

# Neutrino Source Searches with Likelihood Landscapes

# Neutrino Source Searches

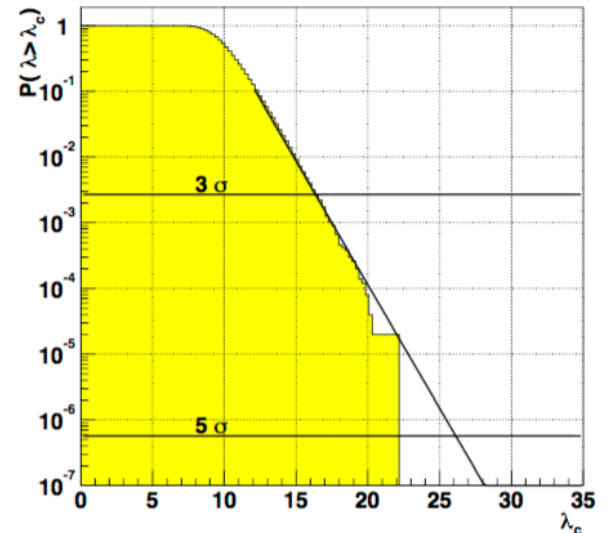
- Hypothesis H0: background only flux
  - Atmospheric neutrino's
  - (Misreconstructed) Atmospheric Muons
- Hypothesis H1: background + signal flux
  - (High energy) Cosmic Neutrinos

# General Procedure

- How compatible is data with  $H_0$  or  $H_1$ ?

$$\lambda = \log \left[ \frac{P(\text{data}|H_1)}{P(\text{data}|H_0)} \right]$$

- When to claim an observation?
  - Accept  $H_1$  if  $\lambda > \lambda_c$
  - $\lambda_c$  such that  
 $P(\text{accept } H_1 \mid H_0 = \text{true}) < 0.00\dots 1$

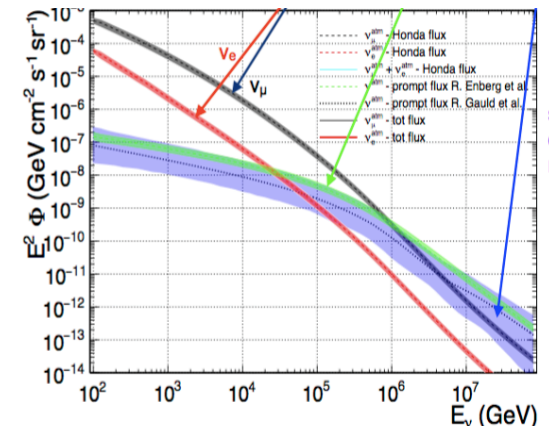
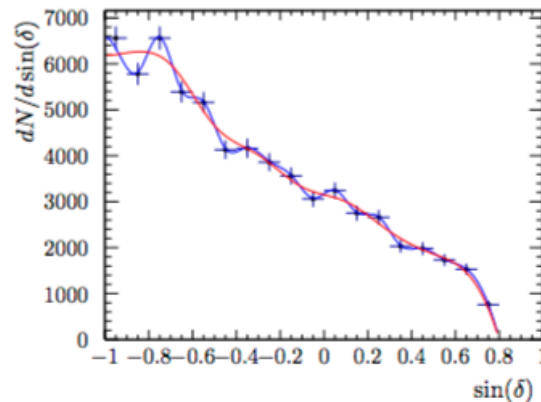
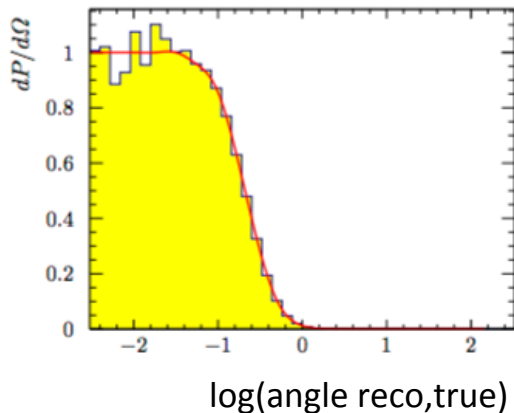


$$\lambda = \log \left[ \frac{P(\text{data}|H_1)}{P(\text{data}|H_0)} \right]$$

# Test Statistic (Conventional)

- Given detected (and selected) events  $\{ev_i\}$

$$P(\text{data}|H) = \sum_i \left[ \log \int \underbrace{P(x_{reco,i}|x_{true})}_{\text{Reconstruction}} \cdot \underbrace{P^{det}(x_{true})}_{\text{Detection efficiency}} \cdot \underbrace{\mu(x_{true}|H)}_{\text{Expected flux}} dx_{true} \right] - \mu^{tot}(H)$$



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- New method:

$$P(\text{data}|H) = \sum_i \left[ \log \int P(ev_i | x_{true}) \cdot P^{det}(x_{true}) \cdot \mu(x_{true} | H) dx_{true} \right] - \mu^{tot}(H)$$

- No big deal?

# New vs. Conventional

## Conventional

- Only best solution kept from reconstruction
- Selection criteria needed to select well-reconstructed events -> events are lost
- Different reconstruction algorithms (showers/tracks/tau double bang) patched together
- Event identification by BDT's and other black magic algorithms
- Parameterizations of MC events
- Fast

## New Method

- Detailed knowledge of event likelihood landscape
- All events can be used
- Single 'reconstruction' algorithm for all events
- Neutrino flavour identification automatically taken into account
- Event-by-event
- Probably slow

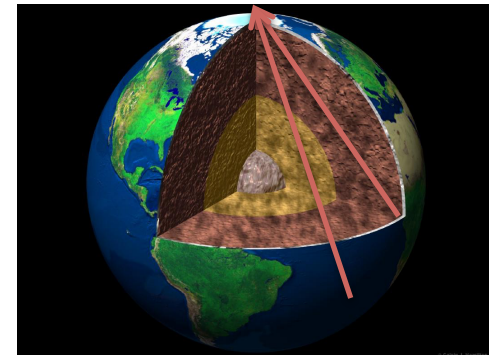
# Likelihood Ingredients

$$P(\text{data}|H) = \sum_i \left[ \log \int P(\text{ev}_i | x_{\text{true}}) \cdot P^{\text{det}}(x_{\text{true}}) \cdot \mu(x_{\text{true}} | H) dx_{\text{true}} \right] - \mu^{\text{tot}}(H)$$

