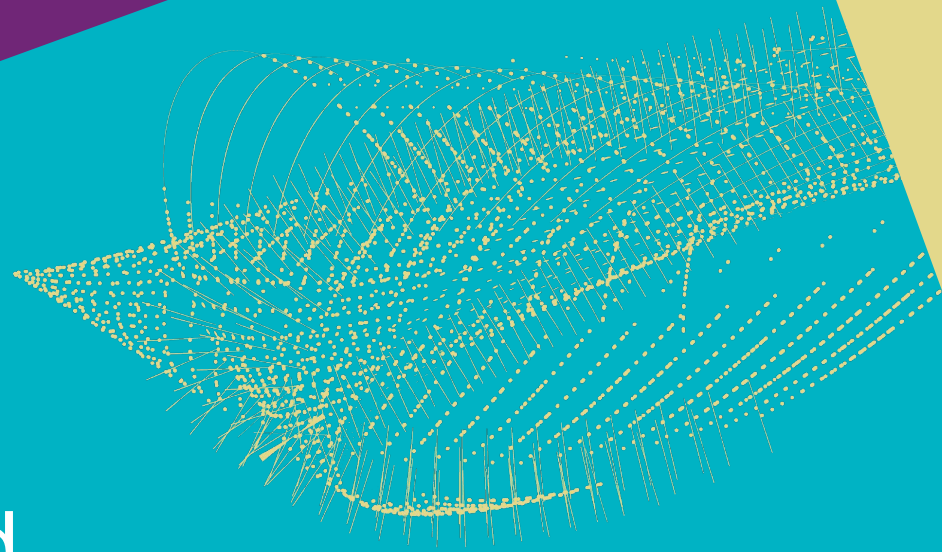


R&D Meeting 10-05-2019

# Measurement and correction of nonlinear optics in the LHC

F. Carlier



# Attempt to summarize a thesis in 15 minutes

## Introduction:

- What are the building blocks of particle accelerators?
- Where do nonlinear perturbations come from?
- How are beam dynamics measured in the LHC

## Thesis:

- Stability under AC dipole excitation
- Correction of nonlinear errors in the LHC
- First measurement of beam-beam nonlinearities

# Attempt to summarize a thesis in ~~15~~ minutes

## Introduction: (80%)

- What are the building blocks of particle accelerators?
- Where do nonlinear perturbations come from?
- How are beam dynamics measured in the LHC

## Thesis: (20%)

- Stability under AC dipole excitation
- Correction of nonlinear errors in the LHC
- First measurement of beam-beam nonlinearities

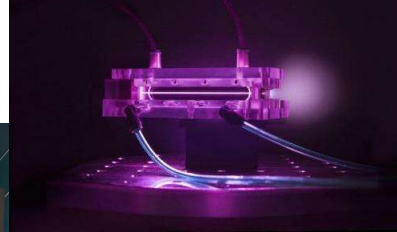
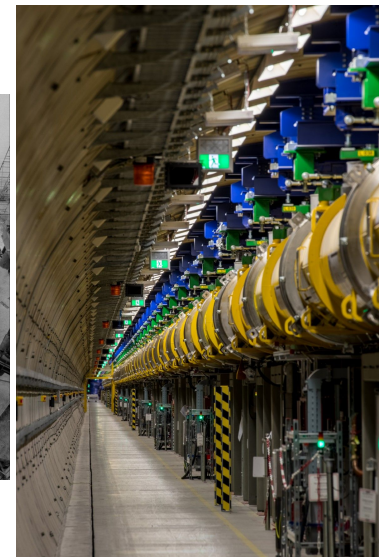
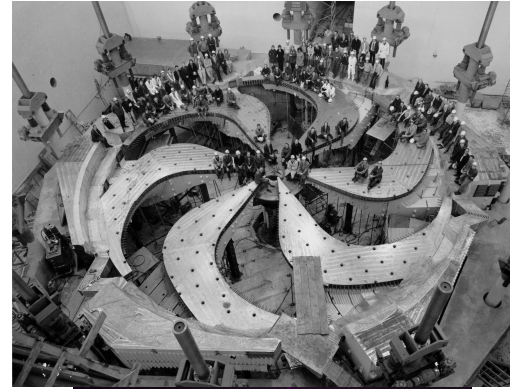
**Disclaimer: Lots of information missing, probably more suitable for a seminar**

# Accelerators are quite common

Accelerator physics is probably the only thing Nikhef does not do. **But it's a huge field!**

About 30000 active particle accelerators in the world:

- Colliders
- Light sources
- Synchrotrons
- Medical accelerators
- Linear accelerators
- Cyclotrons
- Electrostatic accelerators
- Wakefield accelerators
- ....

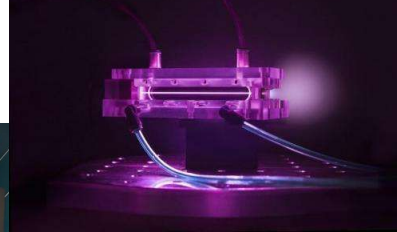
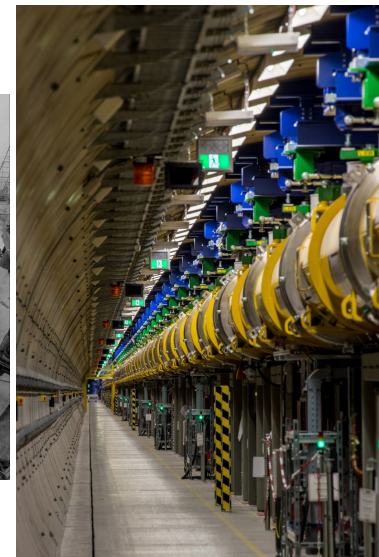
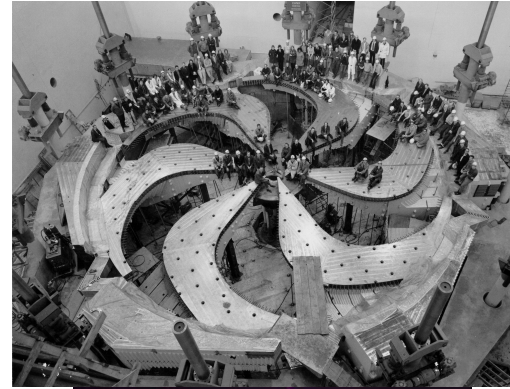


