



The Standard Model EFT:

The top quark sector

Juan Rojo

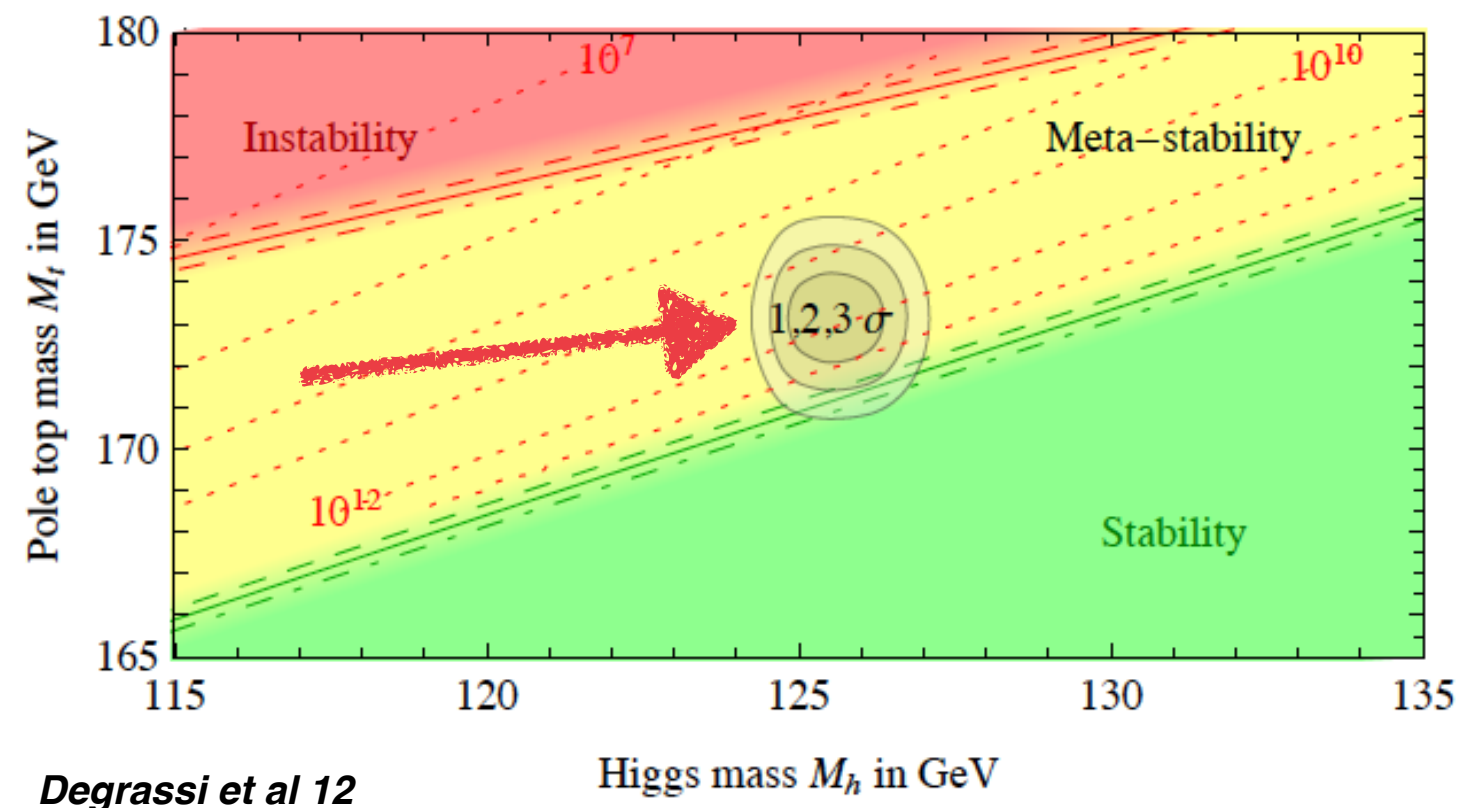
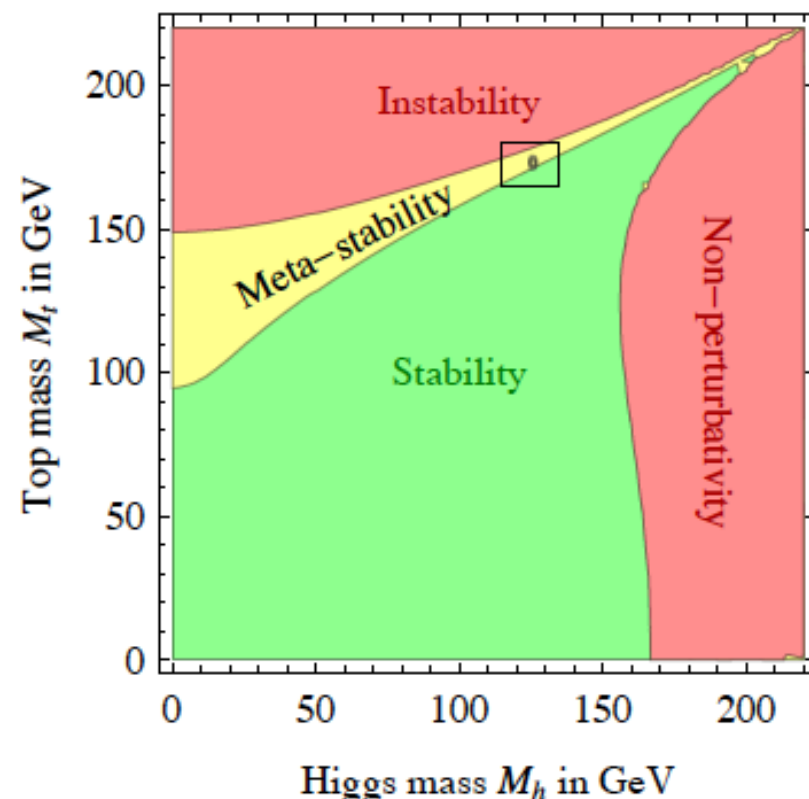
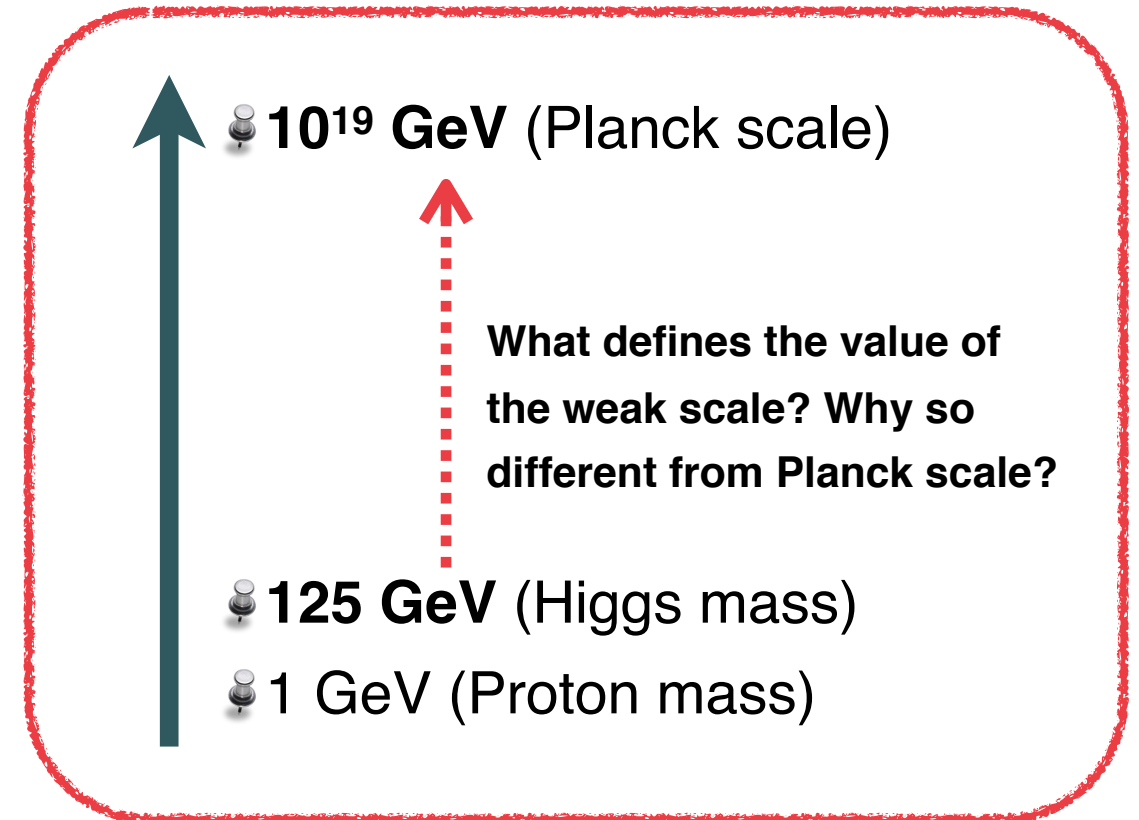
VU Amsterdam & Theory group, Nikhef

Nikhef Topical Lectures on Flavour Physics and CP violation
14th June 2019

Open questions in particle physics

The Higgs boson

- 📌 Huge gap between **weak** and **Planck scales**?
- 📌 **Compositeness**? Non-minimal Higgs sector?
- 📌 Coupling to **Dark Matter**? Role in cosmological phase transitions?
- 📌 Is the **vacuum state of the Universe** stable?



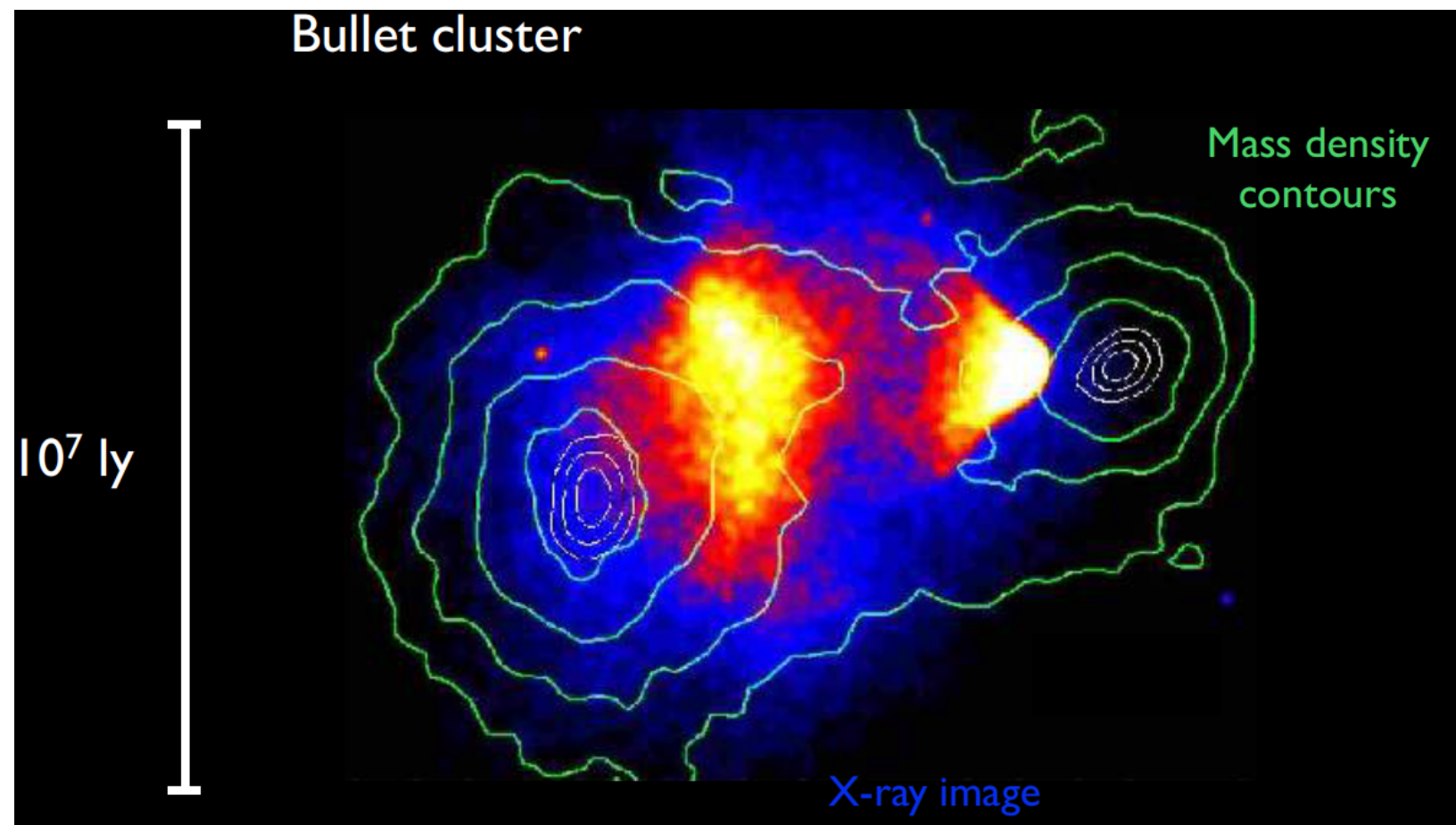
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Dark matter

- 📌 **Weakly interacting massive particles**?
Neutrinos? Ultralight particles (axions)?
- 📌 **Interactions** with SM particles? Self-interactions?
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Open questions in particle physics

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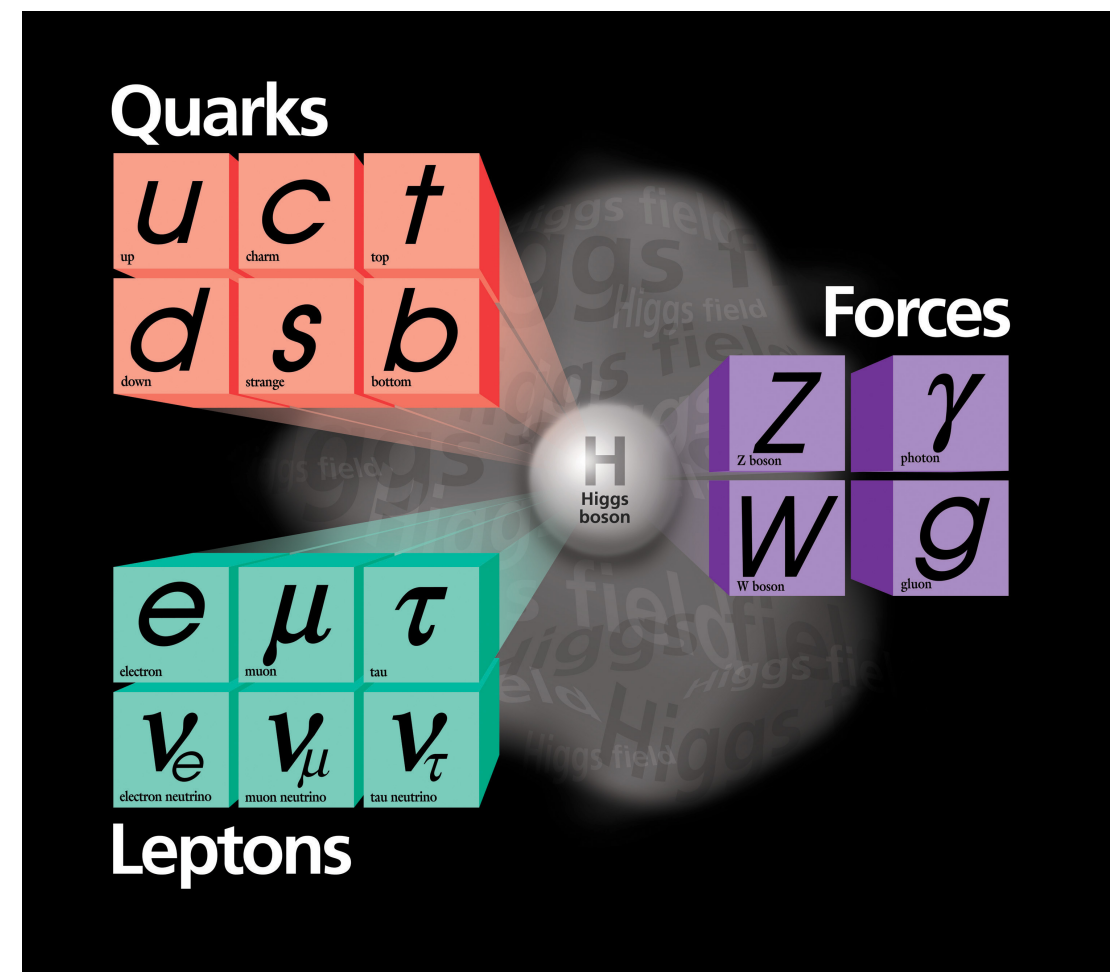
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Quarks and leptons

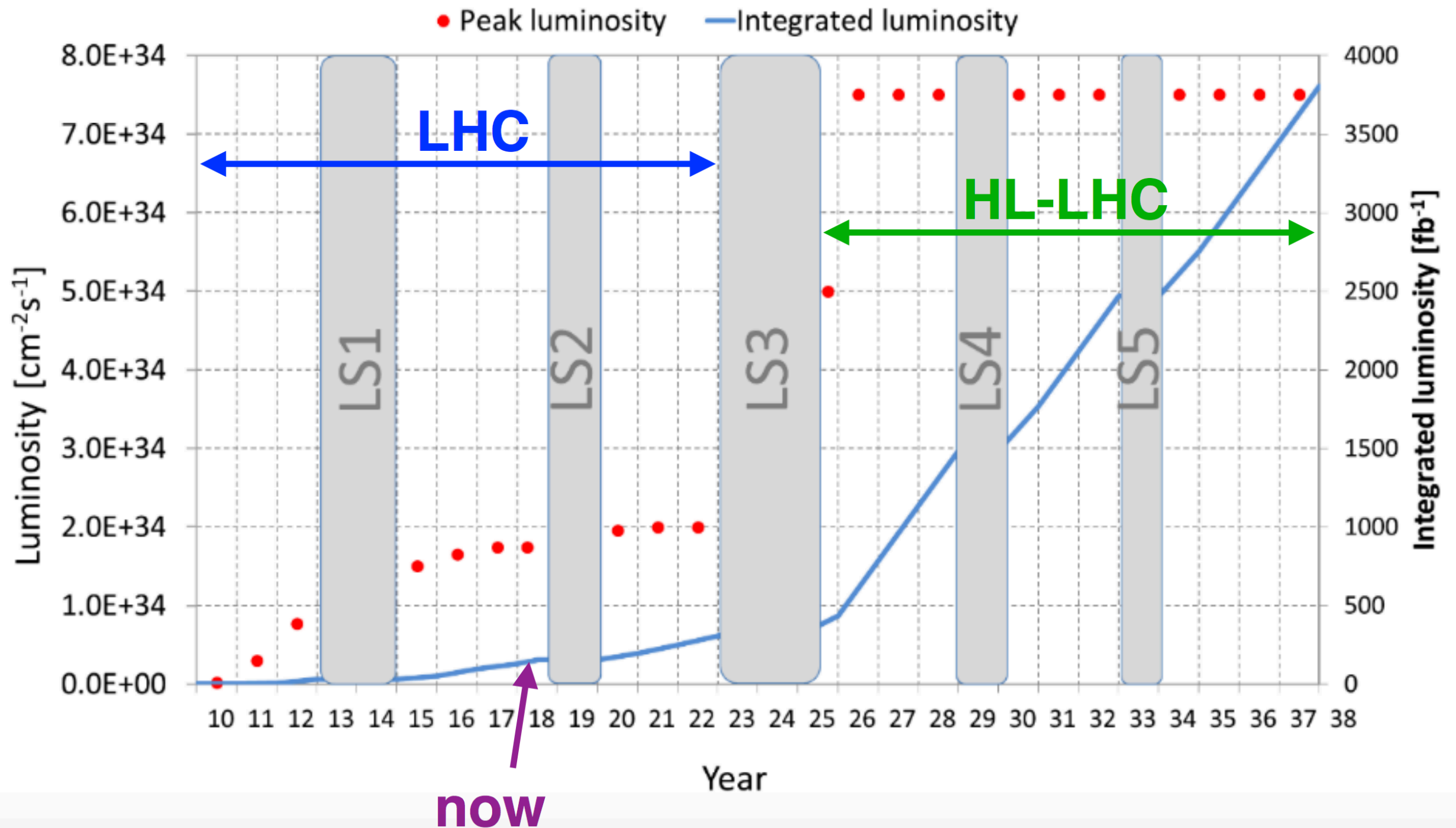
- 📌 Why **3 families**? Origin of **masses, mixings**?
- 📌 Origin of **Matter-Antimatter asymmetry**?
- 📌 Origin of **neutrino masses**? Are **neutrinos Majorana or Dirac**? CP violation in the lepton sector?

Dark matter

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Open questions in particle physics

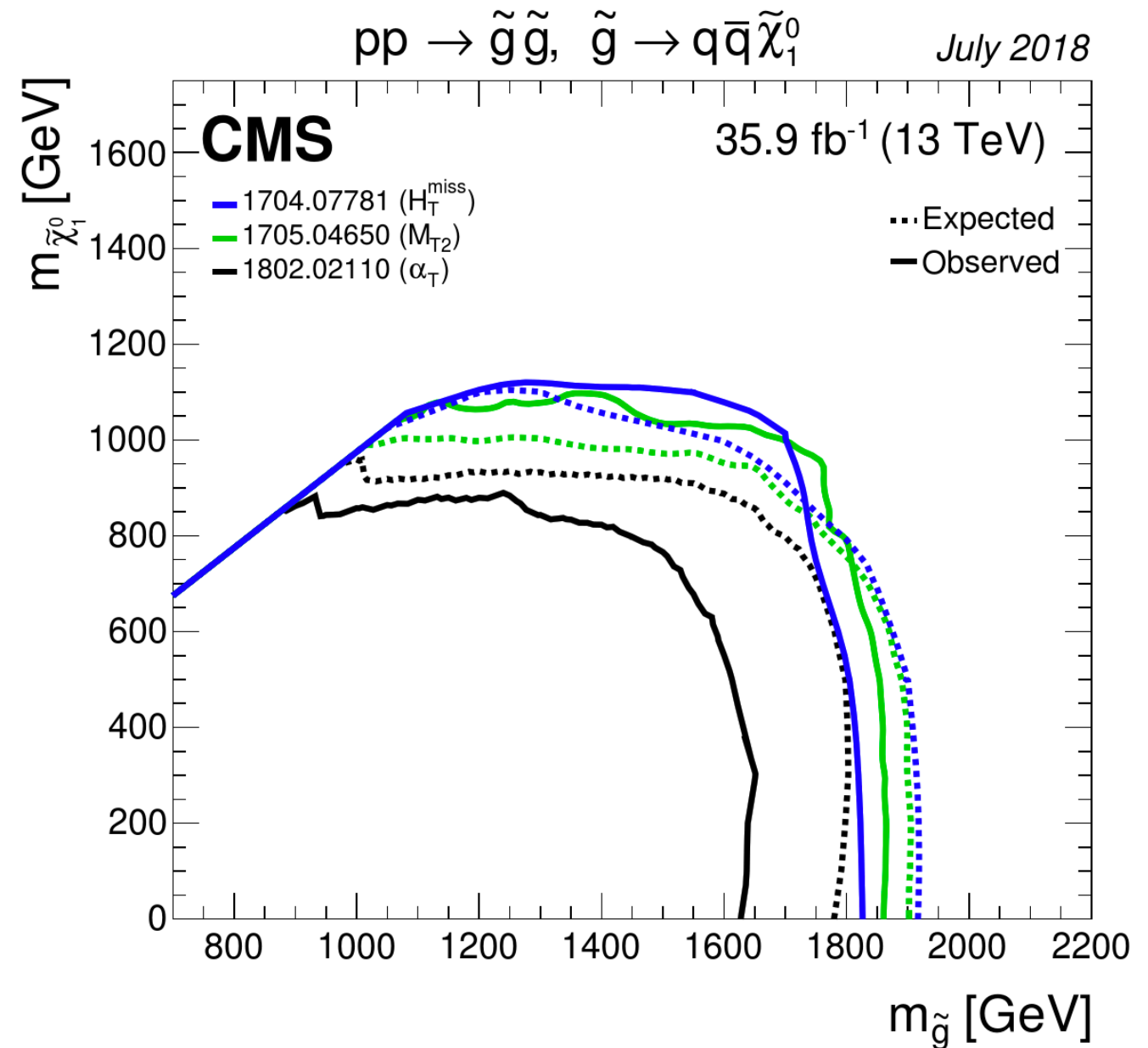


Crucial information on these fundamental questions will be provided by the LHC:
the **exploration of the high-energy frontier** has just started!