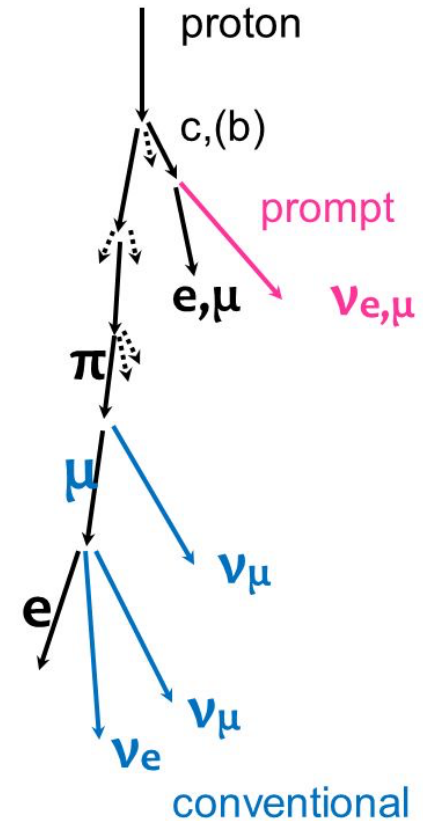
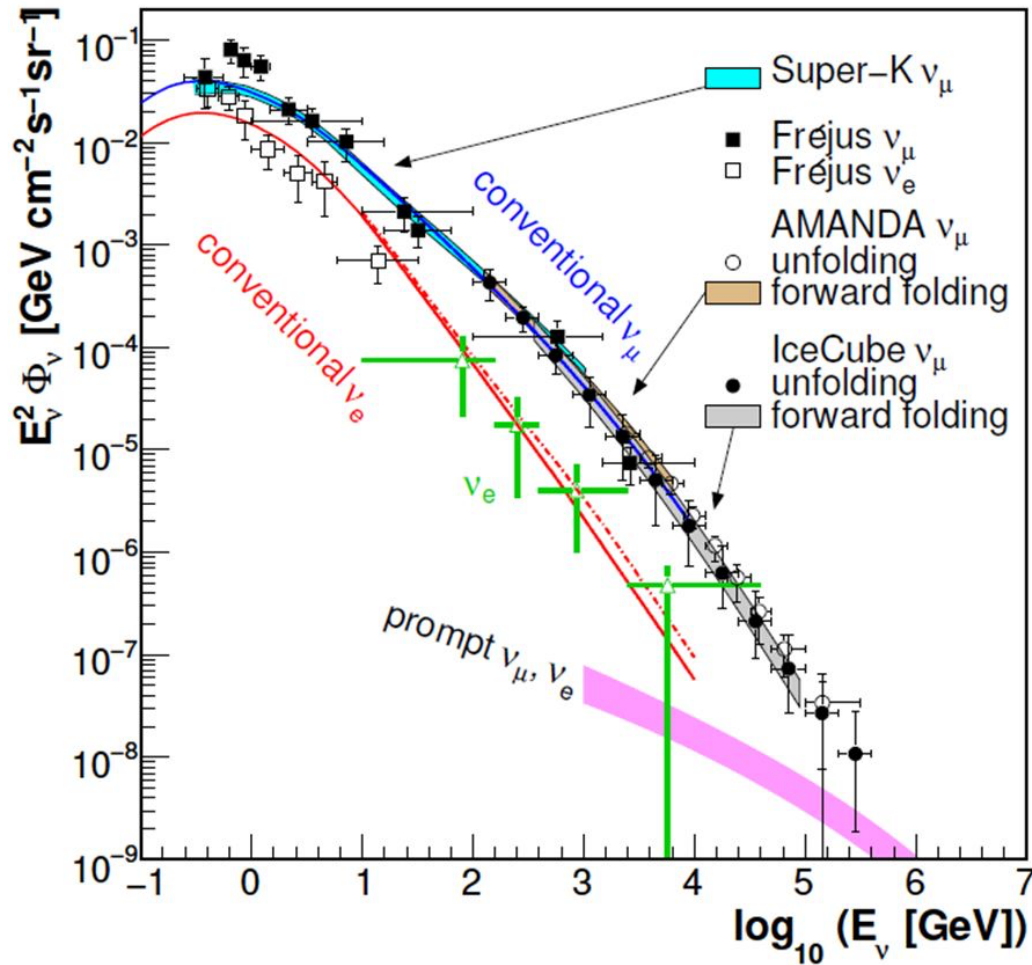
$\mu(x_{\text{true}} | H)$       Number of expected background or signal events in our detector (can)

$P^{\text{det}}(x_{\text{true}})$

$P(\text{ev}_i | x_{\text{true}})$



# Atmospheric Neutrinos



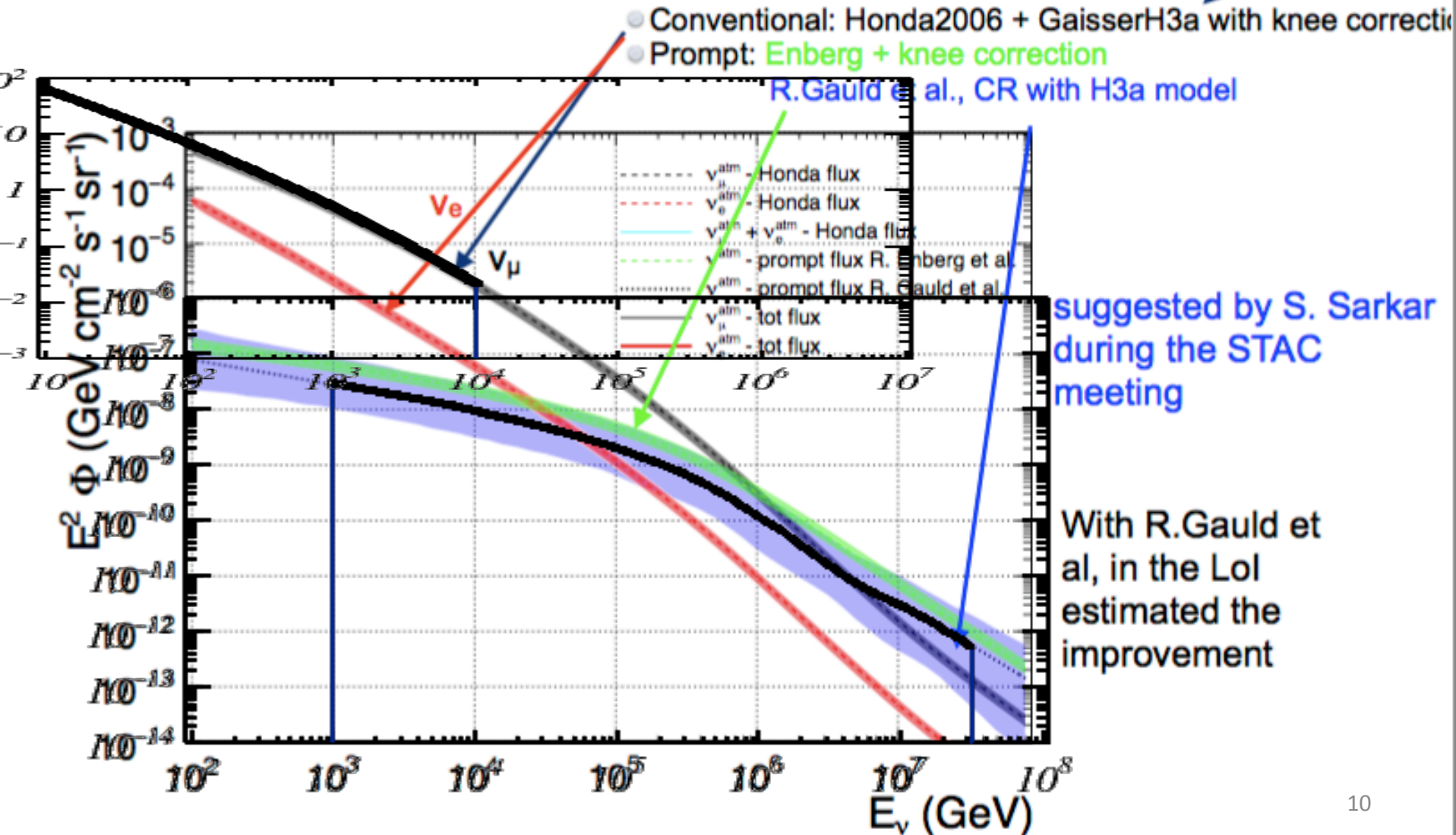


# Current Parameterization

- KM3NeT Letter of Intent
- Based on Seatray
- Polynomial fit of Honda tables
  - Extrapolation to higher energy ranges
  - Outdated? Honda 2006 used.
  - Gaisser H3a knee correction
- Polynomial fit of Gauld tables 2015
  - From PromptNuFlux, L. Rottoli