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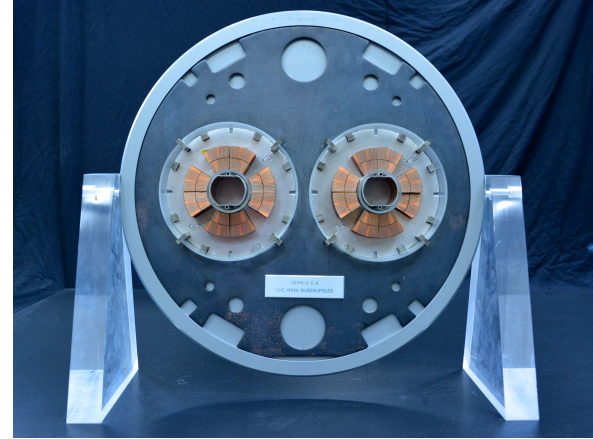
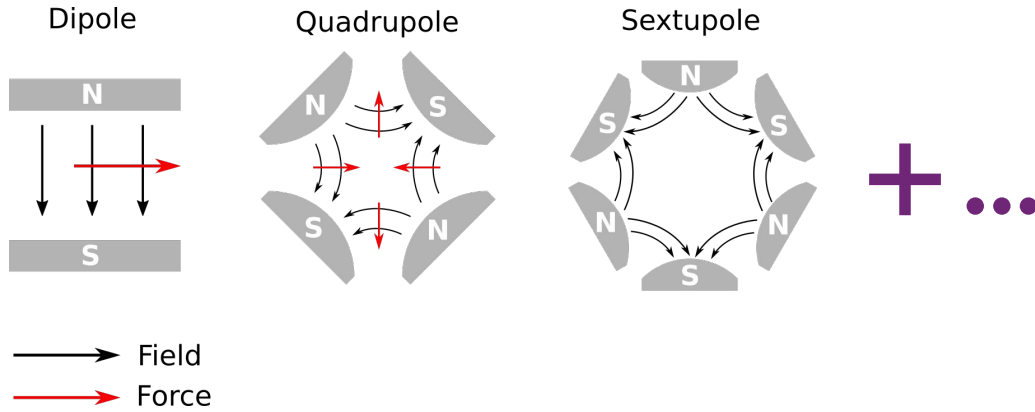




# Building blocks of the LHC are magnets

Magnetic fields are used to bend, shape, and control the beams

- Dipoles: change trajectory of bunch
- Quadrupoles: focus or defocus the bunch
- Higher orders: control the nonlinear optics

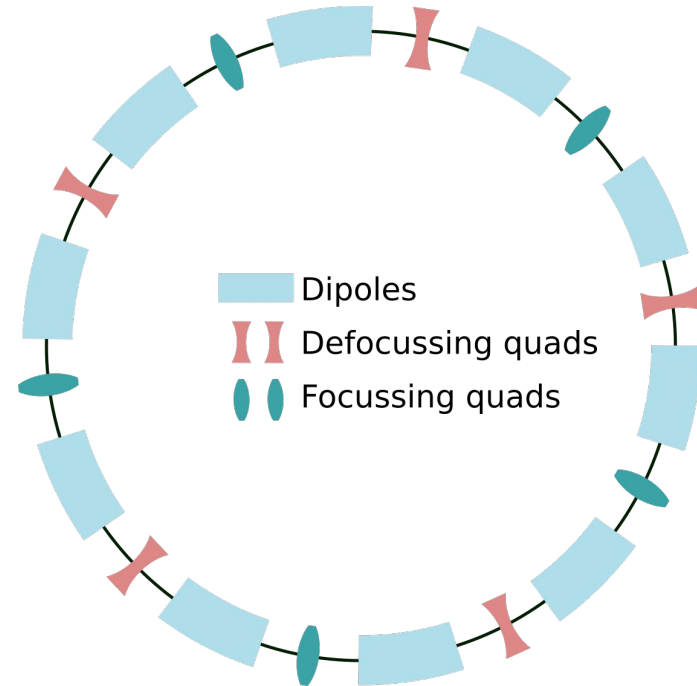


# Basic look of the LHC: A lattice of magnets

Alternating focusing and defocusing quadrupoles, interleaved with dipoles.

Still need to add:

- RF cavities (beam acceleration)
- Injection region
- Collision sections
- 2nd beam and beampipe
- Feedback systems
- All instrumentation
- Beam dump
- etc...



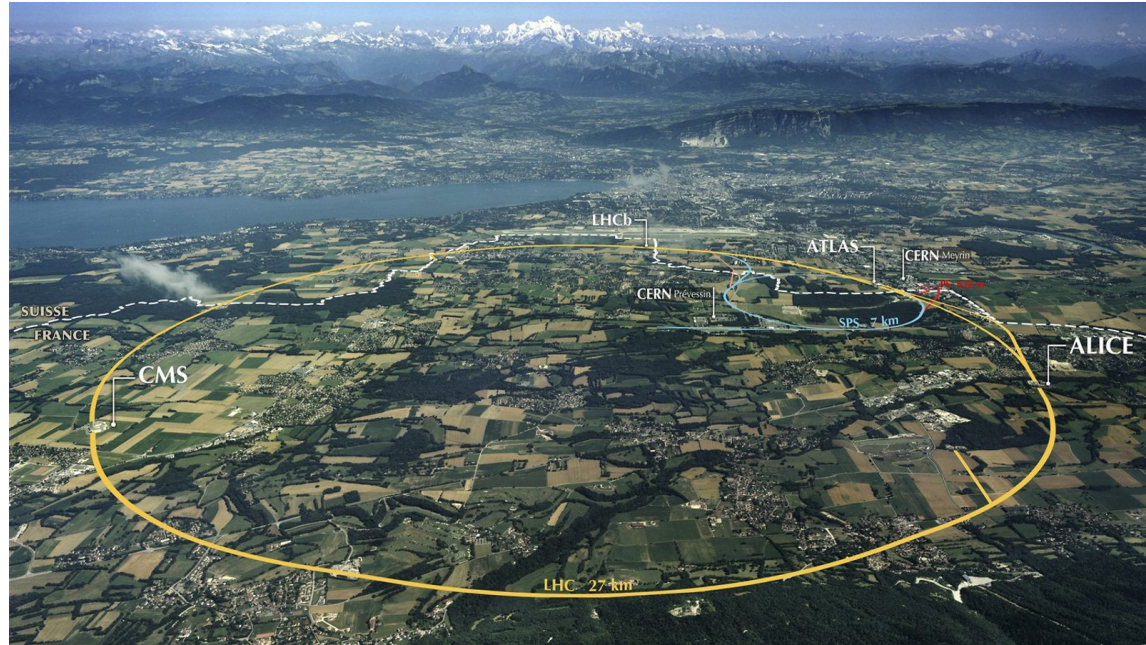
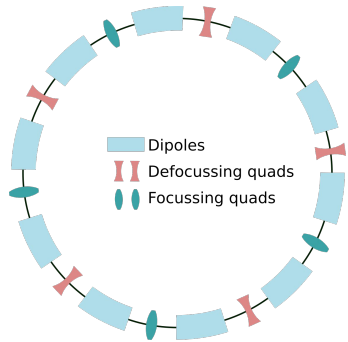
# Basic look of the LHC

