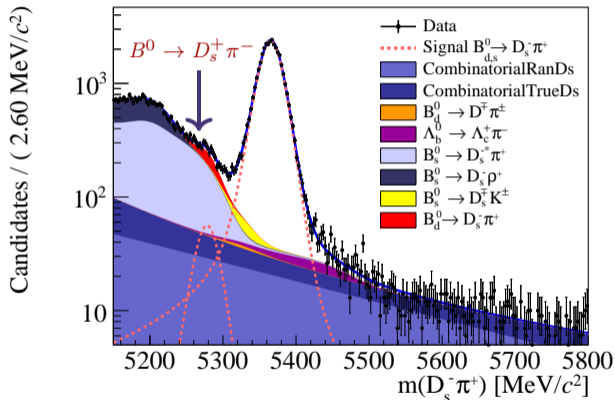


$D_s^+ \pi^-$  data after full selection

# Strategy

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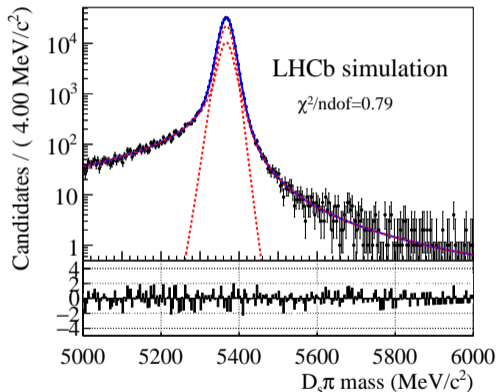


$D_s^+ \pi^-$  data after full selection

# Analysis steps

## Signal shape

- Important to describe  $B_s^0 \rightarrow D_s^- \pi^+$  accurately
- Fit to simulations of  $B^0 \rightarrow D^- \pi^+$  and  $B_s^0 \rightarrow D_s^- \pi^+$ 
  - Use normalisation channel  $B^0 \rightarrow D^- \pi^+$  to check simulation/data differences and constrain  $B_s^0 \rightarrow D_s^- \pi^+$  shape in data
  - Focus on left tail

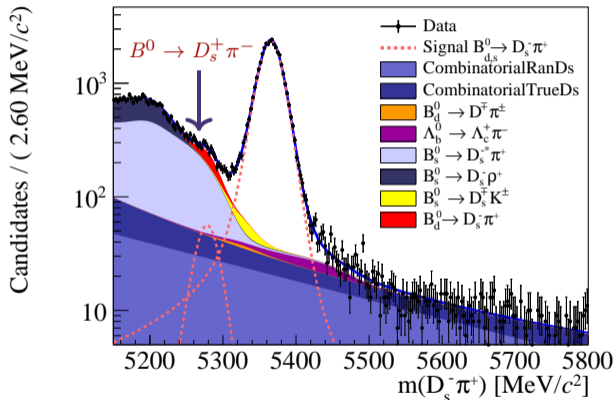


Fit to simulated  $B_s^0 \rightarrow D_s^- \pi^+$  events

# Analysis steps

## Partially reconstructed backgrounds

- $B^0 \rightarrow D_s^+ \pi^-$  signal is relatively small
- Need to control:
  - $B_s^0 \rightarrow D_s^- \pi^+$  shape
- ⇒ **Partially reconstructed backgrounds**
- Misidentified backgrounds
- Combinatorial background



$D_s^+ \pi^-$  data after full selection

# Analysis steps

## Partially reconstructed backgrounds

- Excited state of  $D_s^+$  meson or pion
- Describing the tails of these backgrounds correctly is crucial
- Analytical shape obtained from simulation fits
- Normalisation channel  $B^0 \rightarrow D^- \pi^+$  to investigate simulation/data difference in resolution

### In signal fit

- $B_s^0 \rightarrow D_s^{*-} \pi^+$  ( $D_s^{*-} \rightarrow D_s^- \gamma / \pi^0$ )
- $B_s^0 \rightarrow D_s^- \rho^+$  ( $\rho^+ \rightarrow \pi^+ \pi^0$ )

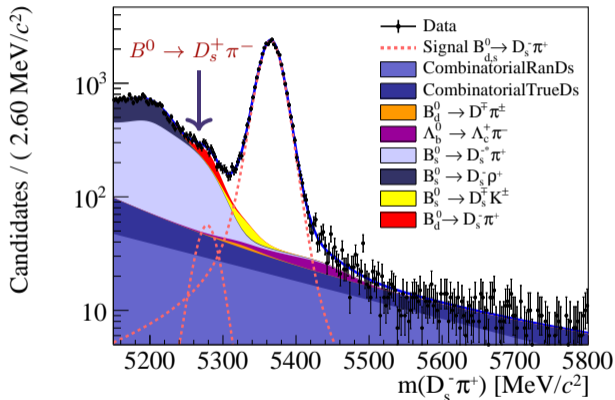
### In normalisation channel fit

- $B^0 \rightarrow D^{*-} \pi^+$  ( $D^{*-} \rightarrow D^- \pi^0$ )
- $B^0 \rightarrow D^- \rho^+$  ( $\rho^+ \rightarrow \pi^+ \pi^0$ )

# Analysis steps

## Misidentified backgrounds

- $B^0 \rightarrow D_s^+ \pi^-$  signal is relatively small
- Need to control:
  - $B_s^0 \rightarrow D_s^- \pi^+$  shape
  - Partially reconstructed backgrounds
- ⇒ **Misidentified backgrounds**
  - Combinatorial background



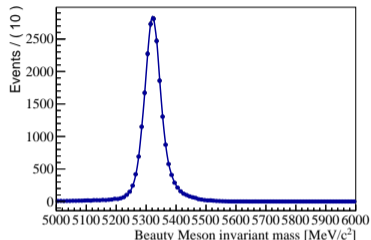
$D_s^+ \pi^-$  data after full selection

# Analysis steps

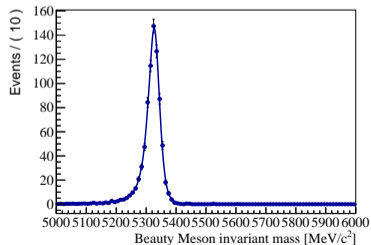
## Misidentified backgrounds

- Other decays with one (or more) final-state particles misidentified
- Shape described by simulation
- Relative yields estimated using
  - Branching fractions of decays
  - Relative production  $B^0$  and  $B_s^0$  mesons
  - Efficiencies using simulation
- Relative yields constrained in fit

Misidentified  
 $B^0 \rightarrow D^- \pi^+$   
( $D^- \rightsquigarrow D_s^-$ )