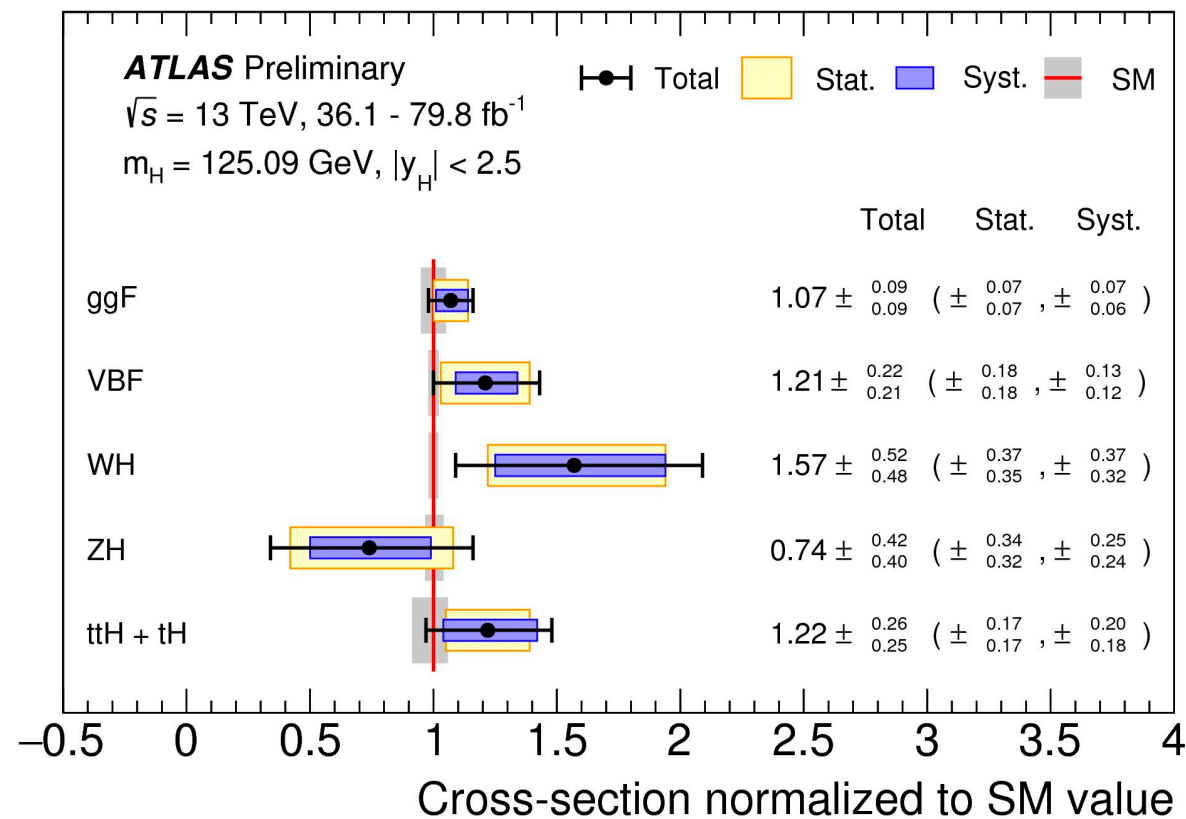
The quest for New Physics at the LHC

Model-Dependent Searches

- ✓ Map parameter space of **specific theories**, or specific realisations of theories (SUSY, Higgs compositeness, ...)
- ✓ **Reinterpretation/recasting** challenging, since requires Monte Carlo showering, detector simulation, ...
- ✓ Ad-hoc **restrictions of the BSM parameter space** to facilitate interpretation
- ✓ Sensitive to **O(1) deviations**

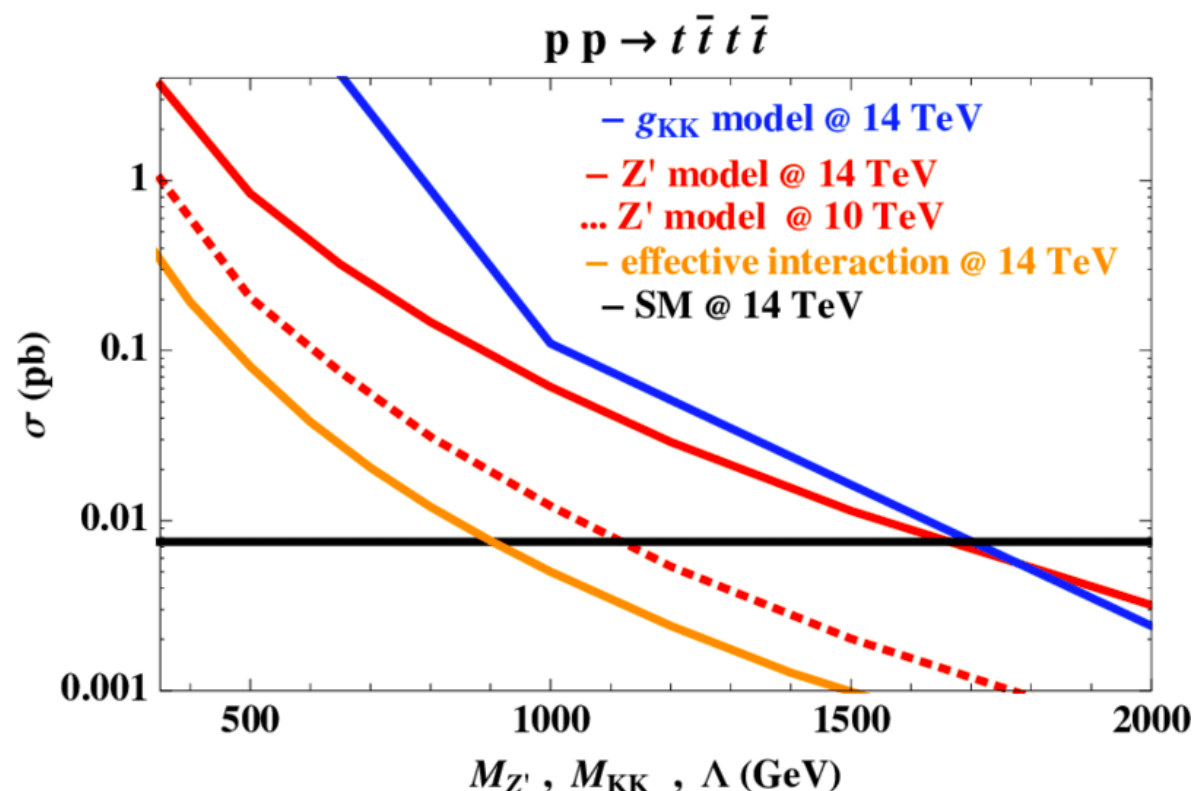


The quest for New Physics at the LHC



Model-Independent Searches

- ☑ ``SM'' measurements to constrain BSM
- ☑ Allows the use of **highest possible precision** in theory calculations
- ☑ Interpreted in **multiple BSM frameworks** (including those not thought of yet!)
- ☑ In the long-term, measurements have the **largest impact** in the HEP community
- ☑ Sensitive to **O(0.1) or O(0.01) deviations**



The quest for New Physics at the LHC

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The Standard Model

Effective Field Theory

The Standard Model EFT

Systematic parametrisation of the **theory space** in vicinity of Standard Model

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_i^{N_{d6}} \frac{c_i}{\Lambda^2} \mathcal{O}_i^{(6)} + \sum_j^{N_{d8}} \frac{b_j}{\Lambda^4} \mathcal{O}_j^{(8)} + \dots$$

- ☑ SMEFT: **low-energy limit** of generic UV-complete theories at high energies
- ☑ Assumes **SM field content and symmetries** (except the accidental ones!)
- ☑ **Complete basis** at any given mass-dimension
- ☑ **Fully renormalizable**, full-fledged QFT: can compute higher orders in QCD and EW
- ☑ Can be matched to **any BSM model** that reduces to the SM at low energies

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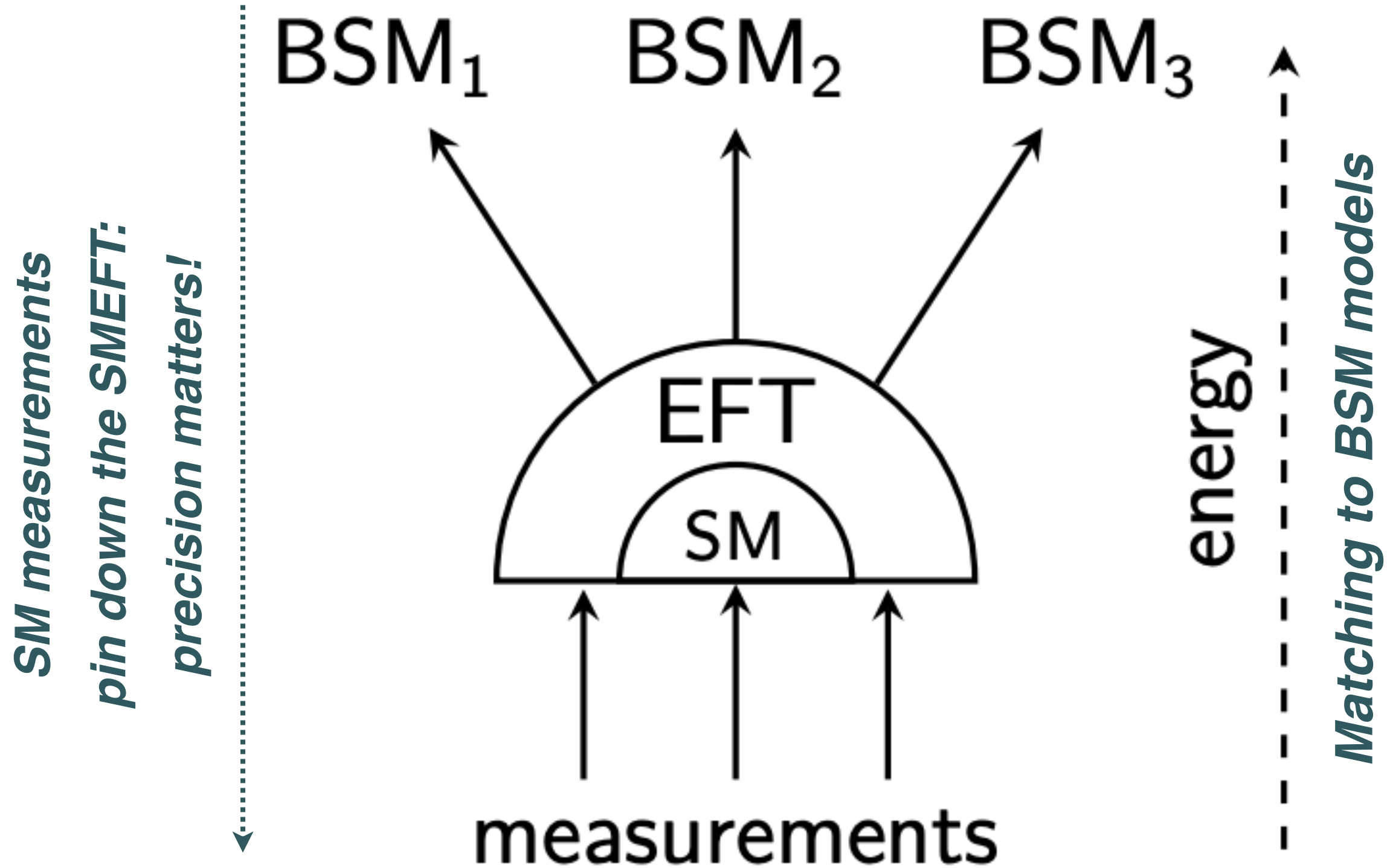
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(...) if one writes down the most general possible Lagrangian, including all terms consistent with assumed symmetry principles, (...) the result will simply be the most general possible S-matrix consistent with analyticity, perturbative unitarity, cluster decomposition and the assumed symmetry. [Phenomenological Lagrangians, Weinberg '79]

The Standard Model EFT



The Standard Model EFT

- Heavy bSM physics beyond the direct reach of the LHC can be **parametrised in a model-independent** in terms of complete basis of **higher-dimensional operators**

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- Some operators induce **growth with the partonic centre-of-mass energy**:
increased sensitivity in LHC cross-sections in the TeV region

$$\sigma(E) = \sigma_{\text{SM}}(E) \left(1 + \sum_i^{N_{d6}} \omega_i \frac{c_i m_{\text{SM}}^2}{\Lambda^2} + \sum_i^{N_{d6}} \tilde{\omega}_i \frac{c_i E^2}{\Lambda^2} + \mathcal{O}(\Lambda^{-4}) \right)$$

*enhanced sensitivity from **TeV-scale processes**:
unique feature of LHC*

The Standard Model EFT

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$$\sigma(\textcolor{red}{E}) = \sigma_{\text{SM}}(\textcolor{red}{E}) \left(1 + \sum_i^{N_{d6}} \omega_i \frac{\textcolor{blue}{c}_i m_{\text{SM}}^2}{\Lambda^2} + \sum_i^{N_{d6}} \widetilde{\omega}_i \frac{\textcolor{blue}{c}_i \textcolor{red}{E}^2}{\Lambda^2} + \mathcal{O}(\Lambda^{-4}) \right)$$

- The number of SMEFT operators is large: **59 non-redundant operators at dimension 6** with Minimal Flavour Violation, **> 2000 operators** without any flavour assumption
- A global SMEFT analysis needs to explore a **huge complicated parameter space**

The Standard Model EFT

Operators involving up-type quarks in the *Warsaw* basis:

[Grzadkowski et al '10]

Four-quark operators (11)

$$O_{qq}^{1(ijkl)} = (\bar{q}_i \gamma^\mu q_j)(\bar{q}_k \gamma_\mu q_l),$$

$$O_{qq}^{3(ijkl)} = (\bar{q}_i \gamma^\mu \tau^I q_j)(\bar{q}_k \gamma_\mu \tau^I q_l),$$

$$O_{qu}^{1(ijkl)} = (\bar{q}_i \gamma^\mu q_j)(\bar{u}_k \gamma_\mu u_l),$$

$$O_{qu}^{8(ijkl)} = (\bar{q}_i \gamma^\mu T^A q_j)(\bar{u}_k \gamma_\mu T^A u_l),$$

$$O_{qd}^{1(ijkl)} = (\bar{q}_i \gamma^\mu q_j)(\bar{d}_k \gamma_\mu d_l),$$

$$O_{qd}^{8(ijkl)} = (\bar{q}_i \gamma^\mu T^A q_j)(\bar{d}_k \gamma_\mu T^A d_l),$$

$$O_{uu}^{(ijkl)} = (\bar{u}_i \gamma^\mu u_j)(\bar{u}_k \gamma_\mu u_l),$$

$$O_{ud}^{1(ijkl)} = (\bar{u}_i \gamma^\mu u_j)(\bar{d}_k \gamma_\mu d_l),$$

$$O_{ud}^{8(ijkl)} = (\bar{u}_i \gamma^\mu T^A u_j)(\bar{d}_k \gamma_\mu T^A d_l),$$

$$O_{quqd}^{1(ijkl)} = (\bar{q}_i u_j) \varepsilon (\bar{q}_k d_l),$$

$$O_{quqd}^{8(ijkl)} = (\bar{q}_i T^A u_j) \varepsilon (\bar{q}_k T^A d_l),$$

Two-quark operators (9)

$$O_{u\varphi}^{(ij)} = \bar{q}_i u_j \tilde{\varphi} (\varphi^\dagger \varphi),$$

$$O_{\varphi q}^{1(ij)} = (\varphi^\dagger \overleftrightarrow{D}_\mu \varphi)(\bar{q}_i \gamma^\mu q_j),$$

$$O_{\varphi q}^{3(ij)} = (\varphi^\dagger \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_i \gamma^\mu \tau^I q_j),$$

$$O_{\varphi u}^{(ij)} = (\varphi^\dagger \overleftrightarrow{D}_\mu \varphi)(\bar{u}_i \gamma^\mu u_j),$$

$$O_{\varphi ud}^{(ij)} = (\tilde{\varphi}^\dagger i D_\mu \varphi)(\bar{u}_i \gamma^\mu d_j),$$

$$O_{uW}^{(ij)} = (\bar{q}_i \sigma^{\mu\nu} \tau^I u_j) \tilde{\varphi} W_{\mu\nu}^I,$$

$$O_{dW}^{(ij)} = (\bar{q}_i \sigma^{\mu\nu} \tau^I d_j) \varphi W_{\mu\nu}^I,$$

$$O_{uB}^{(ij)} = (\bar{q}_i \sigma^{\mu\nu} u_j) \tilde{\varphi} B_{\mu\nu},$$

$$O_{uG}^{(ij)} = (\bar{q}_i \sigma^{\mu\nu} T^A u_j) \tilde{\varphi} G_{\mu\nu}^A,$$

Two-quark-two-lepton operators (8)

$$O_{lq}^{1(ijkl)} = (\bar{l}_j \gamma^\mu l_j)(\bar{q}_k \gamma^\mu q_l),$$

$$O_{lq}^{3(ijkl)} = (\bar{l}_j \gamma^\mu \tau^I l_j)(\bar{q}_k \gamma^\mu \tau^I q_l),$$

$$O_{lu}^{(ijkl)} = (\bar{l}_j \gamma^\mu l_j)(\bar{u}_k \gamma^\mu u_l),$$

$$O_{eq}^{(ijkl)} = (\bar{e}_j \gamma^\mu e_j)(\bar{q}_k \gamma^\mu q_l),$$

$$O_{eu}^{(ijkl)} = (\bar{e}_j \gamma^\mu e_j)(\bar{u}_k \gamma^\mu u_l),$$

$$O_{lequ}^{1(ijkl)} = (\bar{l}_i e_j) \varepsilon (\bar{q}_k u_l),$$

$$O_{lequ}^{3(ijkl)} = (\bar{l}_i \sigma^{\mu\nu} e_j) \varepsilon (\bar{q}_k \sigma_{\mu\nu} u_l),$$

$$O_{ledq}^{(ijkl)} = (\bar{l}_i e_j)(\bar{d}_k q_l),$$

\not{B} and \not{L} operators (5)

$$O_{duq}^{(ijkl)} = (\bar{d}^c_{i\alpha} u_{j\beta})(\bar{q}^c_{k\gamma} \varepsilon l_l) \epsilon^{\alpha\beta\gamma},$$

$$O_{quq}^{(ijkl)} = (\bar{q}^c_{i\alpha} \varepsilon q_{j\beta})(\bar{u}^c_{k\gamma} \varepsilon l_l) \epsilon^{\alpha\beta\gamma},$$

$$O_{qqq}^{1(ijkl)} = (\bar{q}^c_{i\alpha} \varepsilon q_{j\beta})(\bar{q}^c_{k\gamma} \varepsilon l_l) \epsilon^{\alpha\beta\gamma},$$

$$O_{qqq}^{3(ijkl)} = (\bar{q}^c_{i\alpha} \tau^I \varepsilon q_{j\beta})(\bar{q}^c_{k\gamma} \tau^I \varepsilon l_l) \epsilon^{\alpha\beta\gamma},$$

$$O_{duu}^{(ijkl)} = (\bar{d}^c_{i\alpha} u_{j\beta})(\bar{u}^c_{k\gamma} \varepsilon l_l) \epsilon^{\alpha\beta\gamma}.$$

+ $ijkl$ generation index assignments

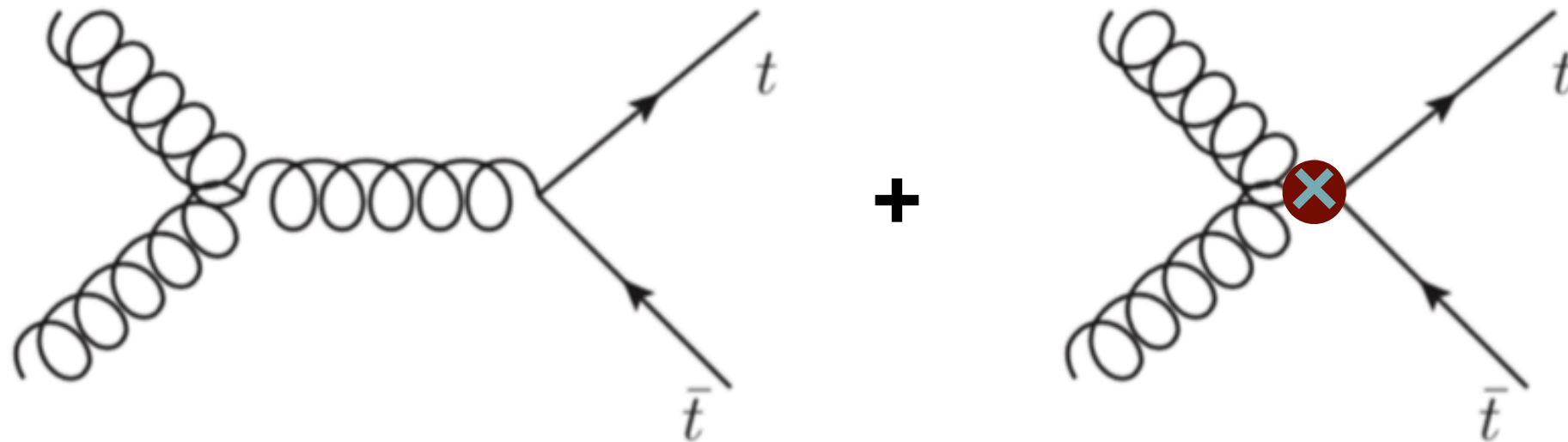
q, l : left-handed doublets

u, d, e : right-h. singlets

SMEFT effects

Standard Model

$$\dagger O_{uG}^{(ij)} = (\bar{q}_i \sigma^{\mu\nu} T^A u_j) \tilde{\varphi} G_{\mu\nu}^A,$$



$$= \sigma_{SM} \times \left(1 + a \frac{c_{tG}}{\Lambda^2} + b \frac{c_{tG}^2}{\Lambda^4} \right)$$

SM: N(NLO) QCD

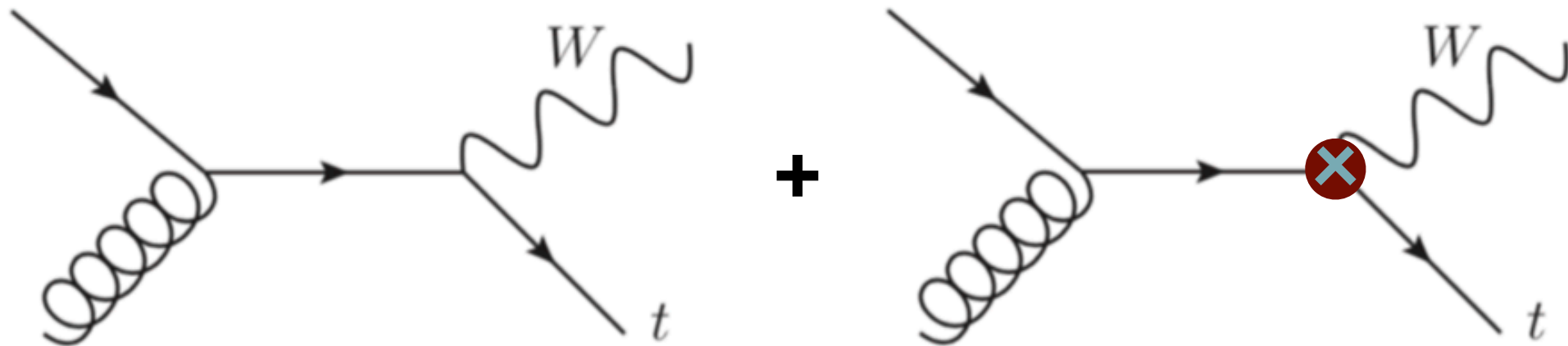
interference

squared

SMEFT effects

Standard Model

$$O_{uW}^{(ij)} = (\bar{q}_i \sigma^{\mu\nu} \tau^I u_j) \tilde{\varphi} W_{\mu\nu}^I$$



