



Automated Parallel Calculation of Collaborative Statistical Models in RooFit

Patrick Bos

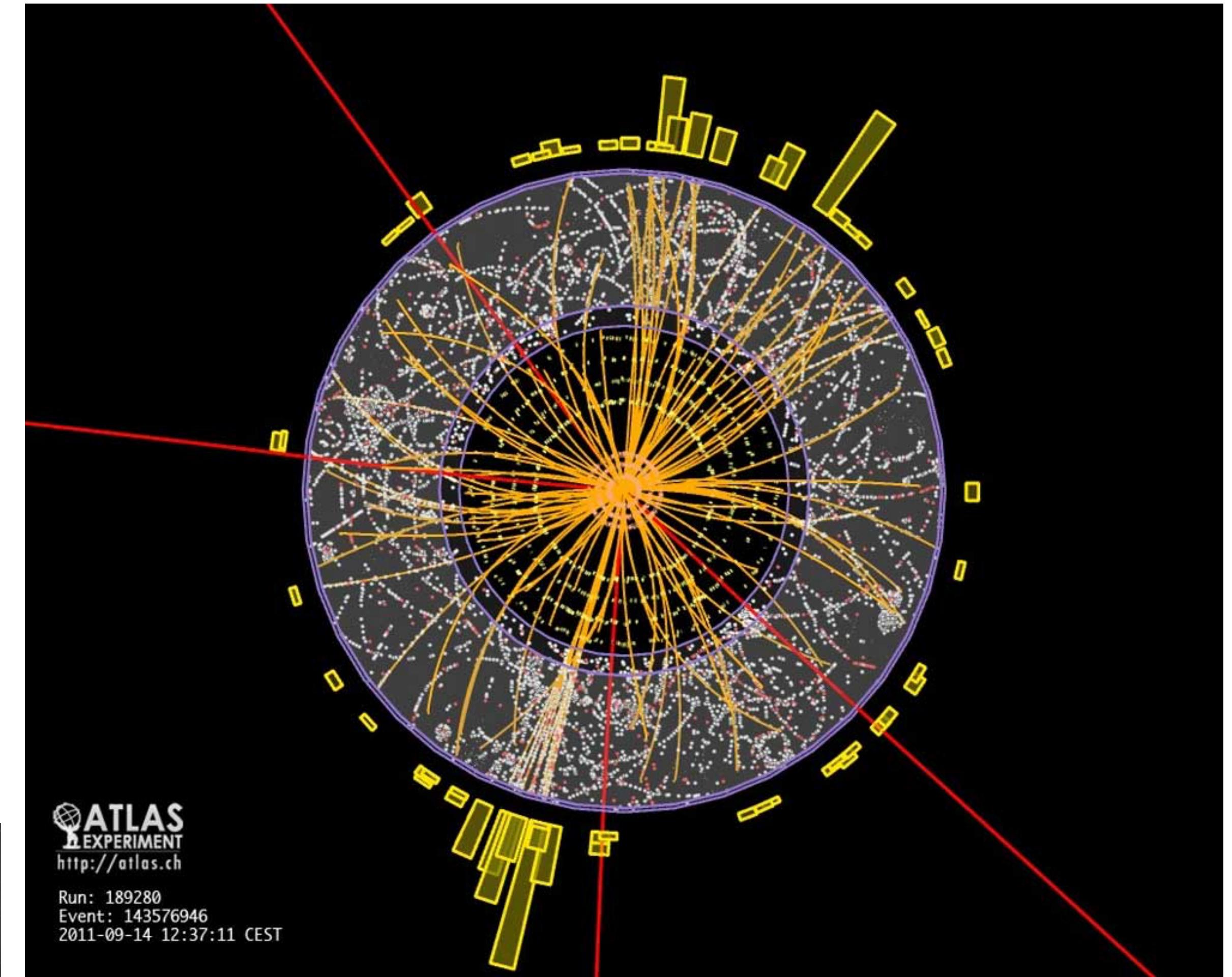
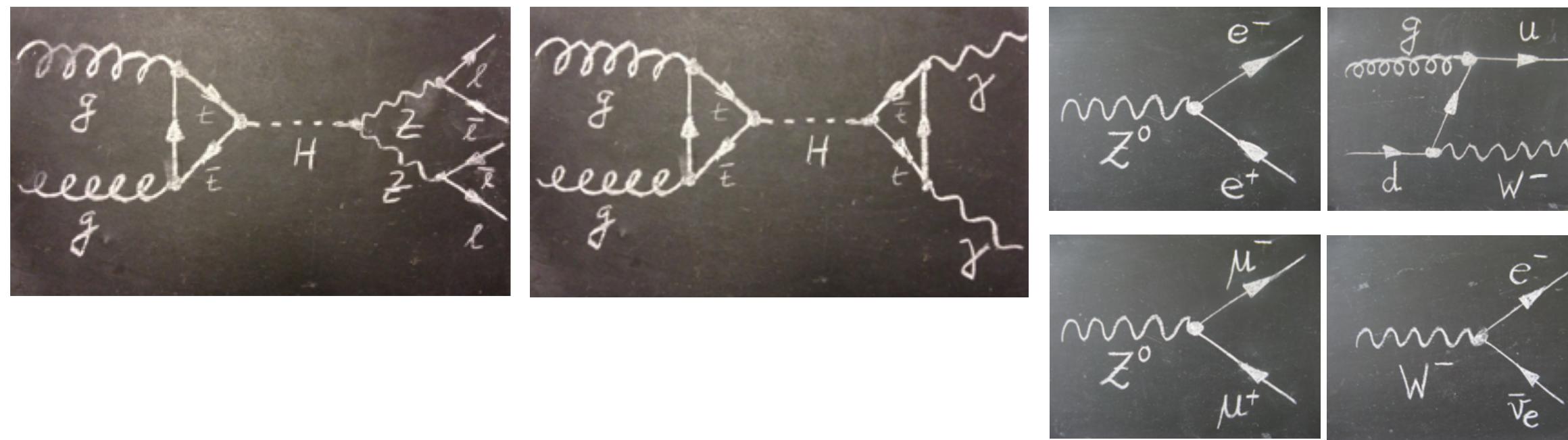
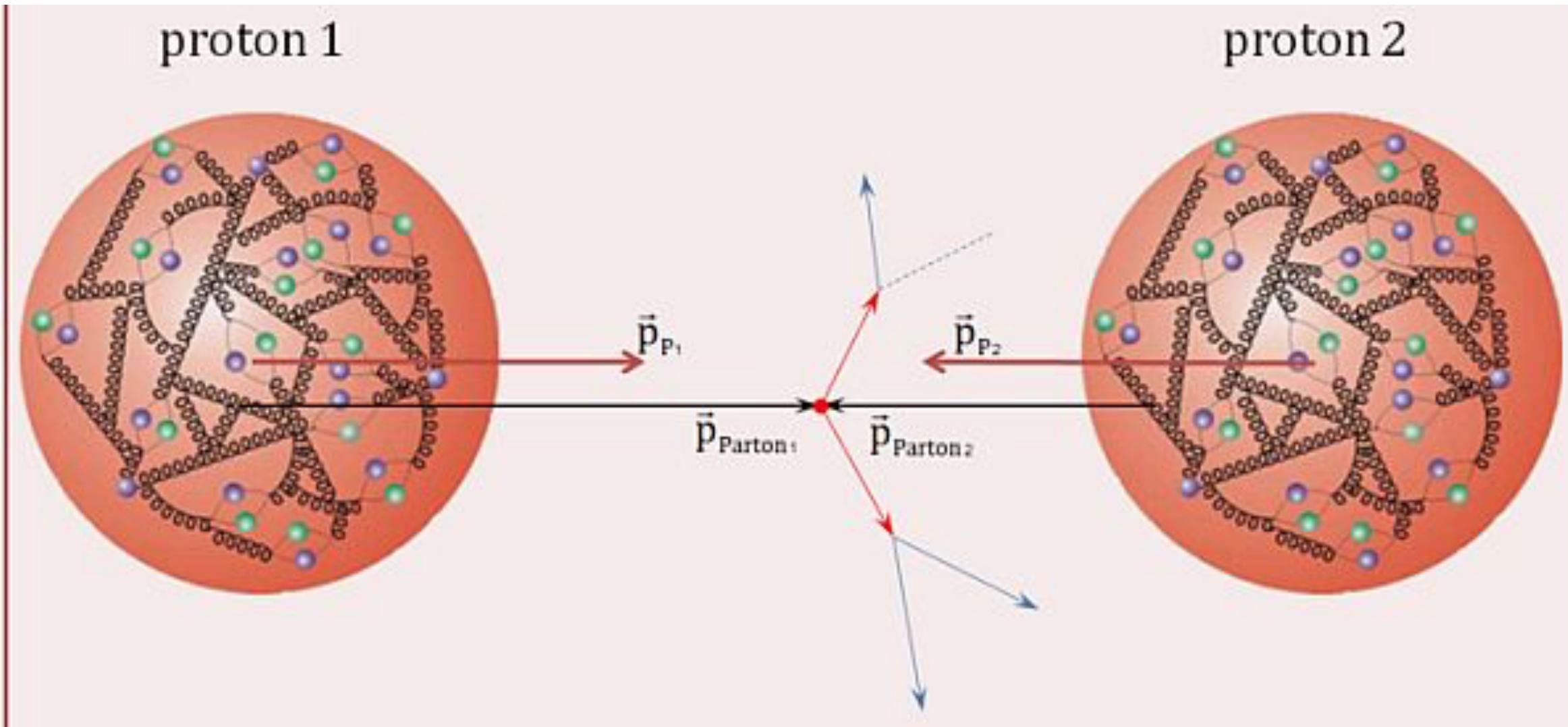
IEEE eScience, Amsterdam, 31 October 2018