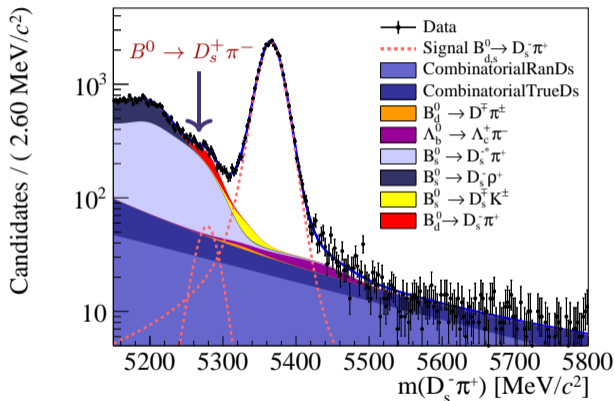
Misidentified  
 $B_s^0 \rightarrow D_s^- K^+$   
( $K^+ \rightsquigarrow \pi^+$ )



# Analysis steps

## Combinatorial background

- $B^0 \rightarrow D_s^+ \pi^-$  signal is relatively small
  - Need to control:
    - $B_s^0 \rightarrow D_s^- \pi^+$  shape
    - Partially reconstructed backgrounds
    - Misidentified backgrounds
- ⇒ **Combinatorial background**



$D_s^+ \pi^-$  data after full selection



# Analysis steps

## Combinatorial background

- Random combinations of final-state particles of  $B^0 \rightarrow D_s^+ \pi^- (D_s^+ \rightarrow K^+ K^- \pi^+)$
- Combinatorial background split in two components
- Simultaneous fit to  $m(D_s^+ \pi^-)$  and  $m(K^+ K^- \pi^+)$  necessary to separate

### Random combinatorial

- Random combinations of final-state particles  $K^+ K^- \pi^+ \pi^-$

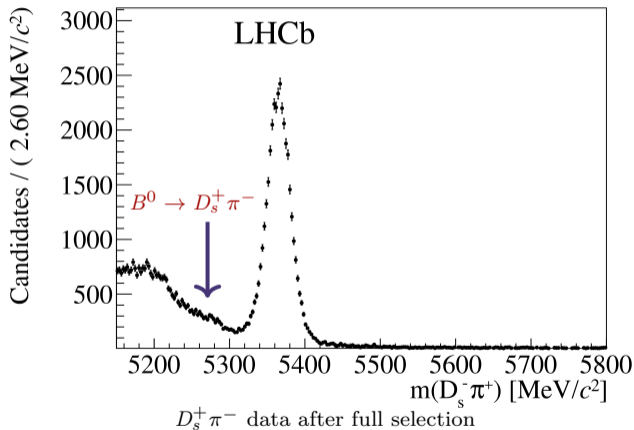
### True- $D_s^+$ combinatorial

- Random combinations of a real  $D_s^+$  meson with  $\pi^-$

# Fits to data

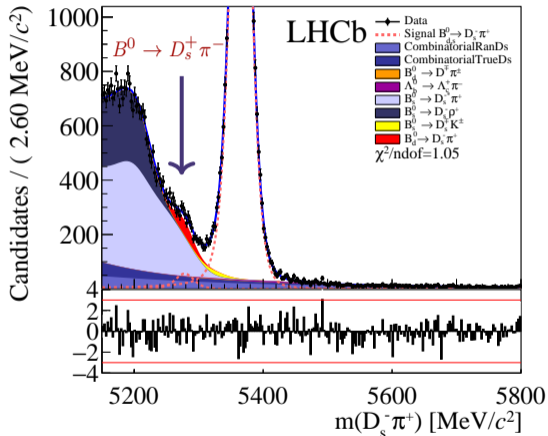
## The data

- All backgrounds and signals are studied
- It is time for the invariant mass fit!

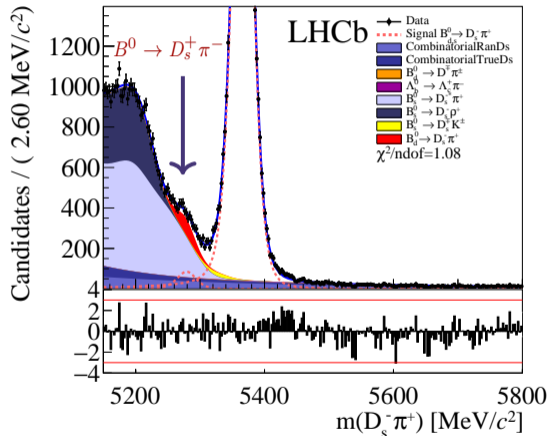


# Fits to data

$B^0 \rightarrow D_s^+ \pi^-$  mass fit



Fit to 2011 + 2012 data



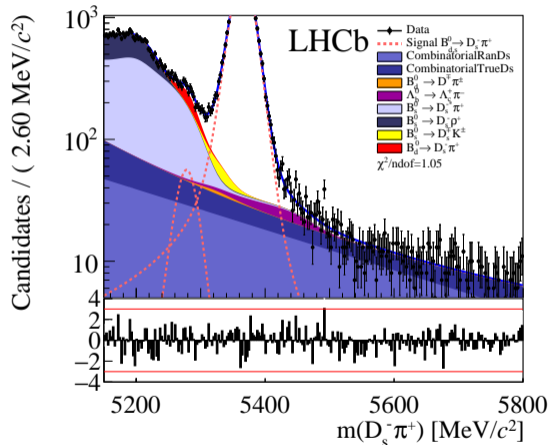
Fit to 2015 + 2016 data

Combined yield:

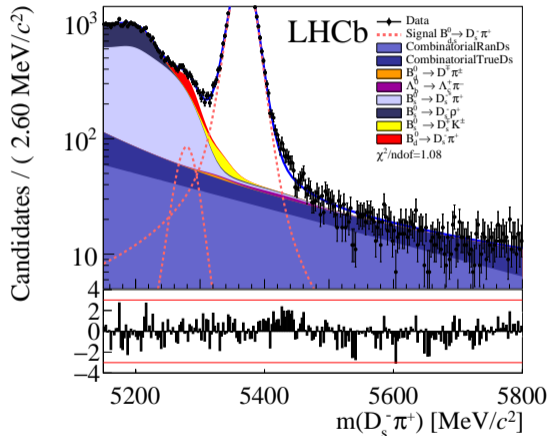
$$N_{B^0 \rightarrow D_s^+ \pi^-} = 2190 \pm 198$$

# Fits to data

$B^0 \rightarrow D_s^+ \pi^-$  mass fit



Fit to 2011 + 2012 data



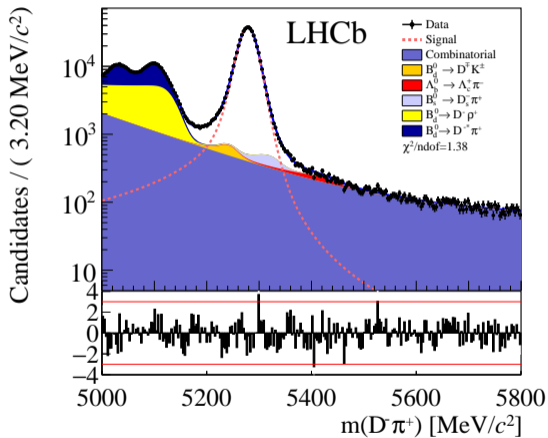
Fit to 2015 + 2016 data

Combined yield:

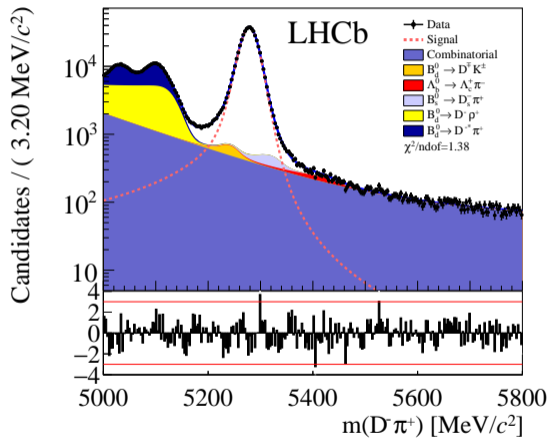
$$N_{B^0 \rightarrow D_s^+ \pi^-} = 2190 \pm 198$$

# Fits to data

$B^0 \rightarrow D^- \pi^+$  mass fit (normalisation channel)



Fit to 2011 + 2012 data



Fit to 2015 + 2016 data

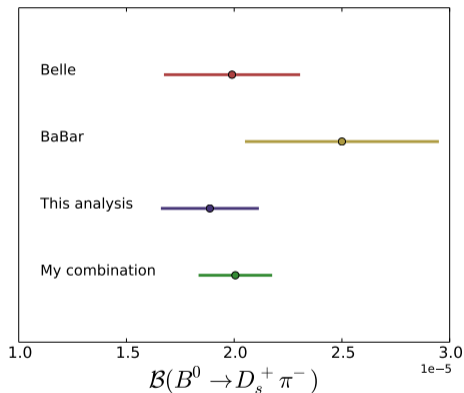
Combined yield:

$$N_{B^0 \rightarrow D^- \pi^+} = 1\,133\,035 \pm 2140$$

# Results

## Branching fraction calculation

- We now have all the ingredients to calculate the branching fraction<sup>1</sup>:  
 $\Rightarrow \mathcal{B}(B^0 \rightarrow D_s^+ \pi^-) = (18.9 \pm 1.7 \text{ (stat)} \pm 0.9 \text{ (syst)} \pm 1.2 \text{ (}\mathcal{B}\text{)}) \cdot 10^{-6}$
- Previous results
  - Belle  $\Rightarrow \mathcal{B}(B^0 \rightarrow D_s^+ \pi^-) = (19.9 \pm 3.2) \cdot 10^{-6}$
  - BaBar  $\Rightarrow \mathcal{B}(B^0 \rightarrow D_s^+ \pi^-) = (25 \pm 4.5) \cdot 10^{-6}$
- Single most precise measurement so far of this branching fraction



<sup>1</sup>Details on relative efficiencies and systematic uncertainties are in the backup slides

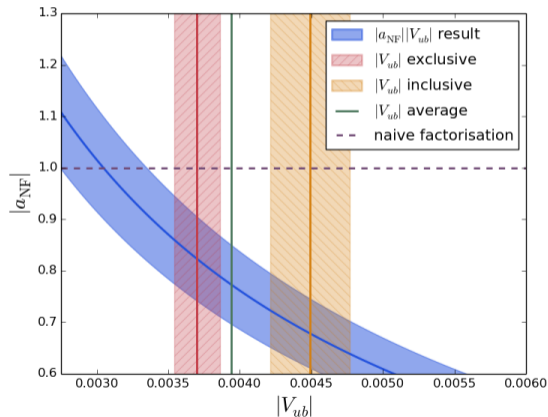
# Results

## Determination of $|V_{ub}||a_{\text{NF}}|$

- Branching fraction probes  $|V_{ub}||a_{\text{NF}}|$

$$\mathcal{B}(B^0 \rightarrow D_s^+ \pi^-) \propto |V_{ub}|^2 |a_{\text{NF}}|^2$$

- $|V_{ub}||a_{\text{NF}}| = (3.05 \pm 0.30) \cdot 10^{-3}$
- Using average  $|V_{ub}|$   
 $\Rightarrow |a_{\text{NF}}| = 0.77 \pm 0.10$



# Results

## Determination of $r_{D\pi}$

- Use branching fraction result:

$$\begin{aligned}\Rightarrow r_{D\pi} &= \tan \theta_c \frac{f_{D^+}}{f_{D_s}} \sqrt{\frac{\mathcal{B}(B^0 \rightarrow D_s^+ \pi^-)}{\mathcal{B}(B^0 \rightarrow D^- \pi^+)}} \\ &= 0.0168 \pm 0.0011 \pm 0.0034\end{aligned}$$

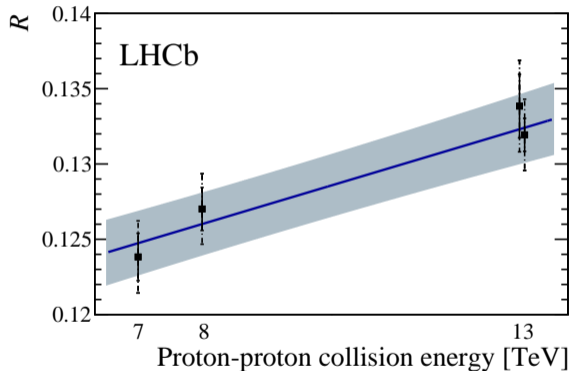
- Necessary for  $CP$  asymmetry measurements in  $B^0 \rightarrow D^\mp \pi^\pm$  decays
- Value used in  $B^0 \rightarrow D^\mp \pi^\pm$  analysis (using PDG for inputs) [1]:  
 $\Rightarrow r_{D\pi} = 0.0182 \pm 0.0012 \pm 0.0036$



# Results

## Hadronisation fraction $f_s/f_d$ collision energy dependence

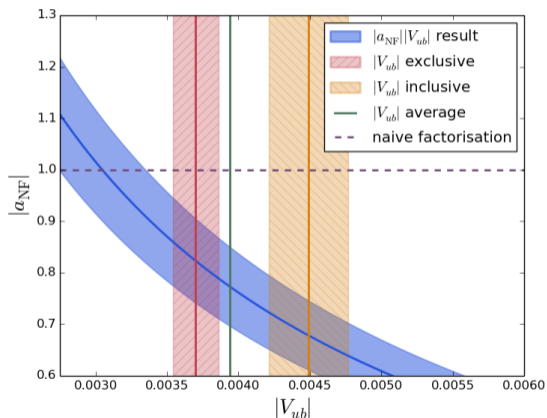
- Using ratio efficiency corrected  $B_s^0 \rightarrow J/\psi\phi$  and  $B^+ \rightarrow J/\psi K^+$  yields (=  $R$ ) [2]:  
$$\Rightarrow \frac{f_s/f_u|_{\sqrt{s}=13 \text{ TeV}}}{f_s/f_u|_{\sqrt{s}=7 \text{ TeV}}} = 1.068 \pm 0.016$$
- Using my efficiency corrected yields of  $B_s^0 \rightarrow D_s^- \pi^+$  and  $B^0 \rightarrow D^- \pi^+$ :  
$$\Rightarrow \frac{f_s/f_d|_{\sqrt{s}=13 \text{ TeV}}}{f_s/f_d|_{\sqrt{s}=7+8 \text{ TeV}}} = 1.049 \pm 0.021$$
- Relatively more  $B_s^0$  wrt  $B^0$  mesons at higher collision energies