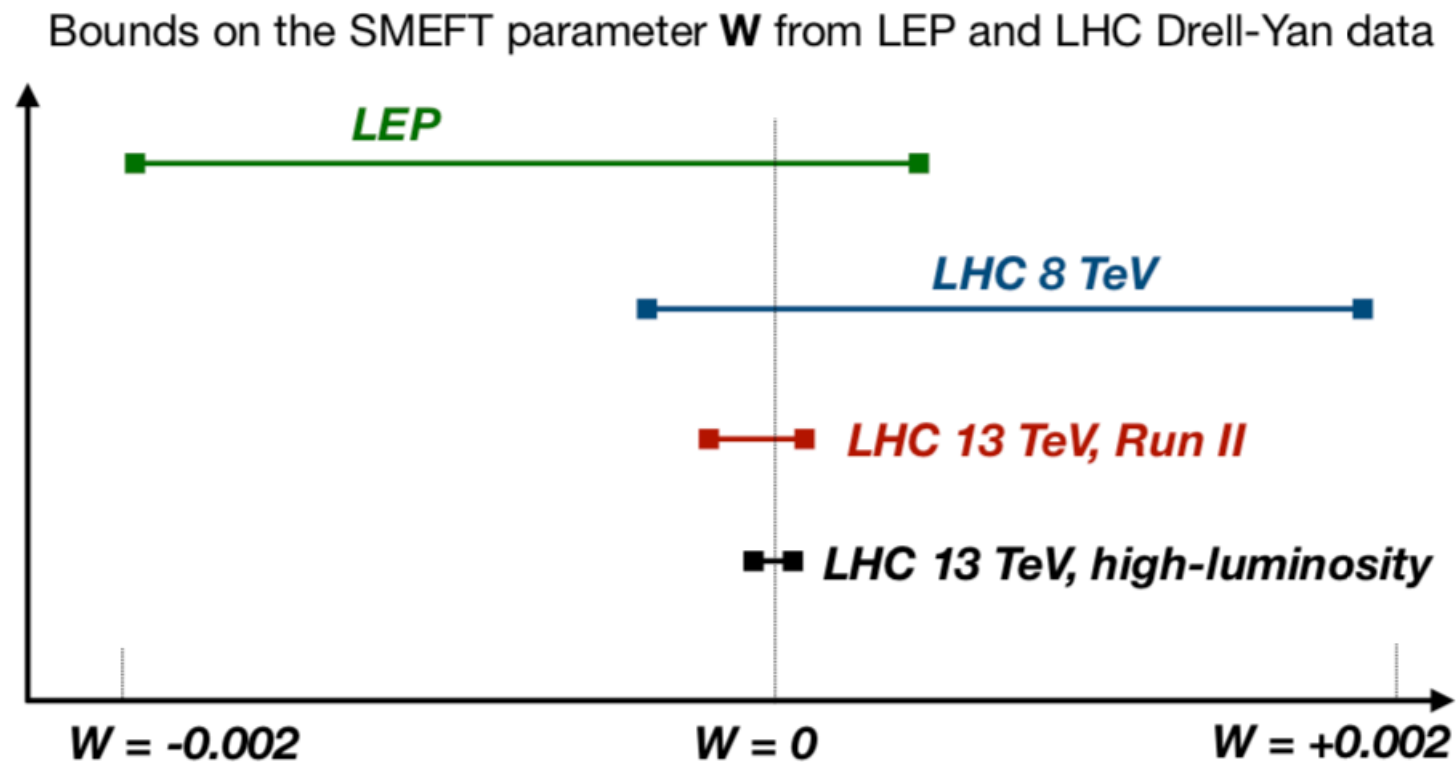
$$= \sigma_{SM} \times \left(1 + a \frac{c_{tW}}{\Lambda^2} + b \frac{c_{tW}^2}{\Lambda^4} \right)$$

SM: N(NLO) QCD

interference

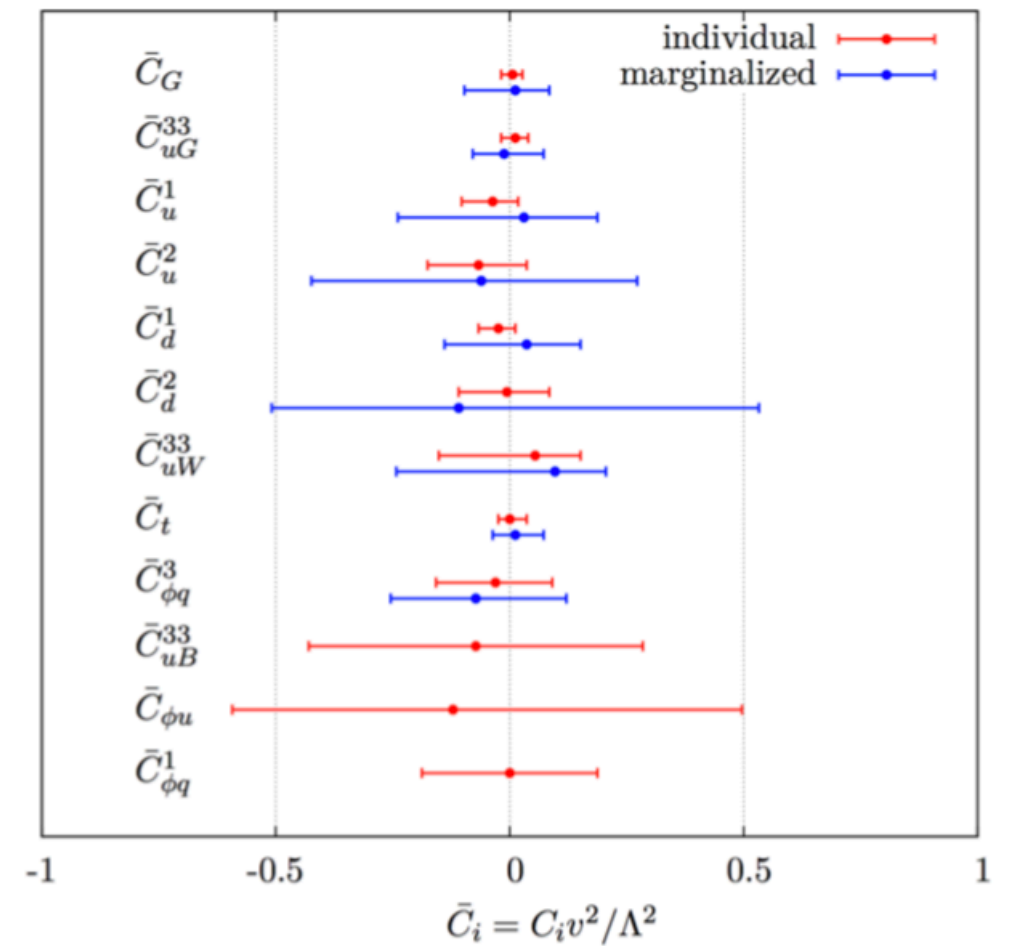
squared

SMEFT constraints from LHC



📍 LHC data can markedly improve the LEP bounds on SMEFT coefficients: **Precision Electroweak Tests at hadron colliders**

Farina et al PLB (16)

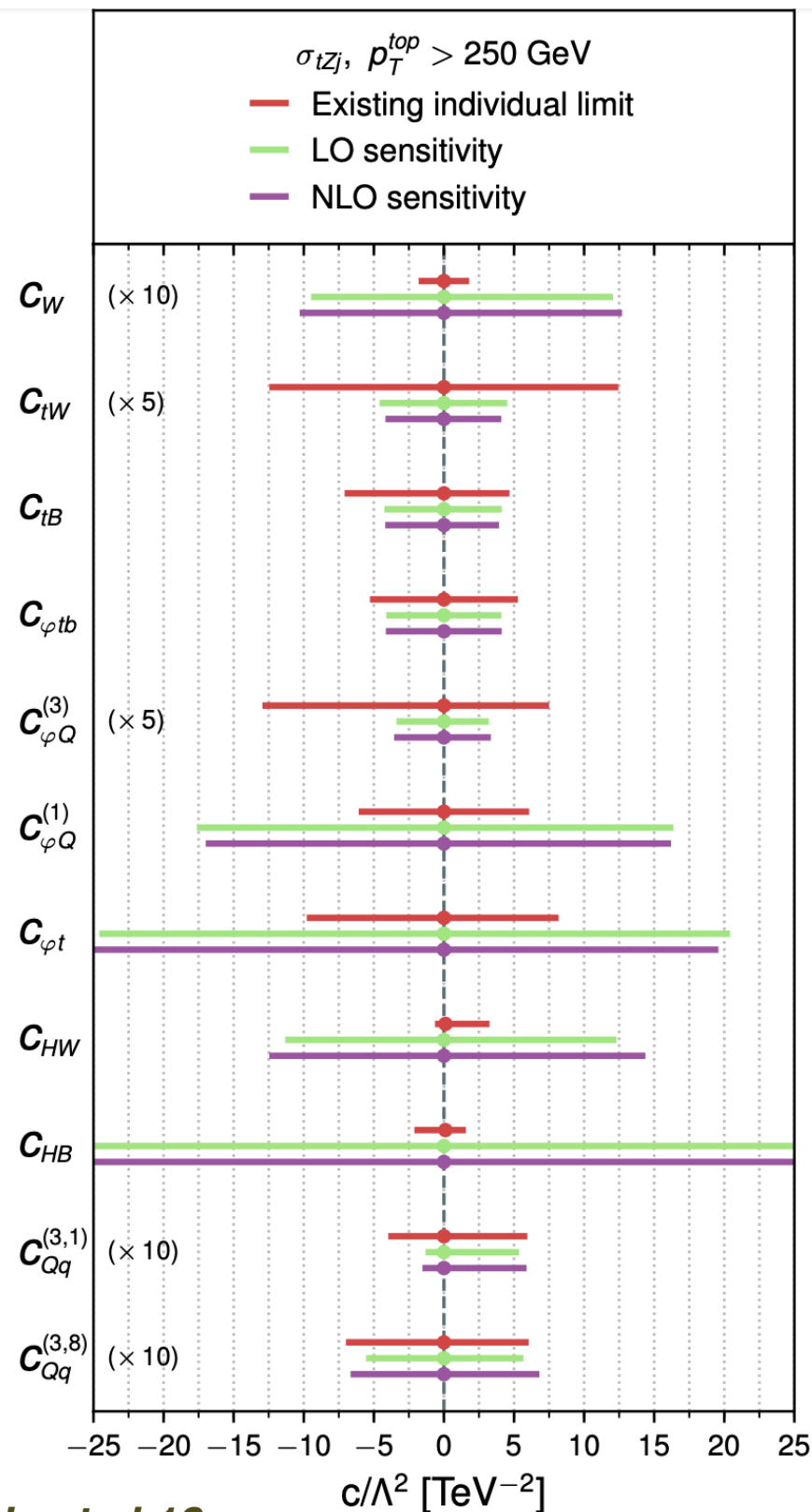


📍 Varying all parameters simultaneously results in **looser bounds** than varying a few parameters at a time due to degeneracies in parameter space

TopFitter, Buckley et al, JHEP (15)

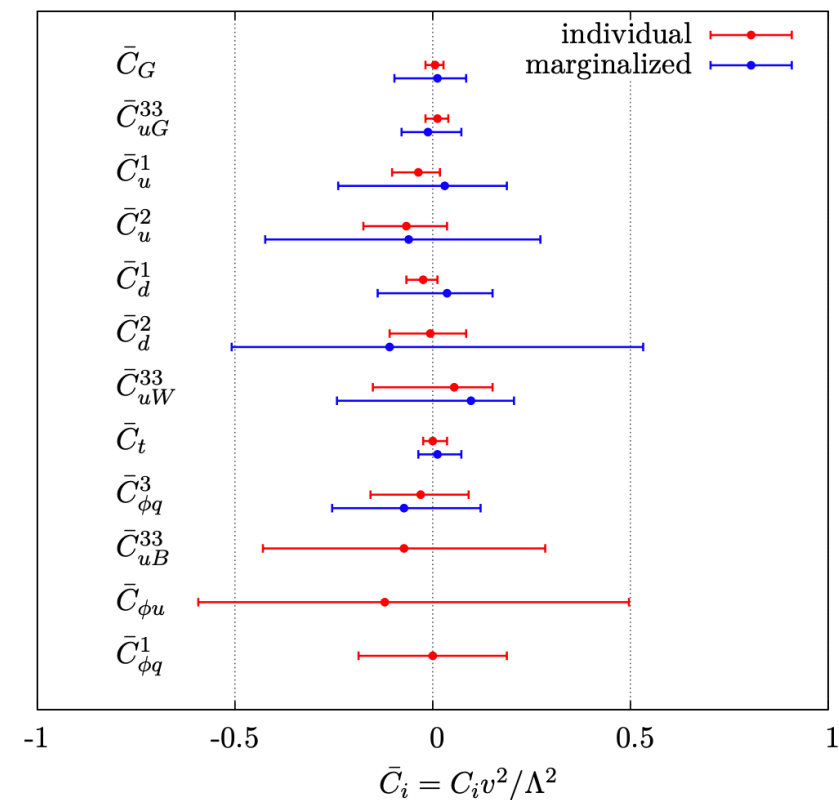
SMEFT constraints from LHC

Exploit **rarer processes** at LHC eg $t+Z+j$



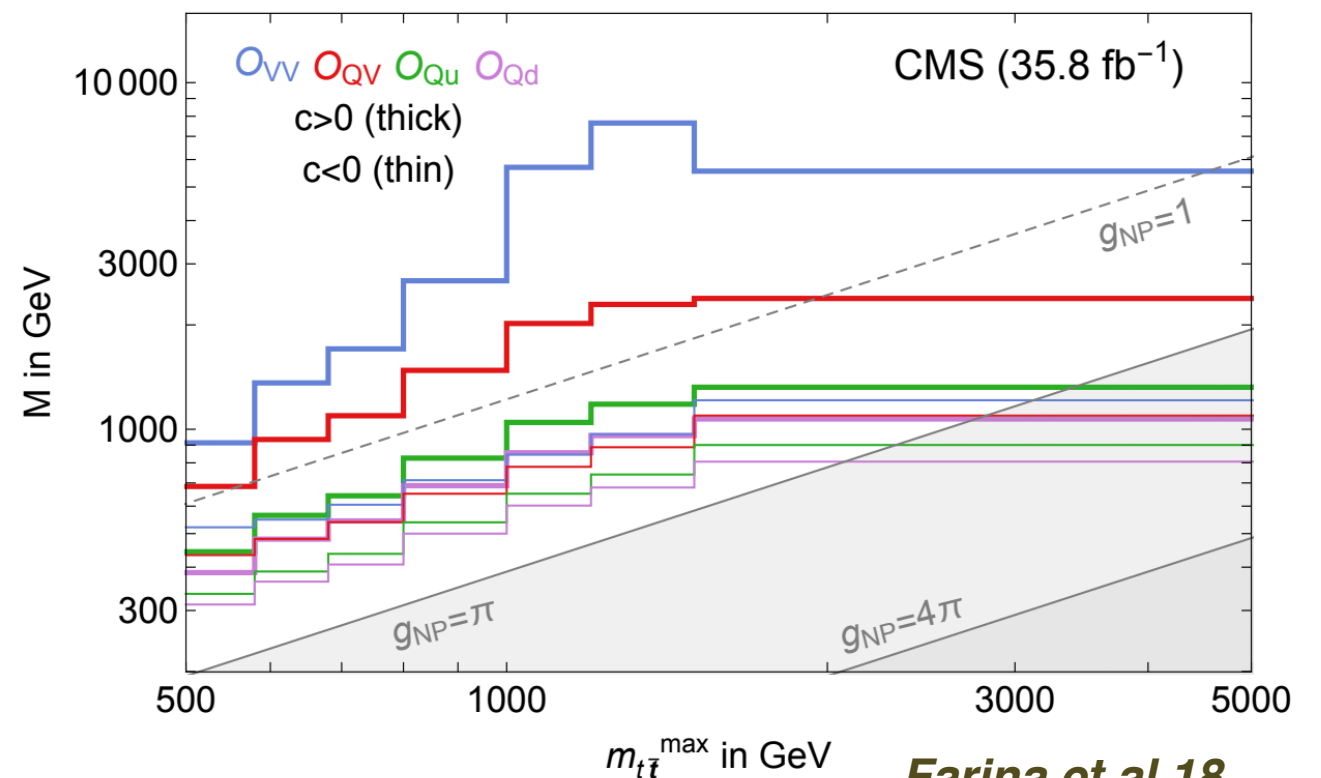
Degrande et al 18

Combine **different processes** in global fit



TopFitter 15

Enhance sensitivity from **high-energy $m_{t\bar{t}}$ tail**



Farina et al 18

Recipe for a global SMEFT analysis

Theory

(N)NLO QCD + NLO EW for SM xsecs
NLO QCD for SMEFT contributions
State-of-the-art Parton Distributions

Data

Higgs and gauge boson production
Top quark and jet production
Precision LEP, low energies, **flavour**

Global SMEFT fit

Bounds can be compared with
specific UV completions

New data incorporated without redoing fit

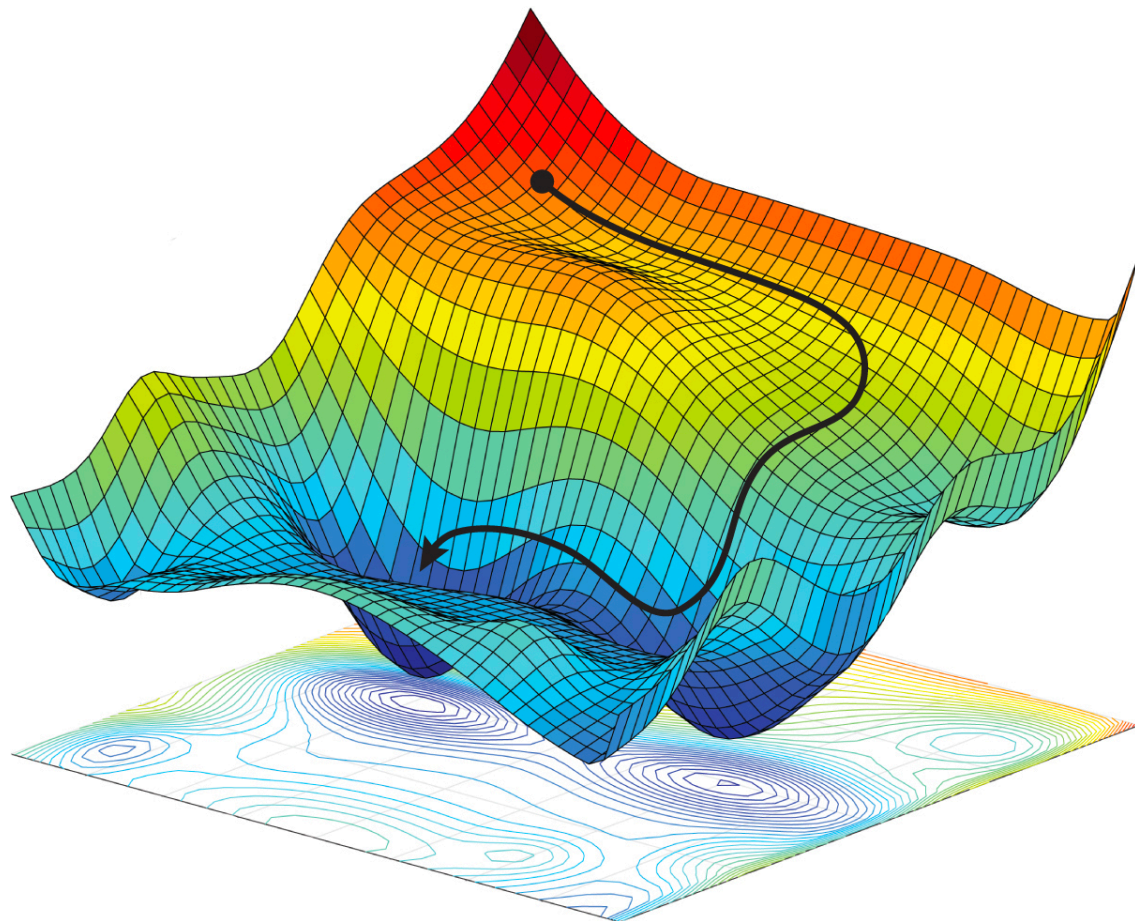
Delivery

Efficient exploration of **parameter space**
Faithful **uncertainty estimate**
Avoiding under- and over-fitting

Methodology

The optimisation conundrum

(Stochastic) Gradient Descent

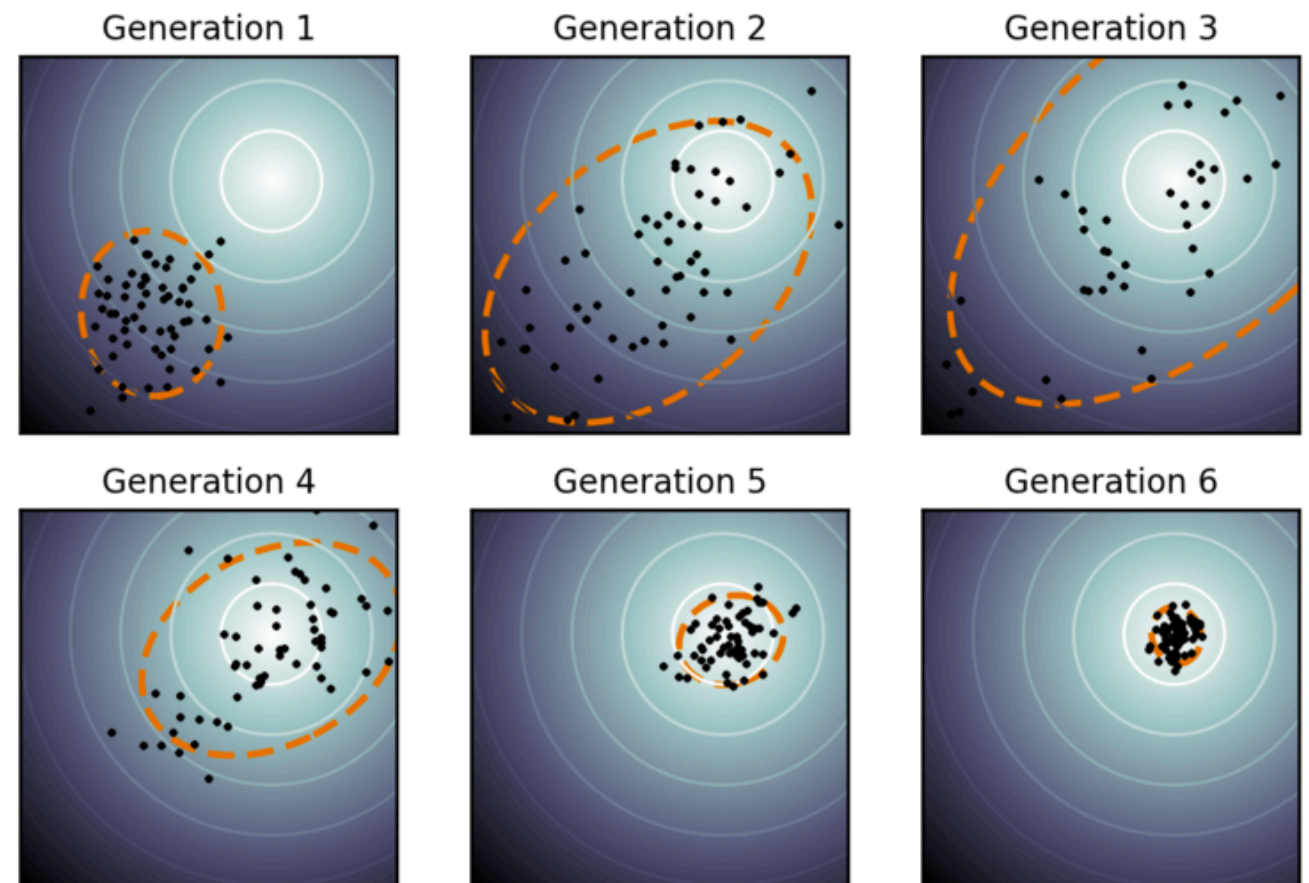


📌 **Deterministic algorithms:** follow the gradient of the cost function

📌 **Evolutionary algorithms:** act on population of solutions with random mutations and selection