Physics: Wouter Verkerke (PI), Vince Croft, Carsten Burgard

eScience: Patrick Bos (yours truly), Inti Pelupessy, Jisk Attema



High energy proton collisions



LHC @ CERN

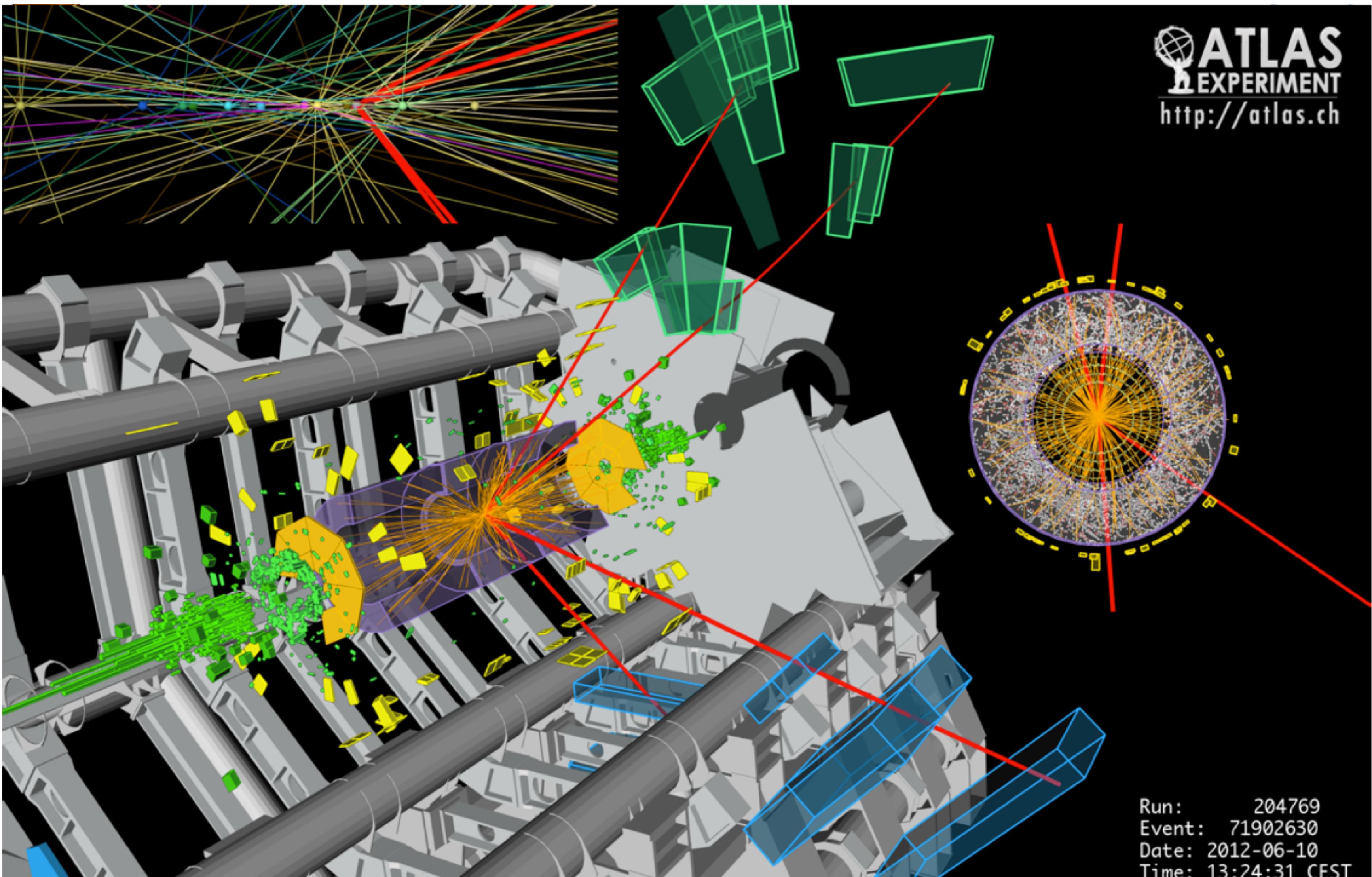
- ATLAS, CMS
- LHCb

10 PB/yr p-p

Reduced to kB-

MBs binned &
unbinned

events



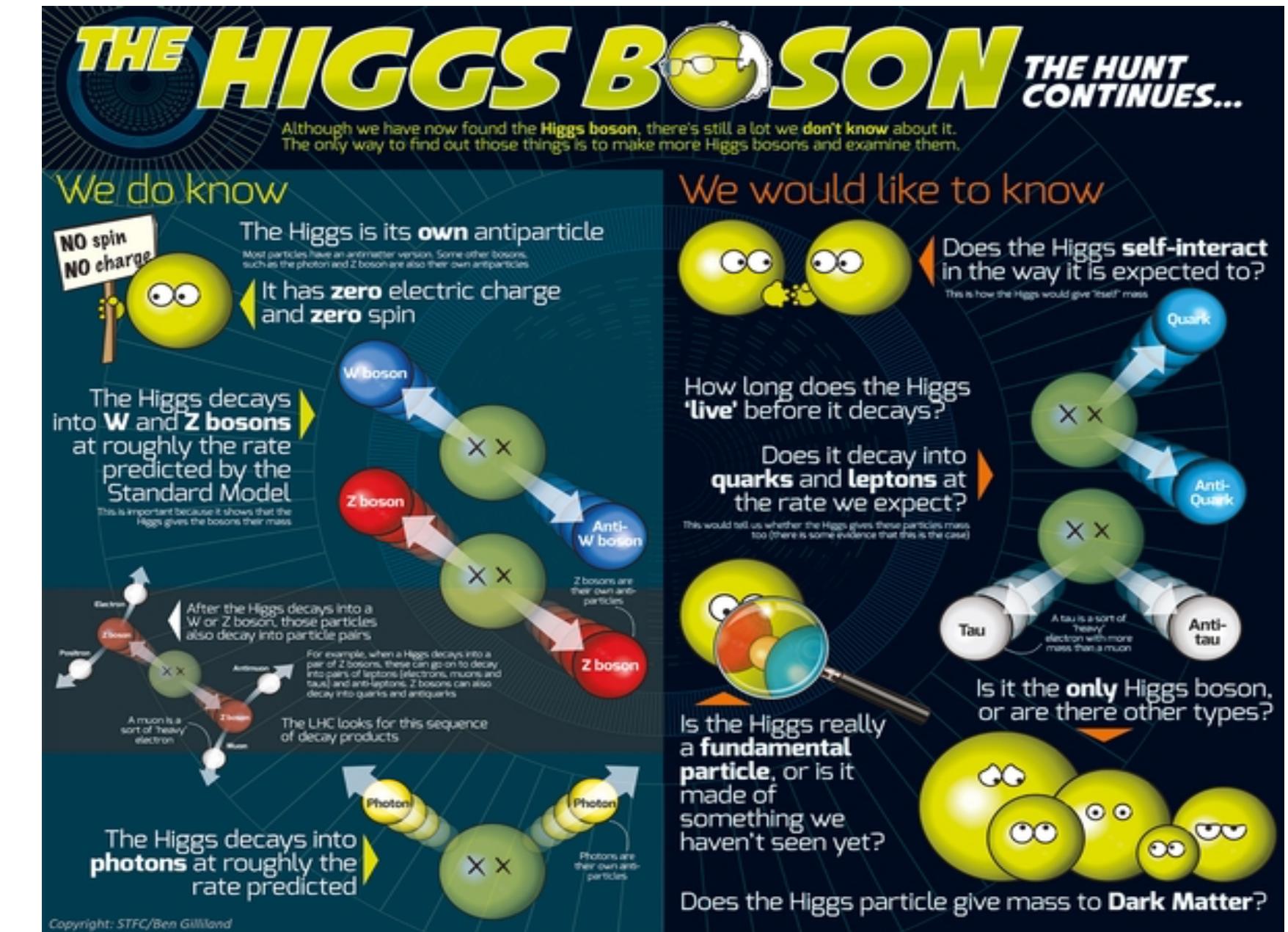
Research questions

Higgs properties

Physics beyond the Standard Model

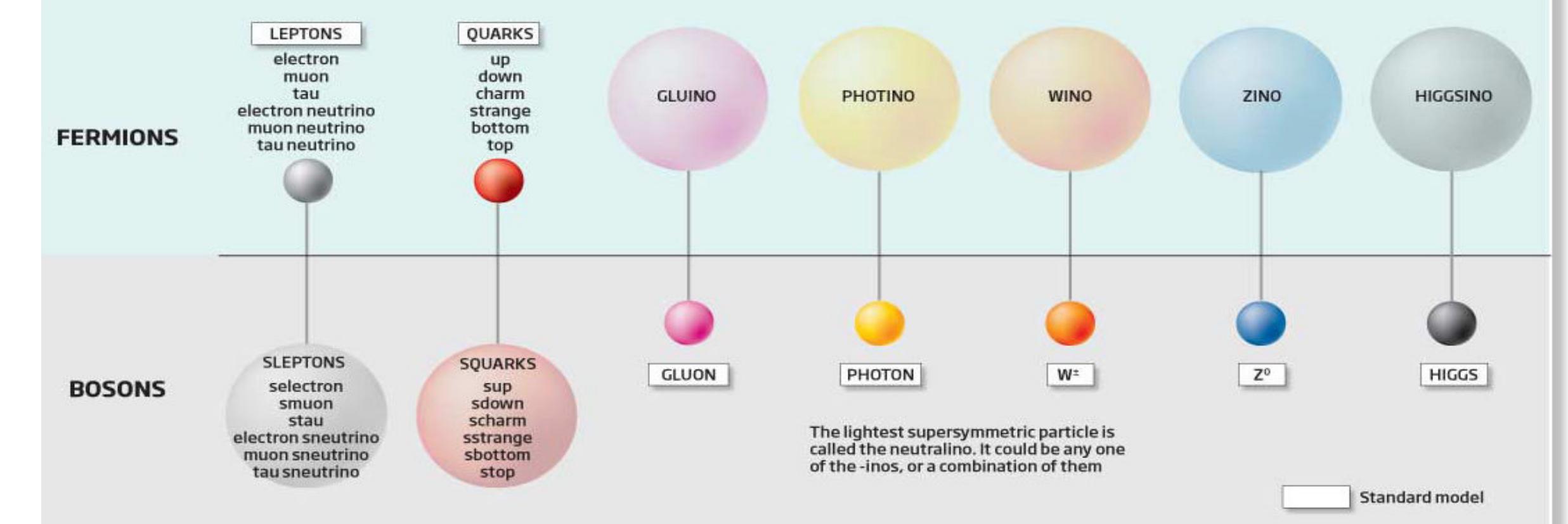
- Supersymmetry?
- Dark matter?

- . . .



Particle zoo

Particles are divided into two families called bosons and fermions. Among them are groups known as leptons, quarks and force-carrying particles like the photon. Supersymmetry doubles the number of particles, giving each fermion a massive boson as a super-partner and vice versa. The LHC is expected to find the first supersymmetric particle



Standard model

RooFit: Collaborative Statistical Modeling

Collaborative Statistical Modeling

- RooFit: build models together
 - Teams 10-100 physicists
 - Collaborations ~3000
 - ~100 teams
 - Exascale collaboration
 - 10^{15} synaptic connections $\times 10^3$ brains = 10^{18} (exa)
 - 1 goal
 - Pretty impressive to an outsider



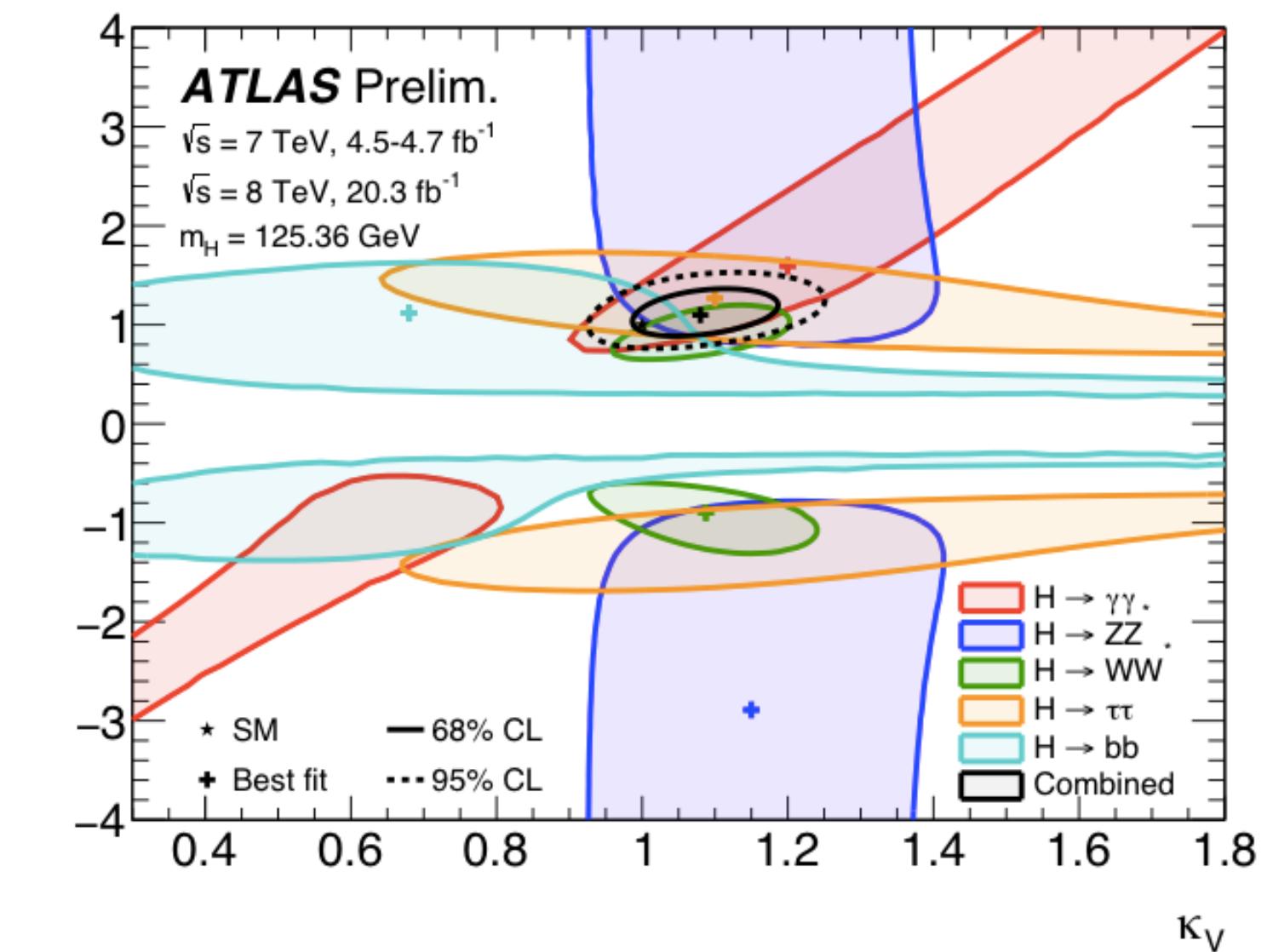
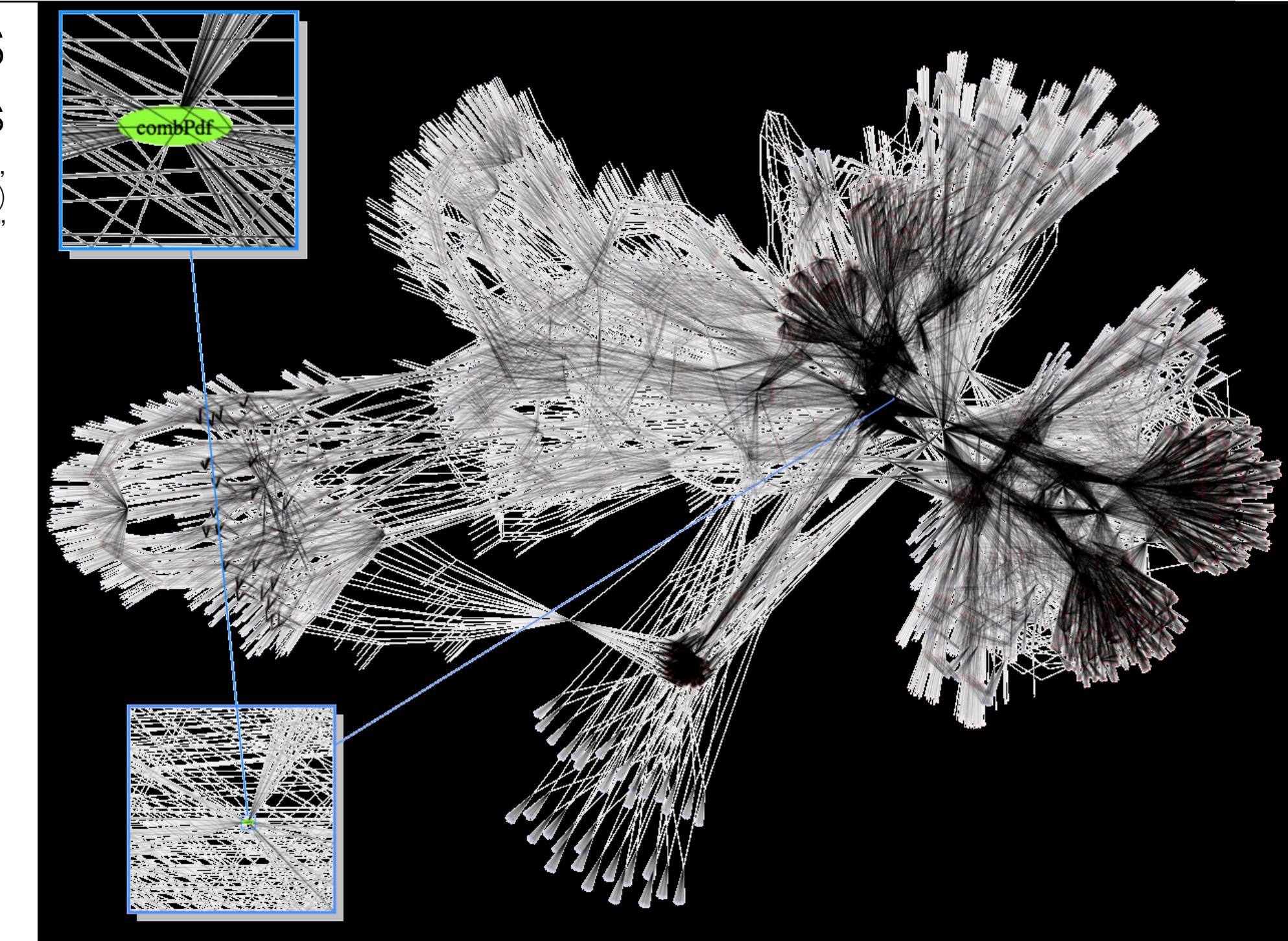
Collaborative Statistical Modeling with RooFit