Collision energy dependent hadronisation fraction [2]

# Conclusion and outlook

- $B^0 \rightarrow D_s^+ \pi^-$  is a challenging and interesting decay channel
- Single most precise measurement  
 $\Rightarrow \mathcal{B}(B^0 \rightarrow D_s^+ \pi^-) = (18.9 \pm 2.3) \cdot 10^{-6}$
- Probed  $|V_{ub}| |a_{\text{NF}}|$   
 $\Rightarrow |V_{ub}| |a_{\text{NF}}| = (3.05 \pm 0.30) \cdot 10^{-3}$
- Next steps:
  - Publish results

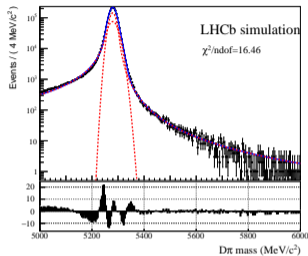


Thanks for your attention!

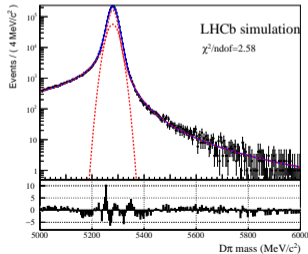
# Backup slides

Determining the probability density function ( $B^0 \rightarrow D^- \pi^+$  MC)

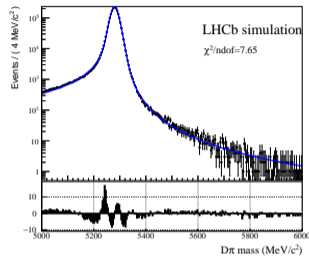
Double  
Crystal Ball



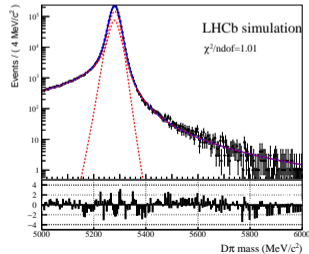
Ipatia plus  
Gaussian



Ipatia



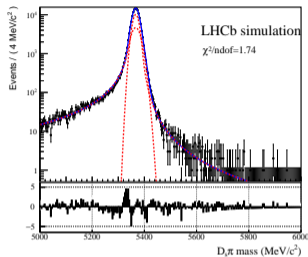
Ipatia plus  
Johnson SU



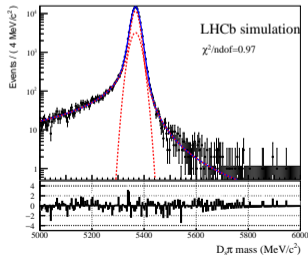
# Backup slides

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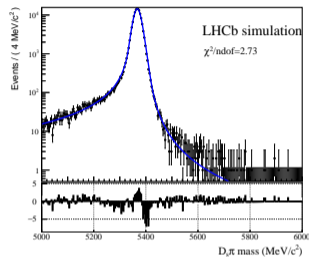
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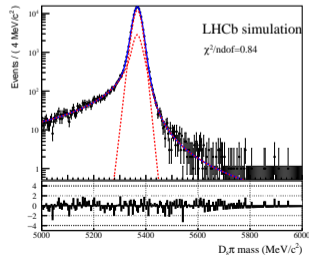
Ipatia plus  
Gaussian



Ipatia

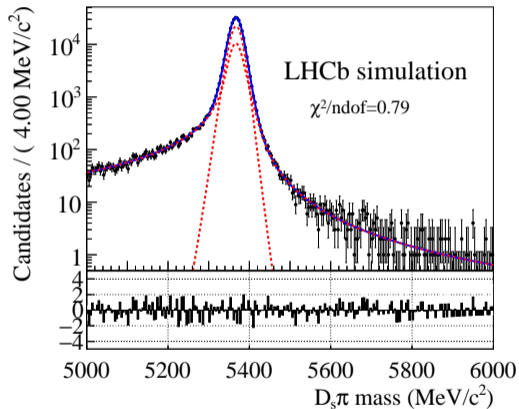


Ipatia plus  
Johnson SU

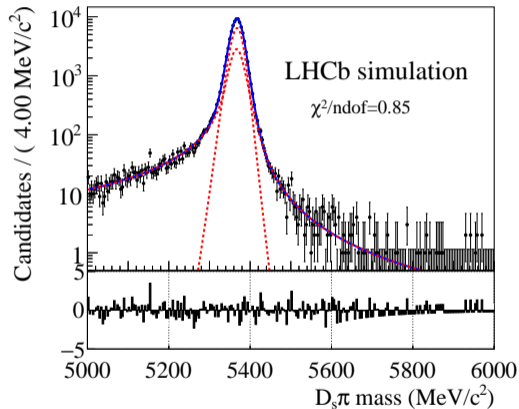


# Backup slides

MC fits  $B_s^0 \rightarrow D_s^- \pi^+$



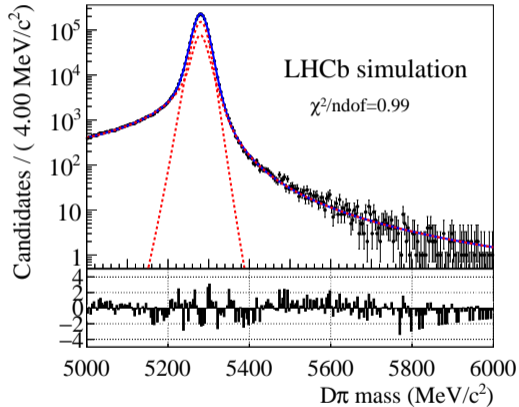
Run 1 fit to  $B_s^0 \rightarrow D_s^- \pi^+$  MC using an Ipatia plus Johnson SU distribution



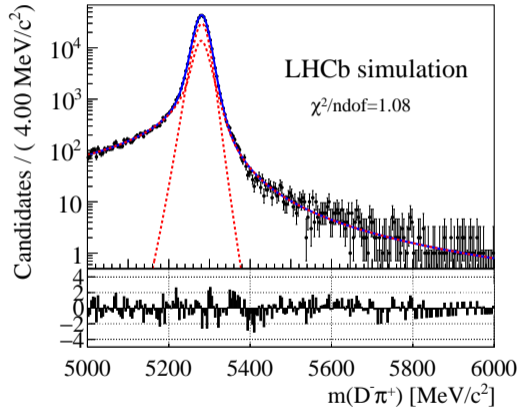
Run 2 fit to  $B_s^0 \rightarrow D_s^- \pi^+$  MC using an Ipatia plus Johnson SU distribution

# Backup slides

MC fits  $B^0 \rightarrow D^- \pi^+$



Run 1 fit to  $B^0 \rightarrow D^- \pi^+$  MC using an Ipatia plus Johnson SU distribution