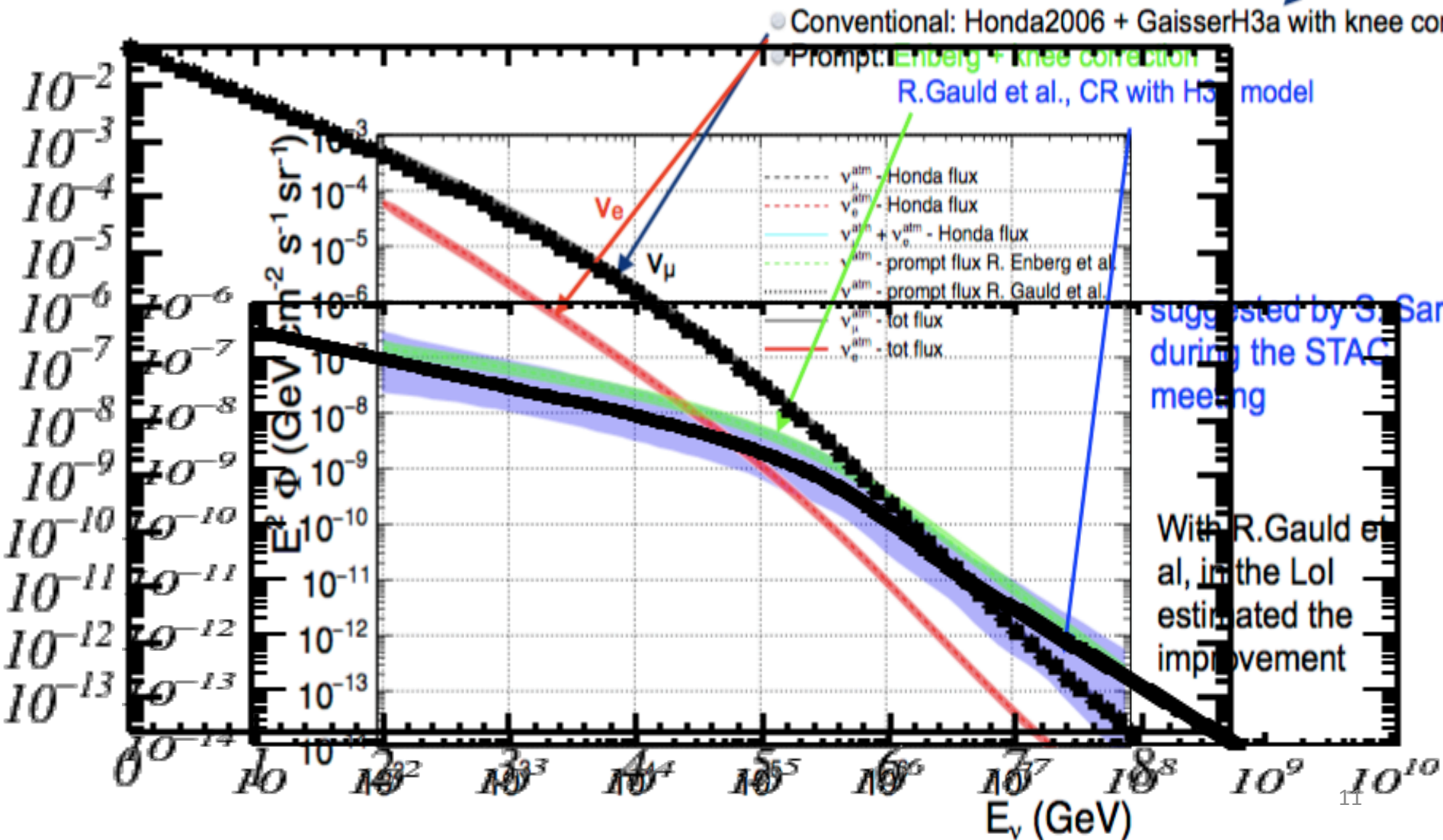
# Honda (2006) and Gauld (2016)

T. Gaisser 2012



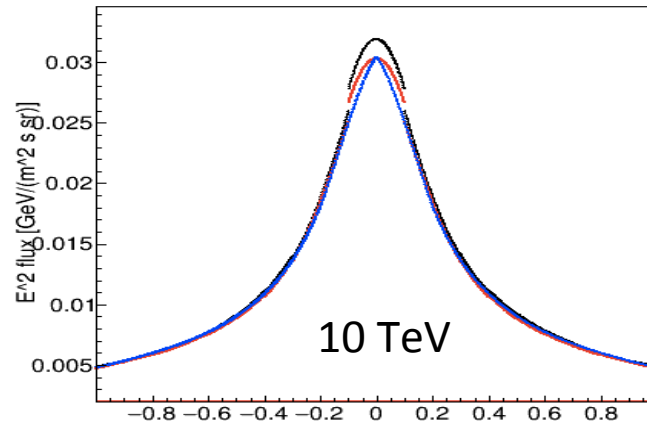
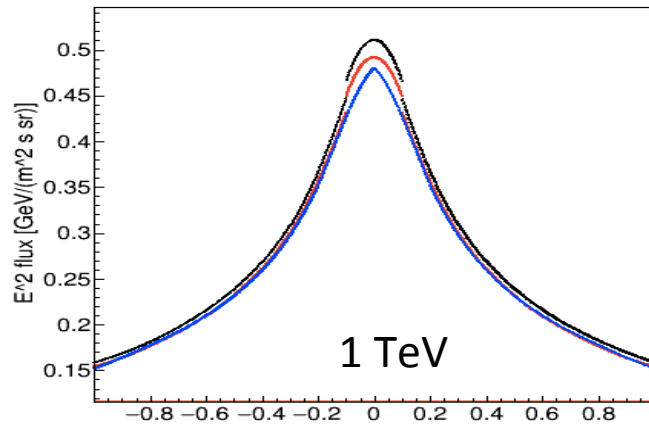
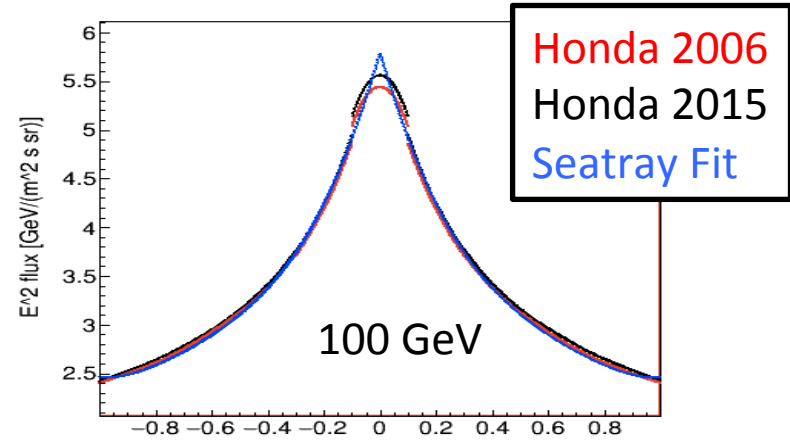
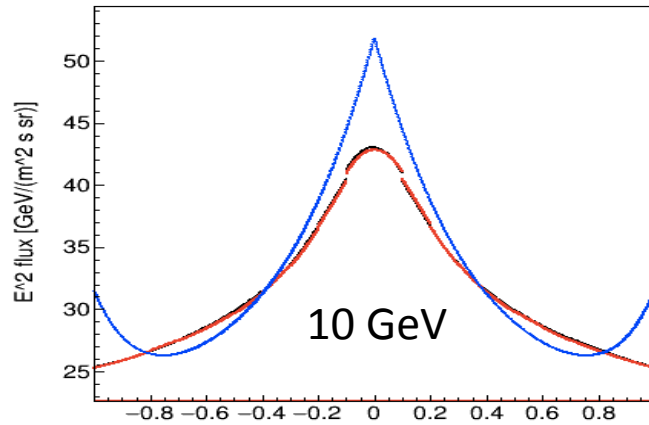
# Both Extrapolated (2)