Higgs @ ATLAS
20k+ nodes, 125k hours
Expression tree of C++ objects for mathematical components (variables, operators, functions, integrals, datasets, etc.)
Couple with data, event “observables”

Making RooFit faster ($\sim 30x$; $\sim h \rightarrow \sim m$)

- More efficient collaboration
 - Faster iteration/debugging
 - Faster feedback between teams
- Next level physics modeling ambitions, retaining **interactive workflow**
 1. Complex likelihood models, e.g.
 - a) Higgs fit to all channels, ~ 200 datasets, $O(1000)$ parameter, now $O(\text{few})$ hours
 - b) EFT framework: again 10-100x more expensive
 2. Unbinned ML fits with very large data samples
 3. Unbinned ML fits with MC-style numeric integrals

exascale complexity!



Goals and Design: Make fitting in RooFit faster
using automated parallel calculation

Making fitting in RooFit faster: how?

Serial:

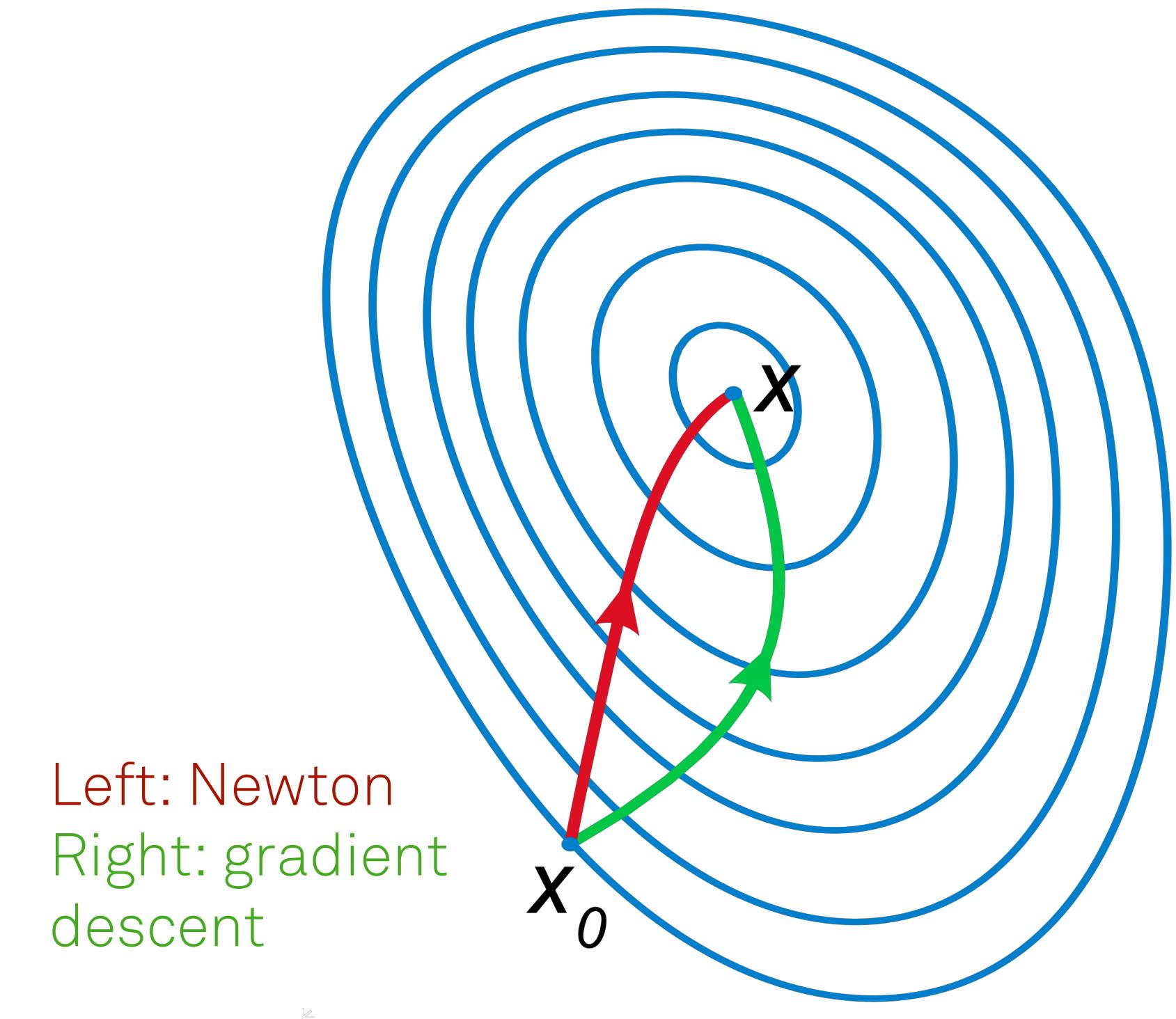
benchmarks show no obvious bottlenecks

RooFit already highly optimized (pre-calculation/memoization, MPFE)

Parallel

Minuit: minimize PDF $f(x; p)$:

- Quasi-Newton **MIGRAD** method
- Gradient + line-search:
 - gradient for N parameters p : $\frac{df}{dp} \approx \frac{f(p-dp)-f(p)}{dp}$
 - line-search: descend along gradient direction



$2N f$ calls \rightarrow parallelize $\frac{df}{dp}$
 $2-3 f$ calls \rightarrow parallelize f

Faster fitting: (how) can we do it?

Levels of parallelism

- 1. Gradient (parameter partial derivatives) in minimizer
- 2. Likelihood (f)