Run 2 fit to  $B^0 \rightarrow D^- \pi^+$  MC using an Ipatia plus Johnson SU distribution

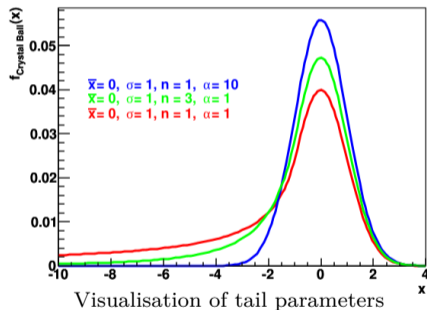
# Backup slides

## Left tail parameters in signal shape

- Left tail described by parameters  $a_1$  and  $n_1$ 
  - Found to be very correlated
  - Fix  $n_1$  to  $B^0 \rightarrow D^- \pi^+$  Run 1 MC result
- Also fixed  $\lambda$  and  $\text{frac}_{\text{Ipatia}}$  to  $B^0 \rightarrow D^- \pi^+$  Run 1 MC result to properly compare fit results
- Use  $B^0 \rightarrow D^- \pi^+$  as control channel to measure tail in data
- Gaussian Constrain  $a_1$  in  $B_{(s)}^0 \rightarrow D_s^+ \pi^-$  data mass fit:

Run 1	$B^0 \rightarrow D^- \pi^+$	$B_s^0 \rightarrow D_s^- \pi^+$	Run 2	$B^0 \rightarrow D^- \pi^+$	$B_s^0 \rightarrow D_s^- \pi^+$
MC	$1.16 \pm 0.20$	$1.20 \pm 0.01$	MC	$1.14 \pm 0.01$	$1.14 \pm 0.02$
Data	$0.97 \pm 0.02$	<b><math>1.1 \pm 0.1^*</math></b>	Data	$1.02 \pm 0.02$	<b><math>1.1 \pm 0.1^*</math></b>

\*Value and uncertainty chosen to cover differences MC and data

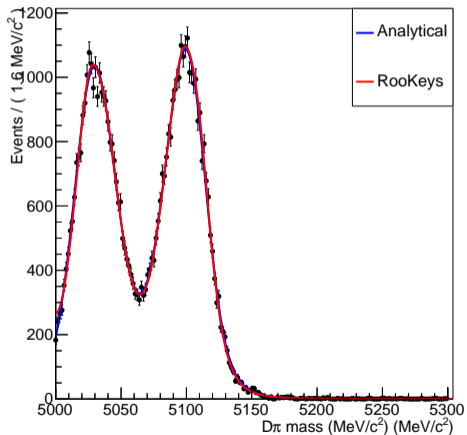




# Backup slides

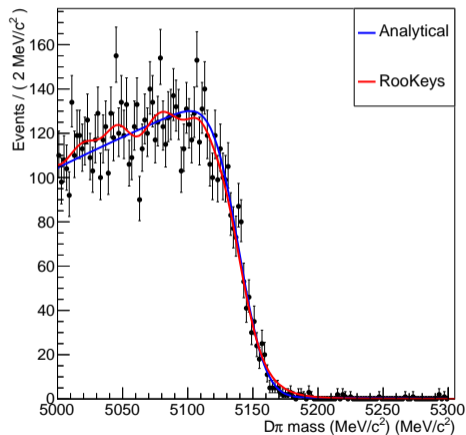
Partially reconstructed backgrounds in  $B^0 \rightarrow D^- \pi^+$  mass fit

A RooPlot of "D $\pi$  mass (MeV/c<sup>2</sup>)"



$B^0 \rightarrow D^{*-} \pi^+$  MC fits (2012)

A RooPlot of "D $\pi$  mass (MeV/c<sup>2</sup>)"

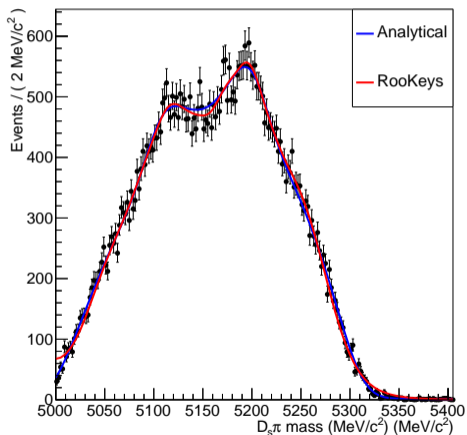


$B^0 \rightarrow D^- \rho^+$  MC fits (2012)

# Backup slides

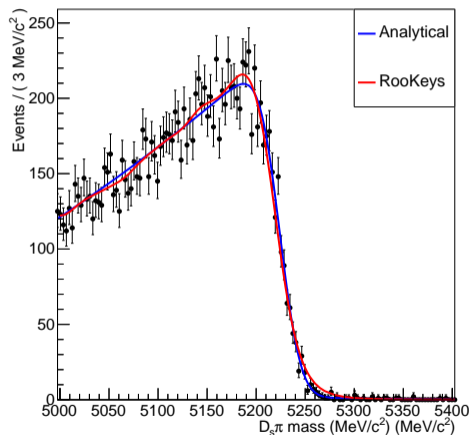
Partially reconstructed backgrounds in  $B_{(s)}^0 \rightarrow D_s^- \pi^+$  mass fit

A RooPlot of "D<sub>s</sub>π mass (MeV/c<sup>2</sup>)"



$B_s^0 \rightarrow D_s^{*-} \pi^+$  MC fits (2012)

A RooPlot of "D<sub>s</sub>π mass (MeV/c<sup>2</sup>)"

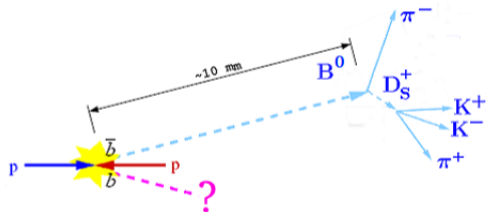


$B_s^0 \rightarrow D_s^- \rho^+$  MC fits (2012)

# Backup slides

## Trigger and Stripping

- Trigger selection
  - Hardware trigger  $\rightarrow$  high  $E_T$  or  $p_T$
  - Software triggers  $\rightarrow$  (partial) event reconstruction
    - Hlt1TrackAllL0Decision (*run1*)
    - Hlt1TrackMVADecision (*run2*)
    - Hlt1TwoTrackMVADecision (*run2*)
    - Hlt2IncPhiDecision
    - Hlt2Topo2BodyBBDTDecision
    - Hlt2Topo3BodyBBDTDecision
- Stripping  $\rightarrow$  B02DPiD2HHHBeauty2CharmLine
  - Stripping versions 21r1, 21, 24r1 and 28r1 used