- 📌 A challenge for any SMEFT global analysis is the efficient exploration of the **huge parameter space**
- 📌 Several pitfalls to be avoided: under-fitting, over-fitting, **local minima**, saddle points,

Genetic Algorithms



The optimisation conundrum

<https://www.youtube.com/watch?v=RiWc0ZDSTyY>

The SMEFiT framework

A Monte Carlo global analysis of the Standard Model Effective Field Theory: the top quark sector,

*Nathan P. Hartland, Fabio Maltoni, Emanuele R. Nocera, Juan Rojo,
Emma Slade, Eleni Vryonidou, Cen Zhang, arXiv:1901.05965, JHEP in press*

The SMEFiT method

- Generate a large sample of **Monte Carlo replicas** to construct the **probability distribution** in the space of experimental data

$$\mathcal{O}_i^{(\text{art})}(k) = S_{i,N}^{(k)} \mathcal{O}_i^{(\text{exp})} \left(1 + \sum_{\alpha=1}^{N_{\text{sys}}} r_{i,\alpha}^{(k)} \sigma_{i,c}^{(\text{sys})} + r_i^{(k)} \sigma_i^{(\text{stat})} \right), \quad k = 1, \dots, N_{\text{rep}}$$

*cross-section for
k-th replica*

*central value
(data)*

*correlated systematic
uncertainties*

*statistical
uncertainties*

MC replicas

The SMEFiT method

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- Construct theory calculations where the SM is **extended by SMEFT corrections**

to be determined from the data

$$\sigma_i^{\text{th}}(\{c_n\}) = \sigma_{\text{SM},i} + \sum_{n=1}^{N_{\text{op}}} \tilde{\sigma}_{i,n} \frac{c_n}{\Lambda^2} + \sum_{n,m=1}^{N_{\text{op}}} \tilde{\sigma}_{i,nm} \frac{c_n c_m}{\Lambda^4}, \quad i = 1 \dots, N_{\text{dat}}$$

*SM: compute
at (N)NLO QCD*

*SMEFT: compute at
(N)LO QCD with aMC@NLO*

The SMEFiT method

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- Determine the SMEFT coefficients **replica-by-replica** by minimising a cost function

$$E(\{c_l^{(k)}\}) \equiv \frac{1}{N_{\text{dat}}} \sum_{i,j=1}^{N_{\text{dat}}} \left(\mathcal{O}_i^{(\text{th})}(\{c_n^{(k)}\}) - \mathcal{O}_i^{(\text{art})}(k) \right) (\text{cov}^{-1})_{ij} \left(\mathcal{O}_j^{(\text{th})}(\{c_n^{(k)}\}) - \mathcal{O}_j^{(\text{art})}(k) \right)$$

The SMEFiT method

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📌 The covariance matrix includes **all sources of experimental errors** + some theory errors

t_0 prescription

$$(\text{cov}_{t_0})_{ij}^{(\text{exp})} \equiv \left(\sigma_i^{(\text{stat})} \right)^2 \delta_{ij} + \left(\sum_{\alpha=1}^{N_{\text{sys}}} \sigma_{i,\alpha}^{(\text{sys})} \sigma_{j,\alpha}^{(\text{sys})} \mathcal{O}_i^{(\text{exp})} \mathcal{O}_j^{(\text{exp})} + \sum_{\beta=1}^{N_{\text{norm}}} \sigma_{i,\beta}^{(\text{norm})} \sigma_{j,\beta}^{(\text{norm})} \mathcal{O}_i^{(\text{th},0)} \mathcal{O}_j^{(\text{th},0)} \right)$$

$$\text{cov}_{ij} = \text{cov}_{ij}^{(\text{exp})} + \text{cov}_{ij}^{(\text{th})}$$

th uncertainties: PDFs

can be extended to MHOUs

$$\text{cov}_{ij}^{(\text{th})} = \left\langle \mathcal{O}_i^{(\text{th})(\text{r})} \mathcal{O}_j^{(\text{th})(\text{r})} \right\rangle_{\text{rep}} - \left\langle \mathcal{O}_i^{(\text{th})(\text{r})} \right\rangle_{\text{rep}} \left\langle \mathcal{O}_j^{(\text{th})(\text{r})} \right\rangle_{\text{rep}},$$

The SMEFiT method

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$$E(\{c_l^{(k)}\}) \equiv \frac{1}{N_{\text{dat}}} \sum_{i,j=1}^{N_{\text{dat}}} \left(\mathcal{O}_i^{(\text{th})}(\{c_n^{(k)}\}) - \mathcal{O}_i^{(\text{art})(k)} \right) (\text{cov}^{-1})_{ij} \left(\mathcal{O}_j^{(\text{th})}(\{c_n^{(k)}\}) - \mathcal{O}_j^{(\text{art})(k)} \right)$$

- 📌 The covariance matrix includes **all sources of experimental errors** + some theory errors

$$\text{cov}_{ij} = \text{cov}_{ij}^{(\text{exp})} + \text{cov}_{ij}^{(\text{th})}$$

- 📌 The ensemble of coefficients $\{c_l^{(k)}\}$ then provides a sampling of the **probability density** in the **SMEFT parameter space**

$$\langle c_l \rangle \equiv \frac{1}{N_{\text{rep}}} \sum_{k=1}^{N_{\text{rep}}} c_l^{(k)} \quad \rho(c_i, c_j) = \frac{\frac{1}{N_{\text{rep}}} \sum_{k=1}^{N_{\text{rep}}} c_i^{(k)} c_j^{(k)} - \langle c_i \rangle \langle c_j \rangle}{\delta c_i \delta c_j}.$$

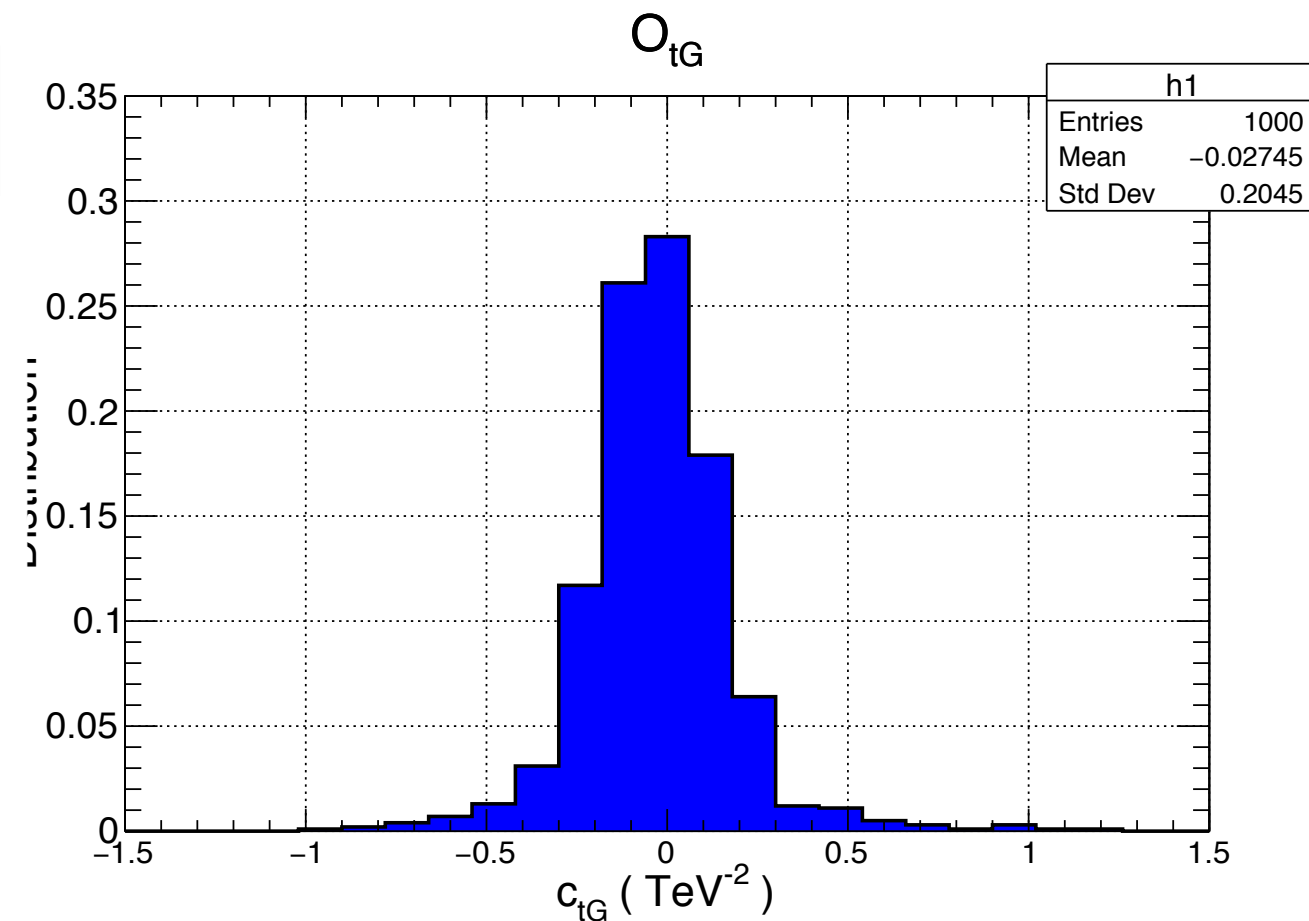
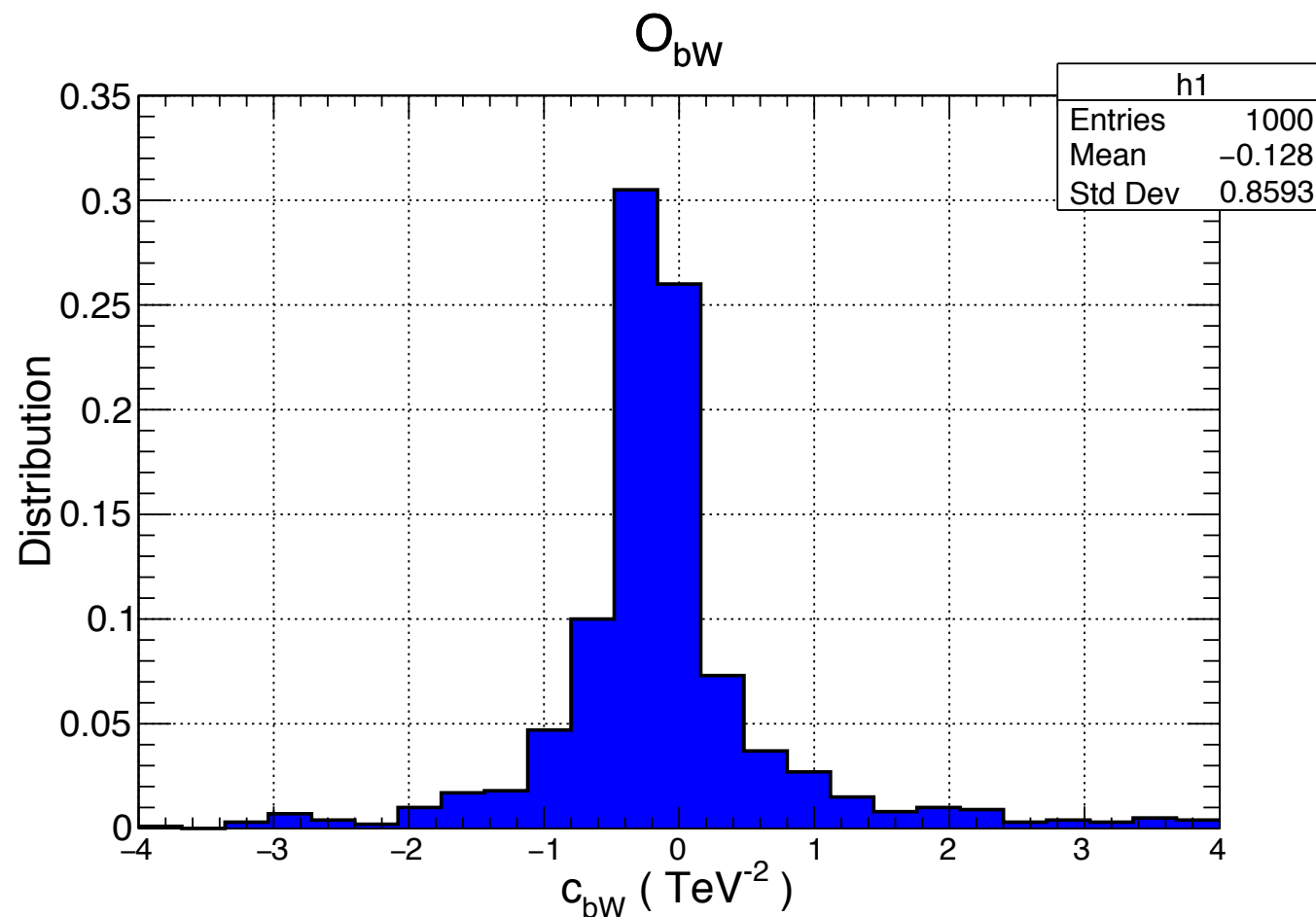
Sampling the SMEFT probability distribution

📌 The output of SMEFiT is a sampling of the **probability distribution** in the SMEFT space

$$\left\{ c_n^{(k)} \right\}, \quad n = 1 \dots, N_{\text{op}}, \quad k = 1 \dots, N_{\text{rep}}$$

📌 Used to **evaluate statistical estimators** such as variances, correlations, higher moments, ...

📌 Distributions are **reasonably Gaussian** for well-constrained degrees of freedom



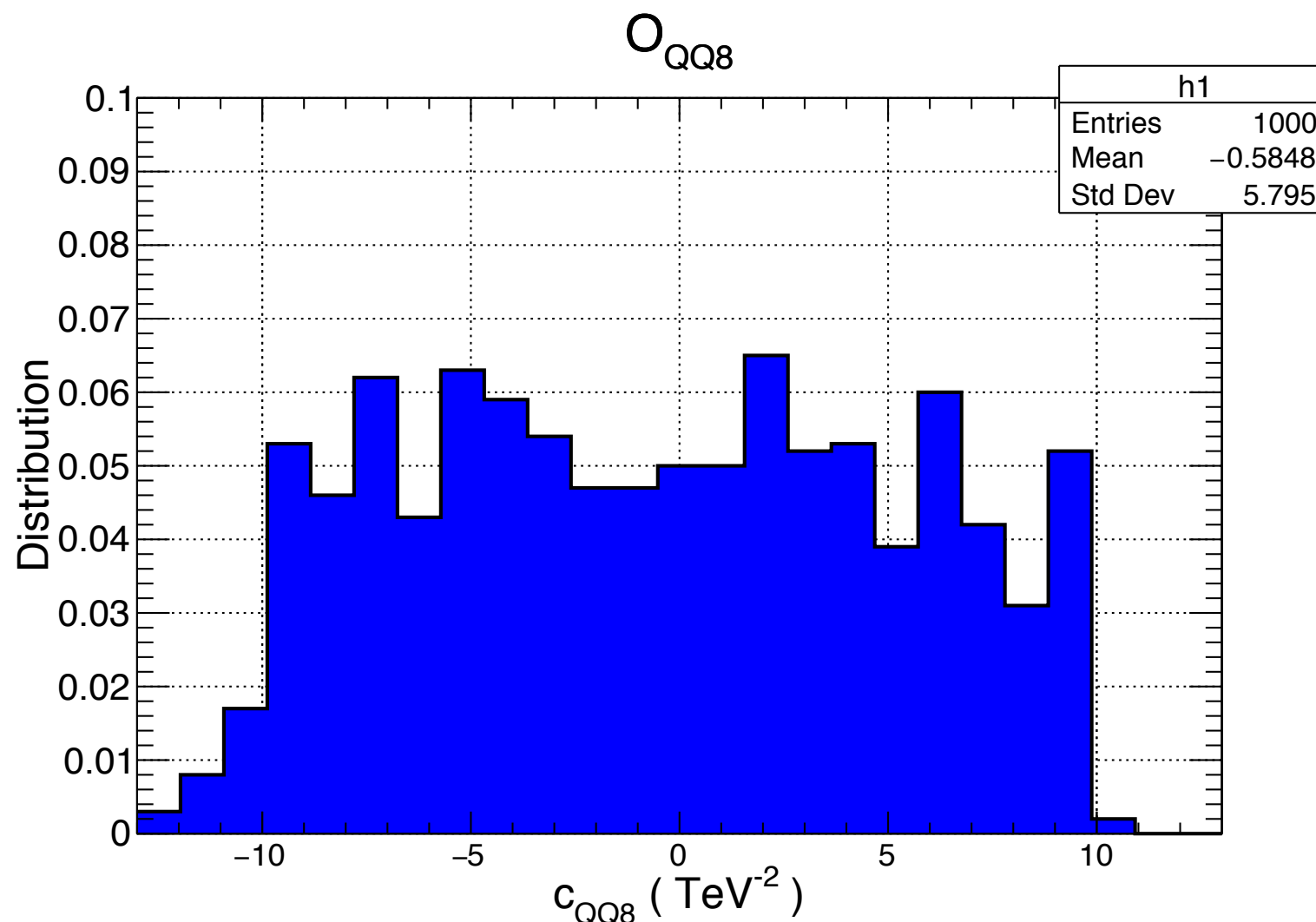
Sampling the SMEFT probability distribution

📌 The output of SMEFiT is a sampling of the **probability distribution** in the SMEFT space

$$\left\{ c_n^{(k)} \right\}, \quad n = 1 \dots, N_{\text{op}}, \quad k = 1 \dots, N_{\text{rep}}$$

📌 Used to **evaluate statistical estimators** such as variances, correlations, higher moments, ...

📌 but much less so for **under-constrained** or **redundant** operators

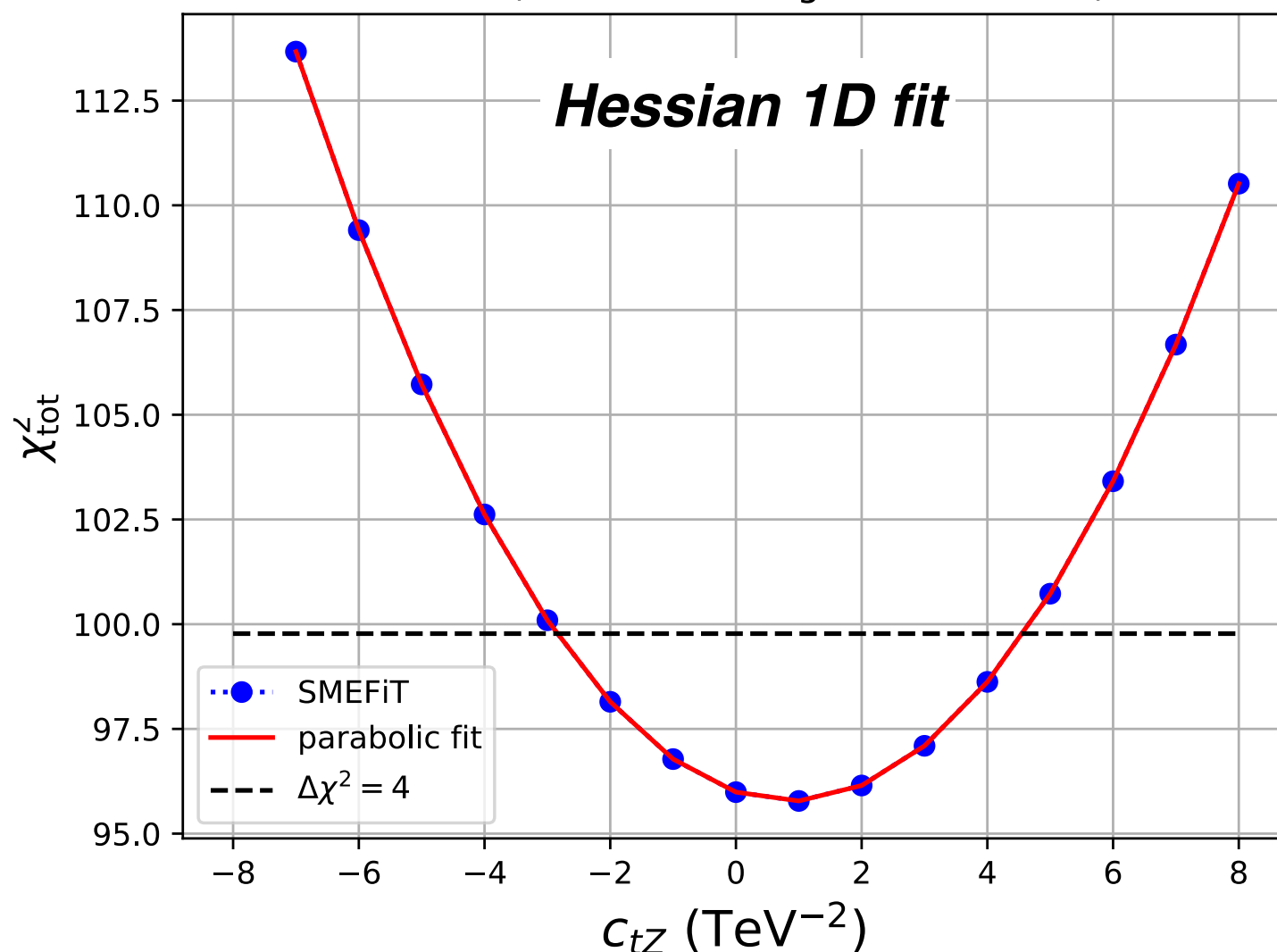


The SMEFiT method

- Uncertainties on the SMEFT degrees of freedom evaluated from **variance of MC sample**

$$(\delta c_n)^2 = \frac{1}{N_{\text{rep}}} \sum_{k=1}^{N_{\text{rep}}} \left(c_n^{(k)} \right)^2 - \langle c_n \rangle^2$$

SMEFiT (baseline settings, individual fit)