- 3. Integrals (normalization) &

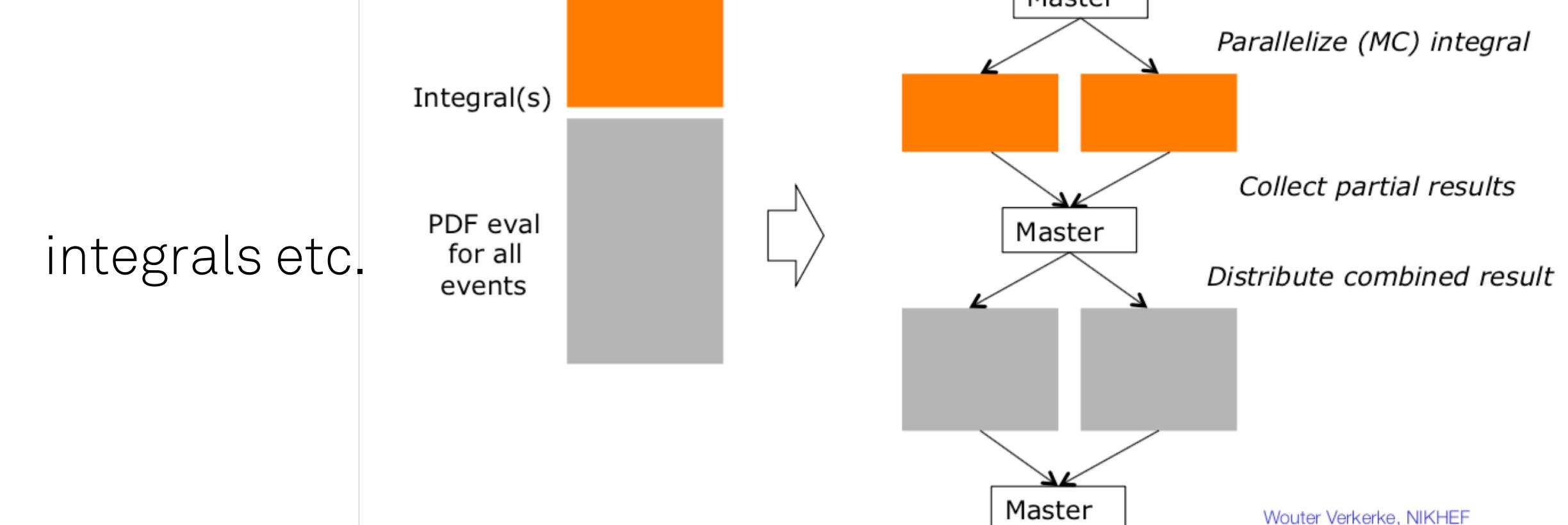
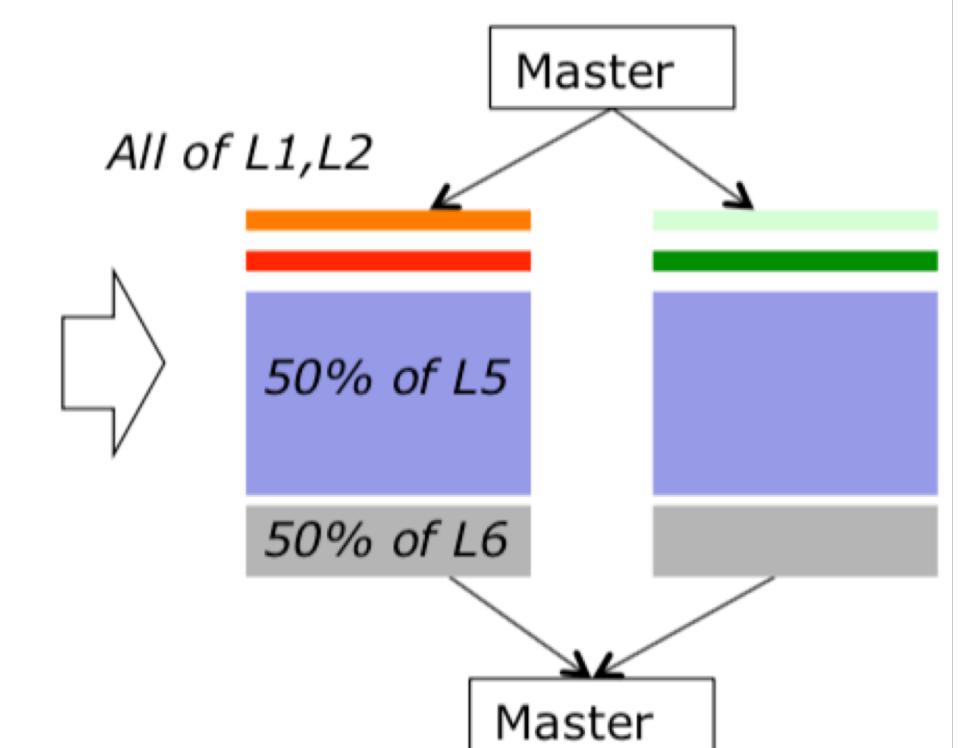
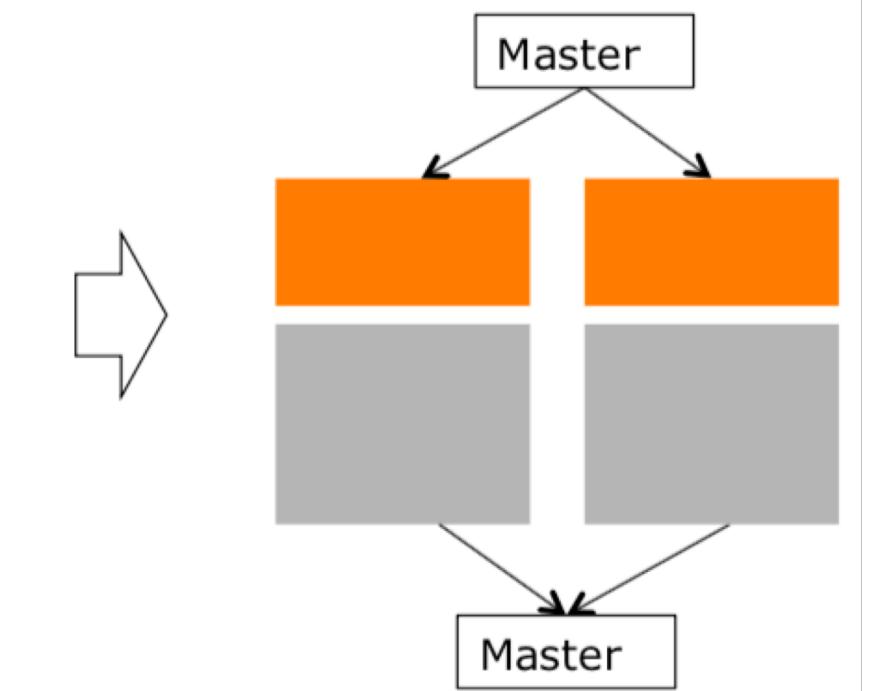
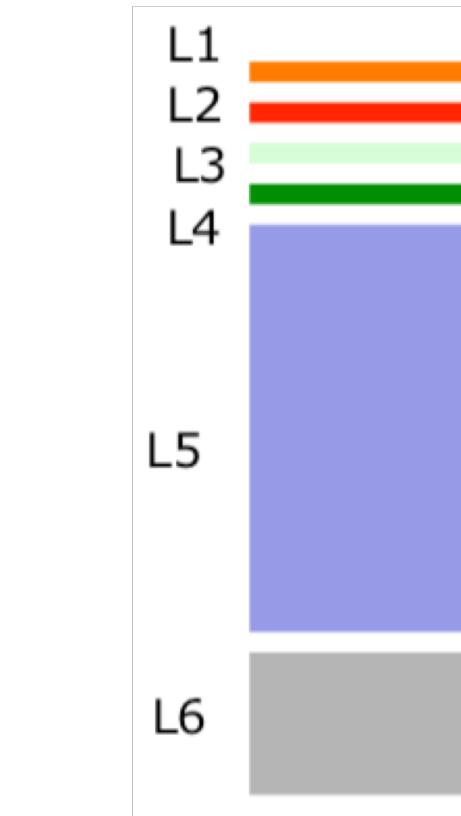
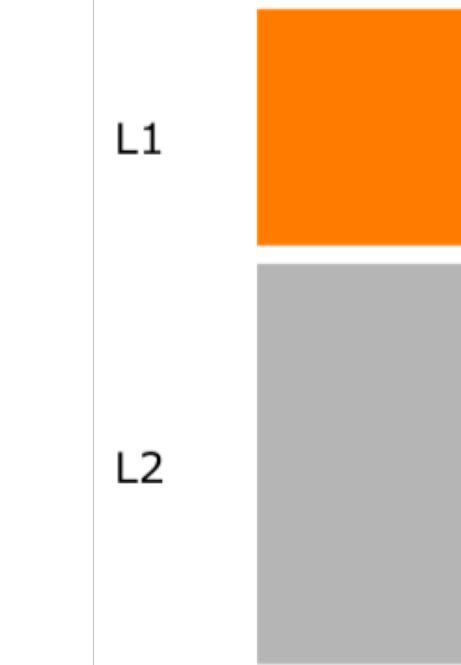
other expensive shared components

“Vector”

likelihood:
events

likelihood:
(unequal)
components

integrals etc.

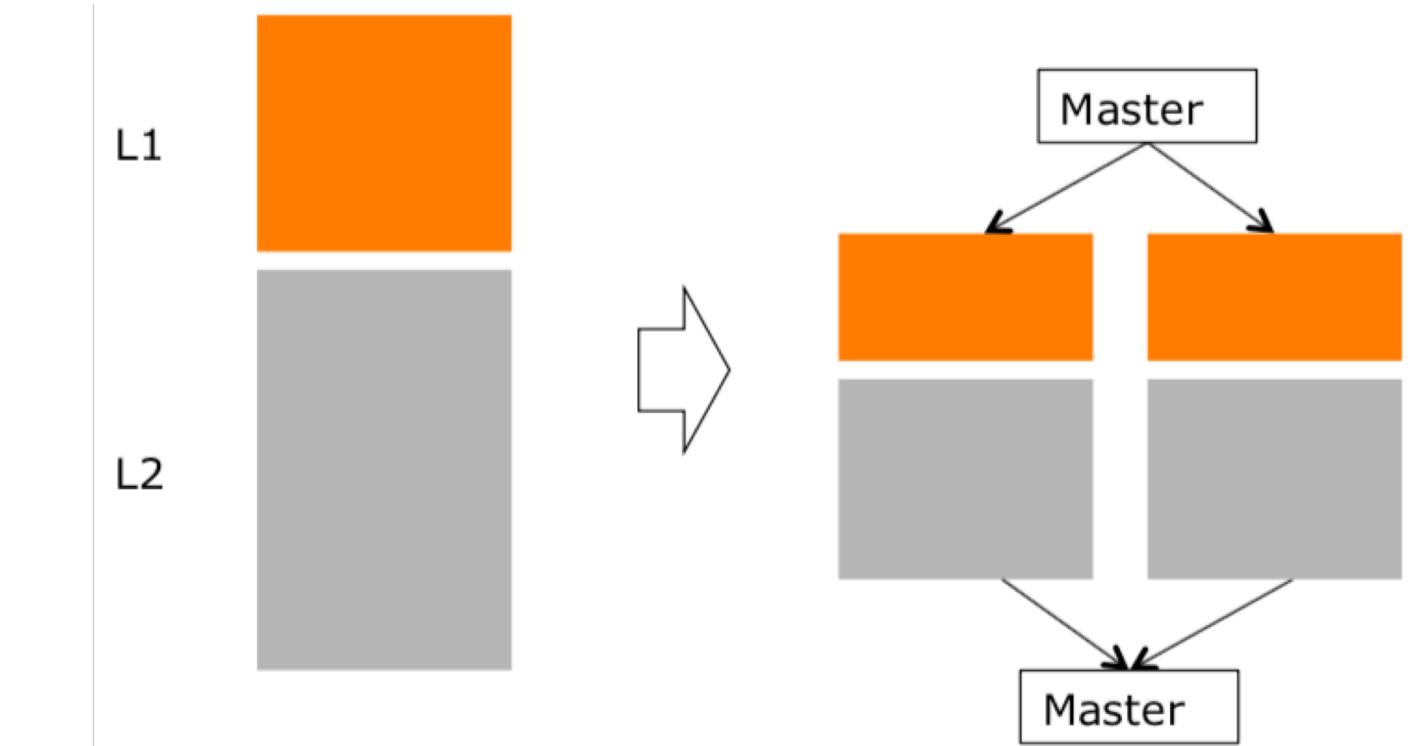


Faster fitting: (how) can we do it?

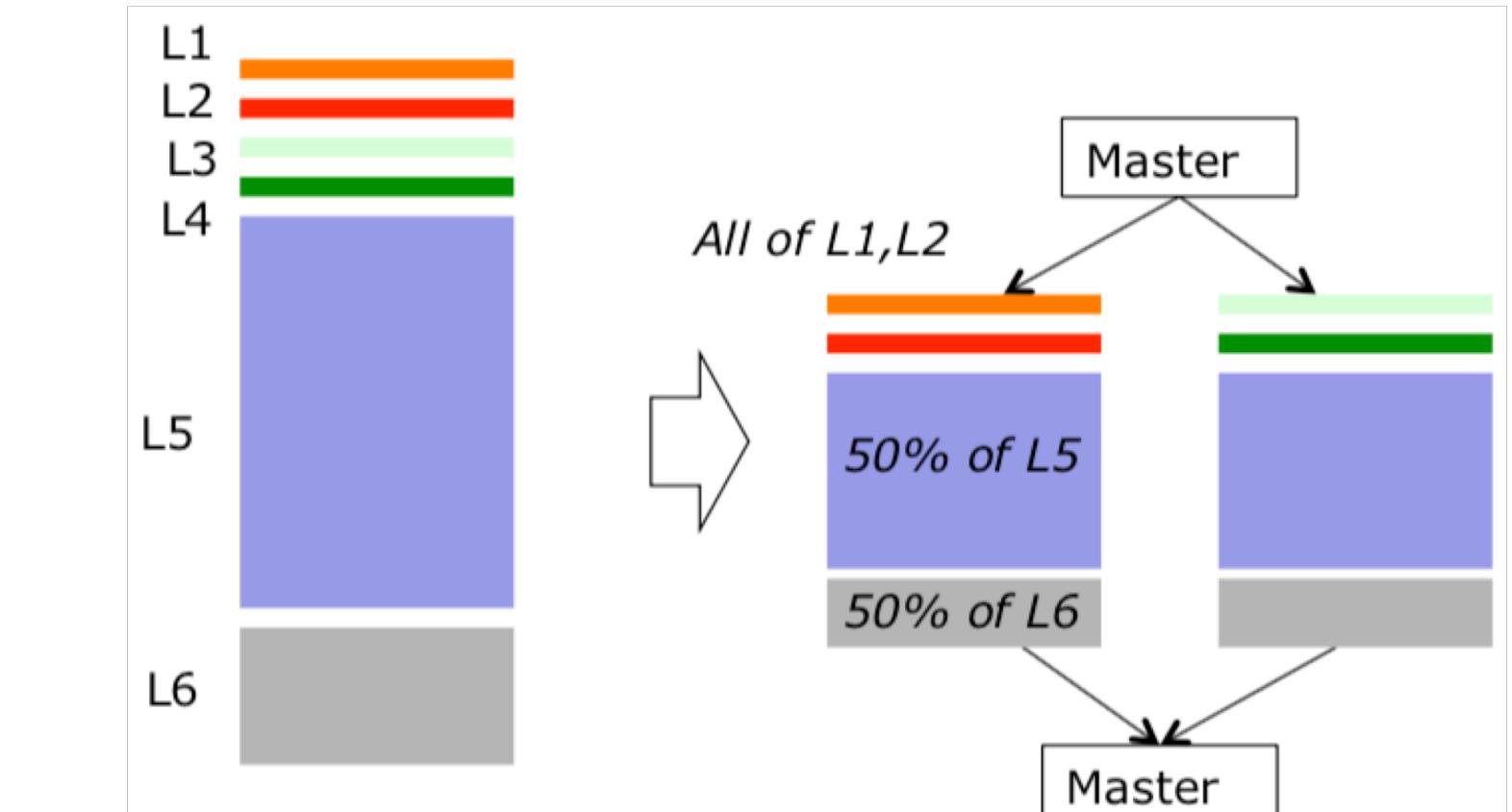
Heterogeneous: sizes, types

- Multiple strategies
 - How to split up?
 - Small components → need low latency/overhead
 - Large components as well...
 - Run time depends on optimizations, differs per parameter, hard to predict
 - How to divide over cores?
 - Load balancing → task-based approach: work stealing
 - ... both for likelihood-level and gradient-level parallelization