# Backup slides

## Offline selection

Description	Requirement
BDT value	$> 0.1$
$m(D_s^- \pi^+)$	$[5150, 5800] \text{ MeV}/c^2$
$m(K^- K^+ \pi^-)$	$[1930, 2065] \text{ MeV}/c^2$
DLL $_{\mu\pi}$ of companion pion	$< 2$
DLL $_{K\pi}$ of companion pion	$< 0$
$D_s^-$ vertex separation $\chi^2$ w.r.t. $B_s^0$	$> 2$
$D_s^-$ lifetime w.r.t. $B_s^0$	$> 0 \text{ ps}$
nTracks	$\in [0, 500]$
Momentum final-state particles	$\in [2, 650] \text{ GeV}/c$
$D^0$ veto:	
$m(K^- K^+)$	$< 1840 \text{ MeV}/c^2$
$D^-$ veto:	
pion veto, same-charge kaon	DLL $_{K\pi} > 10$
or	
$D_s^-$ under $K^+ \pi^- \pi^-$ hypothesis	$\notin [1840, 1900] \text{ MeV}/c^2$
$\Lambda_c^+$ veto:	
proton veto, same-charge kaon	DLL $_{K\pi} - \text{DLL}_{p\pi} > 5$
or	
$D_s^-$ under $pK^- \pi^+$ hypothesis	$\notin [2255, 2315] \text{ MeV}/c^2$

Table 1:  $D_s^- \pi^+$  fit

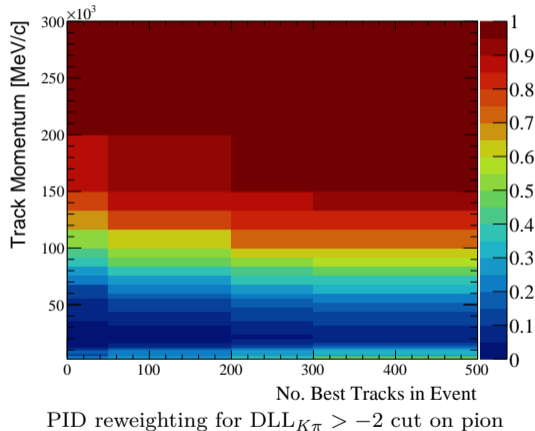
Description	Requirement
BDT value	$> 0.1$
$m(D^- \pi^+)$	$[5000, 5800] \text{ MeV}/c^2$
$m(K^+ \pi^- \pi^-)$	$[1830, 1920] \text{ MeV}/c^2$
DLL $_{\mu\pi}$ of companion pion	$< 2$
DLL $_{K\pi}$ of companion pion	$< 0$
$D^-$ vertex separation $\chi^2$ w.r.t. $B^0$	$> 9$
$D^-$ lifetime w.r.t. $B^0$	$> 0 \text{ ps}$
nTracks	$\in [0, 500]$
Momentum final-state particles	$\in [2, 650] \text{ GeV}/c$
$\Lambda_c^+$ veto:	
proton veto, pions	DLL $_{p\pi} < 0$
or	
$D^-$ under $pK^- \pi^+$ hypothesis	$\notin [2255, 2315] \text{ MeV}/c^2$
$D_s^-$ veto:	
kaon veto, pions	DLL $_{K\pi} < 0$
or	
$D^-$ under $K^- K^+ \pi^-$ hypothesis	$\notin [1950, 2030] \text{ MeV}/c^2$

Table 2:  $D^- \pi^+$  fit

# Backup slides

## PID calibration

- RICH subdetectors used to assign the variables  $DLL_{K\pi}$ ,  $DLL_{p\pi}$ ,  $DLL_{\mu\pi}$  to charged hadrons
- Not well described in MC
- PIDCalib  $\rightarrow$  data-driven method to solve this
- MC samples can be reweighted to take PID cuts into account



# Backup slides

## Fit Results $D_s^- \pi^+$ fit

Parameters	Fit Results		GC
	Run 1	Run 2	
$N_{B^0 \rightarrow D_s^+ \pi^-}$	$860 \pm 126$	$1328 \pm 153$	
$N_{B_s^0 \rightarrow D_s^- \pi^+}$	$36517 \pm 231$	$49959 \pm 333$	
$N_{\text{RandDs Combinatorial}}$	$4347 \pm 146$	$5941 \pm 165$	
$N_{\text{TrueDs Combinatorial}}$	$2521 \pm 492$	$3057 \pm 757$	
$N_{A_0^0 \rightarrow A_1^+ \pi^-}$	$316 \pm 37$	$128 \pm 15$	✓
$\text{relYield}_{B_s^0 \rightarrow D_s^+ \pi^-}$	$0.456 \pm 0.016$	$0.466 \pm 0.014$	
$\text{relYield}_{B_s^0 \rightarrow D_s^- \pi^+}$	$0.208 \pm 0.014$	$0.214 \pm 0.012$	
$\text{relYield}_{B_s^0 \rightarrow D_s^\mp K^\pm}$	$0.00845 \pm 0.00098$	$0.0086 \pm 0.0011$	✓
$B_s^0 \rightarrow D_s^- \pi^+$ BeautyMass:			
mean	$5364.788 \pm 0.097$	$5365.530 \pm 0.084$	
$\sigma_I$	$23.34 \pm 0.87$	$26.4 \pm 1.2$	
$\sigma_J$	$17.02 \pm 0.28$	$16.53 \pm 0.31$	
$a_1$	$1.272 \pm 0.070$	$1.203 \pm 0.067$	✓
$B_s^0 \rightarrow D_s^- \pi^+$ CharmMass:			
mean	$1969.704 \pm 0.029$	$1968.822 \pm 0.024$	
$R$	$1.0463 \pm 0.0054$	$1.0502 \pm 0.0051$	
RandDs Combinatorial BeautyMass:			
$p_1$	$-0.00383 \pm 0.00013$	$-0.00343 \pm 0.00011$	
RandDs Combinatorial CharmMass:			
$p_1$	$-0.00656 \pm 0.00057$	$-0.00702 \pm 0.00049$	
TrueDs Combinatorial BeautyMass:			
$p_1$	$-0.0095 \pm 0.0019$	$-0.0100 \pm 0.0023$	
$f_1$	$0.782 \pm 0.054$	$0.63 \pm 0.10$	
TrueDs Combinatorial CharmMass:			
$R$	$1.60 \pm 0.19$	$1.35 \pm 0.14$	