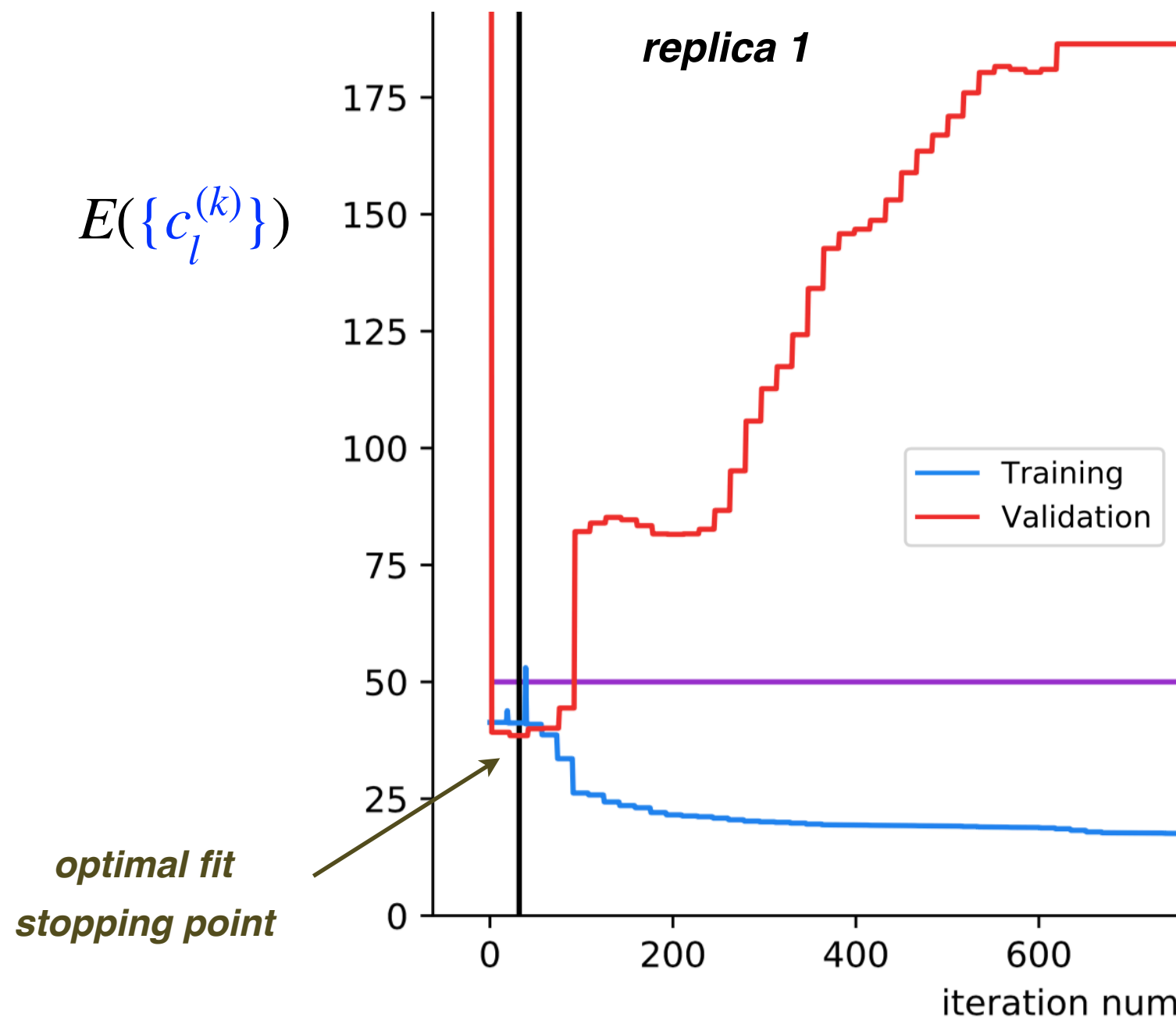


- For single-parameter fits, **Monte Carlo results** benchmarked with **Hessian method**, finding good agreement

- The Hessian method **numerically less stable** as dimensionality of parameter space increases

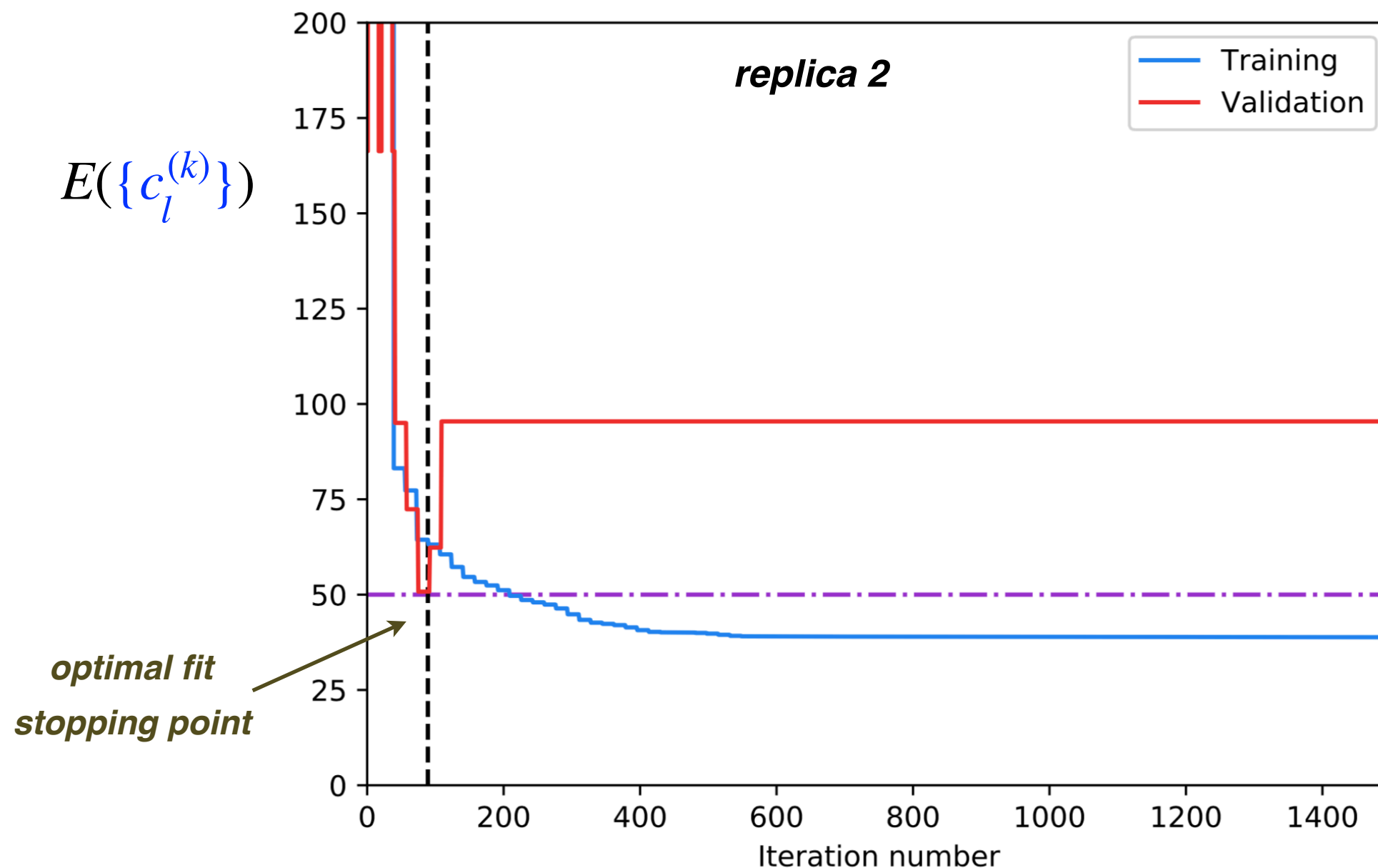
The SMEFiT method

- Since in general there will be **unconstrained/degenerate directions** in the parameter space, it is crucial to avoid overfitting (that is, fitting statistical fluctuations)
- Achieved by the **cross-validation look-back validation stopping** method



The SMEFiT method

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SMEFiT code structure

Stand-alone **Python code**, which exploits functionalities of the **NNPDF framework**

NNPDF code

- 📌 **Experimental data** and covariance matrices
- 📌 **NLO APPLgrids + NNLO** C-factors (for processes used in PDF fit)

aMC@NLO

- 📌 **NLO QCD** (benchmark)
- 📌 **LO, NLO SMEFT**
- 📌 Both $\mathcal{O}(\Lambda^{-2})$ and $\mathcal{O}(\Lambda^{-4})$ from **$d=6$ operators**

MCFM

- 📌 **NLO QCD** (consistent choice of PDFs)
- 📌 Cross-checks of **aMC@NLO**

Python analysis code

- 📌 Assemble **theory predictions** for generic SMEFT Wilson coefficients
- 📌 **Optimisation** with Sequential Quadratic Programming (**SciPy**)
- 📌 Look-back **cross-validation stopping**
- 📌 **Monte Carlo replicas** for uncertainty propagation

SMEFiT:

the top quark case

A Monte Carlo global analysis of the Standard Model Effective Field Theory: the top quark sector,

Nathan P. Hartland, Fabio Maltoni, Emanuele R. Nocera, Juan Rojo,

Emma Slade, Eleni Vryonidou, Cen Zhang, arXiv:1901.05965, JHEP in press

Operator basis

🎧 We follow the same flavour assumptions as in the **LHC Top WG note**

🎧 Minimal Flavour Violation (MFV), diagonal CKM, zero Yukawas for first two quark gens, CP conservation assumed

🎧 Include those SMEFT dimension-6 operators of Warsaw basis with **at least one top quark**

🎧 The fit includes a total of **34 independent degrees of freedom**

🎧 Include both **interference** and **quadratic contributions** from these operators

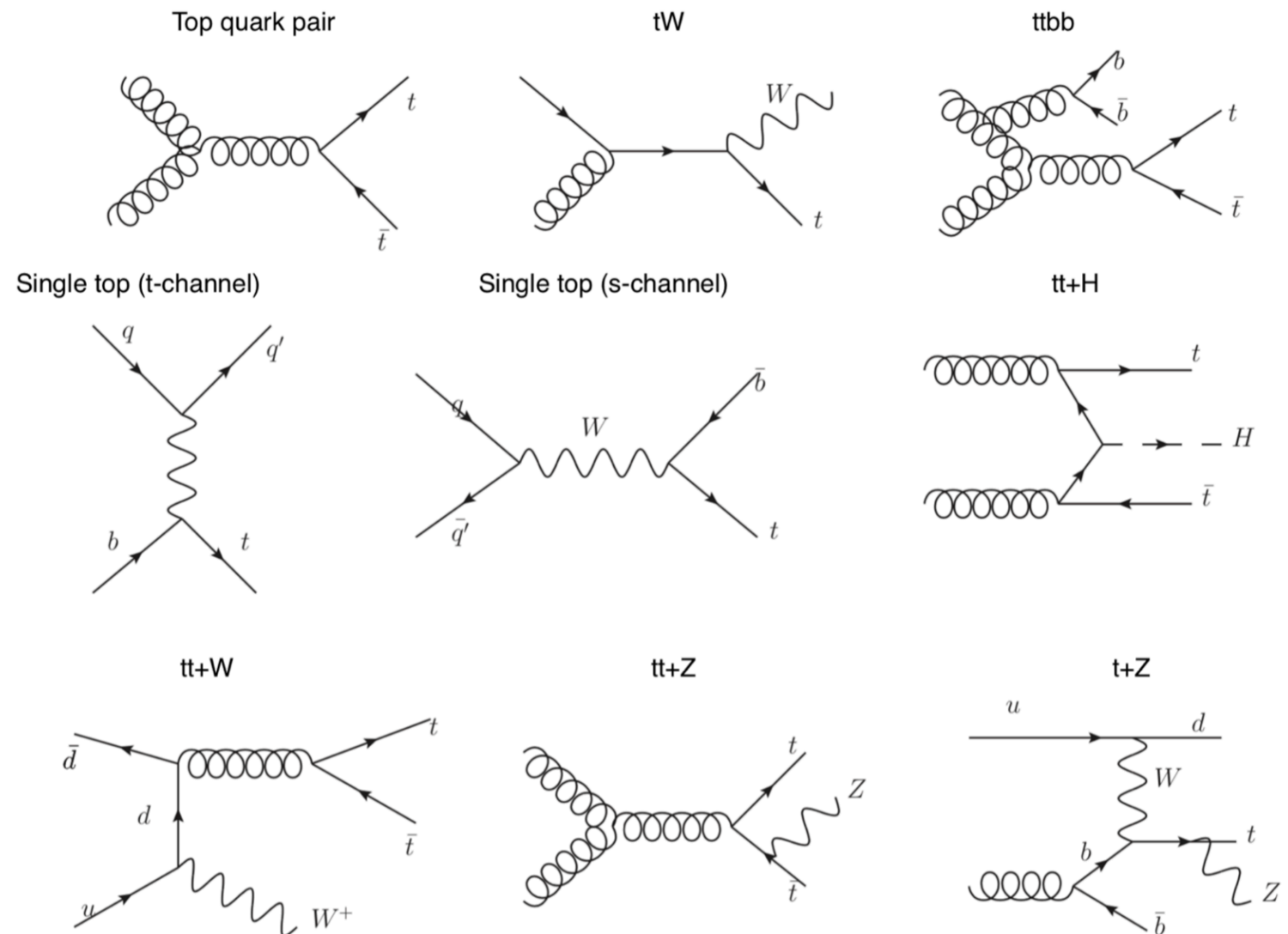
Class	Notation	Degree of Freedom	Operator Definition
4-heavy <i>QQQQ</i>	0QQ1	c_{QQ}^1	$2C_{qq}^{1(3333)} - \frac{2}{3}C_{qq}^{3(3333)}$
	0QQ8	c_{QQ}^8	$8C_{qq}^{3(3333)}$
	0Qt1	c_{Qt}^1	$C_{qu}^{1(3333)}$
	0Qt8	c_{Qt}^8	$C_{qu}^{8(3333)}$
	0Qb1	c_{Qb}^1	$C_{qd}^{1(3333)}$
	0Qb8	c_{Qb}^8	$C_{qd}^{8(3333)}$
	0tt1	c_{tt}^1	$C_{uu}^{(3333)}$
	0tb1	c_{tb}^1	$C_{ud}^{1(3333)}$
	0tb8	c_{tb}^8	$C_{ud}^{8(3333)}$
	0QtQb1	c_{QtQb}^1	$C_{quqd}^{1(3333)}$
	0QtQb8	c_{QtQb}^8	$C_{quqd}^{8(3333)}$
2-heavy-2-light <i>QQqq</i>	081qq	$c_{Qq}^{1,8}$	$C_{qq}^{1(i33i)} + 3C_{qq}^{3(i33i)}$
	011qq	$c_{Qq}^{1,1}$	$C_{qq}^{1(ii33)} + \frac{1}{6}C_{qq}^{1(i33i)} + \frac{1}{2}C_{qq}^{3(i33i)}$
	083qq	$c_{Qq}^{3,8}$	$C_{qq}^{1(i33i)} - C_{qq}^{3(i33i)}$
	013qq	$c_{Qq}^{3,1}$	$C_{qq}^{3(ii33)} + \frac{1}{6}(C_{qq}^{1(i33i)} - C_{qq}^{3(i33i)})$
	08qt	c_{tq}^8	$C_{qu}^{8(ii33)}$
	01qt	c_{tq}^1	$C_{qu}^{1(ii33)}$
	08ut	c_{tu}^8	$2C_{uu}^{(i33i)}$
	01ut	c_{tu}^1	$C_{uu}^{(ii33)} + \frac{1}{3}C_{uu}^{(i33i)}$
	08qu	c_{Qu}^8	$C_{qu}^{8(33ii)}$
	01qu	c_{Qu}^1	$C_{qu}^{1(33ii)}$
	08dt	c_{td}^8	$C_{ud}^{8(33ii)}$
	01dt	c_{td}^1	$C_{ud}^{1(33ii)}$
	08qd	c_{Qd}^8	$C_{qd}^{8(33ii)}$
	01qd	c_{Qd}^1	$C_{qd}^{1(33ii)}$
2-heavy + V/h <i>QQ + V, G, φ</i>	0tG	c_{tG}	$\text{Re}\{C_{uG}^{(33)}\}$
	0tW	c_{tW}	$\text{Re}\{C_{uW}^{(33)}\}$
	0bW	c_{bW}	$\text{Re}\{C_{dW}^{(33)}\}$
	0tZ	c_{tZ}	$\text{Re}\{-s_W C_{uB}^{(33)} + c_W C_{uW}^{(33)}\}$
	0ff	$c_{\varphi tb}$	$\text{Re}\{C_{\varphi ud}^{(33)}\}$
	0fq3	$c_{\varphi Q}^3$	$C_{\varphi q}^{3(33)}$
	0pQM	$c_{\varphi Q}^-$	$C_{\varphi q}^{1(33)} - C_{\varphi q}^{3(33)}$
	0pt	$c_{\varphi t}$	$C_{\varphi u}^{(33)}$
	0tp	$c_{t\varphi}$	$\text{Re}\{C_{u\varphi}^{(33)}\}$

The top quark sector of the SMEFT

A large number of different dimension-6 SMEFT operators modify **top production at LHC**

$$\sigma_i^{\text{th}}(\{c_n\}) = \sigma_{\text{SM},i} + \sum_{n=1}^{N_{\text{op}}} \tilde{\sigma}_{i,n} \frac{c_n}{\Lambda^2} + \sum_{n,m=1}^{N_{\text{op}}} \tilde{\sigma}_{i,nm} \frac{c_n c_m}{\Lambda^4}$$

Notation	Sensitivity at $\mathcal{O}(\Lambda^{-2})$ ($\mathcal{O}(\Lambda^{-4})$)								
	$t\bar{t}$	single-top	tW	tZ	$t\bar{t}W$	$t\bar{t}Z$	$t\bar{t}H$	$t\bar{t}t\bar{t}$	$t\bar{t}b\bar{b}$
0QQ1								✓	✓
0QQ8								✓	✓
0Qt1								✓	✓
0Qt8								✓	✓
0Qb1								(✓)	✓
0Qb8								(✓)	✓
0tt1								✓	✓
0tb1								(✓)	✓
0tb8								✓	✓
0QtQb1									
0QtQb8									
081qq	✓				✓	✓	✓	✓	✓
011qq	✓				(✓)	(✓)	(✓)	✓	✓
083qq	✓	✓		(✓)	✓	✓	✓	✓	✓
013qq	✓	✓		✓	(✓)	(✓)	(✓)	✓	✓
08qt	✓				✓	✓	✓	✓	✓
01qt	✓				(✓)	(✓)	(✓)	✓	✓
08ut	✓					✓	✓	✓	✓
01ut	✓					(✓)	(✓)	✓	✓
08qu	✓					✓	✓	✓	✓
01qu	✓					(✓)	(✓)	✓	✓
08dt	✓					✓	✓	✓	✓
01dt	✓					(✓)	(✓)	✓	✓
08qd	✓					✓	✓	✓	✓
01qd	✓					(✓)	(✓)	✓	✓
0tG	✓				✓	✓	✓	✓	✓
0tW		✓	✓	✓					
0bW		(✓)	(✓)						
0tZ				✓		✓			
0ff		(✓)	(✓)	(✓)					
0fq3		✓	✓	✓		✓			
0pQM				✓		✓			
0pt				✓		✓			
0tp							✓		

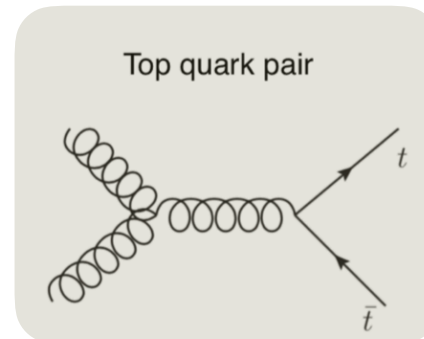


The top quark sector of the SMEFT

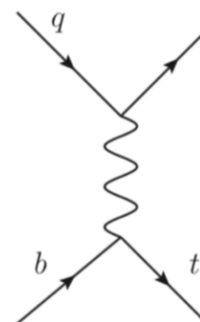
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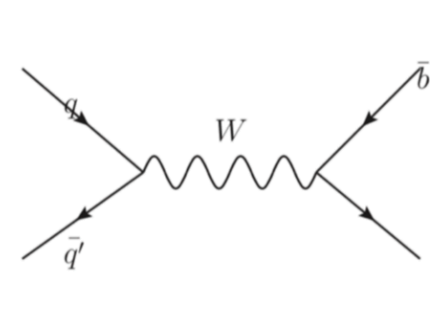
Notation	Sensitivity at $\mathcal{O}(\Lambda^{-2})$ ($\mathcal{O}(\Lambda^{-4})$)								
	$t\bar{t}$	single-top	tW	tZ	$t\bar{t}W$	$t\bar{t}Z$	$t\bar{t}H$	$t\bar{t}t\bar{t}$	$t\bar{t}b\bar{b}$
0QQ1								✓	✓
0QQ8								✓	✓
0Qt1								✓	✓
0Qt8								✓	✓
0Qb1								(✓)	✓
0Qb8								(✓)	✓
0tt1								✓	✓
0tb1								(✓)	✓
0tb8								✓	✓
0QtQb1									
0QtQb8									
081qq	✓				✓	✓	✓	✓	✓
011qq	✓				(✓)	(✓)	(✓)	✓	✓
083qq	✓	✓		(✓)	✓	✓	✓	✓	✓
013qq	✓	✓		✓	(✓)	(✓)	(✓)	✓	✓
08qt	✓				✓	✓	✓	✓	✓
01qt	✓				(✓)	(✓)	(✓)	✓	✓
08ut	✓					✓	✓	✓	✓
01ut	✓					(✓)	(✓)	✓	✓
08qu	✓					✓	✓	✓	✓
01qu	✓					(✓)	(✓)	✓	✓
08dt	✓					✓	✓	✓	✓
01dt	✓					(✓)	(✓)	✓	✓
08qd	✓					✓	✓	✓	✓
01qd	✓					(✓)	(✓)	✓	✓
0tG	✓				✓	✓	✓	✓	✓
0tW		✓	✓	✓					
0bW		(✓)	(✓)						
0tZ				✓		✓			
0ff		(✓)	(✓)	(✓)					
0fq3		✓	✓	✓		✓			
0pQM				✓		✓			
0pt				✓		✓			
0tp							✓		



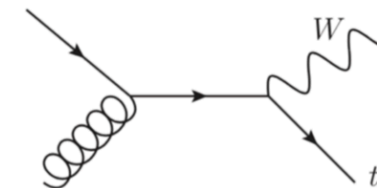
Single top (t-channel)



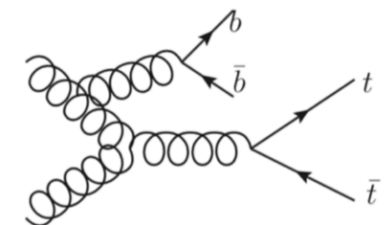
Single top (s-channel)