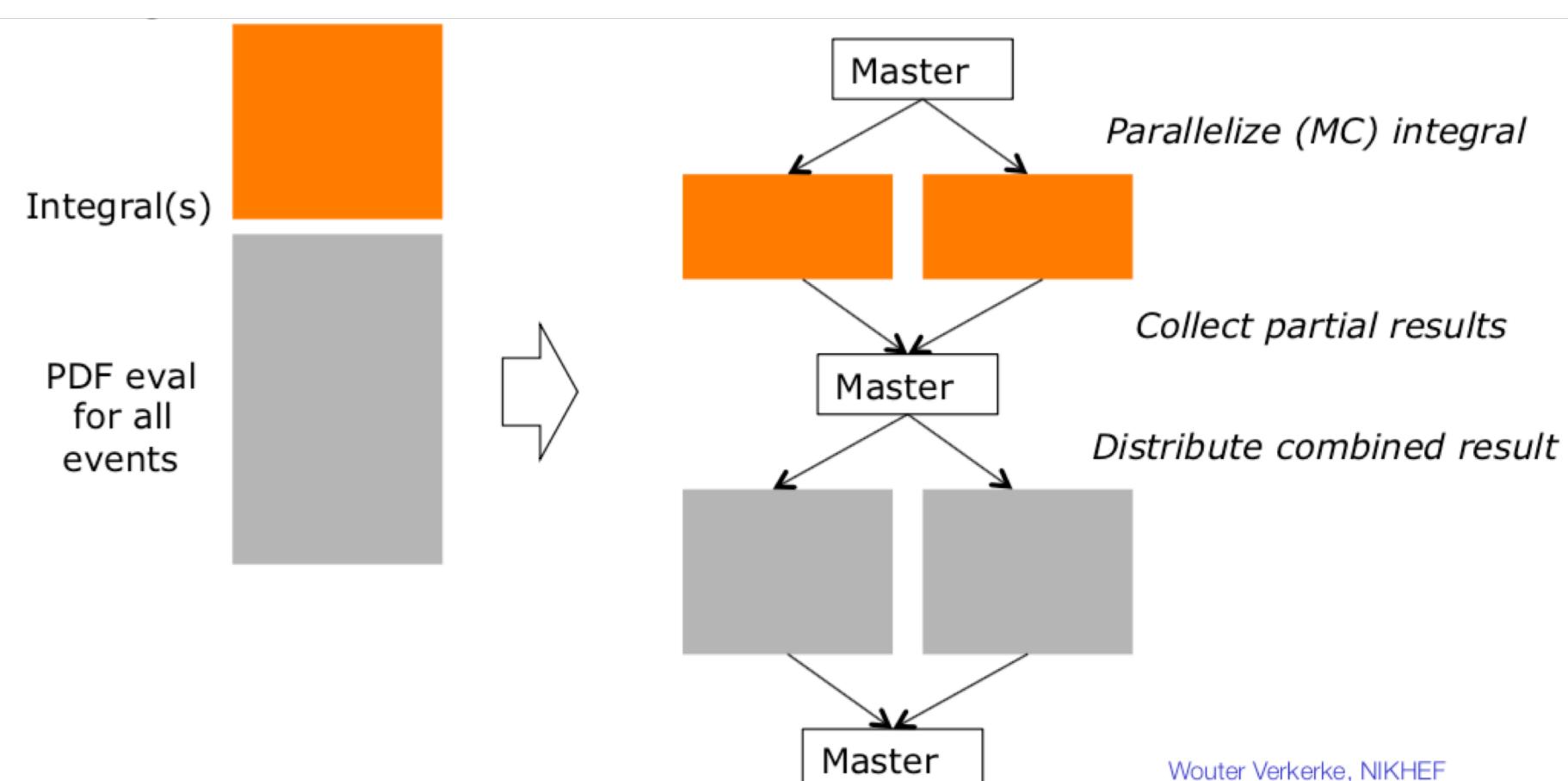
likelihood:
events



likelihood: (unequal) components



integrals etc



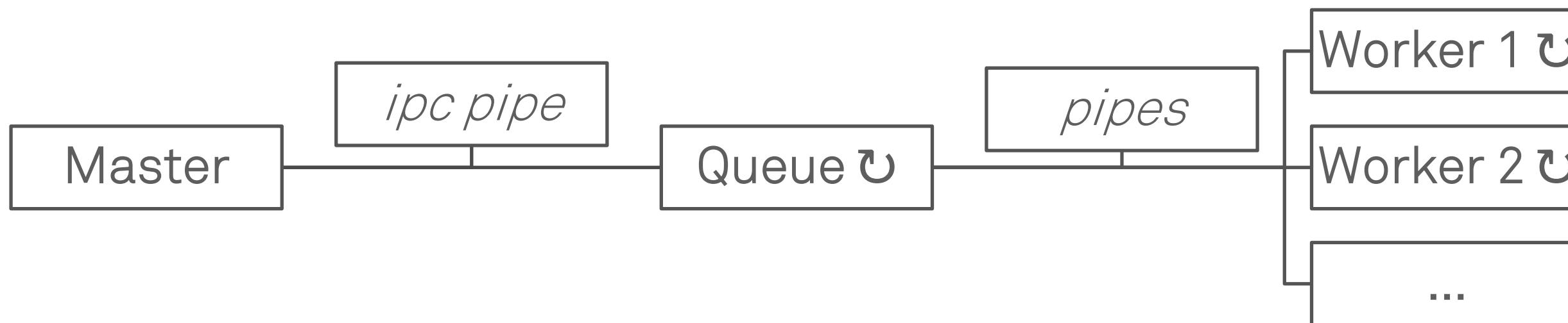
Design: MultiProcess task-stealing framework

Task-stealing, worker pool, executes Job tasks

Job = likelihood component, $\frac{df}{dp}$, ...

No threads, process-based:

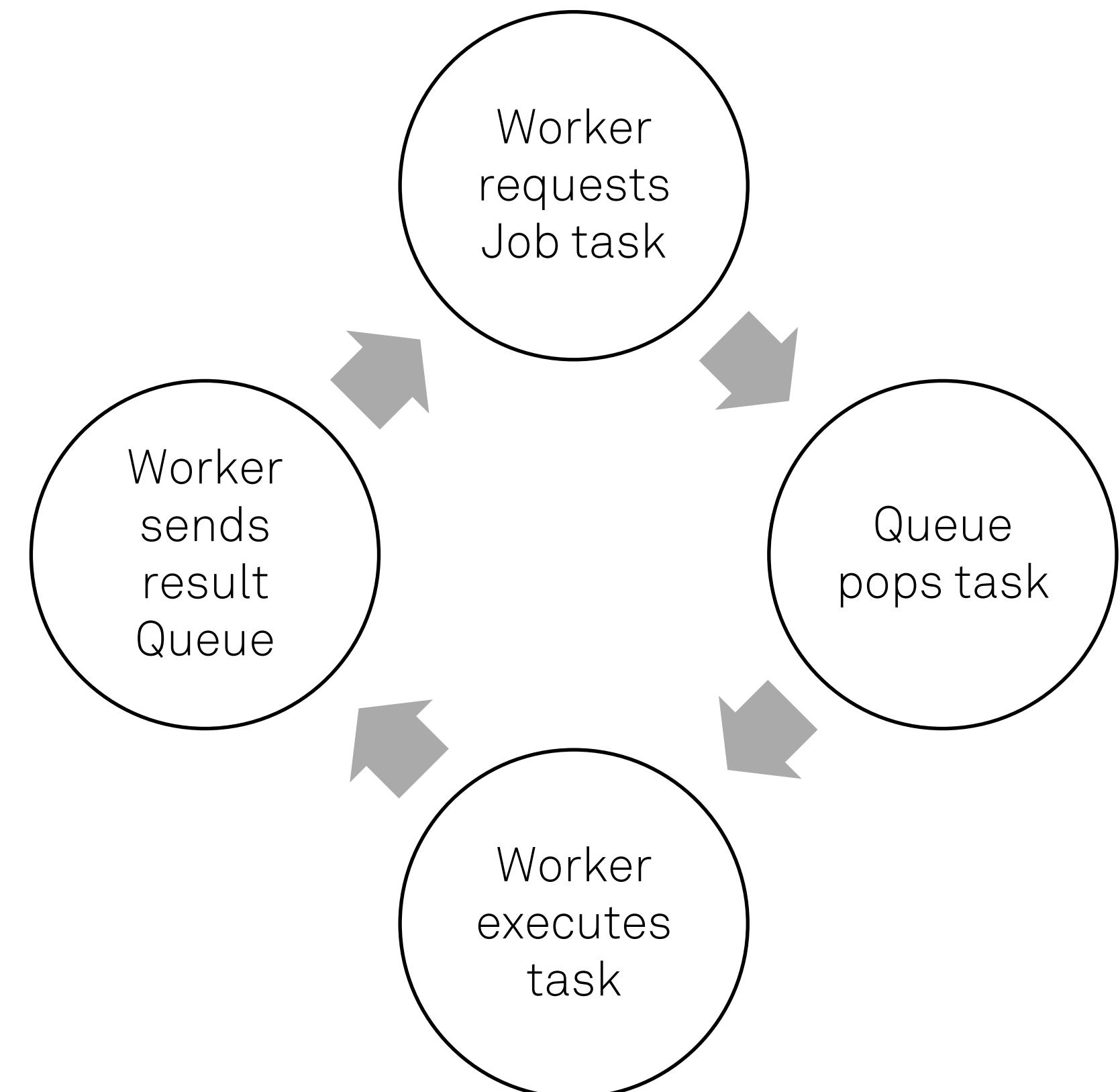
BidirMMapPipe handles fork, mmap, pipes



Master: main RooFit process, submits Jobs to queue, waits for results
(or does other things in between)

Queue loop: act on input from Master or Workers (mainly to avoid loop
in Master / user code) --- collect/distribute Jobs and results

Worker loop:



...until Job done

then Queue sends results
back to Master on request

Parallel performance (MPFE & MP)

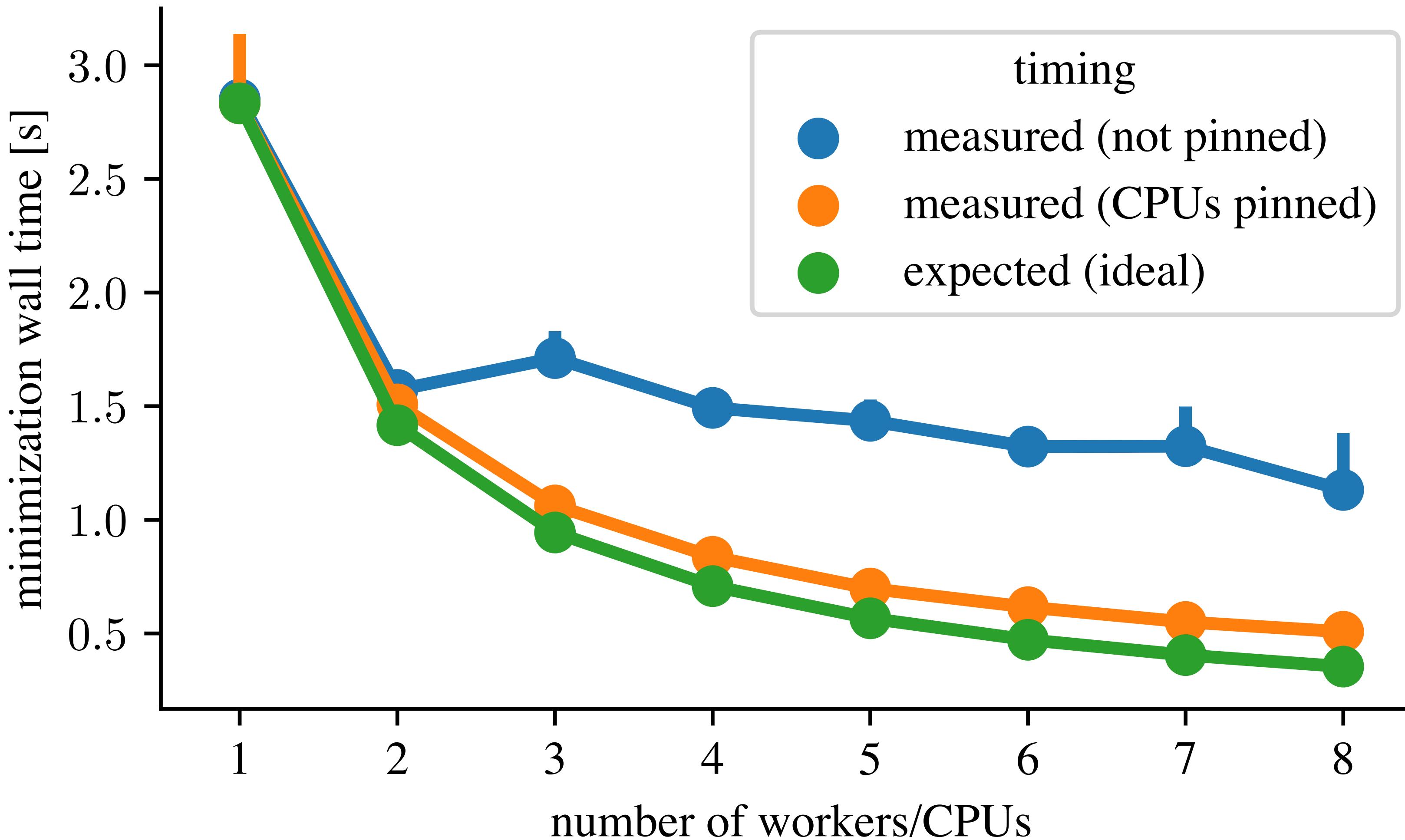
Likelihood fits (unbinned, binned)