And multiply to about:

# dipoles: 1232

# quadrupoles: 392

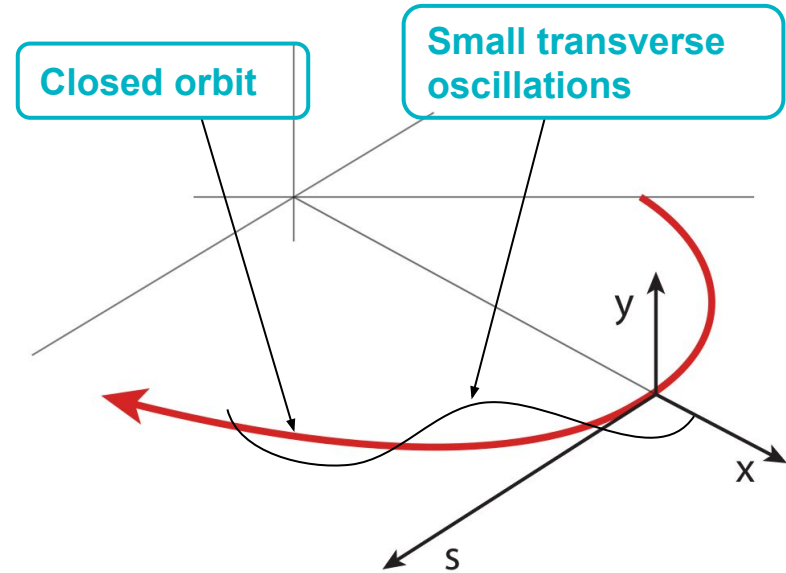
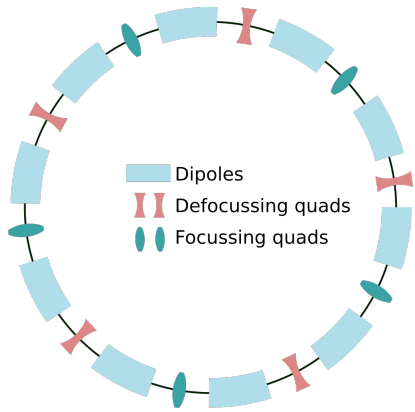
# total magnets: 9593





# Frame of reference moves on ideal orbit

- Closed orbit (reference orbit) is the ideal trajectory as defined by the bending of the dipoles for a particle with design energy.
- Motion of interest is motion **transverse** to the direction of travel on the closed orbit (x & y).



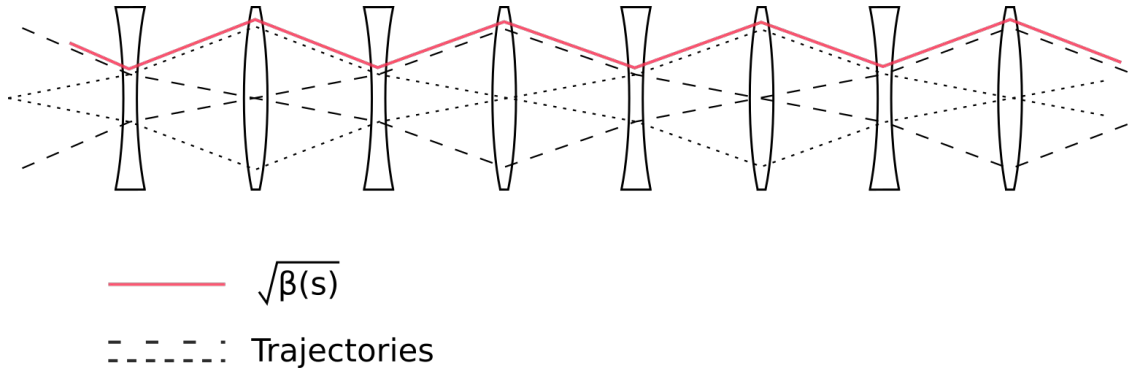
# Linear optics from FODO lattice

Alternating focusing and defocusing quadrupoles known as FODO lattice (like in the LHC)

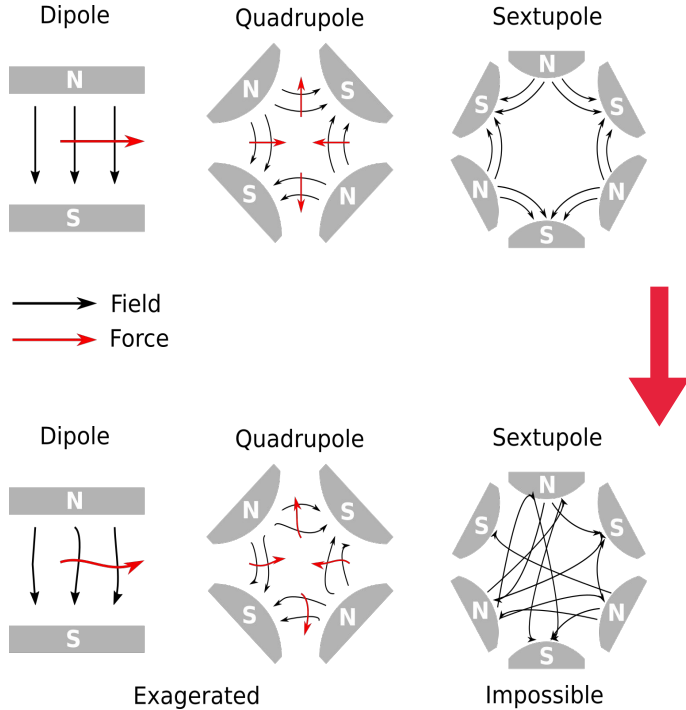
- Defines the linear beam optics
- Beta-function determines the envelope of oscillation amplitude

The total number of oscillations in one turn determines the **tune (Q)**

- Frequency of main linear mode
- Most important design parameter
- Determines resonant modes or not



# Unfortunately nothing is perfect



## Sources of errors

- Magnetic errors (design or manufactured)
- Misalignment and rotation of magnets

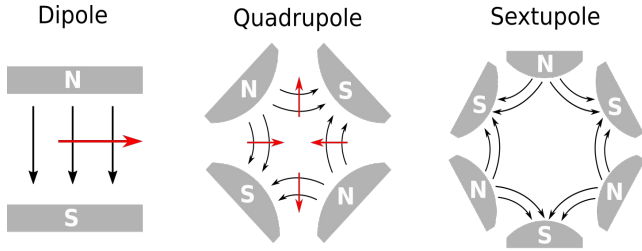
Can be described by a multipolar expansion

$$B_y + iB_x = B_r \sum_{n=1}^{\infty} [b_n(s) + ia_n(s)] \left( \frac{x + iy}{R_r} \right)^{n-1}$$