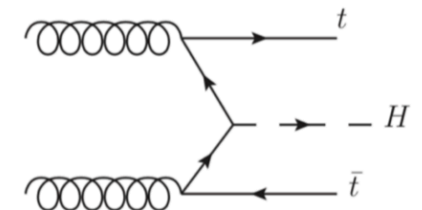
tW



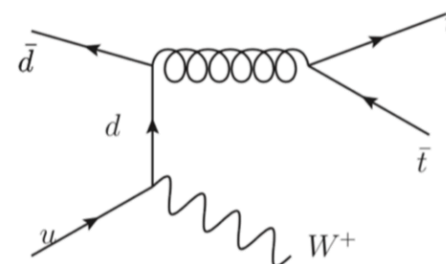
ttbb



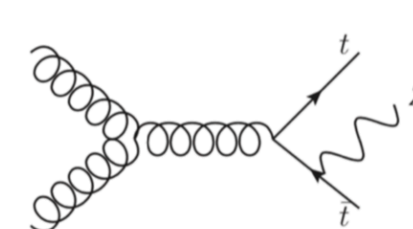
tt+H



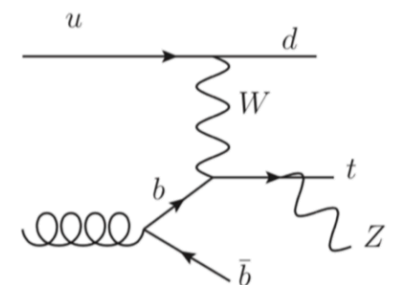
tt+W



tt+Z



t+Z

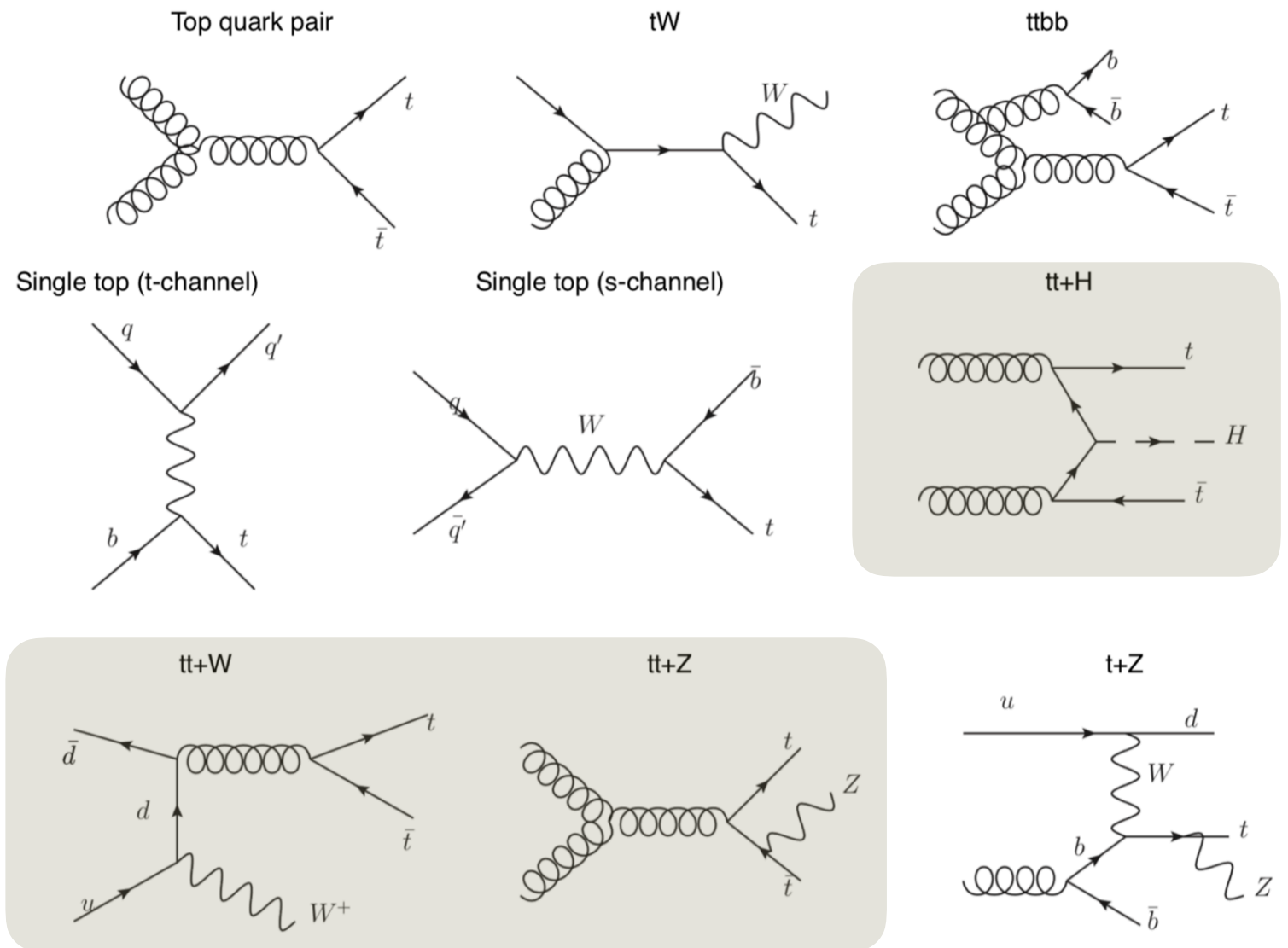


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0QQ1								✓	✓
0QQ8								✓	✓
0Qt1								✓	✓
0Qt8								✓	✓
0Qb1								(✓)	✓
0Qb8								(✓)	✓
0tt1								✓	✓
0tb1								(✓)	✓
0tb8								✓	✓
0QtQb1									
0QtQb8									
081qq	✓				✓	✓	✓	✓	✓
011qq	✓				(✓)	(✓)	(✓)	✓	✓
083qq	✓	✓		(✓)	✓	✓	✓	✓	✓
013qq	✓	✓		✓	(✓)	(✓)	(✓)	✓	✓
08qt	✓				✓	✓	✓	✓	✓
01qt	✓				(✓)	(✓)	(✓)	✓	✓
08ut	✓					✓	✓	✓	✓
01ut	✓					(✓)	(✓)	✓	✓
08qu	✓					✓	✓	✓	✓
01qu	✓					(✓)	(✓)	✓	✓
08dt	✓					✓	✓	✓	✓
01dt	✓					(✓)	(✓)	✓	✓
08qd	✓					✓	✓	✓	✓
01qd	✓					(✓)	(✓)	✓	✓
0tG	✓				✓	✓	✓	✓	✓
0tW		✓	✓	✓					
0bW		(✓)	(✓)						
0tZ				✓		✓			
0ff		(✓)	(✓)	(✓)					
0fq3		✓	✓	✓		✓			
0pQM				✓		✓			
0pt				✓		✓			
0tp						✓			



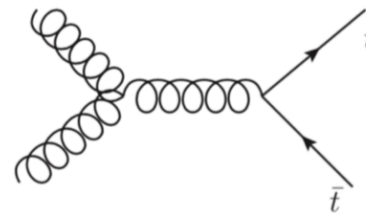
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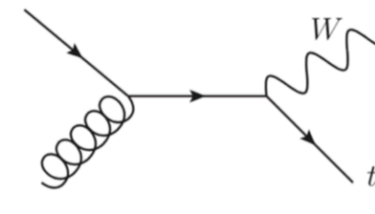
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0QQ1								✓	✓
0QQ8								✓	✓
0Qt1								✓	✓
0Qt8								✓	✓
0Qb1								(✓)	✓
0Qb8								(✓)	✓
0tt1								✓	✓
0tb1								(✓)	✓
0tb8								✓	✓
0QtQb1									
0QtQb8									
081qq	✓				✓	✓	✓	✓	✓
011qq	✓				(✓)	(✓)	(✓)	✓	✓
083qq	✓	✓		(✓)	✓	✓	✓	✓	✓
013qq	✓	✓		✓	(✓)	(✓)	(✓)	✓	✓
08qt	✓				✓	✓	✓	✓	✓
01qt	✓				(✓)	(✓)	(✓)	✓	✓
08ut	✓					✓	✓	✓	✓
01ut	✓					(✓)	(✓)	✓	✓
08qu	✓					✓	✓	✓	✓
01qu	✓					(✓)	(✓)	✓	✓
08dt	✓					✓	✓	✓	✓
01dt	✓					(✓)	(✓)	✓	✓
08qd	✓					✓	✓	✓	✓
01qd	✓					(✓)	(✓)	✓	✓
0tG	✓				✓	✓	✓	✓	✓
0tW		✓	✓	✓					
0bW		(✓)	(✓)						
0tZ				✓		✓			
0ff		(✓)	(✓)	(✓)					
0fq3		✓	✓	✓		✓			
0pQM				✓		✓			
0pt				✓		✓			
0tp						✓			

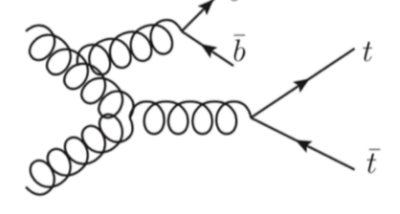
Top quark pair



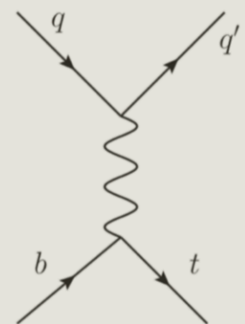
tW



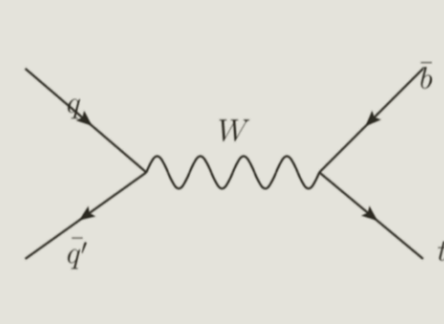
ttbb



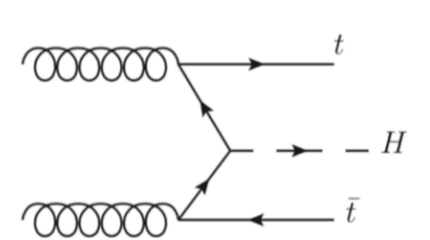
Single top (t-channel)



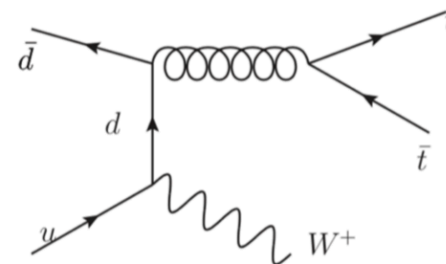
Single top (s-channel)



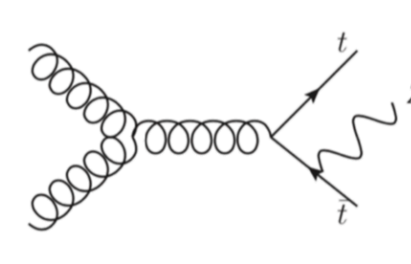
tt+H



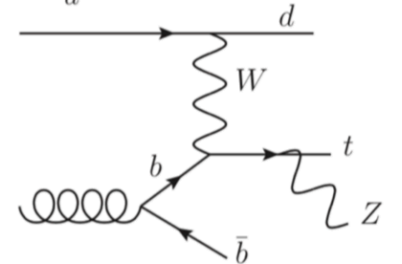
tt+W



tt+Z



t+Z



Input dataset (I)

Process	Dataset	\sqrt{s}	Info	Observables	N_{dat}	Ref
$t\bar{t}$	ATLAS_tt_8TeV_1jets	8 TeV	lepton+jets	$d\sigma/d y_t $, $d\sigma/dp_t^T$, $d\sigma/dm_{t\bar{t}}$, $d\sigma/d y_{t\bar{t}} $	5, 8, 7, 5	[77]
$t\bar{t}$	CMS_tt_8TeV_1jets	8 TeV	lepton+jets	$d\sigma/dy_t$, $d\sigma/dp_t^T$, $d\sigma/dm_{t\bar{t}}$, $d\sigma/dy_{t\bar{t}}$	10, 8, 7, 10	[78]
$t\bar{t}$	CMS_tt2D_8TeV_dilep	8 TeV	dileptons	$d^2\sigma/dy_t dp_t^T$, $d^2\sigma/dy_t dm_{t\bar{t}}$, $d^2\sigma/dp_{t\bar{t}}^T dm_{t\bar{t}}$, $d^2\sigma/dy_{t\bar{t}} dm_{t\bar{t}}$	16, 16, 16, 16	[79]
$t\bar{t}$	CMS_tt_13TeV_1jets	13 TeV	lepton+jets	$d\sigma/d y_t $, $d\sigma/dp_t^T$, $d\sigma/dm_{t\bar{t}}$, $d\sigma/d y_{t\bar{t}} $	7, 9, 8, 6	[83]
$t\bar{t}$	CMS_tt_13TeV_1jets2	13 TeV	lepton+jets	$d\sigma/d y_t $, $d\sigma/dp_t^T$, $d\sigma/dm_{t\bar{t}}$, $d\sigma/d y_{t\bar{t}} $	11, 12, 10, 10	[85]
$t\bar{t}$	CMS_tt_13TeV_dilep	13 TeV	dileptons	$d\sigma/dy_t$, $d\sigma/dp_t^T$, $d\sigma/dm_{t\bar{t}}$, $d\sigma/dy_{t\bar{t}}$	8, 6, 6, 8	[86]
$t\bar{t}$	ATLASCMS_AcMtt_8TeV	8 TeV	Asymm comb	$A_C(m_{t\bar{t}})$, Eq. (3.1)	6	[80]
$t\bar{t}$	ATLAS_WhelF_8TeV	8 TeV	W helicity fract	F_0, F_L, F_R	3	[81]
$t\bar{t}$	CMS_WhelF_8TeV	8 TeV	W helicity fract	F_0, F_L, F_R	3	[82]

Input dataset (II)

Process	Dataset	\sqrt{s}	Info	Observables	N_{dat}	Ref
Single t	CMS_t_tch_8TeV_inc	8 TeV	t -channel	$\sigma_{\text{tot}}(t), \sigma_{\text{tot}}(\bar{t})$ (R_t)	2 (1)	[95]
Single t	CMS_t_sch_8TeV	8 TeV	s -channel	$\sigma_{\text{tot}}(t + \bar{t})$	1	[96]
Single t	ATLAS_t_sch_8TeV	8 TeV	s -channel	$\sigma_{\text{tot}}(t + \bar{t})$	1	[97]
Single t	ATLAS_t_tch_8TeV	8 TeV	t -channel	$d\sigma(tq)/dp_T^t, d\sigma(\bar{t}q)/dp_T^{\bar{t}}$ $d\sigma(tq)/dy_t, d\sigma(\bar{t}q)/dy_t$	5, 4 4, 4	[98]
Single t	ATLAS_t_tch_13TeV	13 TeV	t -channel	$\sigma_{\text{tot}}(t), \sigma_{\text{tot}}(\bar{t})$ (R_t)	2 (1)	[99]
Single t	CMS_t_tch_13TeV_inc	13 TeV	t -channel	$\sigma_{\text{tot}}(t + \bar{t})$ (R_t)	1 (1)	[100]
Single t	CMS_t_tch_8TeV_dif	8 TeV	t -channel	$d\sigma/dp_T^{(t+\bar{t})},$ $d\sigma/d y^{(t+\bar{t})} $	6 6	[101]
Single t	CMS_t_tch_13TeV_dif	13 TeV	t -channel	$d\sigma/dp_T^{(t+\bar{t})},$ $d\sigma/d y^{(t+\bar{t})} $	4 4	[102]
tW	ATLAS_tW_inc_8TeV	8 TeV	inclusive	$\sigma_{\text{tot}}(tW)$	1	[103]
tW	CMS_tW_inc_8TeV	8 TeV	inclusive	$\sigma_{\text{tot}}(tW)$	1	[104]
tW	ATLAS_tW_inc_13TeV	13 TeV	inclusive	$\sigma_{\text{tot}}(tW)$	1	[105]
tW	CMS_tW_inc_13TeV	13 TeV	inclusive	$\sigma_{\text{tot}}(tW)$	1	[106]
tZ	CMS_tZ_inc_13TeV	13 TeV	inclusive	$\sigma_{\text{fid}}(Wbl^+l^-q)$	1	[107]
tZ	ATLAS_tZ_inc_13TeV	13 TeV	inclusive	$\sigma_{\text{tot}}(tZq)$	1	[108]

Input dataset (III)

Process	Dataset	\sqrt{s}	Info	Observables	N_{dat}	Ref
$t\bar{t}b\bar{b}$	CMS_ttbb_13TeV	13 TeV	total xsec	$\sigma_{\text{tot}}(t\bar{t}b\bar{b})$	1	[87]
$t\bar{t}t\bar{t}$	CMS_tttt_13TeV	13 TeV	total xsec	$\sigma_{\text{tot}}(t\bar{t}t\bar{t})$	1	[88]
$t\bar{t}Z$	CMS_ttZ_8_13TeV	8+13 TeV	total xsec	$\sigma_{\text{tot}}(t\bar{t}Z)$	2	[89, 90]
$t\bar{t}Z$	ATLAS_ttZ_8_13TeV	8+13 TeV	total xsec	$\sigma_{\text{tot}}(t\bar{t}Z)$	2	[91, 92]
$t\bar{t}W$	CMS_ttW_8_13TeV	8+13 TeV	total xsec	$\sigma_{\text{tot}}(t\bar{t}W)$	2	[89, 90]
$t\bar{t}W$	ATLAS_ttW_8_13TeV	8+13 TeV	total xsec	$\sigma_{\text{tot}}(t\bar{t}W)$	2	[91, 92]
$t\bar{t}H$	CMS_tth_13TeV	13 TeV	signal strength	$\mu_{t\bar{t}H}$	1	[93]
$t\bar{t}H$	ATLAS_tth_13TeV	13 TeV	total xsec	$\sigma_{\text{tot}}(t\bar{t}H)$	1	[94]

The fit includes more than **100 cross-section measurements** at 8 and 13 TeV from **10 different top-quark production processes**

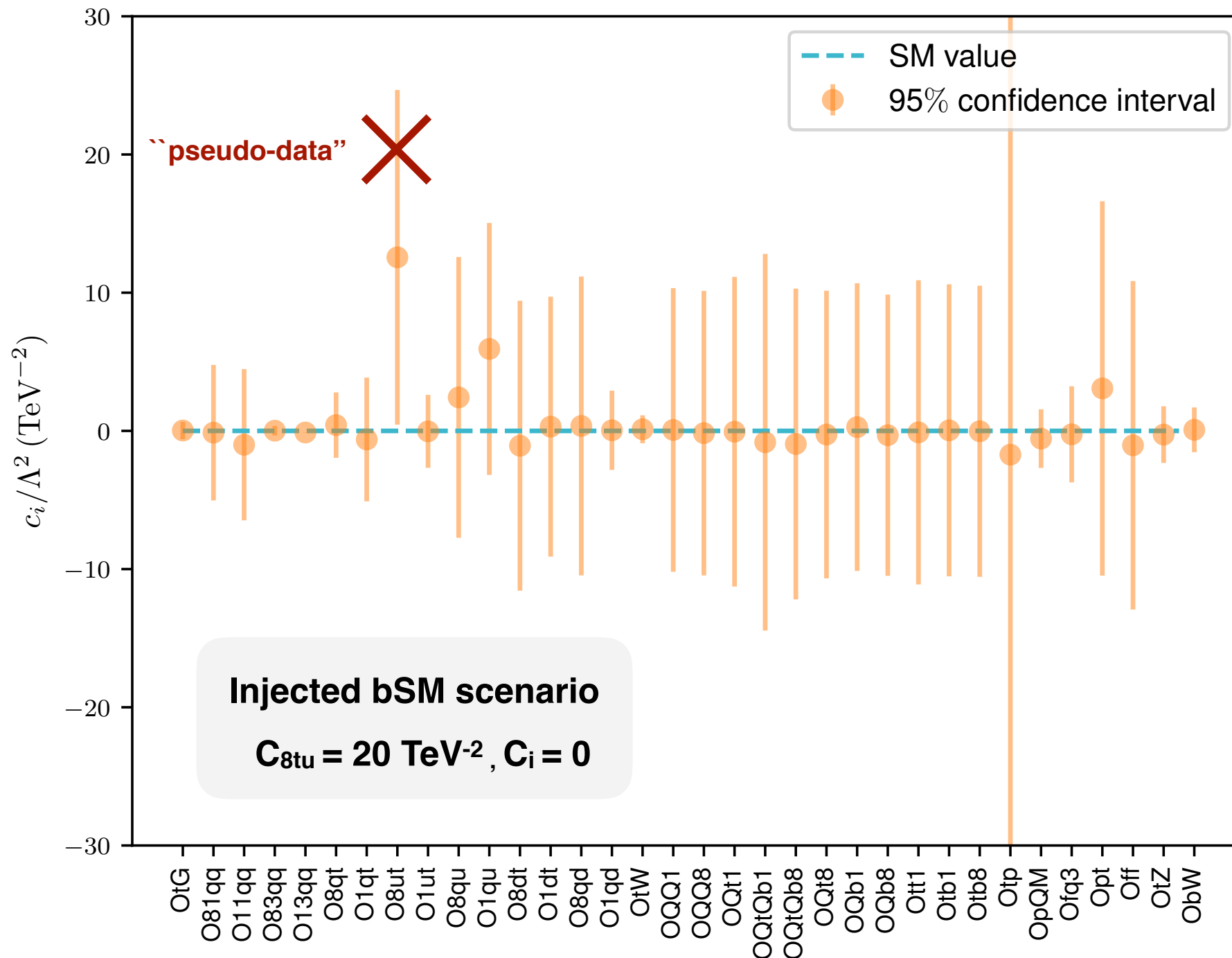
Theory calculations

Process	SM	Code	SMEFT	Code
$t\bar{t}$	NNLO QCD	MCFM/SHERPA NLO + NNLO K -factors	NLO QCD	MG5_aMC
single- t (t -ch)	NNLO QCD	MCFM NLO + NNLO K -factors	NLO QCD	MG5_aMC
single- t (s -ch)	NLO QCD	MCFM	NLO QCD	MG5_aMC
tW	NLO QCD	MG5_aMC	NLO QCD	MG5_aMC
tZ	NLO QCD	MG5_aMC	LO QCD + NLO SM K -factors	MG5_aMC
$t\bar{t}W(Z)$	NLO QCD	MG5_aMC	LO QCD + NLO SM K -factors	MG5_aMC
$t\bar{t}h$	NLO QCD	MG5_aMC	LO QCD + NLO SM K -factors	MG5_aMC
$t\bar{t}t\bar{t}$	NLO QCD	MG5_aMC	LO QCD + NLO SM K -factors	MG5_aMC
$t\bar{t}b\bar{b}$	NLO QCD	MG5_aMC	LO QCD + NLO SM K -factors	MG5_aMC

PDF set: **NNPDF3.1 NNLO no-top**

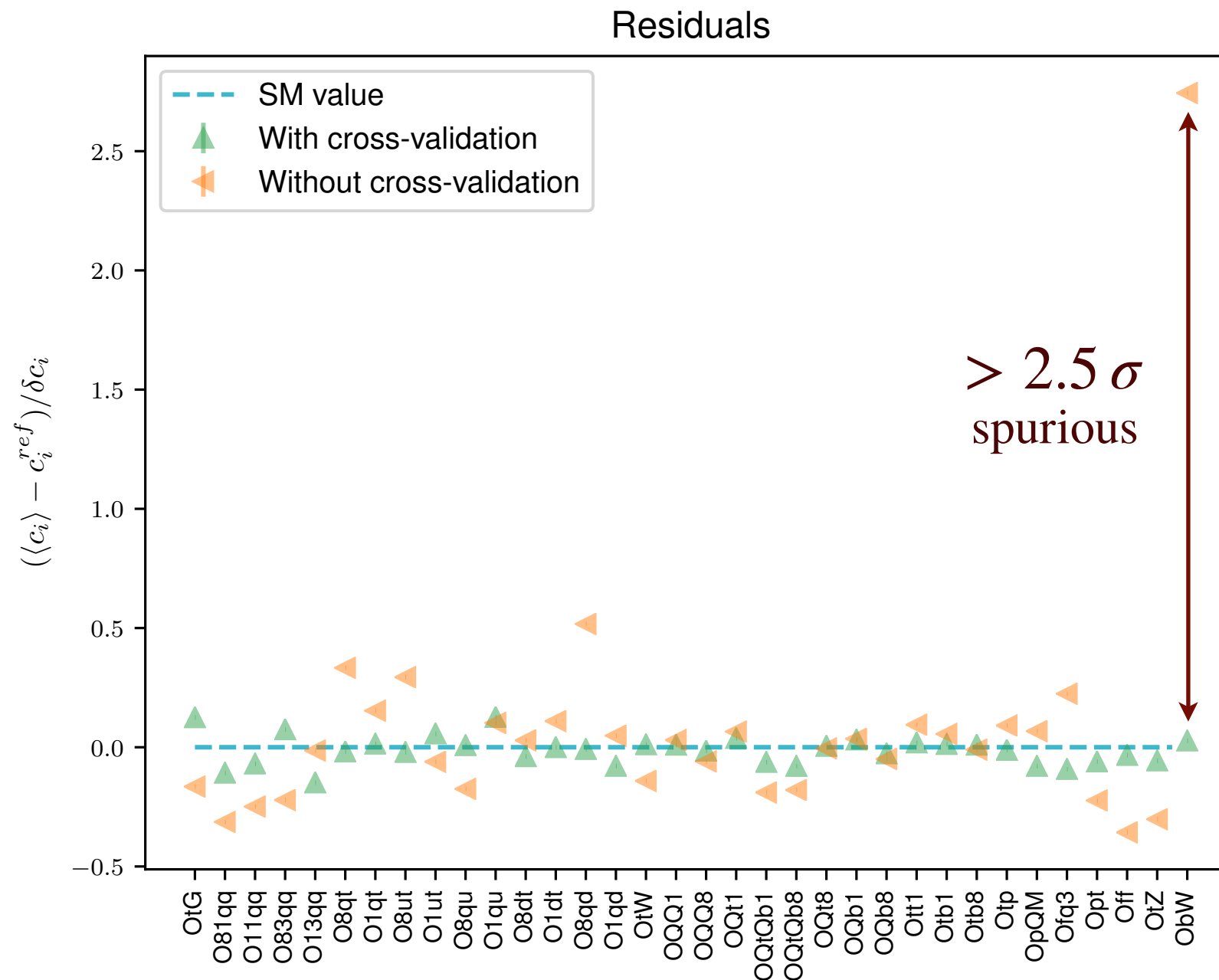
Closure Tests

- Generate **pseudo-data based** on a given scenario (SM or BSM) and check that the correct (known) results are reproduced after the fit
- Allows quantifying the **expected statistical significance** for BSM deviations