T. Gaisser 2012



# Honda: Zenith Dependence

$E^2 \times \text{flux} [\text{GeV}/(\text{m}^2 \text{ s sr})]$



$\cos(\text{Zenith})$

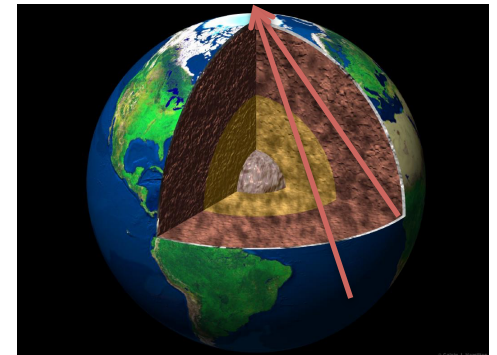
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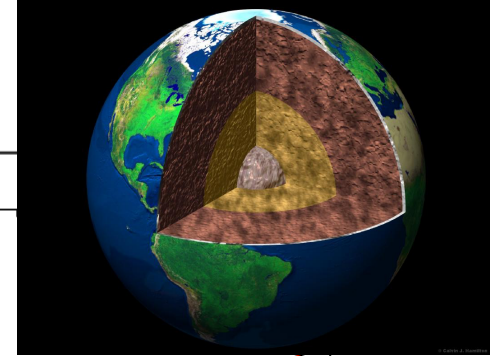
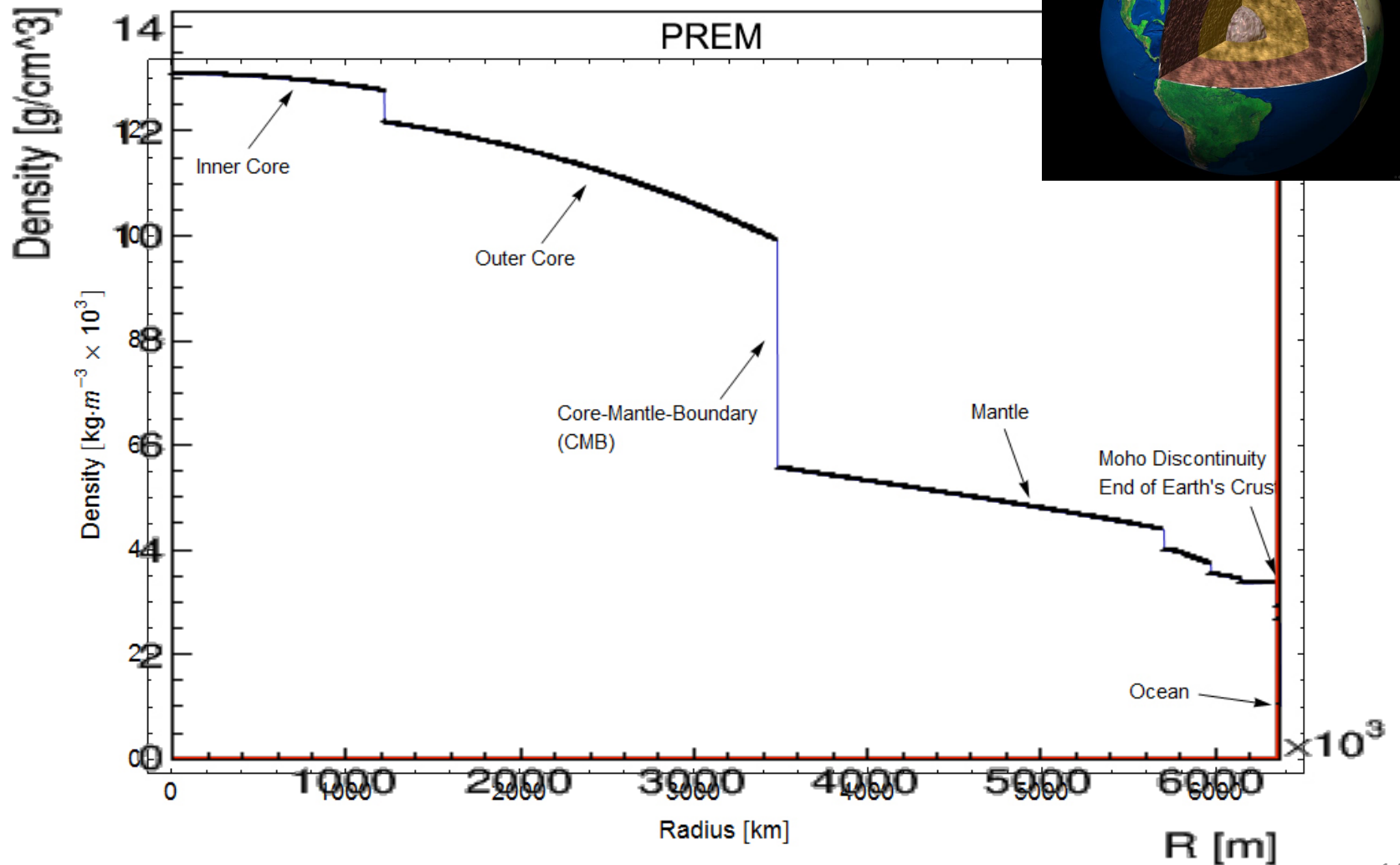
$\mu(x_{\text{true}} | H)$       Number of expected background or signal events in our detector (can)

$P^{\text{det}}(x_{\text{true}})$

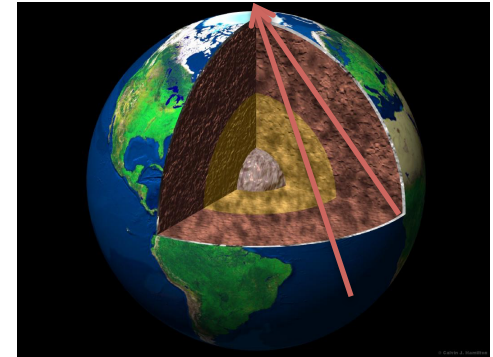
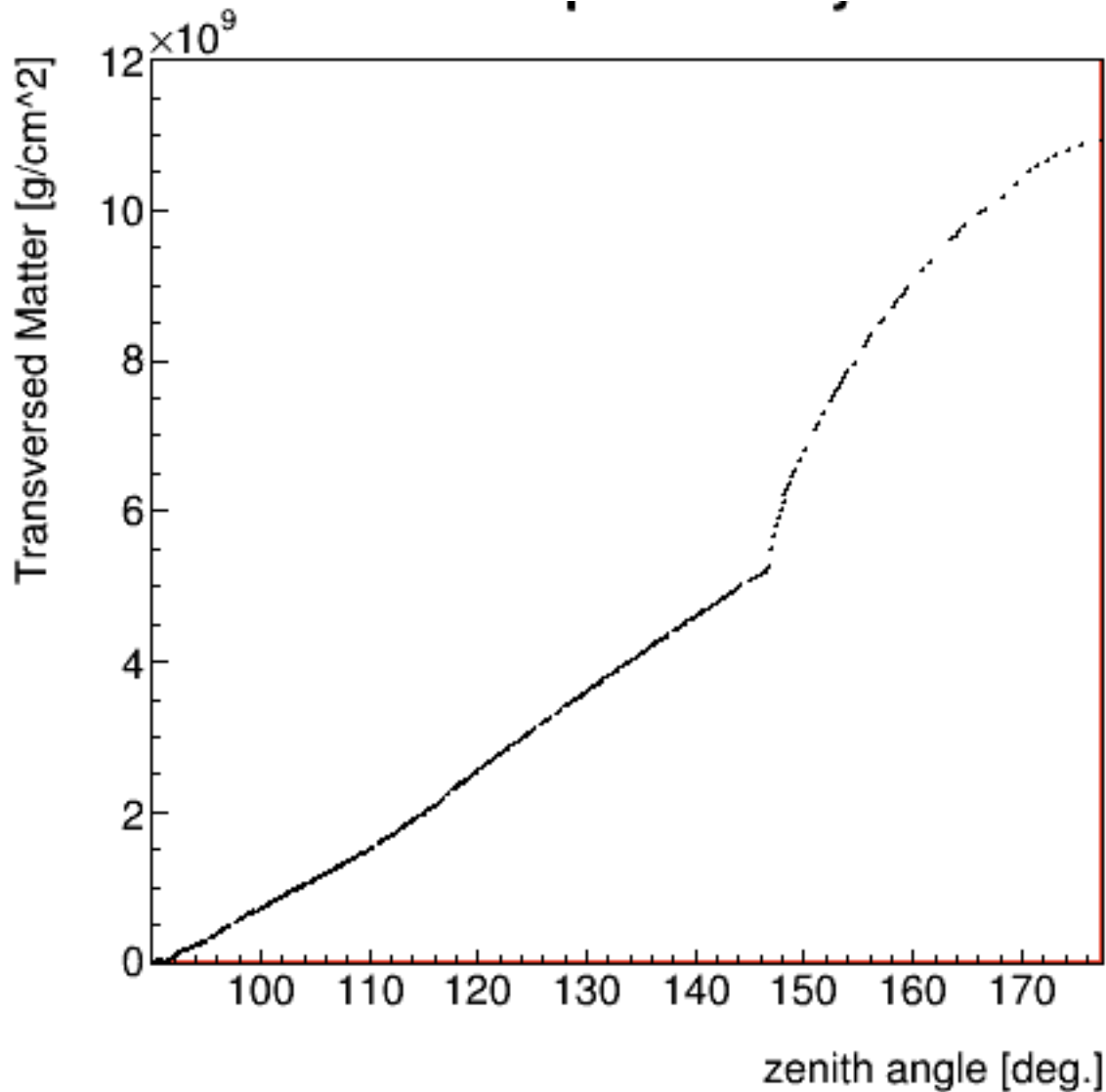
$P(\text{ev}_i | x_{\text{true}})$