Gradients

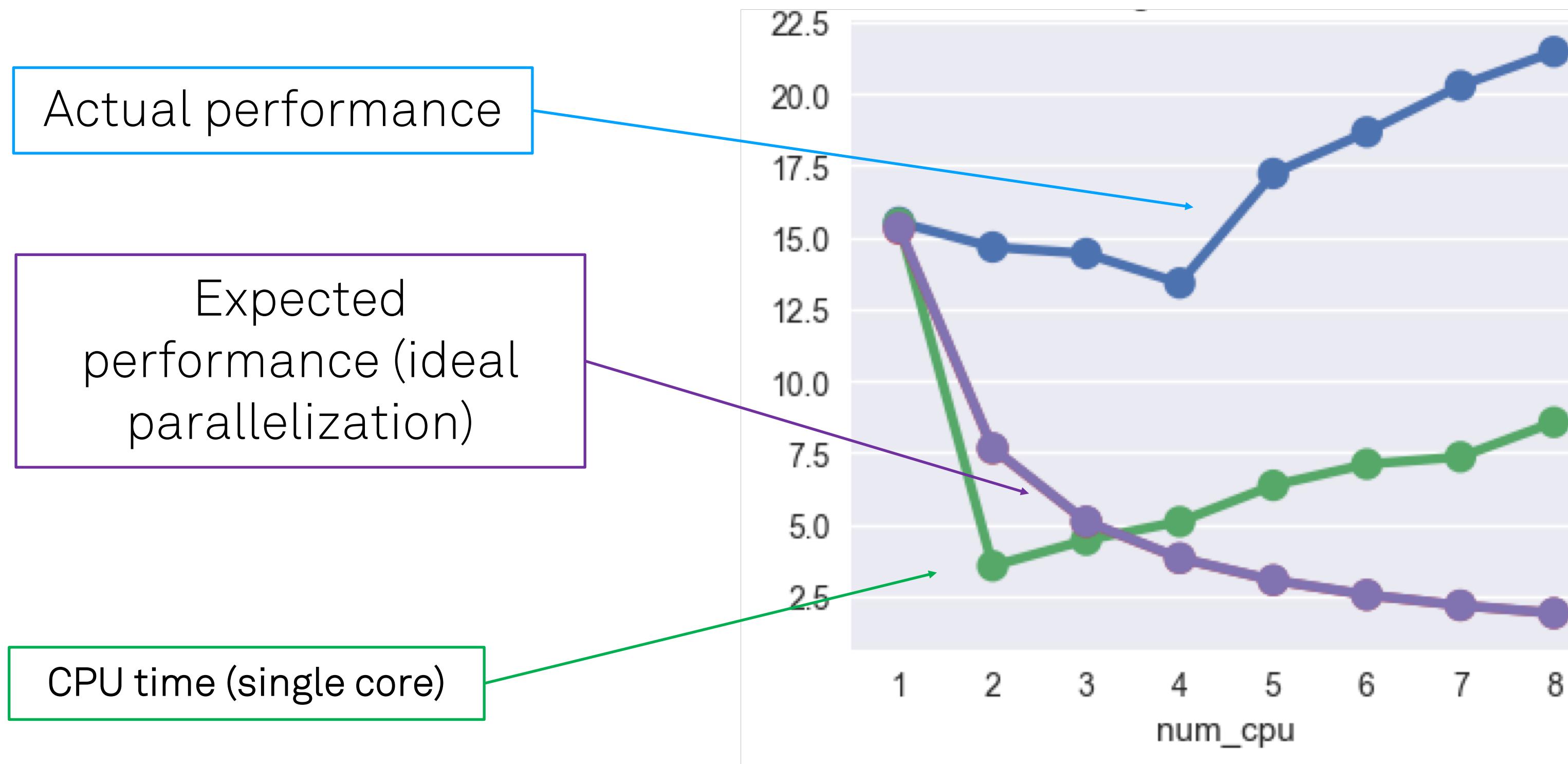
Run-time vs N(cores): simple N-dim Gaussian, many events

Before: max ~2x

Now (with CPU pinning fixed):
max ~20x (more for larger fits)



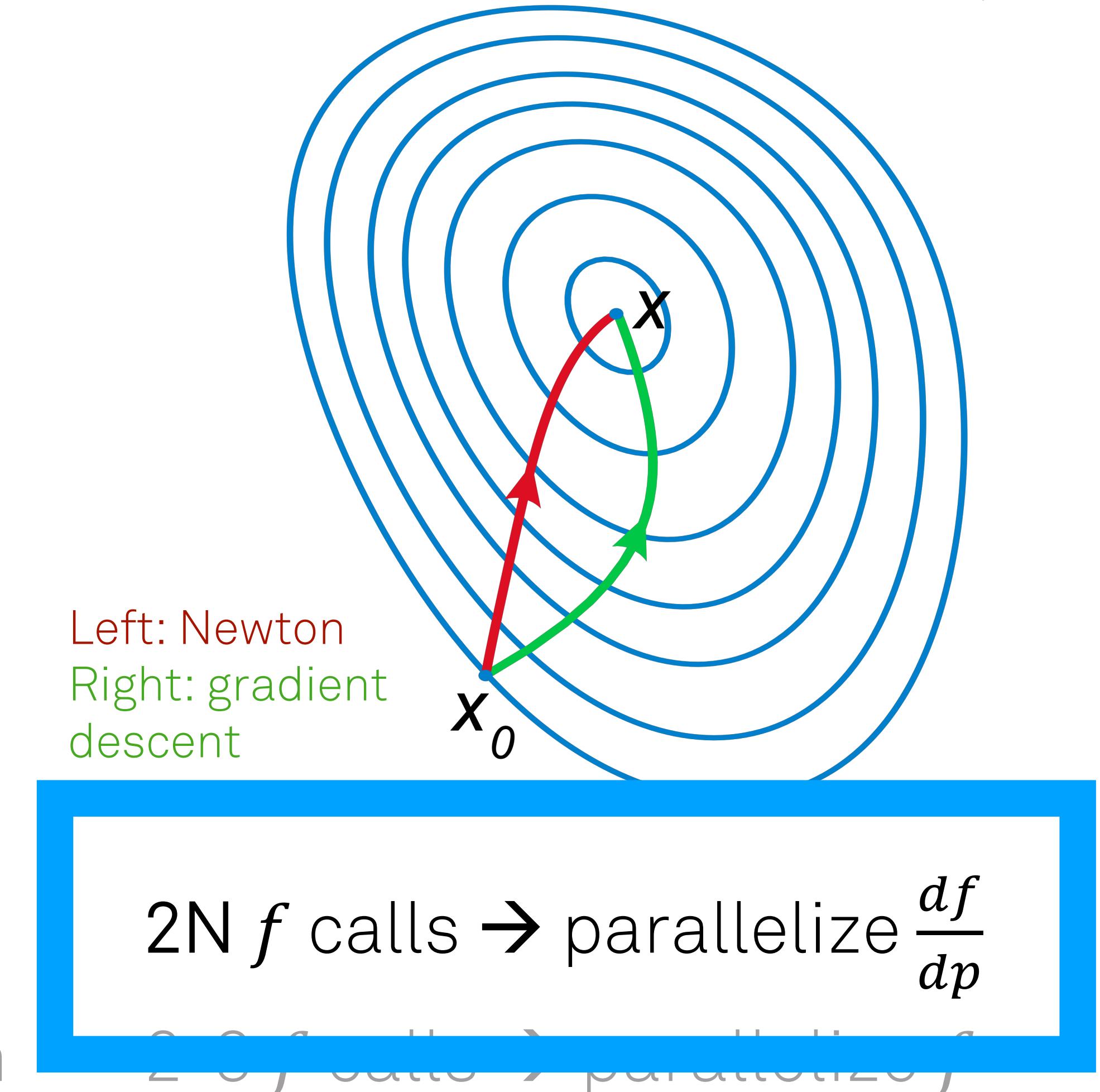
Run-time vs N(cores): certain types of binned fits



under investigation

Minuit: minimize PDF $f(x; p)$:

- Quasi-Newton MIGRAD method
- Gradient - line-search:
 - gradient for N parameters p : $\frac{df}{dp} \approx \frac{f(p-dp)-f(p)}{dp}$
 - line-search: descend along gradient direction
- Important: serial & parallel results same
 - non-trivial, Minuit internal transformations



Gradient parallelization

First benchmarks:

“*ggF*model” (gluon-gluon fusion → Higgs boson), **MIGRAD** fit

realistic, non-trivial (265 parameters)

scaling not perfect and erratic (+/- 5s)

likely caused by communication protocol - under investigation

RooMinimizer	MultiProcess GradMinimizer					
-	1 worker	2 workers	3 workers	4 workers	6 workers	8 workers
28s	33s	20s	15s	14s	17s (...)	11s

Conclusions

Interactive study of complex LHC physics fits (e.g. Higgs) requires parallelization

We improved scaling performance of likelihood-level parallelization

Bottlenecks still exist for certain classes of models

New flexible framework: multi-level parallelization (likelihood, gradient)

First working version, now analysis and tuning performance

Let's stay in touch

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Encore

Load balancing

PDF timings change dynamically due to RooFit precalculation strategies
... not a problem for numerical integrals

Analytical derivatives (automated? CLAD)