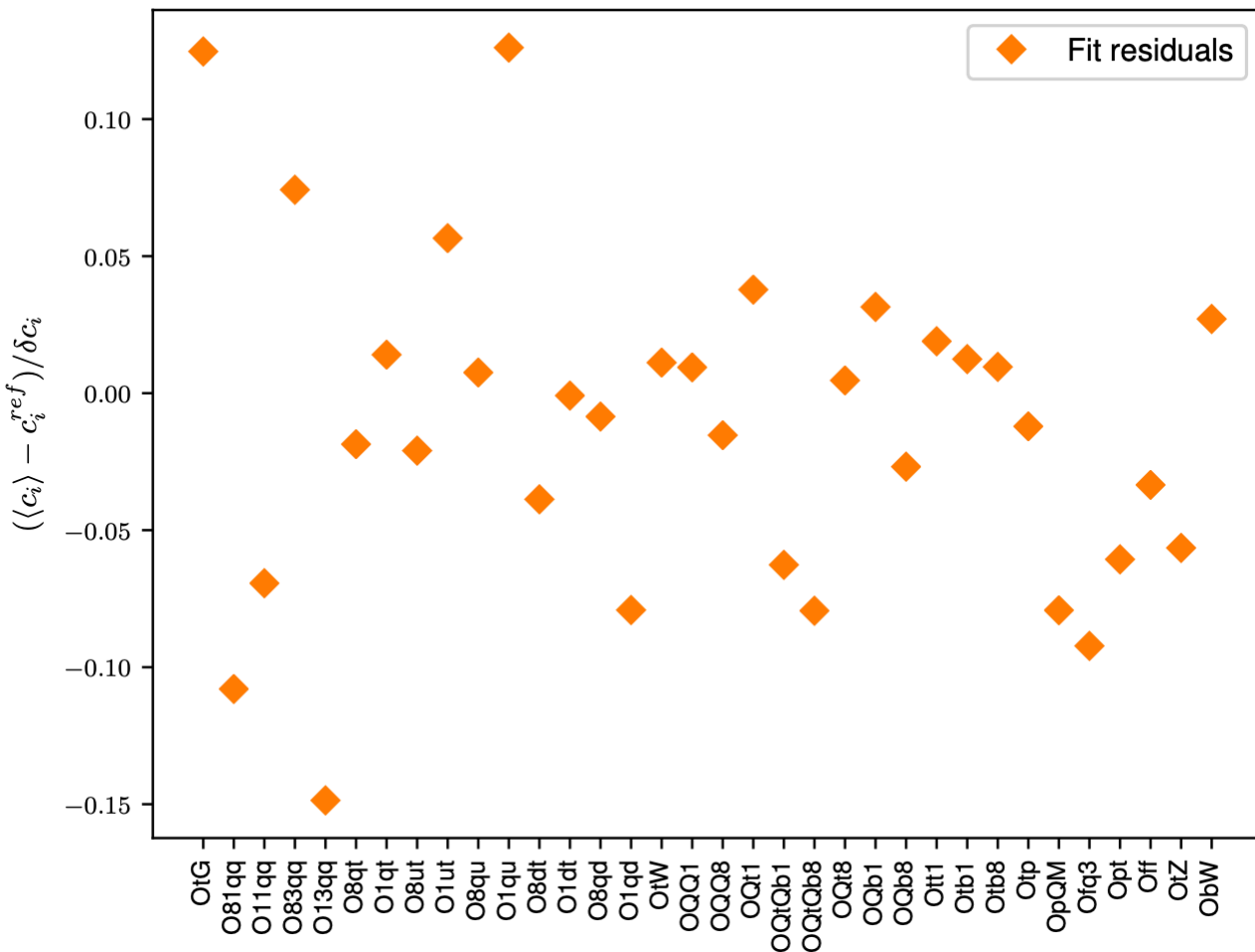
Cross-validation

- Since N_{par} is not too different from N_{dat} , overfitting will take place for an efficient optimiser
- Artificial tensions with the SM** are likely to be generated by overfitting!
- Fit residuals **consistent with true result (SM)** only with cross-validation

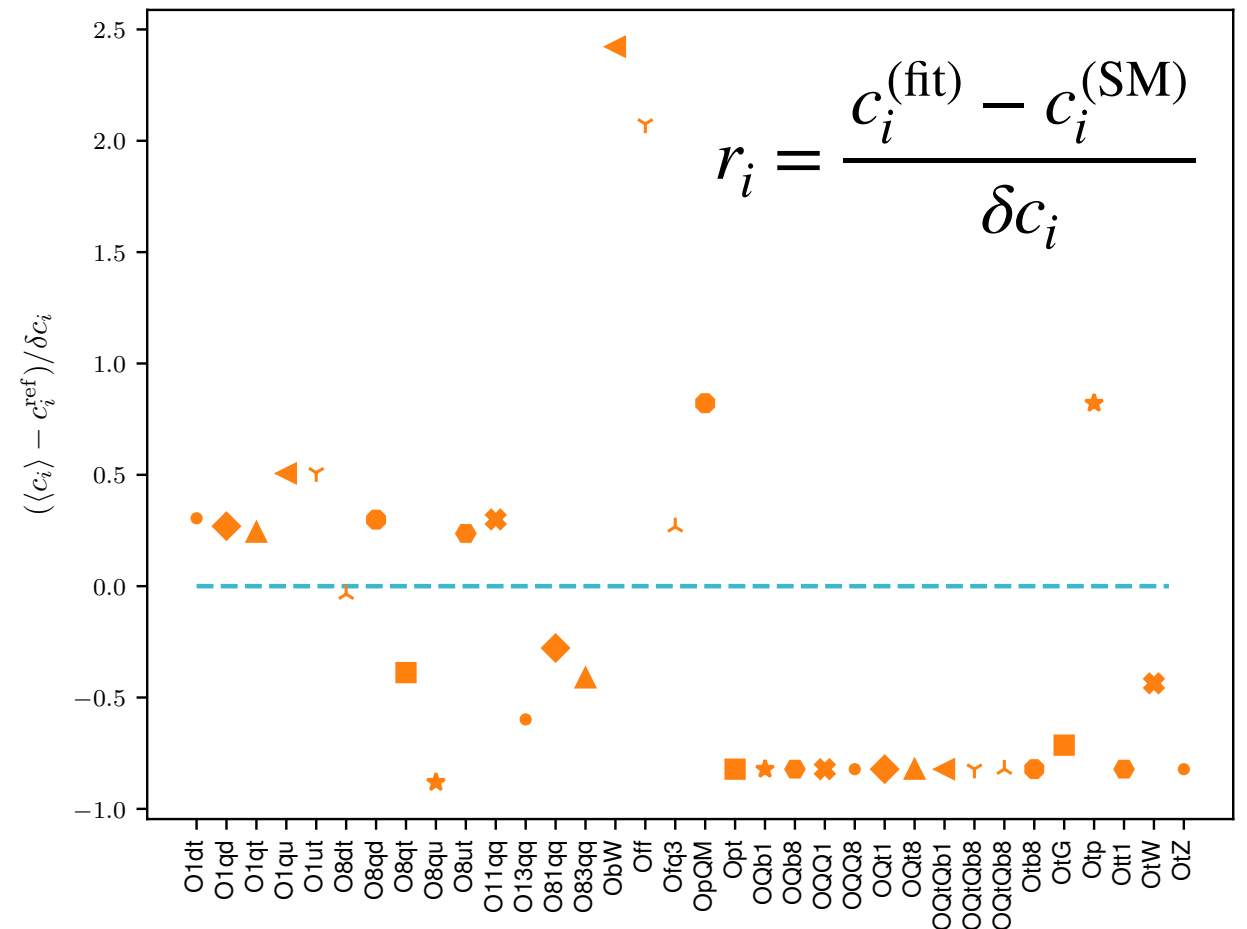


Global vs individual fits

Global fits (all params fitted)



Individual fits (one param at a time)



- 🔧 If each operator was a truly **independent random variable**, we would expect that at least **2 operators** have residuals $|r| > 1$ (bounds are 95% CL)
- 🔧 This is far from being the case when all operators are fitted simultaneously
- 🔧 Explained by **correlations between operators + degeneracies in parameter space**:
much larger fluctuations if we fit one operator at a time

Fit quality

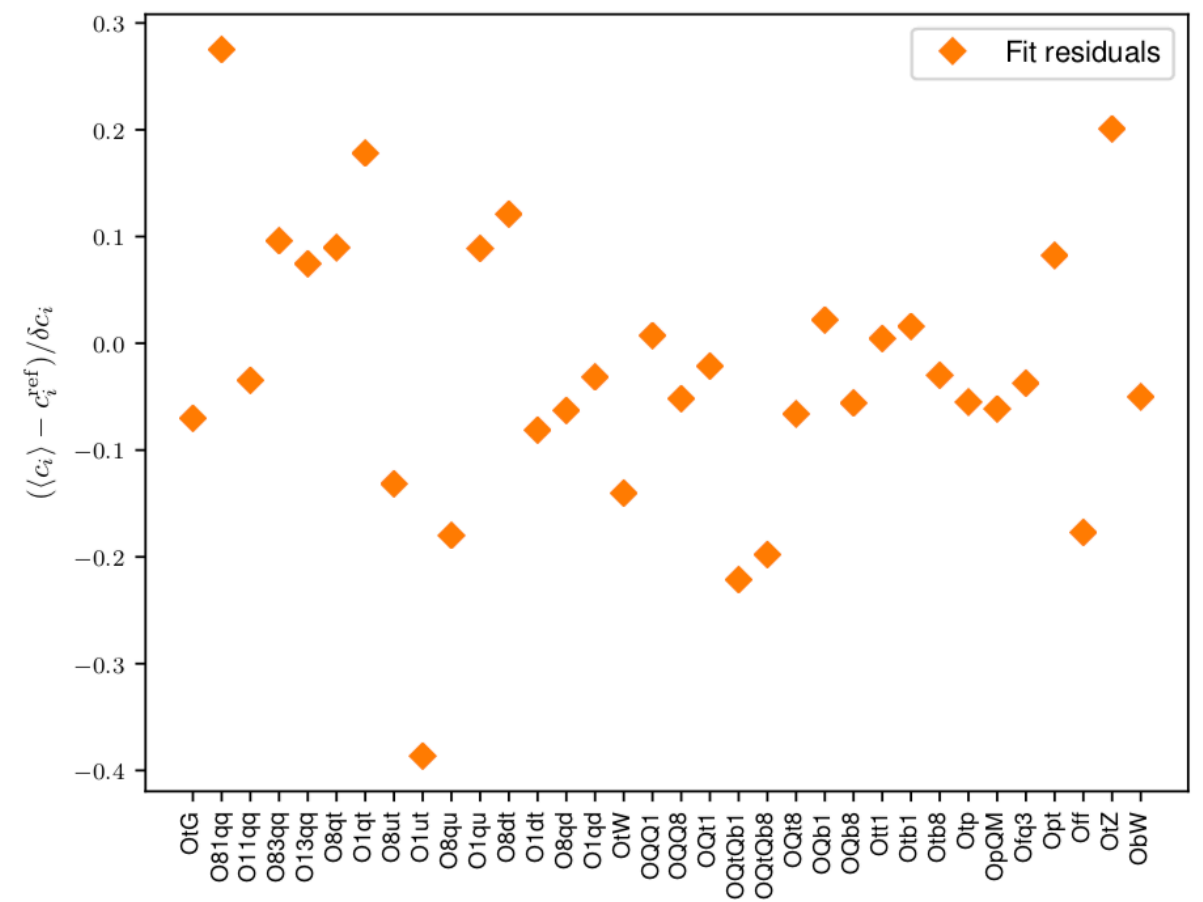
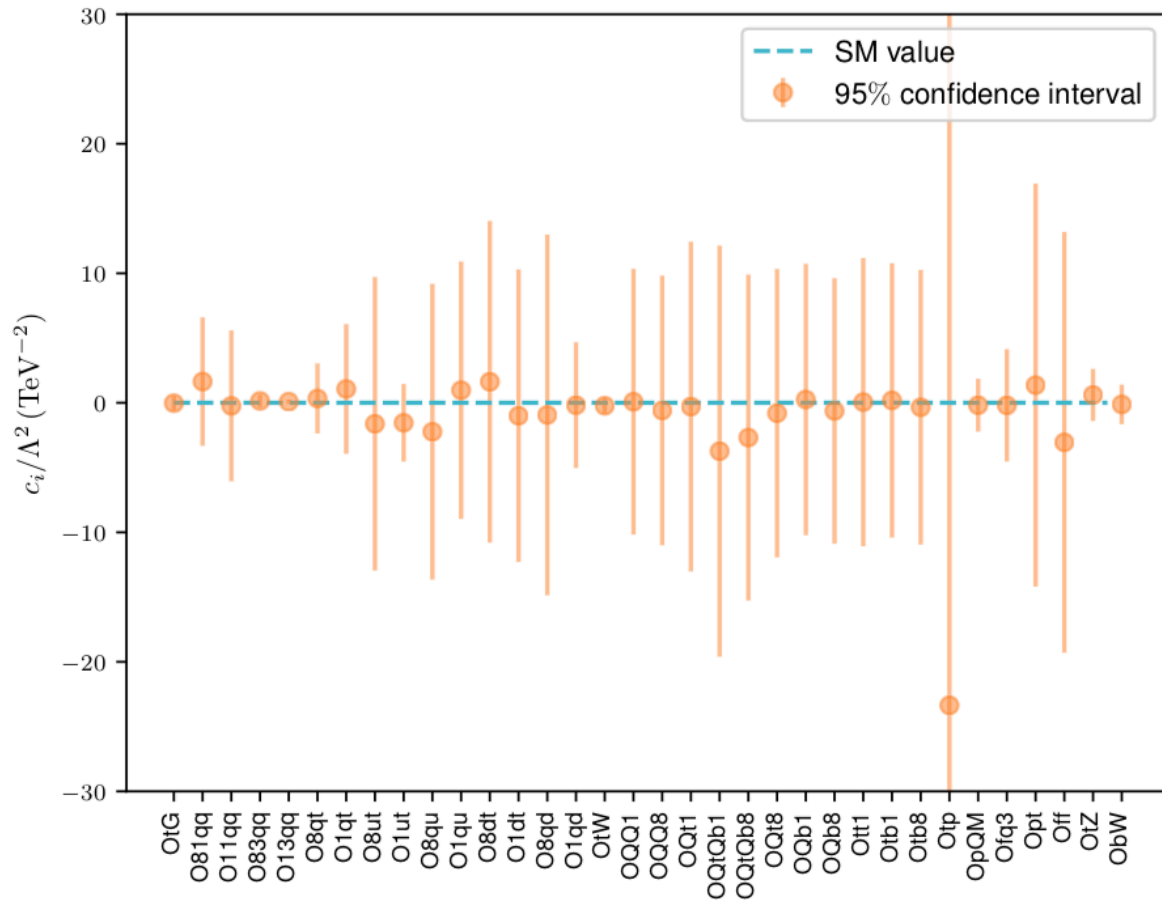
📌 **Good agreement** between theory (SM and SMEFT) and data for most datasets

📌 For the **103 fitted cross-sections**, we find χ^2/n_{dat} of **1.11 (1.06)** before (after) fit

📌 Including SMEFT effects improves agreement with data: need to quantify how **significant** this improvement is

Dataset	χ^2/n_{dat} (prior)	χ^2/n_{dat} (fit)	n_{dat}
ATLAS_tt_8TeV_ljets [$m_{t\bar{t}}$]	1.51	1.25	7
CMS_tt_8TeV_ljets [$y_{t\bar{t}}$]	1.17	1.17	10
CMS_tt2D_8TeV_dilep [$(m_{t\bar{t}}, y_t)$]	1.38	1.38	16
CMS_tt_13TeV_ljets2 [$m_{t\bar{t}}$]	1.09	1.28	8
CMS_tt_13TeV_dilep [$m_{t\bar{t}}$]	1.34	1.42	6
CMS_tt_13TeV_ljets_2016 [$m_{t\bar{t}}$]	1.87	1.87	10
ATLAS_WhelF_8TeV	1.98	0.27	3
CMS_WhelF_8TeV	0.31	1.18	3
CMS_ttbb_13TeV	5.00	1.29	1
CMS_tttt_13TeV	0.05	0.02	1
ATLAS_tth_13TeV	1.61	0.55	1
CMS_tth_13TeV	0.34	0.01	1
ATLAS_ttZ_8TeV	1.32	5.29	1
ATLAS_ttZ_13TeV	0.01	1.06	1
CMS_ttZ_8TeV	0.04	0.06	1
CMS_ttZ_13TeV	0.90	0.67	1
ATLAS_ttW_8TeV	1.34	0.27	1
ATLAS_ttW_13TeV	0.82	0.65	1
CMS_ttW_8TeV	1.54	0.54	1
CMS_ttW_13TeV	0.03	0.09	1
CMS_t_tch_8TeV_dif	0.11	0.32	6
ATLAS_t_tch_8TeV [y_t]	0.91	0.43	4
ATLAS_t_tch_8TeV [$y_{\bar{t}}$]	0.39	0.45	4
ATLAS_t_sch_8TeV	0.08	1.92	1
ATLAS_t_tch_13TeV	0.02	0.09	2
CMS_t_tch_13TeV_dif [y_t]	0.46	0.49	4
CMS_t_sch_8TeV	1.26	0.76	1
ATLAS_tW_inc_8TeV	0.02	0.06	1
CMS_tW_inc_8TeV	0.00	0.07	1
ATLAS_tW_inc_13TeV	0.52	0.82	1
CMS_tW_inc_13TeV	4.29	1.68	1
ATLAS_tZ_inc_13TeV	0.00	0.00	1
CMS_tZ_inc_13TeV	0.66	0.34	1
Total	1.11	1.06	103

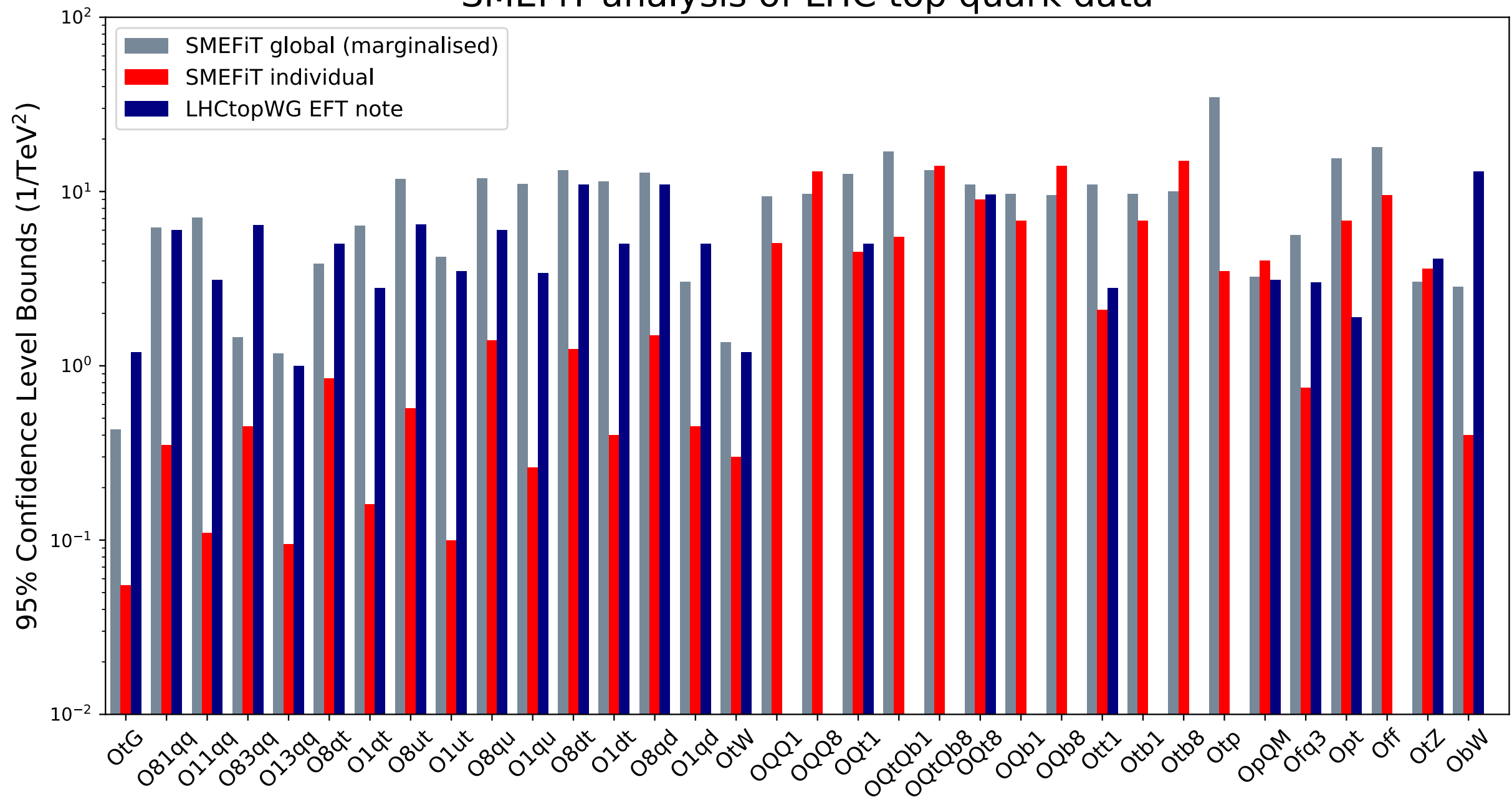
SMEFiT results



- 📌 Agreement with the SM expectation **within uncertainties**
- 📌 Bounds on individual operators are in general largely **correlated among them**
- 📌 Large differences between the bounds obtained from each operator

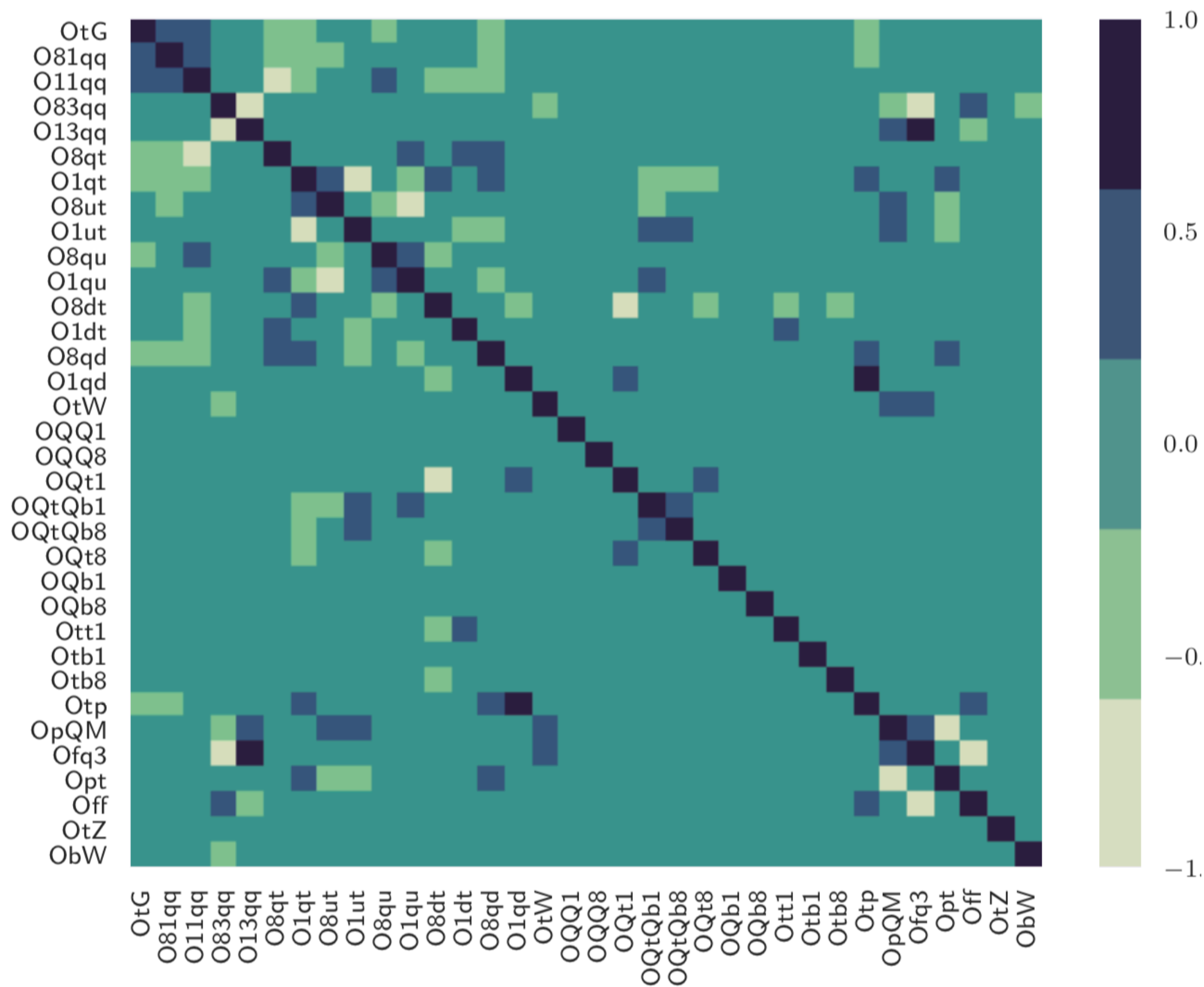
Comparison with 1D fits and previous bounds