# Earth Propagation

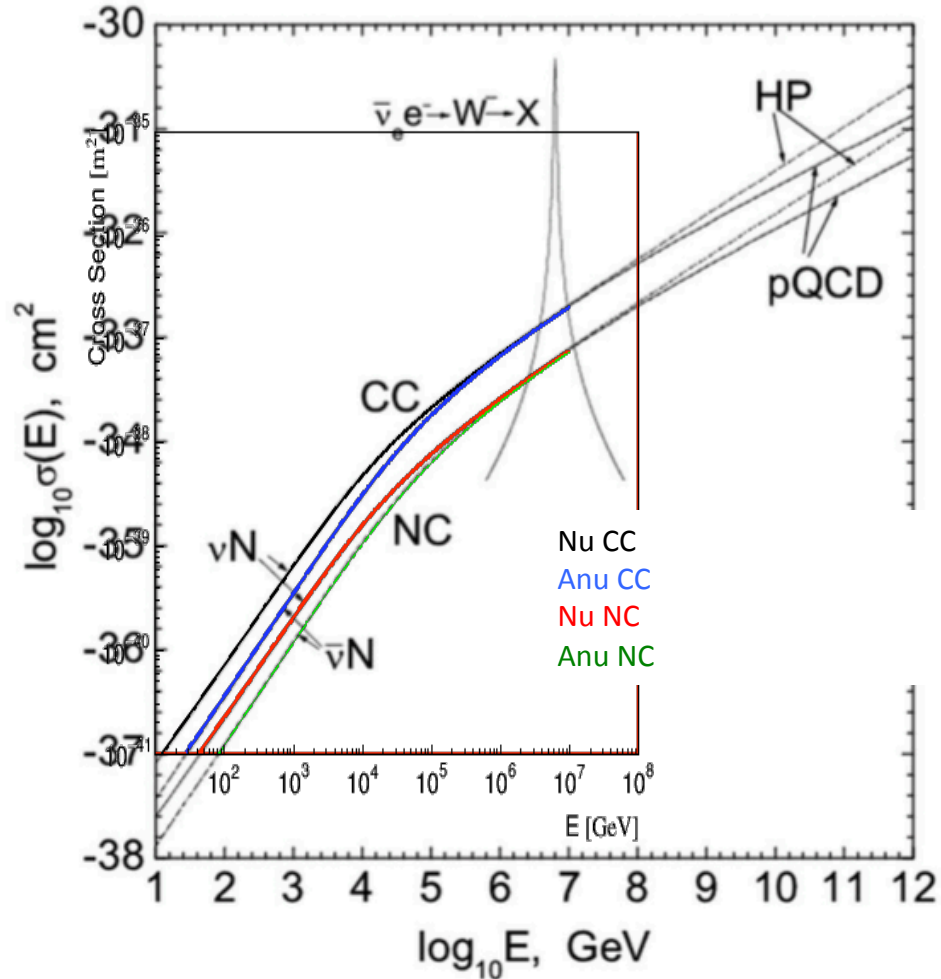


# Transversed Matter Density



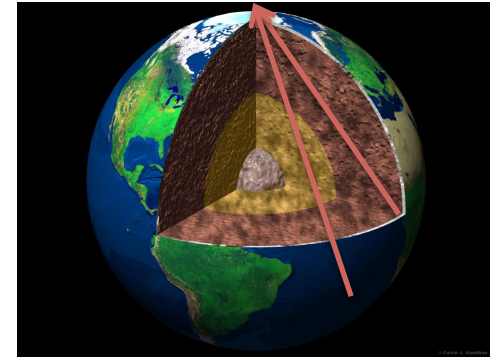
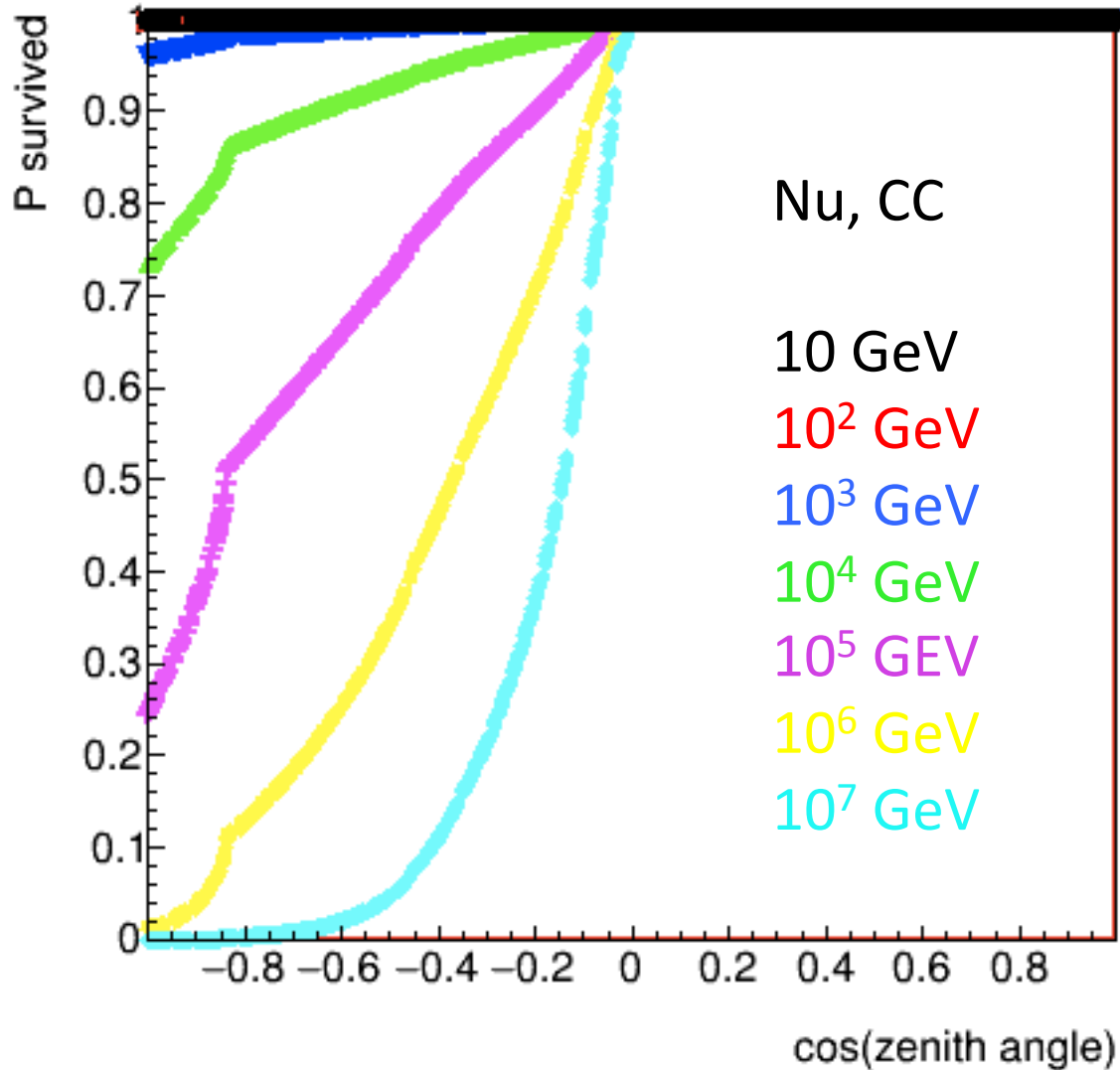
Analytically derived -> very fast