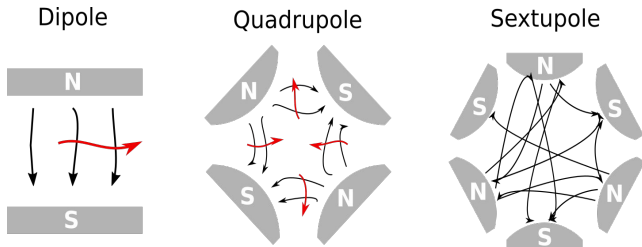
Quadrupole is a linear element ( $n=2$ )

- But will contain nonlinear error components ( $n > 2$ )
- Referred to as **nonlinear errors or sources**

# Unfortunately nothing is perfect



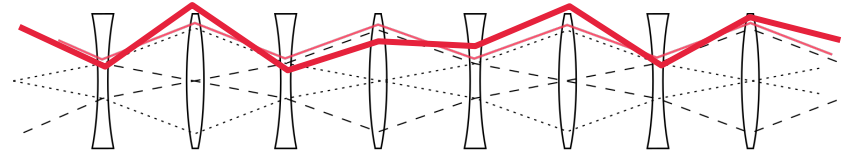
Field  
 Force



Exaggerated

Impossible

Cause distortion of beam optics!

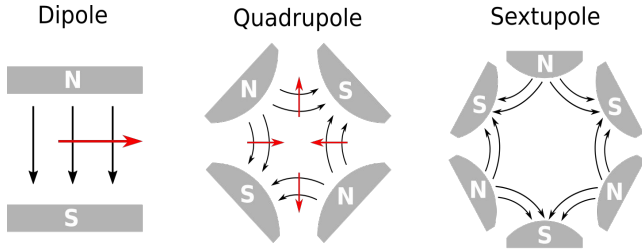


$\sqrt{\beta(s)}$   
 Trajectories

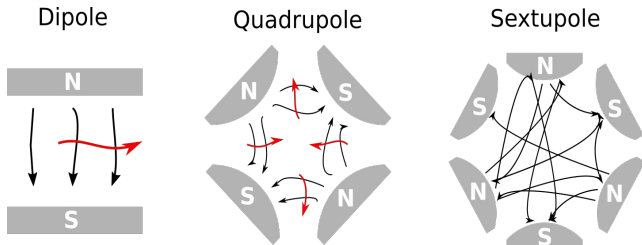
Nonlinear errors cause:

- Reduction of stable phase-space
- Resonances
- Beam loss
- Instabilities
- Detuning of machine
- etc...

# Unfortunately nothing is perfect



→ Field  
→ Force

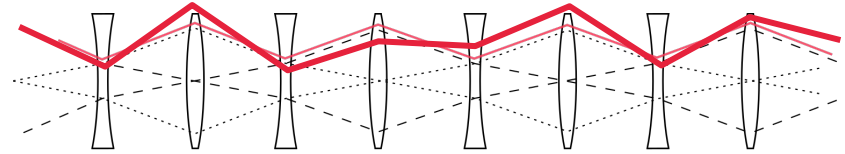


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## Cause distortion of beam optics!



—  $\sqrt{\beta(s)}$

- - - - - Trajectories

## Nonlinear errors cause:

- Reduction of stable phase-space
- Resonances
- Beam loss
- Instabilities
- Detuning of machine
- etc...

**Needs to be  
measured &  
corrected!**



# Measuring beam dynamics in accelerators - Overview

Create transverse oscillation of beam

Measure beam Position (x & y)

Spectral analysis beam position

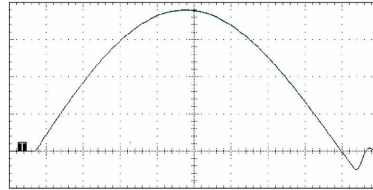
Relate spectral content to sources



Usually in the middle of the night in the CERN Control Center..

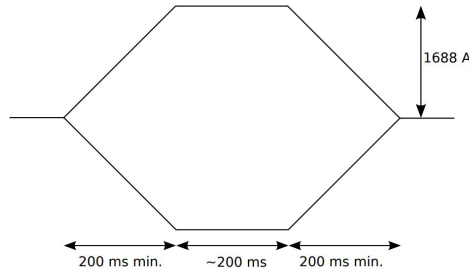
# Creating transverse oscillations with AC dipole

Single dipole pulse kick:

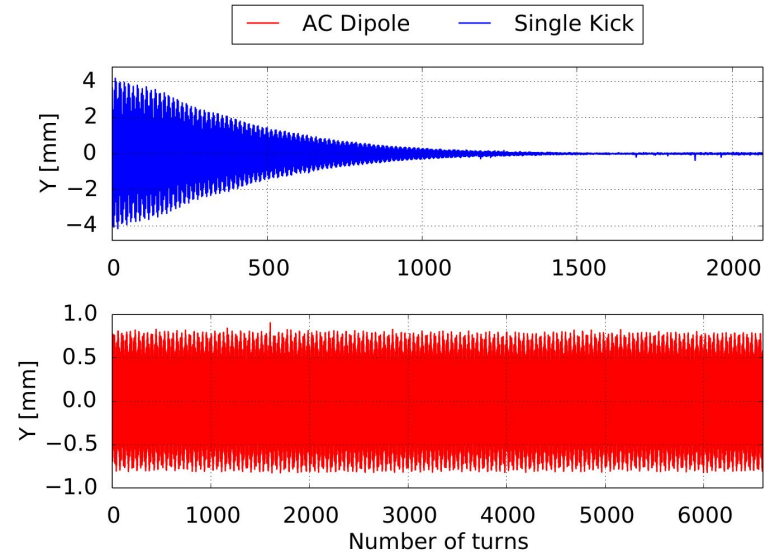


AC dipole with:

- Frequency close to tune, close to resonant
- ramp up, flattop, ramp down of current