SMEFiT analysis of LHC top quark data

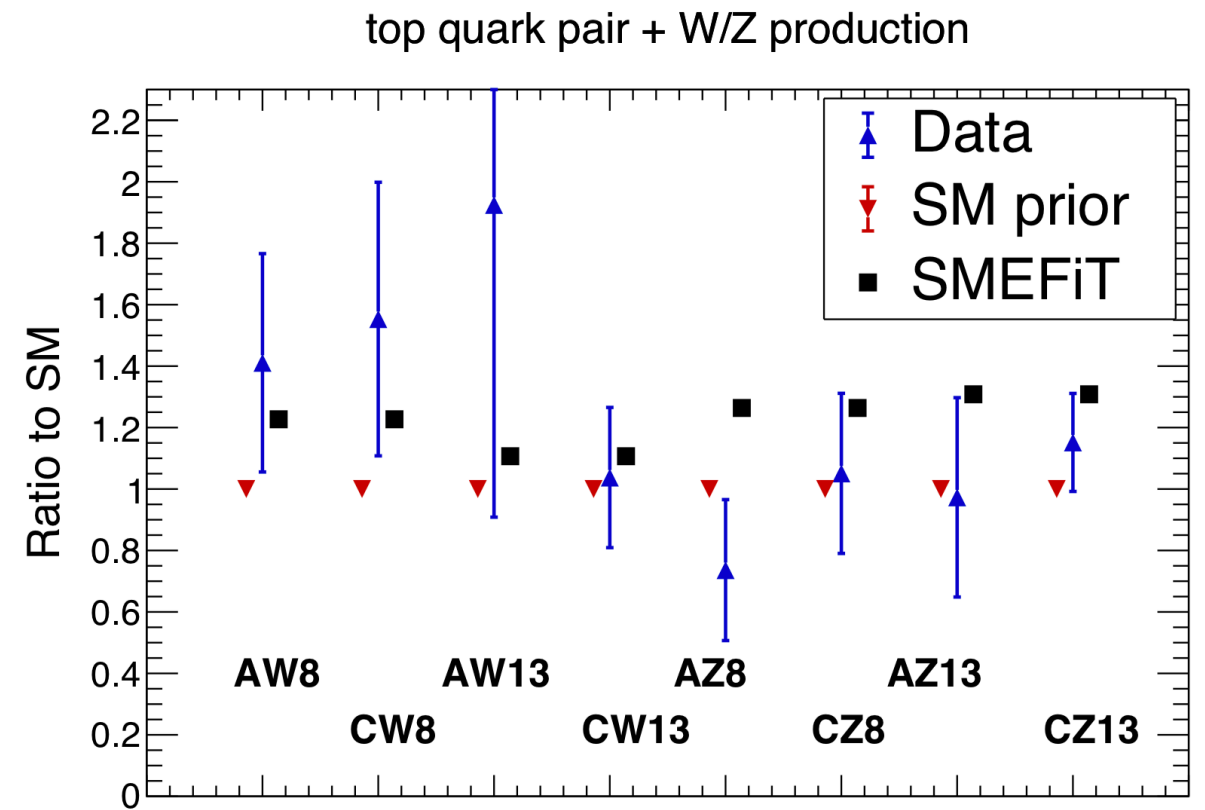
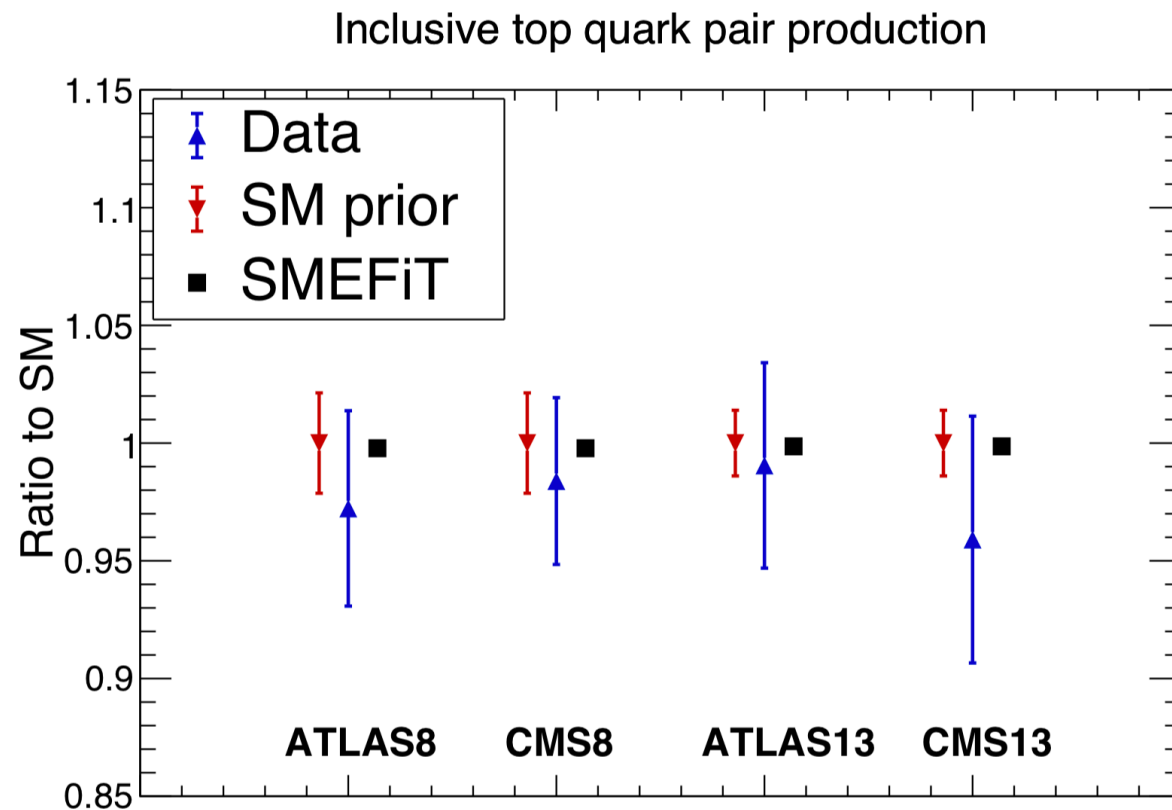


- 📌 **Improvement** found (more stringent bounds) in most fitted degrees of freedom
- 📌 For some specific operators **our bounds are the first ones** to be reported
- 📌 Individual bounds can dramatically **overestimate** the actual (marginalised) bounds

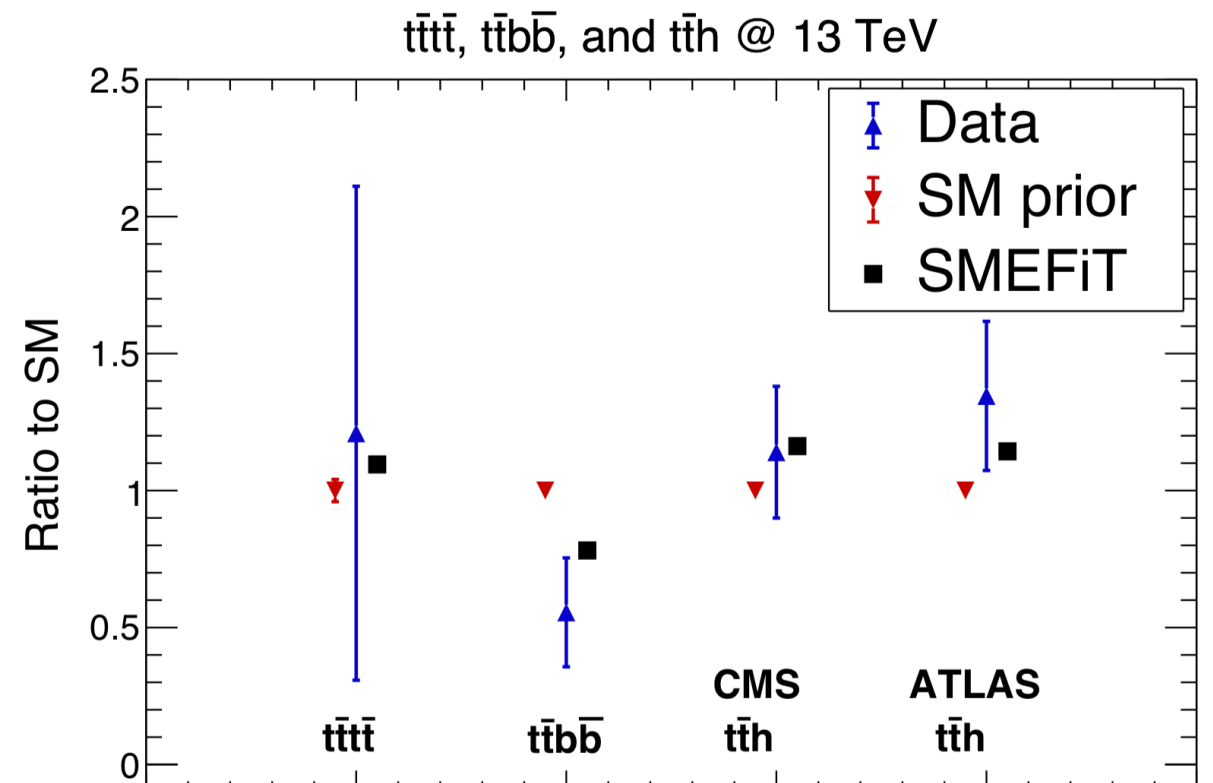
Correlation map



Comparison with data

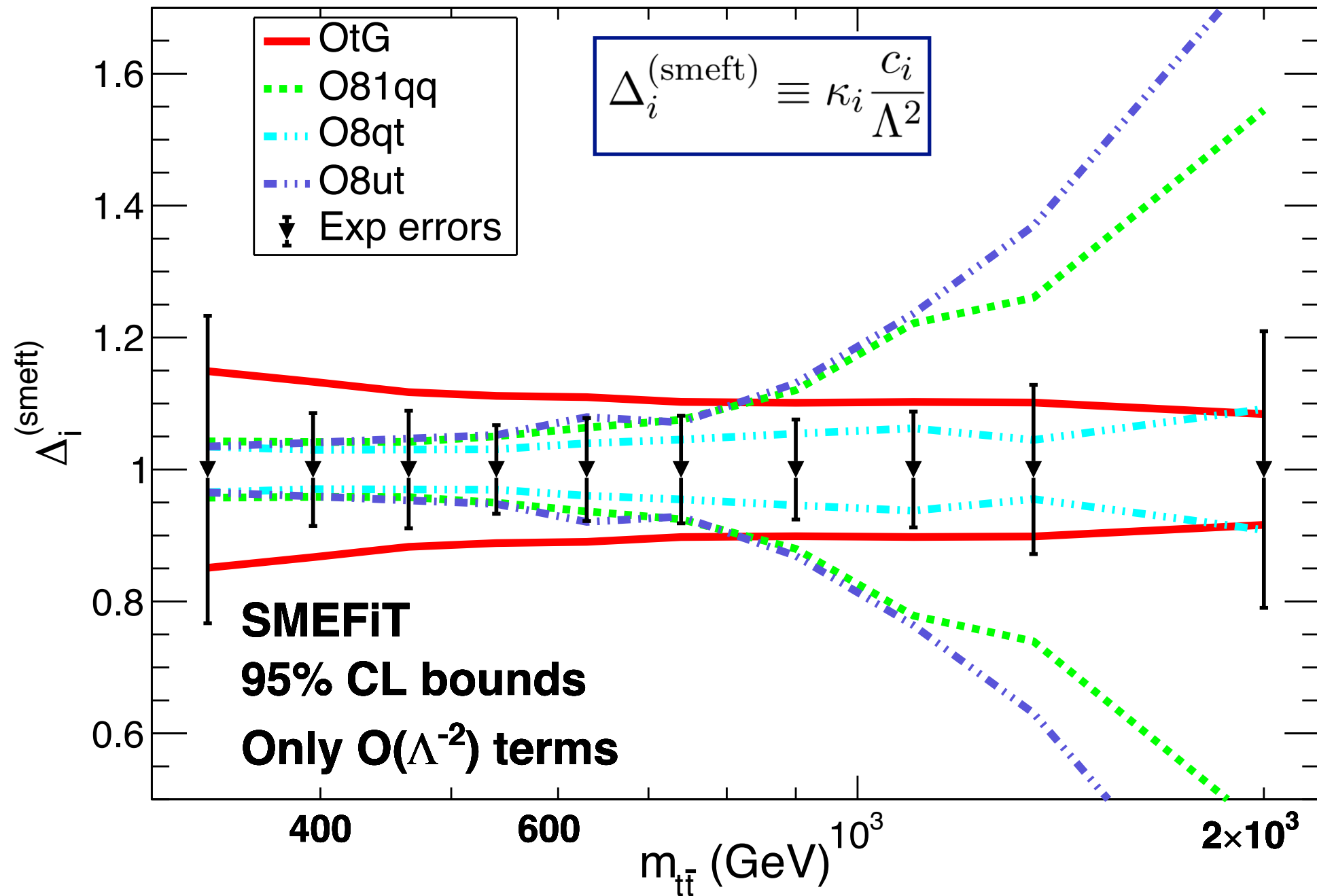


- The **best-fit SMEFT-induced shift** wrt the SM calculation depends on the process
- For inclusive top quark pair and single top, the SMEFT shifts are $< 2\%$
- For $t\bar{t}t\bar{t}$, $t\bar{t}b\bar{b}$, and $t\bar{t}h$ the SMEFT shifts can be as large as 20% (reflecting the larger experimental errors)



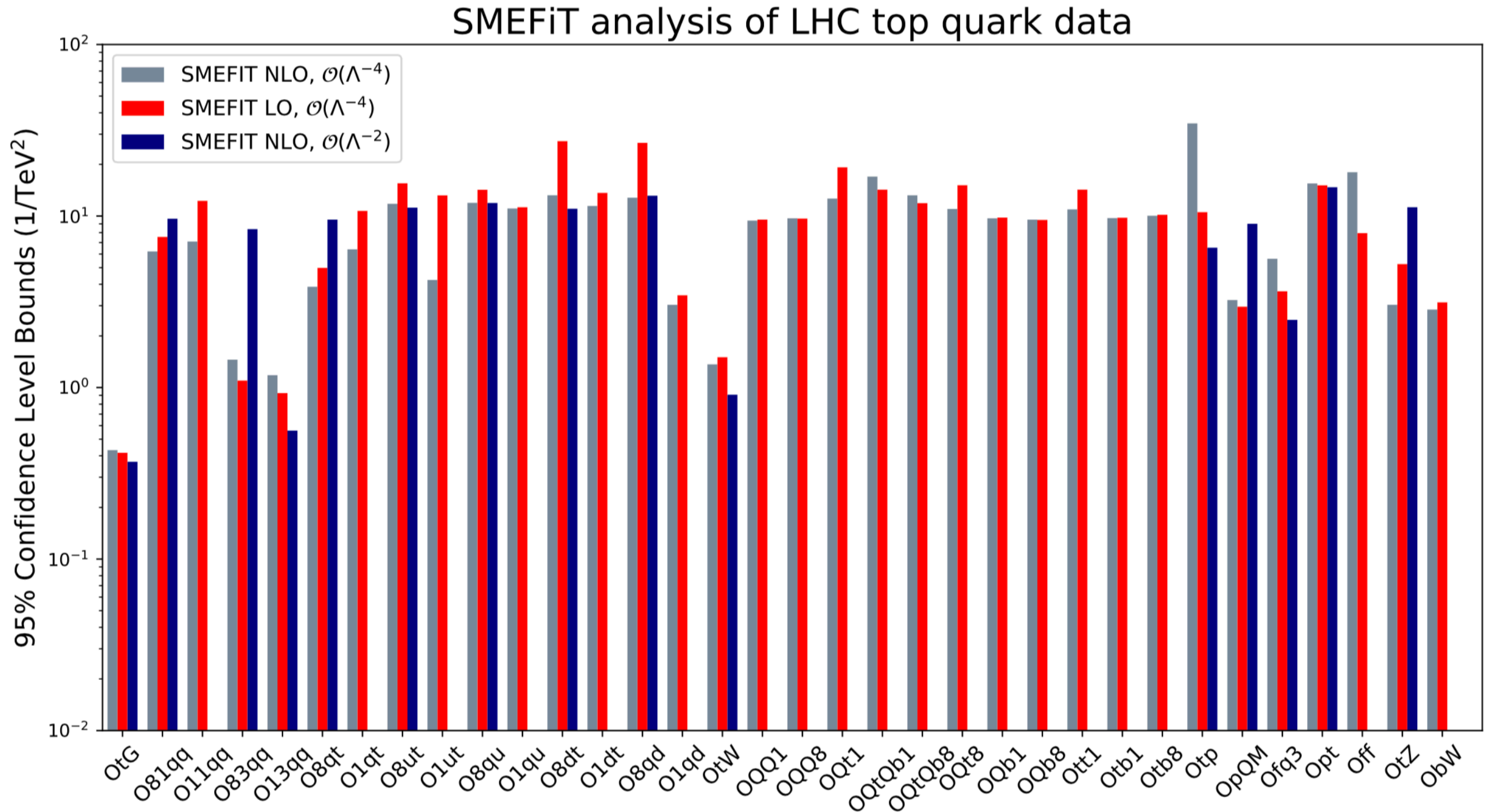
High-energy behaviour

$t\bar{t}$ production @ 13 TeV, CMS lepton+jets $L=36 \text{ fb}^{-1}$



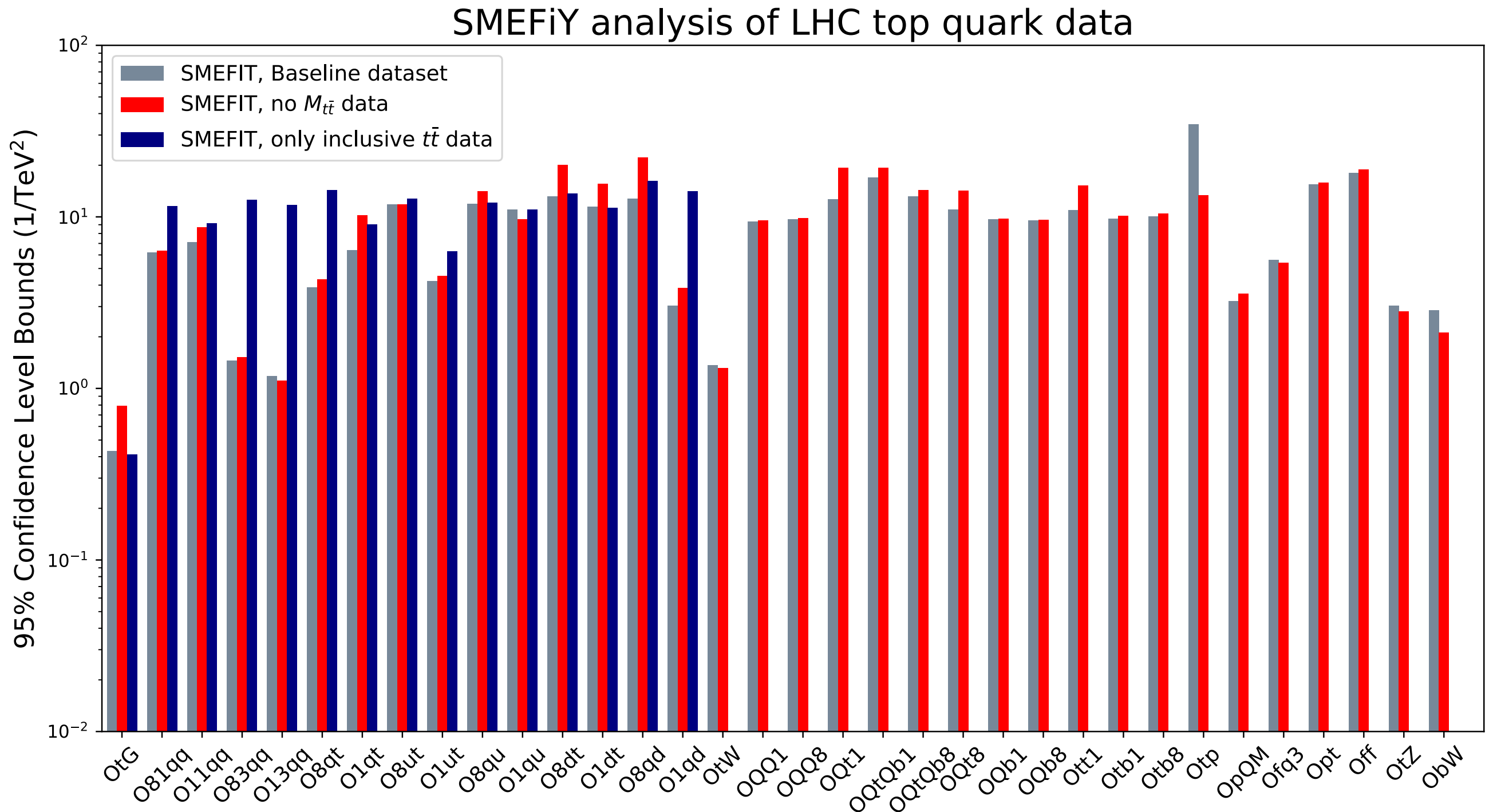
Energy-growing effects enhance sensitivity to SMEFT effects with **TeV-scale cross-sections**
 but need to be careful to ensure **validity of EFT description**

Dependence on theory settings



Accounting for the **quadratic $\mathcal{O}(\Lambda^{-4})$ terms** strengthens bounds for several operators

Dependence on dataset



Reasonable stability of the fit results with respect to the **choice of dataset**

Summary and outlook

- 📌 Presented a novel framework, **SMEFiT**, suitable for global analyses of the SMEFT, which exploit expertise inherited from global PDF fits
- 📌 As a proof-of-concept, applied this framework to the exploration of the constraints in the SMEFT parameter space provided by **LHC top quark data**
- 📌 **Improved constraints** compared to previous studies (first-even bounds in some cases)
- 📌 Demonstrated **Bayesian reweighting** for the *a posteriori* inclusion of the constraints from new measurements on SMEFiT without need of redoing fit
- 📌 Next steps: enlarge the operator fitting basis and include **additional LHC cross-sections** (Higgs, electroweak, jets) as well as flavour and low-energy observables, and explore implications for specific **UV-complete models**