# Neutrino Cross Sections

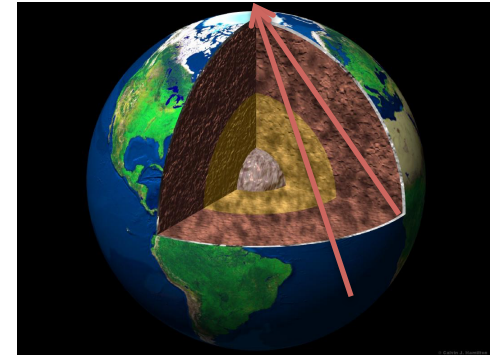
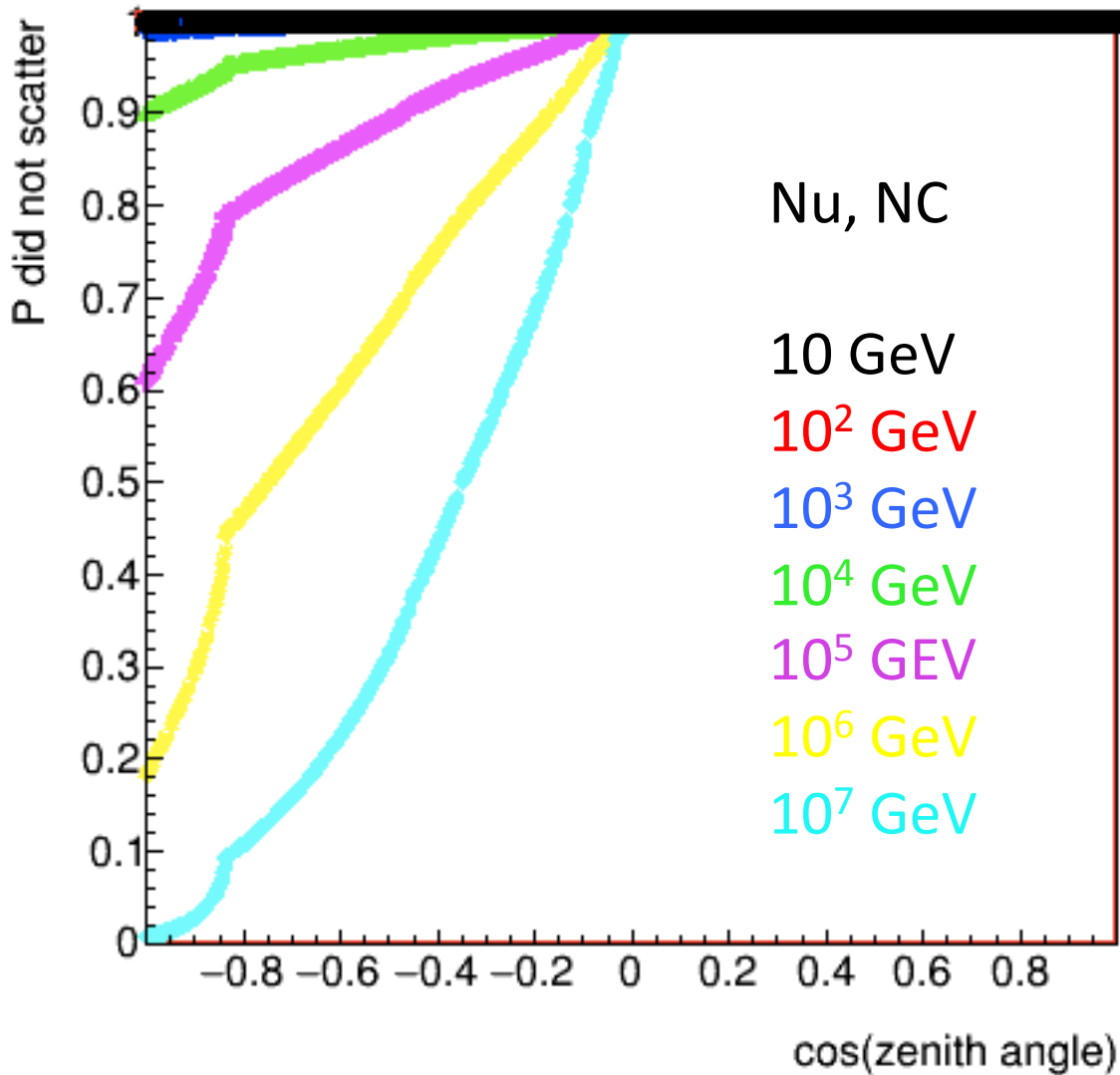




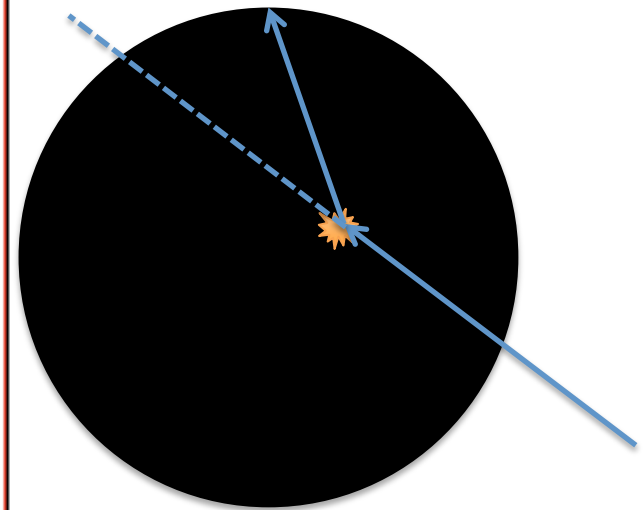
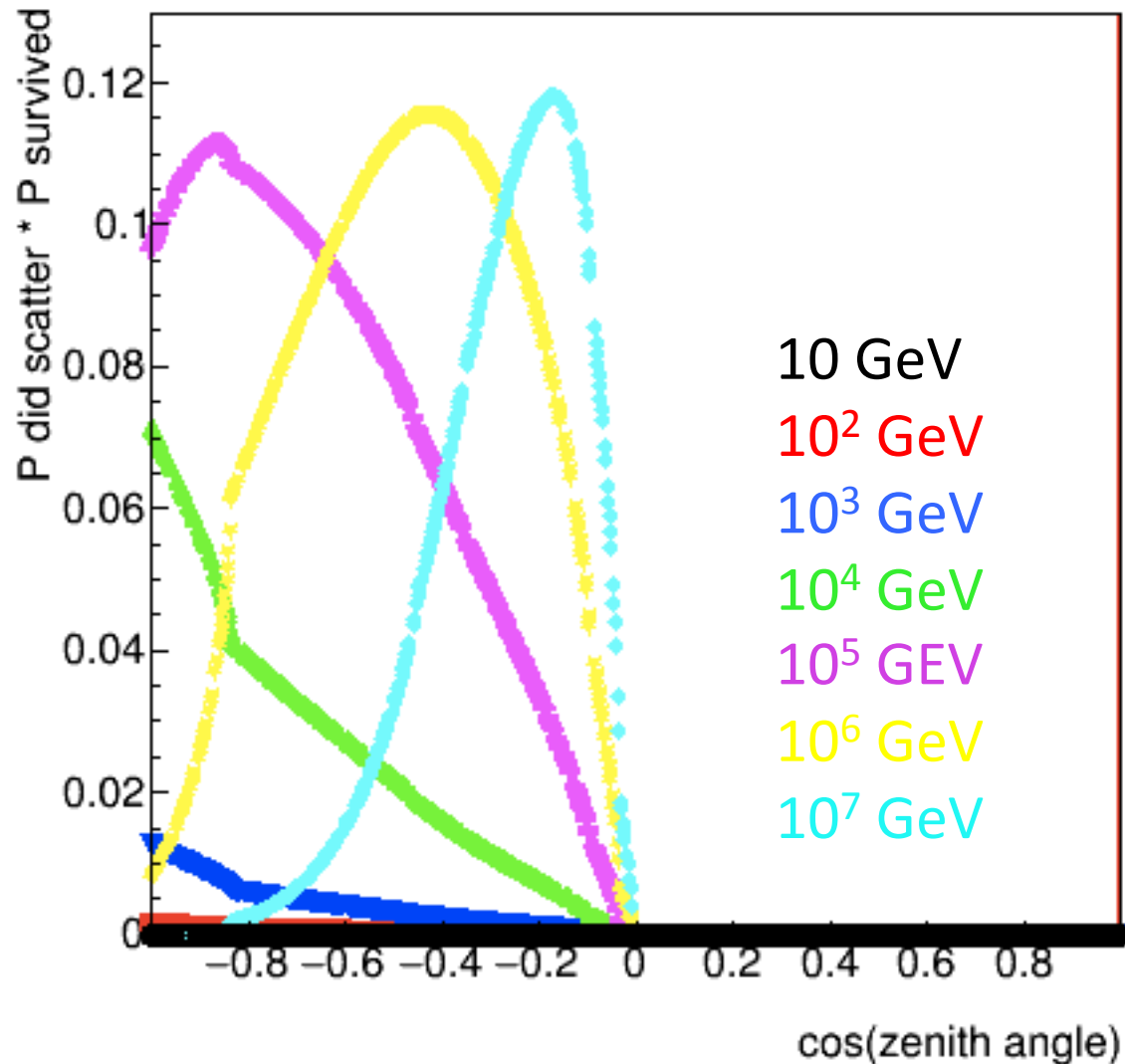
# Neutrino Absorption