Measured beam oscillation amplitude



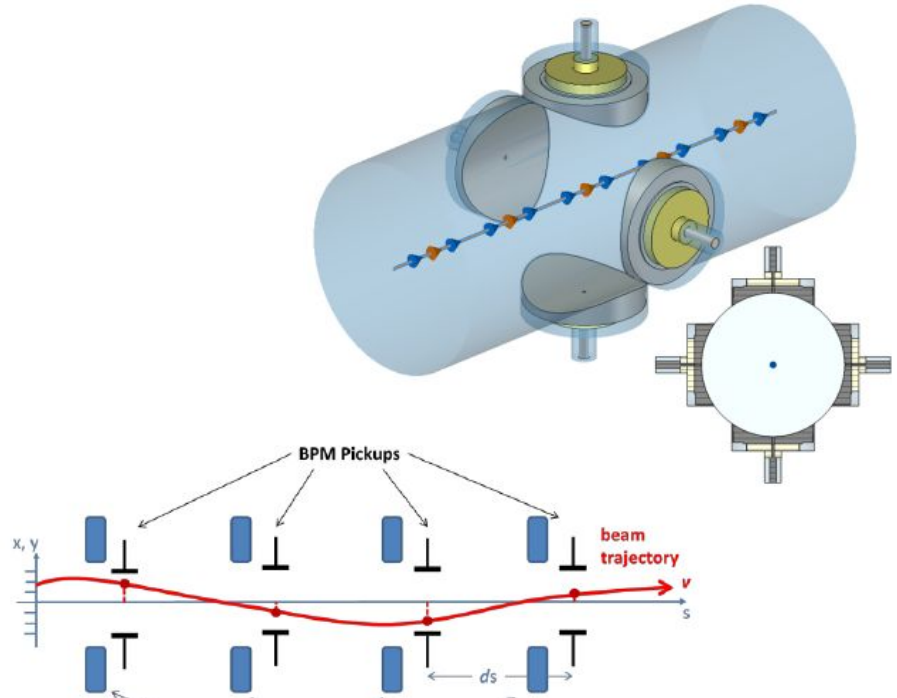
# Beam position monitor (BPM) to measure oscillating beam

Two opposing pick-ups:

- Charge center of bunch induces different pulses in pick-ups  
s → Transverse position

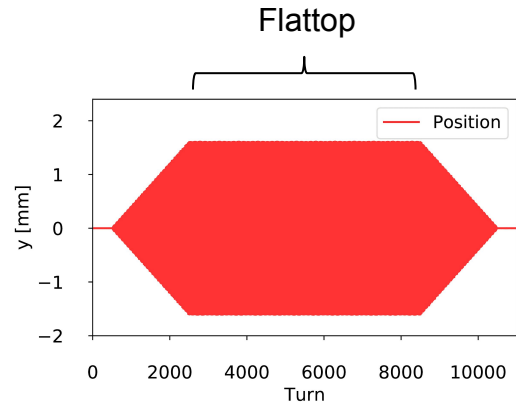
BPMs allow a turn-by-turn read out of the transverse beam position

- 550 BPMs per beam in the LHC

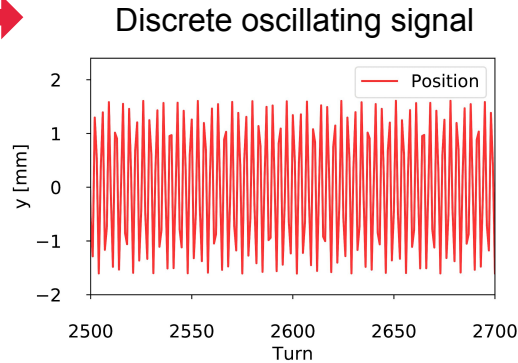


# TbT data contains all information on transverse dynamics

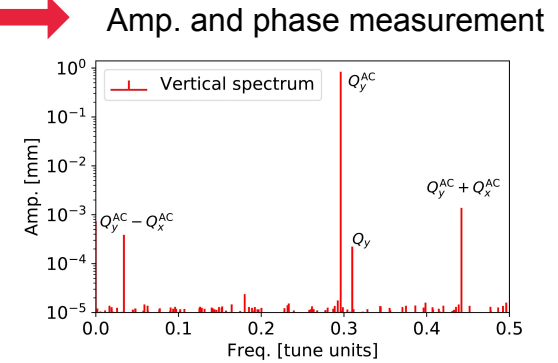
1. Turn-by-turn data as measured by BPMs



2. Use only flattop data at peak oscillation amplitude



3. Spectral analysis reveals all linear and nonlinear modes



So much for the introduction..

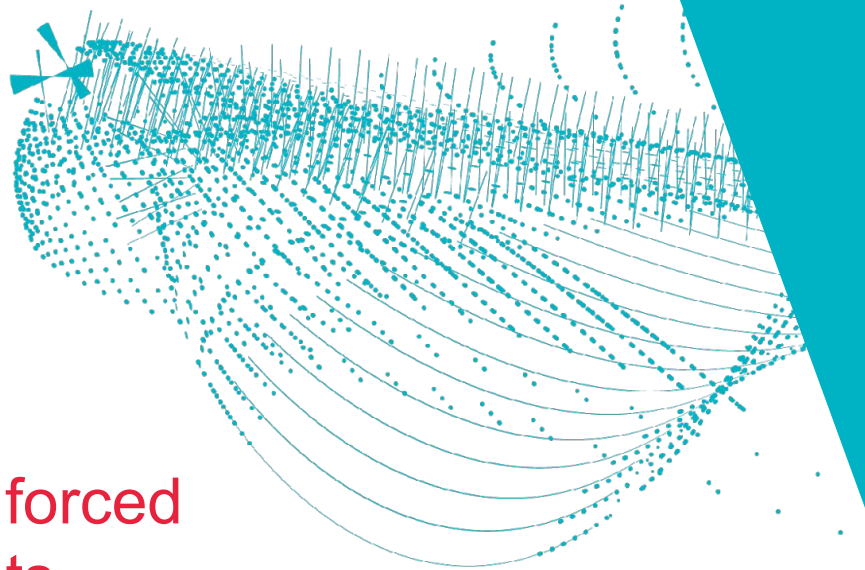


## Project I

Experimental demonstration of forced dynamic aperture measurements.