# Backup slides

Efficiencies  $B^0 \rightarrow D_s^+ \pi^-$

Cut	Run 1		Run2	
	$\epsilon_{rel}$ (%)	$\epsilon_{cum}$ (%)	$\epsilon_{rel}$ (%)	$\epsilon_{cum}$ (%)
Generator level efficiency	$17.368 \pm 0.028$	$17.368 \pm 0.028$	$18.055 \pm 0.024$	$18.055 \pm 0.024$
Reconstruction and stripping	$3.768 \pm 0.006$	$0.6544 \pm 0.0015$	$4.827 \pm 0.007$	$0.8715 \pm 0.0017$
Trigger cuts	$94.26 \pm 0.09$	$0.6169 \pm 0.0015$	$93.82 \pm 0.08$	$0.8176 \pm 0.0017$
$B_s^0$ mass window cuts	$98.04 \pm 0.06$	$0.6048 \pm 0.0015$	$98.08 \pm 0.05$	$0.8019 \pm 0.0018$
$D_s^\pm$ mass window cuts	$99.26 \pm 0.04$	$0.6003 \pm 0.0015$	$99.15 \pm 0.03$	$0.7951 \pm 0.0018$
nTracks and Momentum cuts	$99.90 \pm 0.01$	$0.5997 \pm 0.0015$	$99.83 \pm 0.01$	$0.7938 \pm 0.0018$
Vertex separation cuts	$88.03 \pm 0.14$	$0.5279 \pm 0.0016$	$85.82 \pm 0.12$	$0.6812 \pm 0.0018$
Lifetime cut	$98.38 \pm 0.06$	$0.5193 \pm 0.0016$	$98.61 \pm 0.04$	$0.6718 \pm 0.0018$
BDT cuts	$96.03 \pm 0.09$	$0.4987 \pm 0.0016$	$97.45 \pm 0.06$	$0.6547 \pm 0.0018$
$D_s^- \rightarrow \phi \pi^-$ mode selection	$41.24 \pm 0.23$	$0.2057 \pm 0.0013$	$41.59 \pm 0.18$	$0.2723 \pm 0.0014$
PID cuts + vetoes	$74.12 \pm 0.14$	$0.1524 \pm 0.0010$	$75.34 \pm 0.19$	$0.2051 \pm 0.0012$

Table 3: Efficiencies  $B^0 \rightarrow D^- \pi^+$  signal.

# Backup slides

Efficiencies  $B^0 \rightarrow D^- \pi^+$

Cut	Run 1		Run2	
	$\epsilon_{rel}$ (%)	$\epsilon_{cum}$ (%)	$\epsilon_{rel}$ (%)	$\epsilon_{cum}$ (%)
Generator level efficiency	$16.56 \pm 0.05$	$16.56 \pm 0.05$	$17.189 \pm 0.024$	$17.189 \pm 0.024$
Reconstruction and stripping	$3.7343 \pm 0.0034$	$0.6184 \pm 0.0020$	$4.5647 \pm 0.0024$	$0.7846 \pm 0.0012$
Trigger cuts	$94.14 \pm 0.05$	$0.5821 \pm 0.0019$	$96.29 \pm 0.03$	$0.7555 \pm 0.0011$
$B_s^0$ mass window cuts	$99.35 \pm 0.02$	$0.5784 \pm 0.0019$	$99.30 \pm 0.01$	$0.7502 \pm 0.0011$
$D_s^\pm$ mass window cuts	$98.52 \pm 0.03$	$0.5698 \pm 0.0018$	$98.34 \pm 0.02$	$0.7377 \pm 0.0011$
nTracks and Momentum cuts	$99.91 \pm 0.01$	$0.5693 \pm 0.0018$	$99.86 \pm 0.01$	$0.7367 \pm 0.0011$
Vertex separation cuts	$86.79 \pm 0.08$	$0.4941 \pm 0.0017$	$83.58 \pm 0.05$	$0.6157 \pm 0.0010$
Lifetime cut	$99.93 \pm 0.01$	$0.4937 \pm 0.0017$	$99.94 \pm 0.00$	$0.6154 \pm 0.0010$
BDT cuts	$95.98 \pm 0.05$	$0.4739 \pm 0.0016$	$97.55 \pm 0.02$	$0.6003 \pm 0.0010$
PID cuts + vetoes	$74.93 \pm 0.16$	$0.3551 \pm 0.0014$	$77.00 \pm 0.15$	$0.4622 \pm 0.0012$

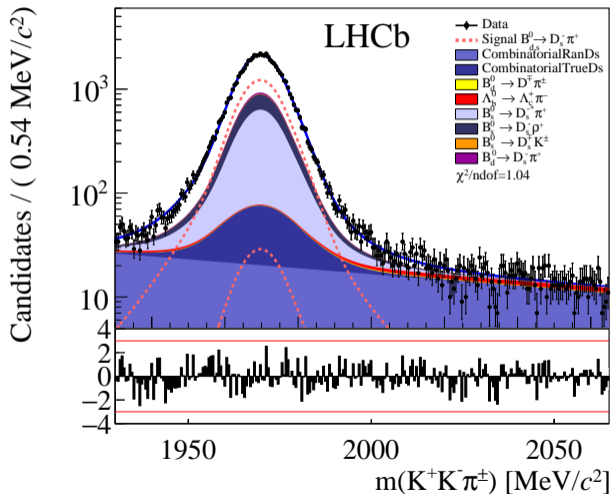
Table 4: Efficiencies  $B^0 \rightarrow D^- \pi^+$  signal.



# Backup slides

## $B^0 \rightarrow D_s^- \pi^+$ mass fit

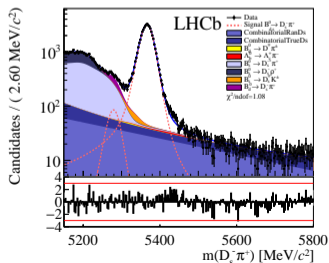
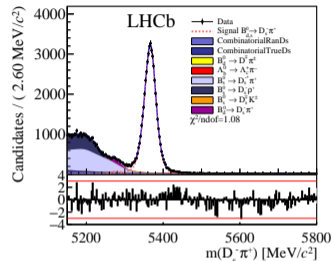
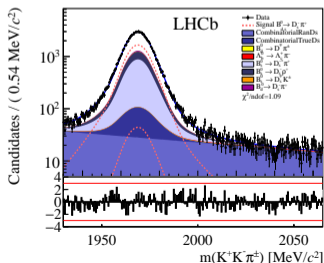
- Run 1 fit (2011+2012)
- Fitted yields, using **all** data:
  - $N_{B^0 \rightarrow D_s^+ \pi^-} = 2190 \pm 198$



# Backup slides

## $B_{(s)}^0 \rightarrow D_s^- \pi^+$ mass fit

- Run 2 fit (2015+2016)
- Fitted yields:
  - $N_{B^0 \rightarrow D_s^+ \pi^-} = 1328 \pm 153$



# Backup slides

## Systematic Uncertainties (1/2)

- Partially Reconstructed backgrounds
  - Vary resolution of analytical shapes by  $\pm 1.0$
  - Run 1  $\rightarrow 4.6\%$ , Run 2  $\rightarrow 4.3\%$
- PID selection
  - Reduce/increase amount of bins with a third
  - Assign additional uncertainty to  $p > 100 \text{ GeV}/c$  and  $p > 300 \text{ GeV}/c$  final-state particles
  - 1.1 systematic uncertainty
- Offline selection
  - Compare variables between MC and sWeighted data
  - Reweight variable and check change in efficiency
  - Run 1  $\rightarrow 0.1\%$ , Run 2  $\rightarrow 0.6\%$