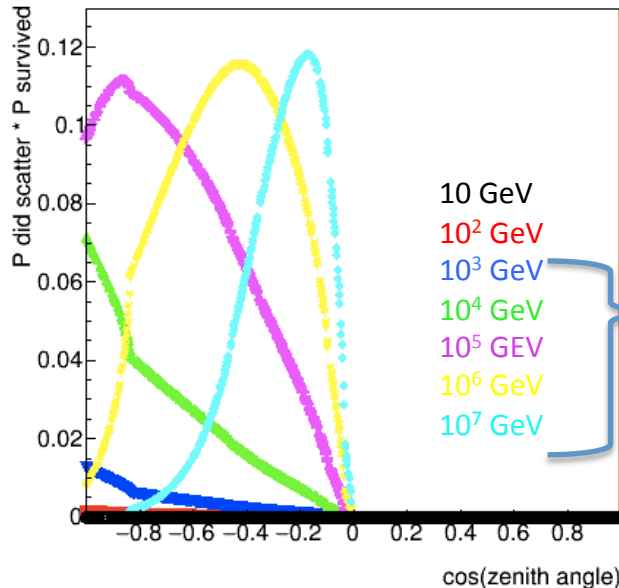
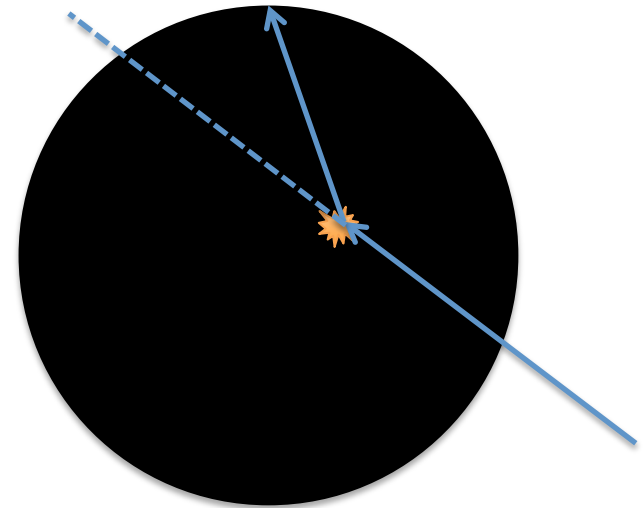
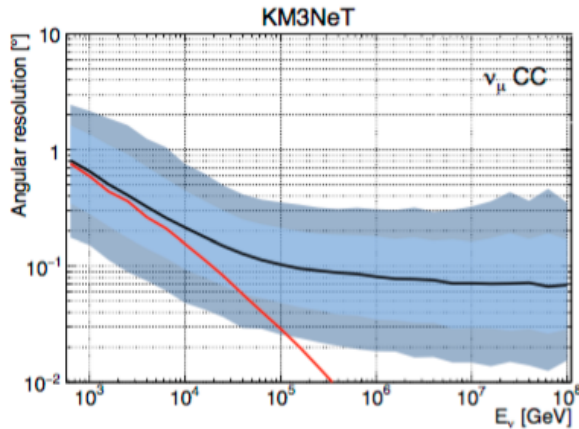
# Neutrino NC Scattering (1)



# Neutrino NC Scattering (2)



# Neutrino NC Scattering (3)



- Change in direction:  $\approx 0.6$  degrees for  $E_{\text{neu}} > 10^3$  GeV
- Change in Energy???

Effects on expected atm. Neutrino flux neglected

# Neutrino Oscillations

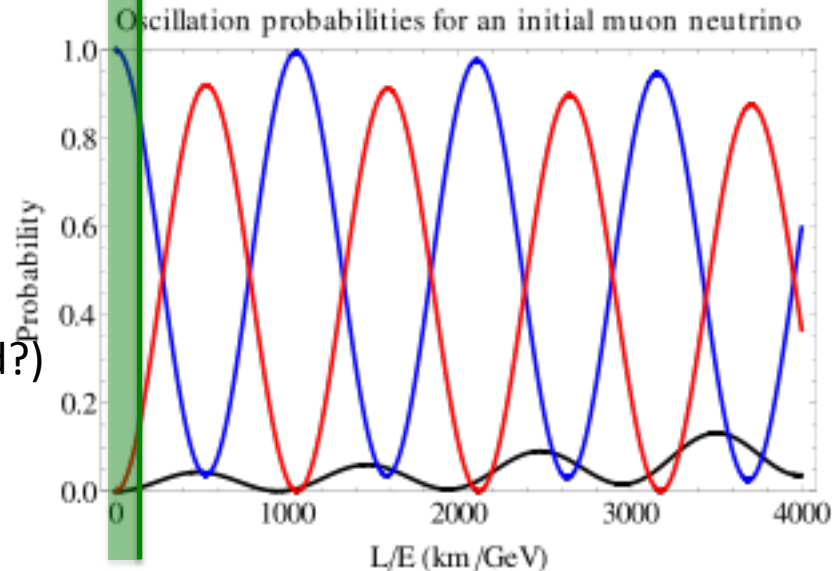
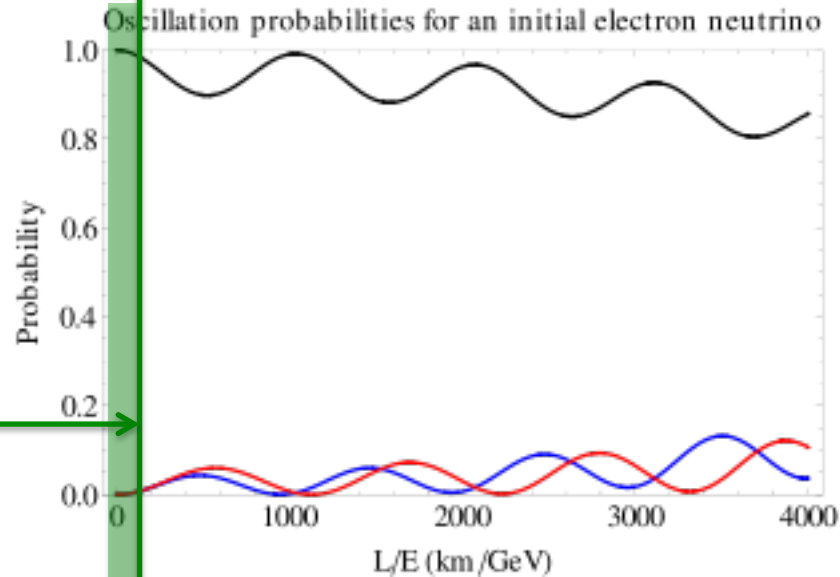
Earth radius =  $6.4 \times 10^3$  km  
 100 GeV neutrino

$L/E = 1.28 \times 10^2$  km/GeV

Earth covers one oscillation period  
 P(oscilate) up to:

- ~0.01 (electron  $\rightarrow$  muon/tau)
- ~0.2 (muon  $\rightarrow$  tau)
- ~0.2 (tau  $\rightarrow$  muon)

For now: Ignore.... (to be continued?)