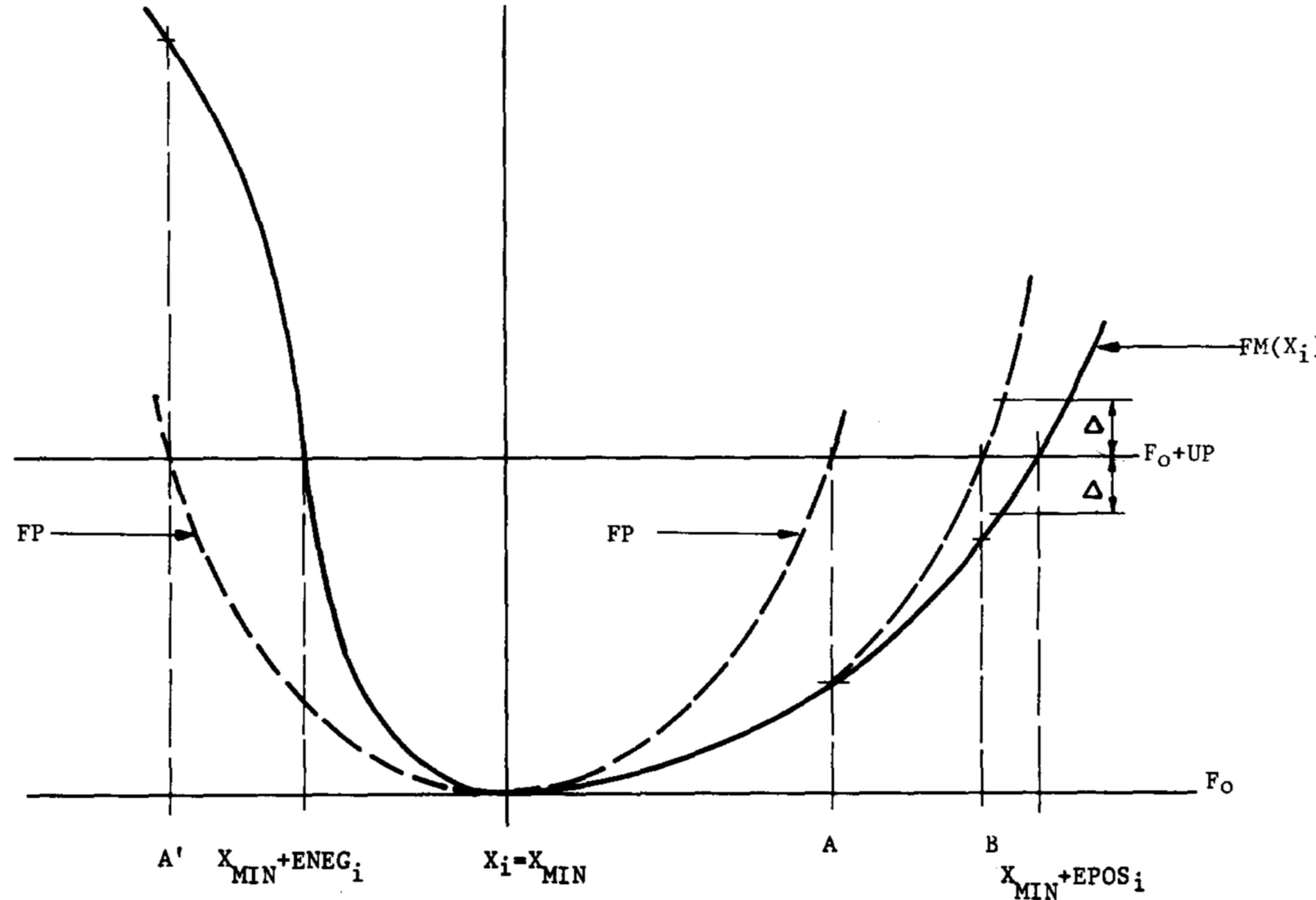
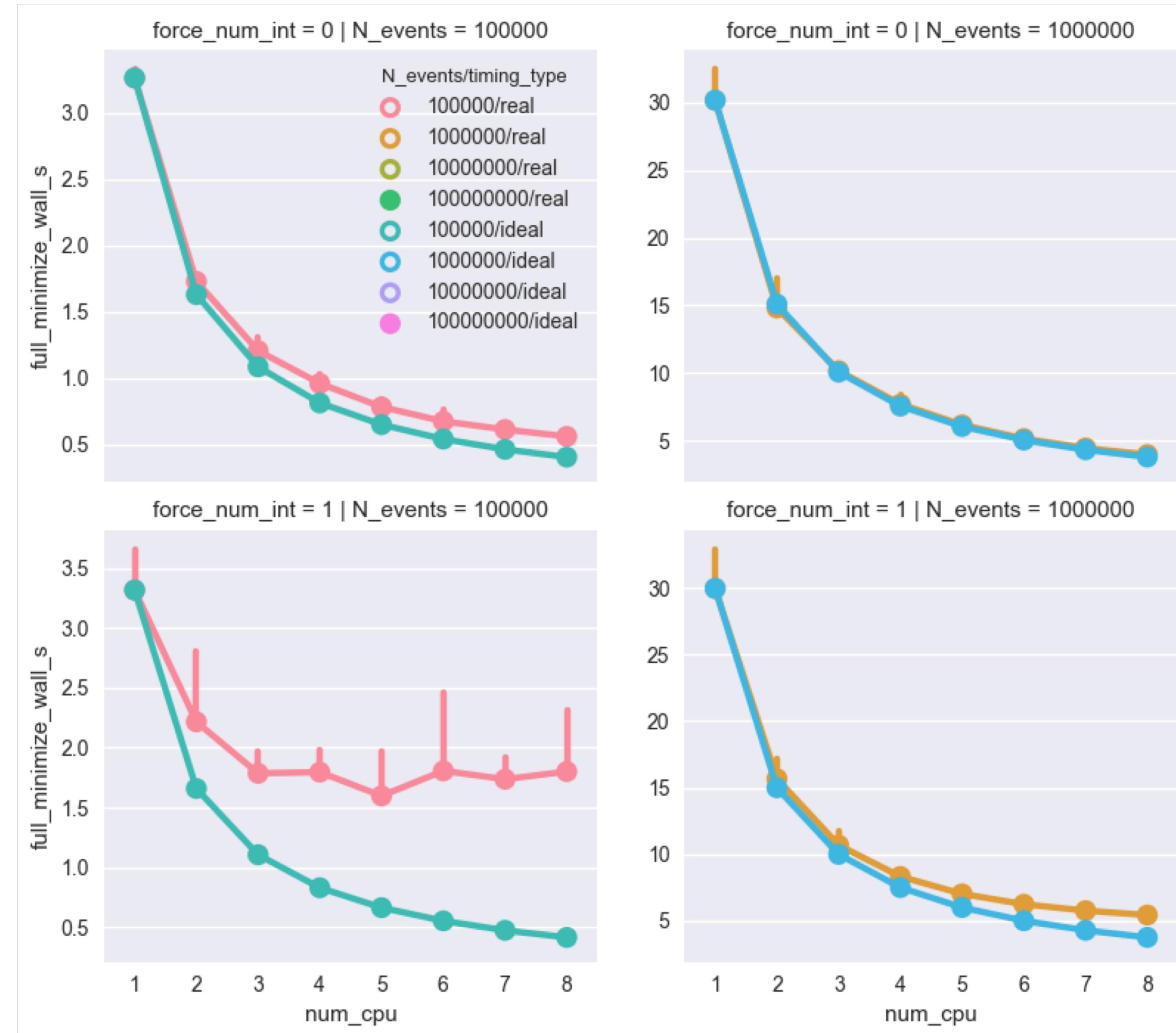
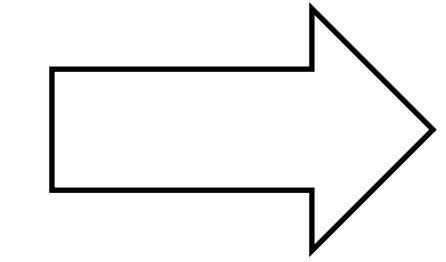


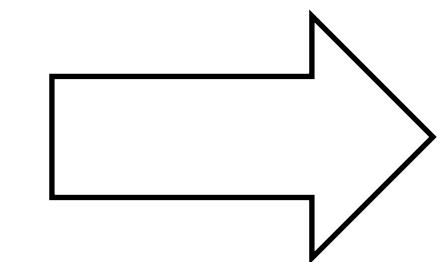
Fig. 2. Calculation of MINOS errors of parameter i . The (symmetric) dotted parabola FP is predicted from the covariance matrix, but the nonlinearity of the problem results in the solid curve FM which gives the asymmetric errors $EPOS$ and $ENEG$ (see text).

Numerical integrals

“Analytical” integrals



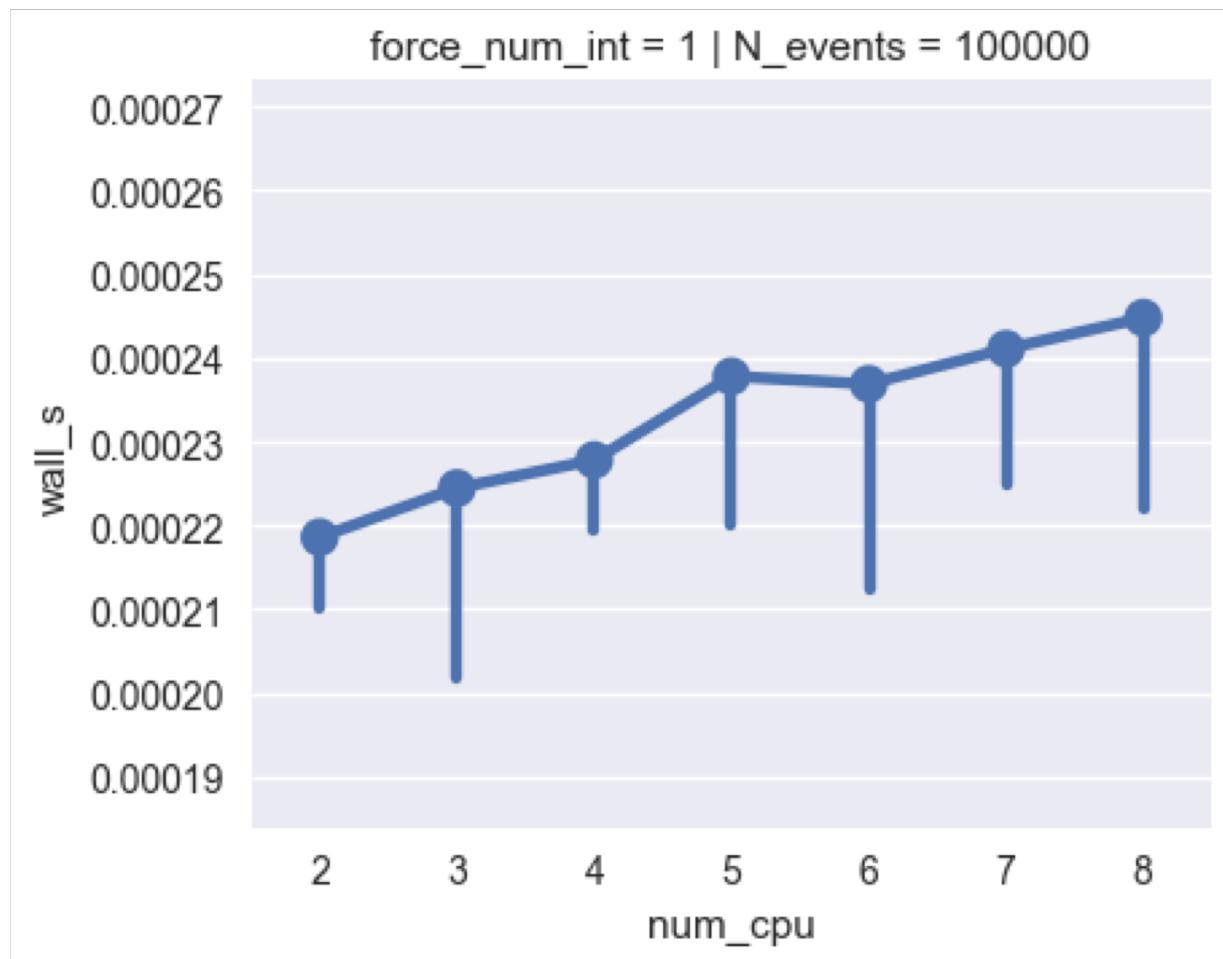
Forced numerical (Monte Carlo) integrals
(Higgs fits didn't have them)



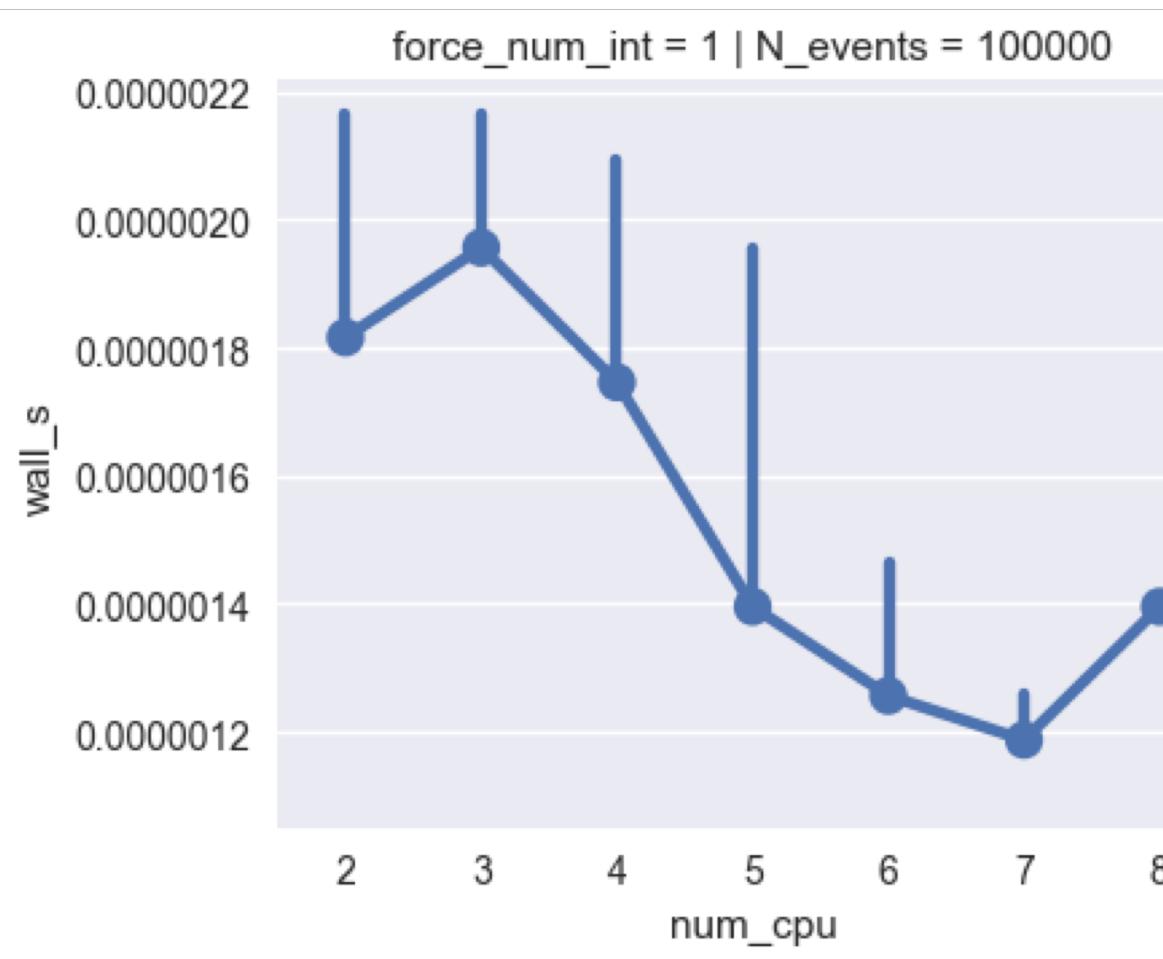
Numerical integrals

Individual NI timings
(variation in runs and iterations)