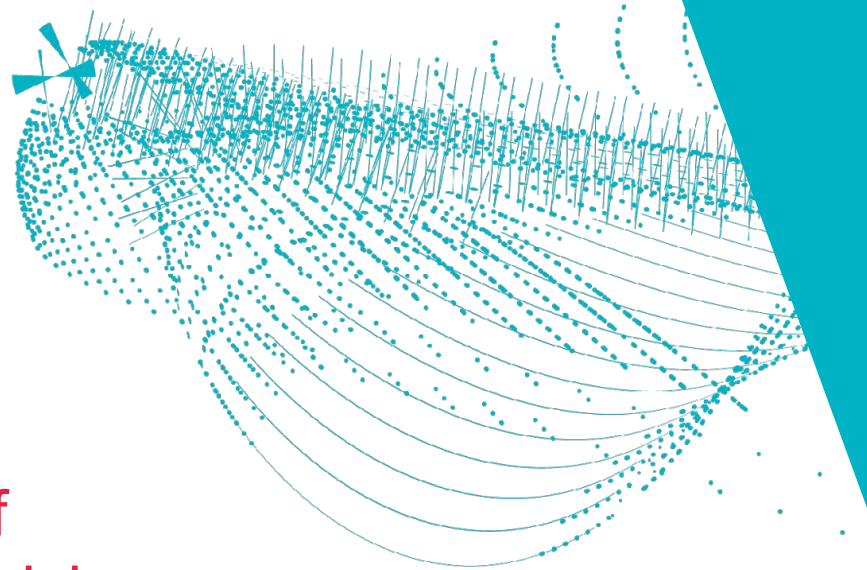
Not discussed today, but published in:

<https://journals.aps.org/prab/abstract/10.1103/PhysRevAccelBeams.22.031002>



Project II

Measurement and correction of nonlinearities with resonance driving terms (RDT)

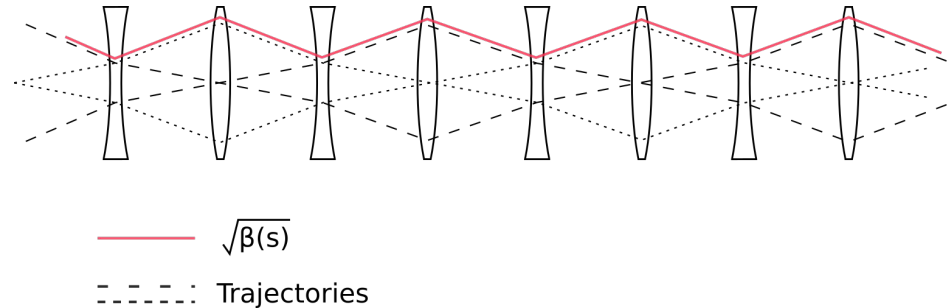
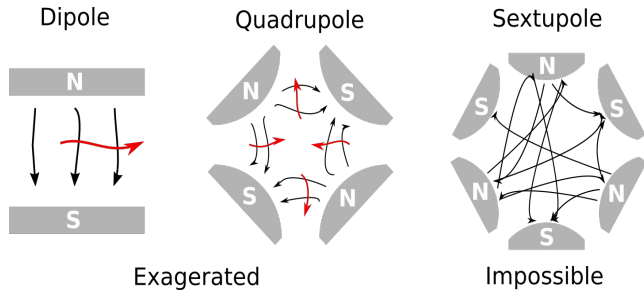


# What about nonlinear errors in the LHC?

Effect of nonlinear errors is proportional to the beta-functions

So LHC suffers from nonlinear sources at locations where:

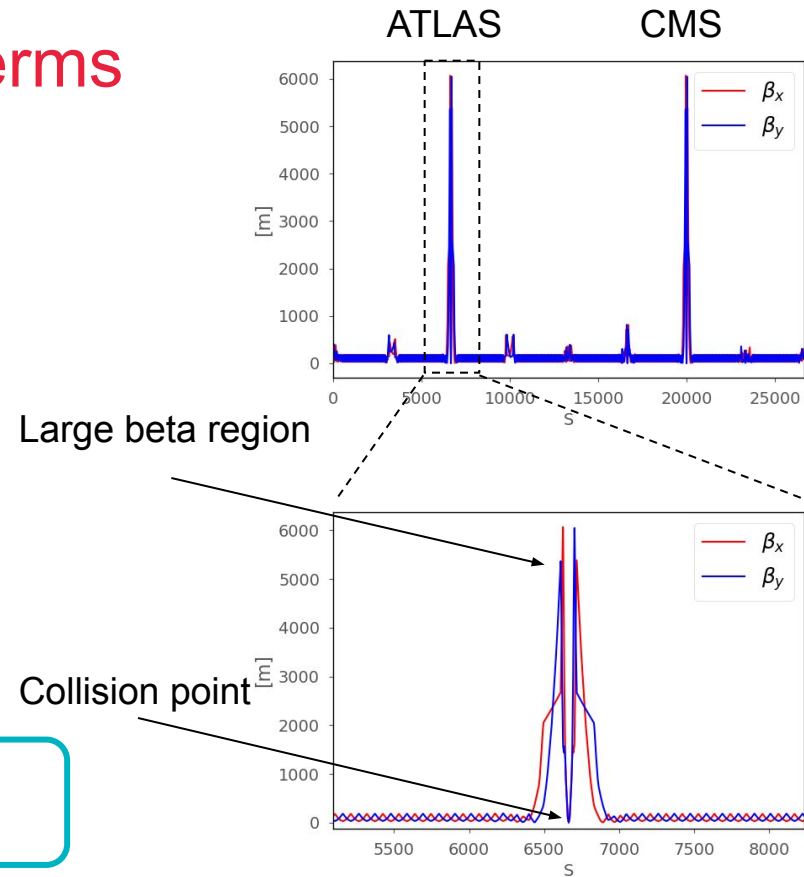
- errors are large
- or betas are large



# Correction of resonance driving terms

- Focussing regions around ATLAS & CMS are designed with huge beta-functions
  - needed for the final focus.
  - these areas are critical!
- Almost all nonlinear limitations today are due to errors in focussing regions of experiments.

These sources need to be measured and corrected



# From spectral content to resonance driving terms

Spectral content reveals all linear and nonlinear modes in the particle motion.

$f'_{jklm,H}$  are the Resonance driving terms, and  $\xi_{x,-}$  is a short notation for a big sausage equation.

$$\xi_{x,-} = |\delta_{x,-}| e^{\mp i(2\pi Q_{xD}\tau - \eta_{x,-})} - |\delta_{x,+}| e^{\pm i(2\pi Q_{xD}\tau + \eta_{x,+})}$$