# Backup slides

## Systematic Uncertainties (2/2)

- L0 trigger efficiency
  - Detection efficiency asymmetry between pions and kaons
  - $\sim 0.2\%$
- MisID backgrounds
  - Free yield of  $\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^-$  misidentified background in  $D_s^+ \pi^-$  fit
  - Run 1  $\rightarrow 0.6\%$ , Run 2  $\rightarrow 1.4\%$
- $B^0 \rightarrow D_s^+ \pi^-$  signal width
  - Scale the  $B^0 \rightarrow D_s^+ \pi^-$  signal width with  $B^0$  and  $B_s^0$  masses
  - Run 1  $\rightarrow 1.0\%$ , Run 2  $\rightarrow 1.2\%$
- Total systematic uncertainty
  - Run 1  $\rightarrow 4.9\%$ , Run 2  $\rightarrow 4.8\%$

# Backup slides

## Detailed branching fraction results

- We now have all the ingredients to calculate the branching fraction:

	Run 1	Run 2
$\epsilon_{B^0 \rightarrow D_s^+ \pi^-}$ (%)	$0.1524 \pm 0.0010$	$0.2051 \pm 0.0012$
$\epsilon_{B^0 \rightarrow D^- \pi^+}$ (%)	$0.3551 \pm 0.0014$	$0.4622 \pm 0.0012$
$N_{B^0 \rightarrow D_s^+ \pi^-}$	$860 \pm 126$	$1328 \pm 153$
$N_{B^0 \rightarrow D^- \pi^+}$	$500908 \pm 1315$	$632127 \pm 1596$

- Result:

- $\mathcal{B}(B^0 \rightarrow D_s^+ \pi^-) = (17.2 \pm 2.5 \text{ (stat)} \pm 0.8 \text{ (syst)} \pm 1.1 \text{ (}\mathcal{B}\text{)}) \cdot 10^{-6}$  (Run 1)
- $\mathcal{B}(B^0 \rightarrow D_s^+ \pi^-) = (20.3 \pm 2.3 \text{ (stat)} \pm 1.0 \text{ (syst)} \pm 1.3 \text{ (}\mathcal{B}\text{)}) \cdot 10^{-6}$  (Run 2)
- $\mathcal{B}(B^0 \rightarrow D_s^+ \pi^-) = (18.9 \pm 1.7 \text{ (stat)} \pm 0.9 \text{ (syst)} \pm 1.2 \text{ (}\mathcal{B}\text{)}) \cdot 10^{-6}$  (Combined)

# Backup slides

## Fit Results $D_s^+ \pi^-$ fit

Parameters	Fit Results		GC
	Run 1	Run 2	
$N_{B^0 \rightarrow D_s^+ \pi^-}$	$860 \pm 126$	$1328 \pm 153$	
$N_{B_s^0 \rightarrow D_s^- \pi^+}$	$36517 \pm 231$	$49959 \pm 333$	
$N_{\text{RandDs Combinatorial}}$	$4347 \pm 146$	$5941 \pm 165$	
$N_{\text{TrueDs Combinatorial}}$	$2521 \pm 492$	$3057 \pm 757$	
$N_{A_0^0 \rightarrow A_1^+ \pi^-}$	$316 \pm 37$	$128 \pm 15$	✓
$\text{relYield}_{B_s^0 \rightarrow D_s^+ \pi^-}$	$0.456 \pm 0.016$	$0.466 \pm 0.014$	
$\text{relYield}_{B_s^0 \rightarrow D_s^- \pi^+}$	$0.208 \pm 0.014$	$0.214 \pm 0.012$	
$\text{relYield}_{B_s^0 \rightarrow D_s^\mp K^\pm}$	$0.00845 \pm 0.00098$	$0.0086 \pm 0.0011$	✓
$B_s^0 \rightarrow D_s^- \pi^+$ BeautyMass:			
mean	$5364.788 \pm 0.097$	$5365.530 \pm 0.084$	
$\sigma_I$	$23.34 \pm 0.87$	$26.4 \pm 1.2$	
$\sigma_J$	$17.02 \pm 0.28$	$16.53 \pm 0.31$	
$a_1$	$1.272 \pm 0.070$	$1.203 \pm 0.067$	✓
$B_s^0 \rightarrow D_s^- \pi^+$ CharmMass:			
mean	$1969.704 \pm 0.029$	$1968.822 \pm 0.024$	
$R$	$1.0463 \pm 0.0054$	$1.0502 \pm 0.0051$	
RandDs Combinatorial BeautyMass:			
$p_1$	$-0.00383 \pm 0.00013$	$-0.00343 \pm 0.00011$	
RandDs Combinatorial CharmMass:			
$p_1$	$-0.00656 \pm 0.00057$	$-0.00702 \pm 0.00049$	
TrueDs Combinatorial BeautyMass:			
$p_1$	$-0.0095 \pm 0.0019$	$-0.0100 \pm 0.0023$	
$f_1$	$0.782 \pm 0.054$	$0.63 \pm 0.10$	
TrueDs Combinatorial CharmMass:			
$R$	$1.60 \pm 0.19$	$1.35 \pm 0.14$	

# Backup slides

## Fit Results $D^- \pi^+$ fit

Parameters	Fit Results		GC
	Run 1	Run 2	
$N_{B^0 \rightarrow D^- \pi^+}$	$500908 \pm 1426$	$632127 \pm 1596$	
$N_{B^0 \rightarrow D^+ \pi^-}$	$164612 \pm 5744$	$189315 \pm 4391$	
$N_{B^0 \rightarrow D^- \rho^+}$	$169264 \pm 6134$	$235087 \pm 4655$	
$N_{\text{Combinatorial}}$	$112431 \pm 2736$	$196906 \pm 2876$	
$\text{relYield}_{B^0 \rightarrow D^- K^+}$	$0.0069 \pm 0.0010$	$0.00679 \pm 0.00093$	✓
$\text{relYield}_{B^0 \rightarrow D^- \pi^+}$	$0.00651 \pm 0.00084$	$0.00803 \pm 0.00081$	✓
$\text{relYield}_{A_0^0 \rightarrow A_1^+ \pi^-}$	$0.00355 \pm 0.00055$	$0.00243 \pm 0.00028$	✓
$B^0 \rightarrow D^- \pi^+$ BeautyMass:			
mean	$5277.758 \pm 0.030$	$5278.046 \pm 0.028$	
$\sigma_J$	$27.05 \pm 0.44$	$28.25 \pm 0.41$	
$\sigma_J$	$16.91 \pm 0.10$	$17.171 \pm 0.090$	
$a_1$	$0.974 \pm 0.021$	$1.028 \pm 0.019$	
Partially reconstructed BeautyMass:			
$\sigma_{B^0 \rightarrow D^+ \pi^-}$	$15.65 \pm 0.29$	$15.05 \pm 0.21$	
$\sigma_{B^0 \rightarrow D^- \rho^+}$	$17.65 \pm 0.35$	$18.15 \pm 0.30$	
shift	$-1.95 \pm 0.13$	$-1.66 \pm 0.11$	
Combinatorial BeautyMass:			
$p_1$	$-0.00637 \pm 0.00012$	$-0.006132 \pm 0.000091$	
$f_1$	$0.8619 \pm 0.0064$	$0.8030 \pm 0.0048$	