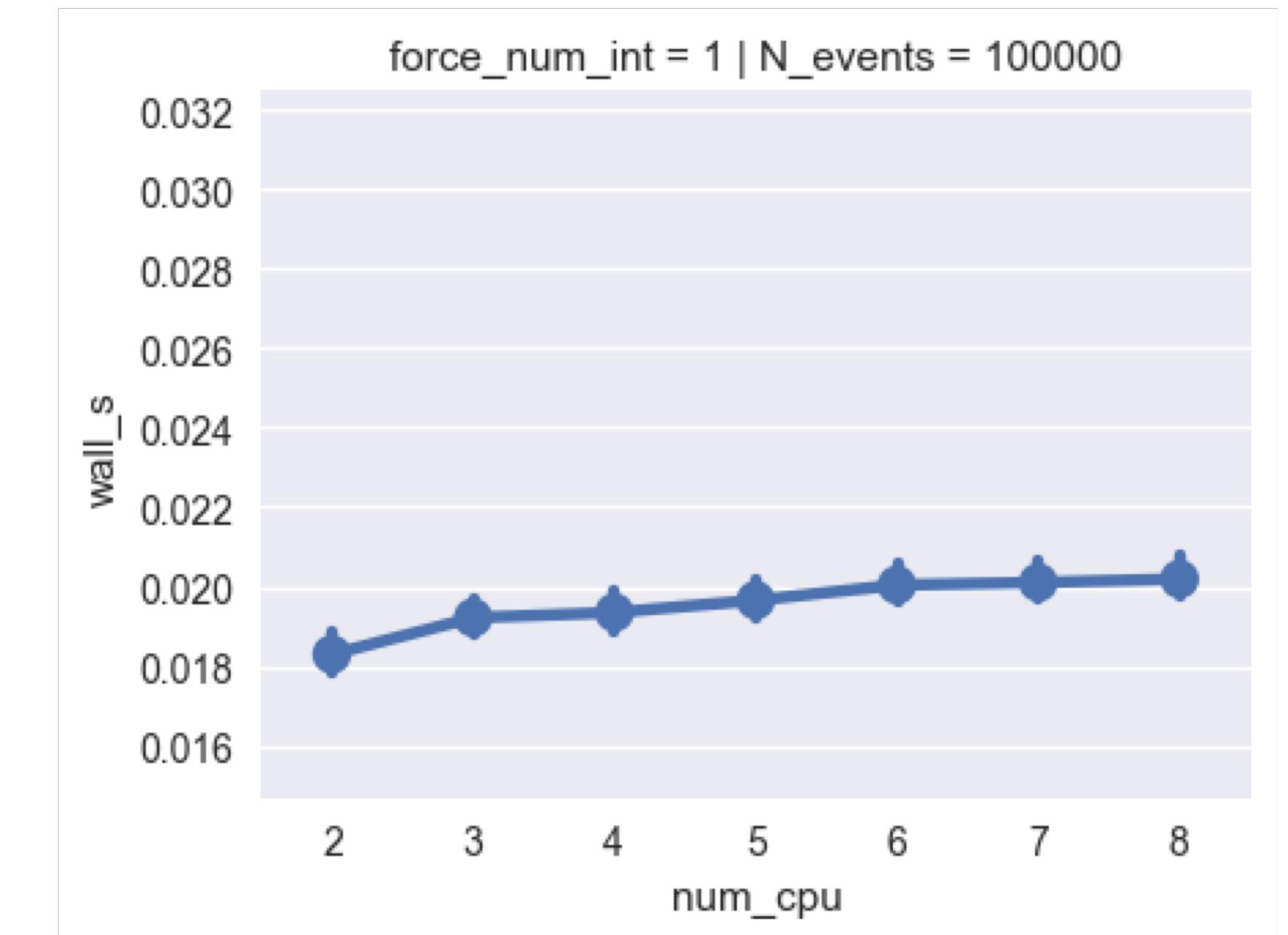
Maxima



Minima



Sum of slowest integrals/cores
per iteration over the entire run



(single core total runtime: 3.2s)

RooFit::MultiProcess::Vector<YourSerialClass>

Serial class: likelihood (e.g. RooNLLVar) or gradient (Minuit)

Interface: subclass + MP

Define "vector elements"

Group elements into tasks (to be executed in parallel)

RooFit::MultiProcess::SharedArg<T>

RooFit::MultiProcess::TaskManager

Faster fitting: MultiProcess design

`RooFit::MultiProcess::Vector<YourSerialClass>`

`RooFit::MultiProcess::SharedArg<T>`

Normalization integrals or other shared expensive objects

Parallel task definition specific to type of object

... design in progress

`RooFit::MultiProcess::TaskManager`

RooFit::MultiProcess::Vector<YourSerialClass>

RooFit::MultiProcess::SharedArg<T>

RooFit::MultiProcess::TaskManager

Queue gathers tasks and communicates with worker pool

Workers steal tasks from queue

Worker pool: forked processes (BidiRMMapPipe)

- performant and already used in RooFit
- no thread-safety concerns
- instead: communication concerns
- ... flexible design, implementation can be replaced (e.g. TBB)

MultiProcess for users

```
vector<double> x {1, 4, 5, 6.48074};

xSquaredSerial xsq_serial(x);

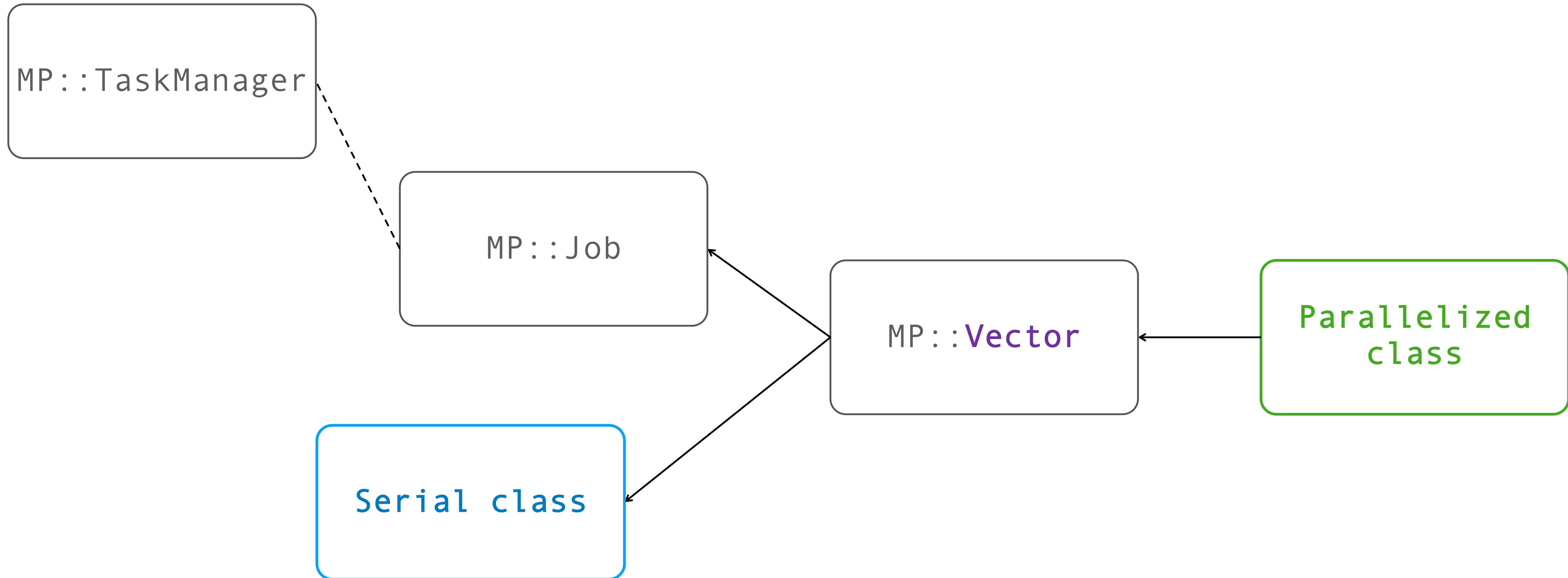
size_t N_workers = 4;
xSquaredParallel xsq_parallel(N_workers, x);

// get the same results, but now faster:
xsq_serial.get_result();
xsq_parallel.get_result();

// use parallelized version in your existing functions
void some_function(xSquaredSerial* xsq);

some_function(&xsq_parallel); // no problem!
```

MultiProcess usage for devs



```
template <class T> class MP::Vector : public T, public MP::Job  
class Parallel : public MP::Vector<Serial>
```

MultiProcess usage for devs

```
class xSquaredSerial {
public:
    xSquaredSerial(vector<double> x_init)
        : x(move(x_init))
        , result(x.size()) {}

    virtual void evaluate() {
        for (size_t ix = 0; ix < x.size(); ++ix) {
            x_squared[ix] = x[ix] * x[ix];
        }
    }

    vector<double> get_result() {
        evaluate();
        return x_squared;
    }

protected:
    vector<double> x;
    vector<double> x_squared;
};
```

```
class xSquaredParallel
    : public RooFit::MultiProcess::Vector<xSquaredSerial> {
public:
    xSquaredParallel(size_t N_workers, vector<double> x_init) :
        RooFit::MultiProcess::Vector<xSquaredSerial>(N_workers, x_init)
    {}

private:
    void evaluate_task(size_t task) override {
        result[task] = x[task] * x[task];
    }

public:
    void evaluate() override {
        if (get_manager()->is_master()) {
            // do necessary synchronization before work_mode

            // enable work mode: workers will start stealing work from queue
            get_manager()->set_work_mode(true);

            // master fills queue with tasks
            for (size_t task_id = 0; task_id < x.size(); ++task_id) {
                get_manager()->to_queue(JobTask(id, task_id));
            }

            // wait for task results back from workers to master
            gather_worker_results();

            // end work mode
            get_manager()->set_work_mode(false);

            // put gathered results in desired container (same as used in serial class)
            for (size_t task_id = 0; task_id < x.size(); ++task_id) {
                x_squared[task_id] = results[task_id];
            }
        }
    }
};
```

```
template <class T> class MP::Vector : public T, public MP::Job
```

Single core profiling and improvements

Higgs `ggf` & `9 channel` fits (workspaces by Lydia Brenner)

Most time spent on:

1. Memory access → `RooVectorDataStore::get()` (`4%` / `32%`), 0.3% LL cache misses (expensive!)
 - Row-wise access pattern on column-wise data store (and `std::vector<std::vector>`)
2. Logarithms: `12%`
3. Interpolation → `RooStats::HistFactory::FlexibleInterpVar` (`10%`)

Faster fitting: single core improvements

RooLinkedList::findArg: ~ 5% of memory access instructions

RooLinkedList::At took considerable time in Gaussian test fit (*Vince*)

std::vector lookup → 1.6x speedup! WIP

Faster fitting: future work

Reorder tree evaluation → CPU cache use, vectorization

Smarter fitting (stochastic minimizer, analytical gradient, CLAD)

Front-end / back-end separation (e.g. TensorFlow back-end)

Faster fitting: single core profiling meta-conclusions

profiling functions & classes

valgrind

gprof

Instruments

... etc.

profiling objects (e.g. call-trees, e.g. RooFit...)

... DIY?

More Multi-Core

RooRealMPFE / BidirMMapPipe

Custom multi-process message passing protocol

- POSIX fork, pipe, mmap

Communication “overhead” (delay between sending and receiving messages): ~ 1e-4 seconds

- `serverLoop` waits for message & runs server-side code
- messages used sparingly
- data transfer over memory-mapped pipes

TensorFlow experiments

	RooFit (MINUIT)	TensorFlow (BFGS)
Unbinned fit	0.1s	0.01 - 0.1s (dep. on precision)
Binned fit	0.7ms	2.3ms

Fits on identical model & data (single i7 machine)

TensorFlow: No pre-calculation / caching!

Major advantage of RooFit for binned fits (e.g. morphing histograms)
(feature request for memoization <https://github.com/tensorflow/tensorflow/issues/5323>)

N.B.: measured before CPU affinity fixing

RooFit now even faster (but limited to running one machine)