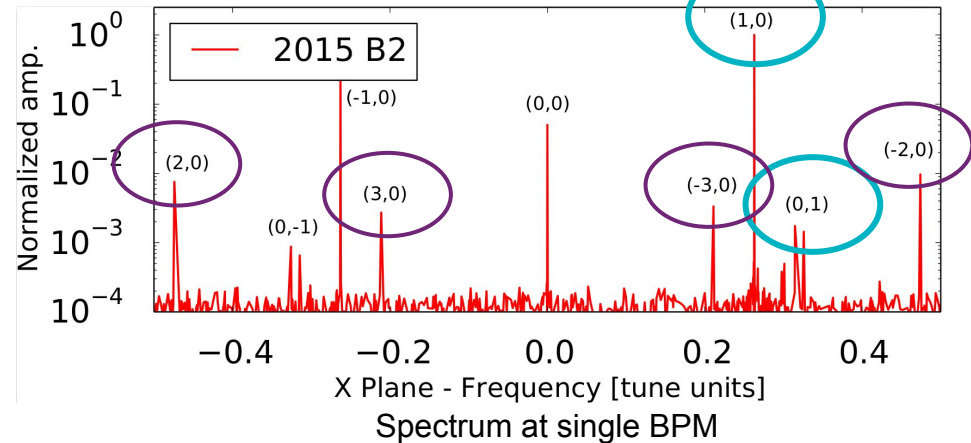
$$-2i \sum_{jklm} f'_{jklm,H} |\delta_{x,-}|^{j-1+k} |\delta_{y,-}|^{l+m}$$

$$\times e^{i2\pi\{[k-j+1]Q_{xD}\tau + [m-l]Q_{yD}\tau\}}$$

$$\times e^{i\{[k-j+1]\eta_{x,-} + [m-l]\eta_{y,-}\}}.$$

Nonlinear modes

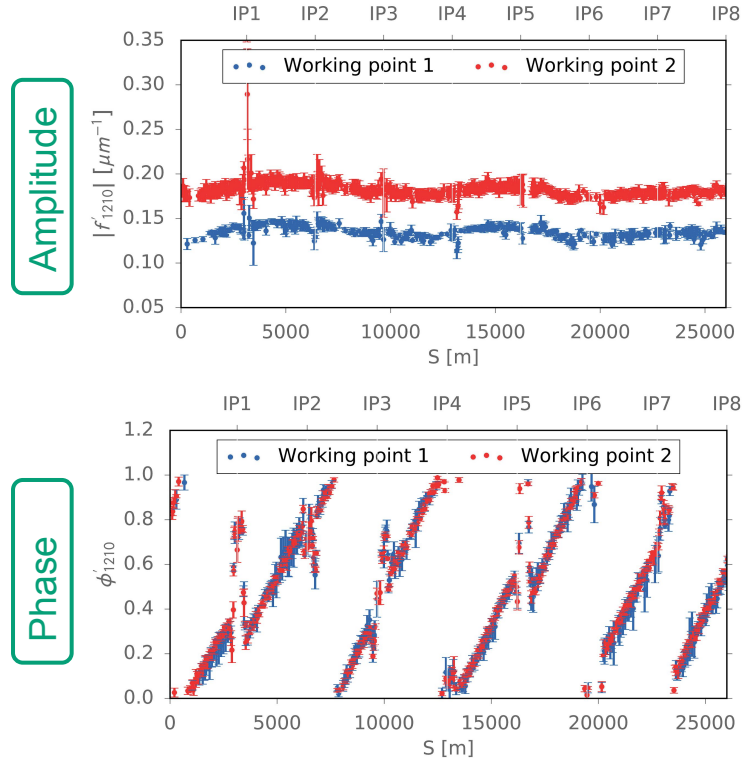
Linear modes





# The procedure for correcting using RDTs

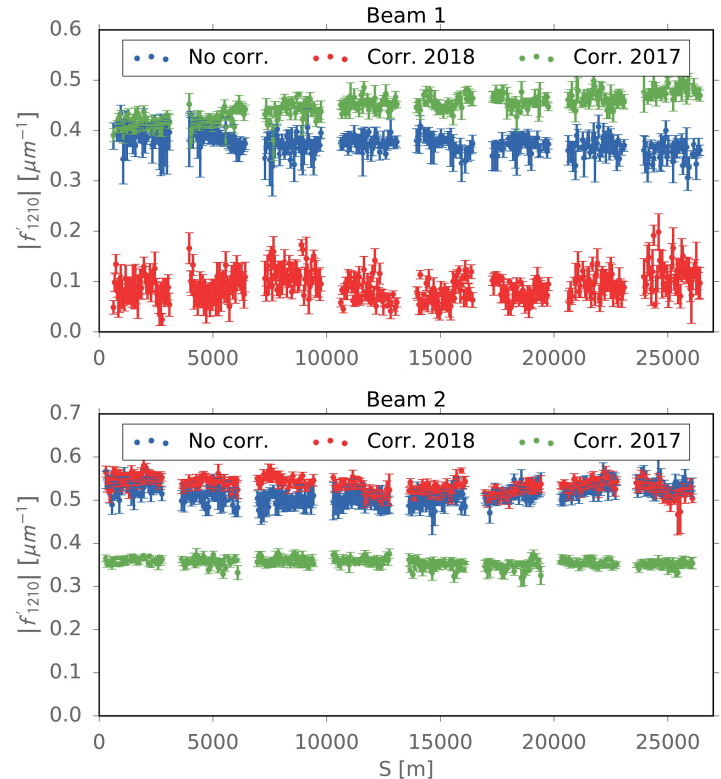
1. Measure amplitude and phase of  $f'_{jklm,H}$
2. Match model to measured values
3. Find magnet strengths of dedicated correction magnets in insertion regions
4. Check experimentally



# Corrections of Resonance driving terms

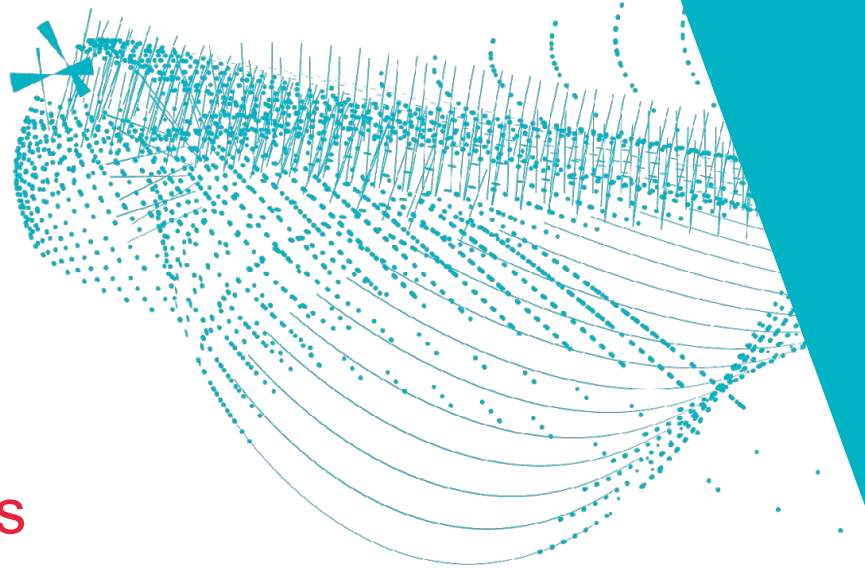
Quite successful!

- First correction of RDTs in the LHC
- First correction of skew octupolar sources in a synchrotron
- First correction of nonlinear sources using ac dipoles
- *Still some theoretical aspects that are challenging*



Project III

Measurements of nonlinearities  
arising from colliding beams



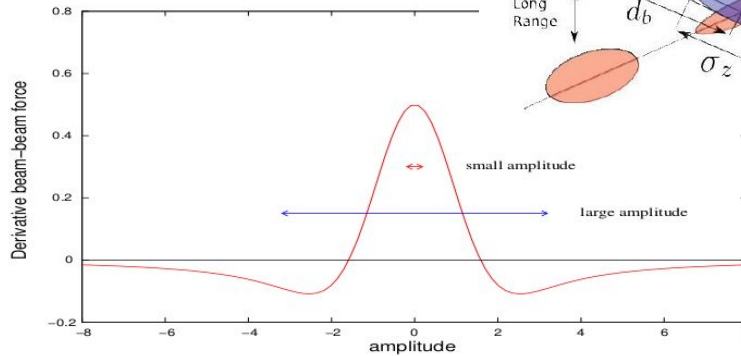
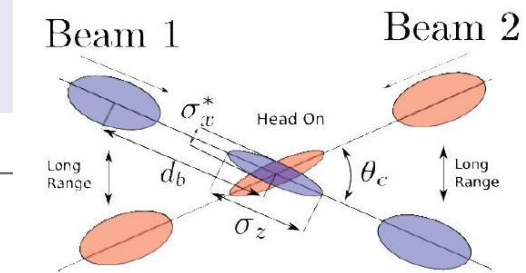
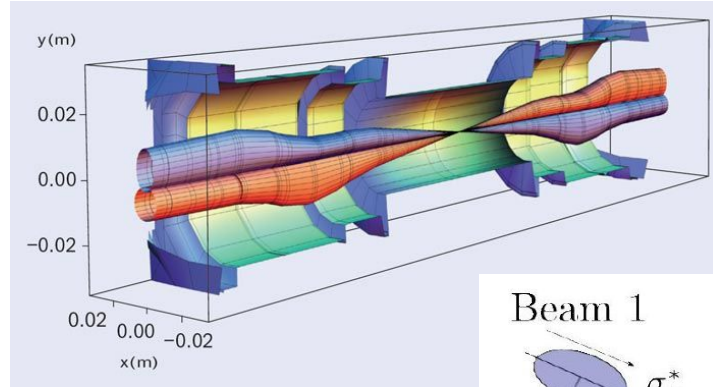
# Beam-beam effect coming from colliding beams

What happens when colliding?

The other Gaussian beam will cause a huge force on the particles

- Big distortion of optics
- Very nonlinear
- Called Beam-beam force

This is one of the next big limitations for operation of future colliders.

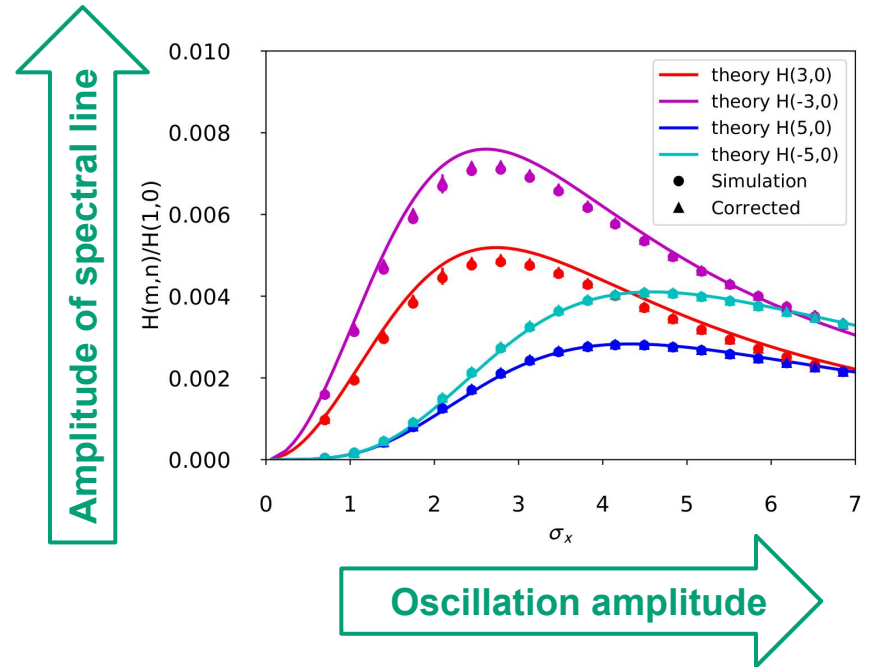


# How to apply the RDT method to this problem?

Strength of nonlinearity is dependent on amplitude of oscillation.

- So need a new theoretical approach

Focus on spectral line amplitude instead of specific RDTs.

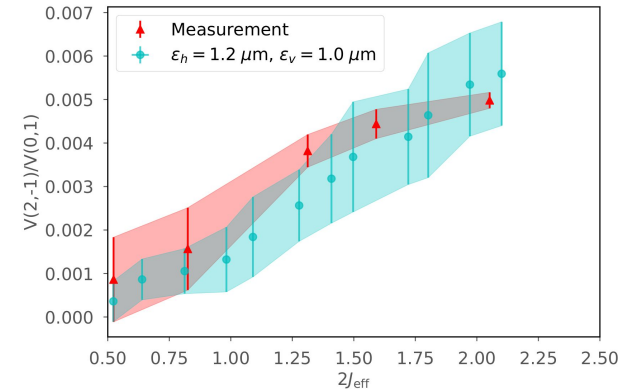
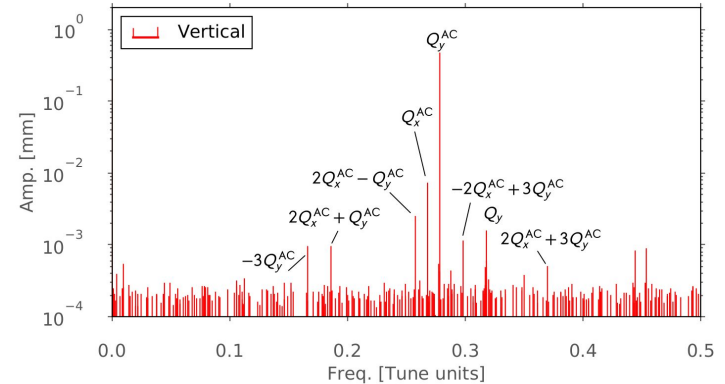




# First measurement of beam-beam RDTs in an accelerator

Quite successful!

- Very good agreement between theory and simulation
- First ever measurements of Beam-beam RDTs in an accelerator
- Good agreement between models and measurements



# Thank you

(Hopefully I managed to make some things clear)