# Likelihood Ingredients

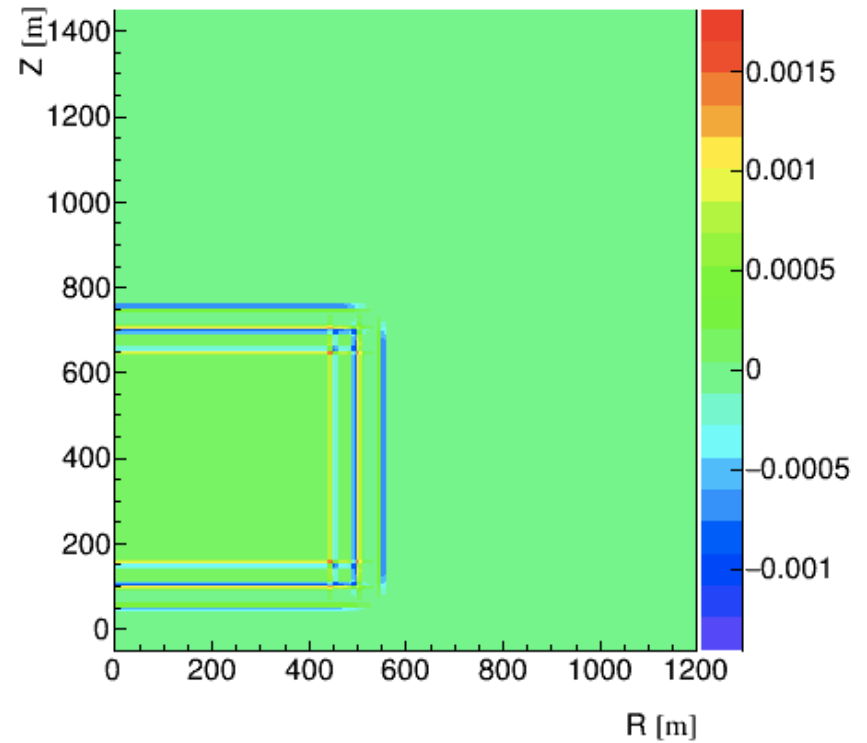
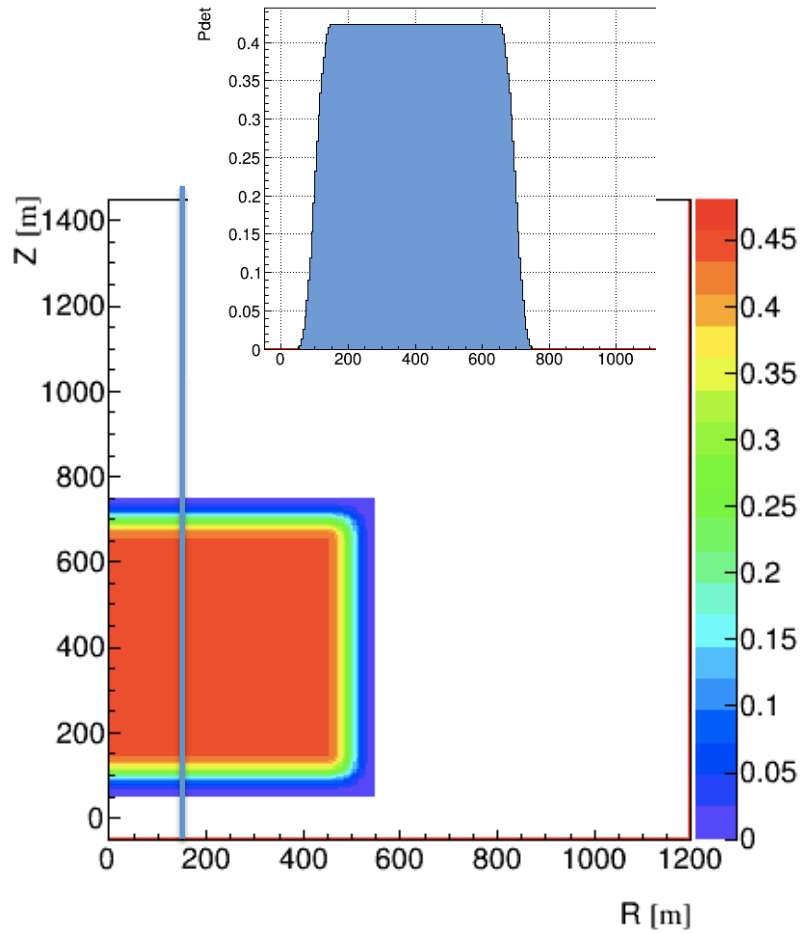
$$P(\text{data}|H) = \sum_i \left[ \log \int P(\text{ev}_i | x_{\text{true}}) \cdot P^{\text{det}}(x_{\text{true}}) \cdot \mu(x_{\text{true}} | H) dx_{\text{true}} \right] - \mu^{\text{tot}}(H)$$

$\mu(x_{\text{true}} | H)$       Number of expected background or signal events in our detector (can)

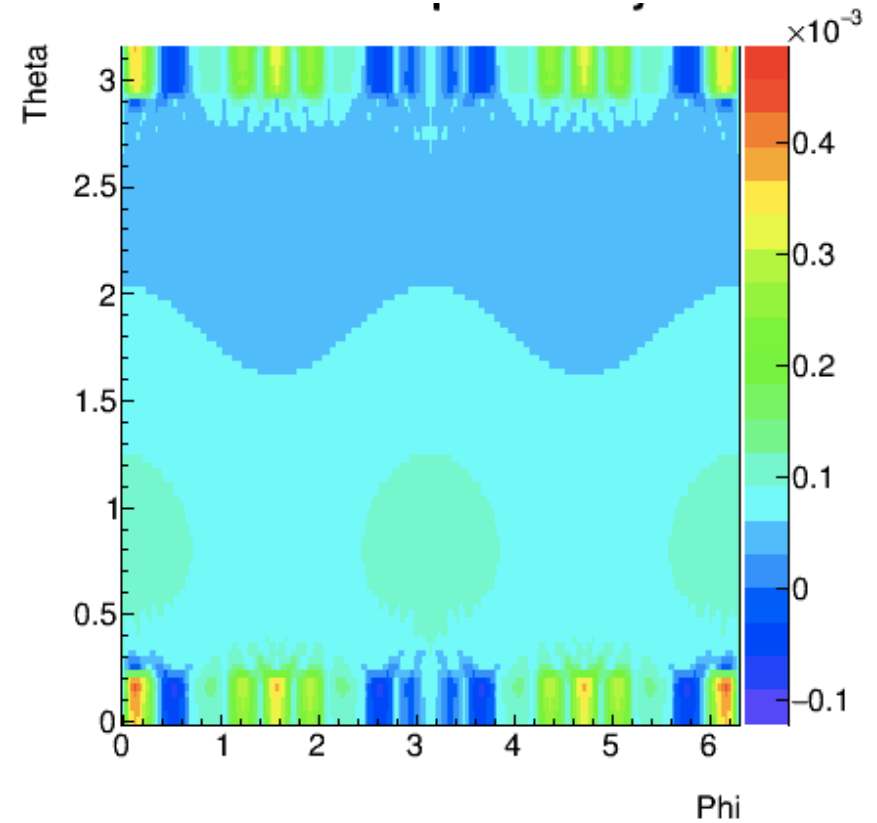
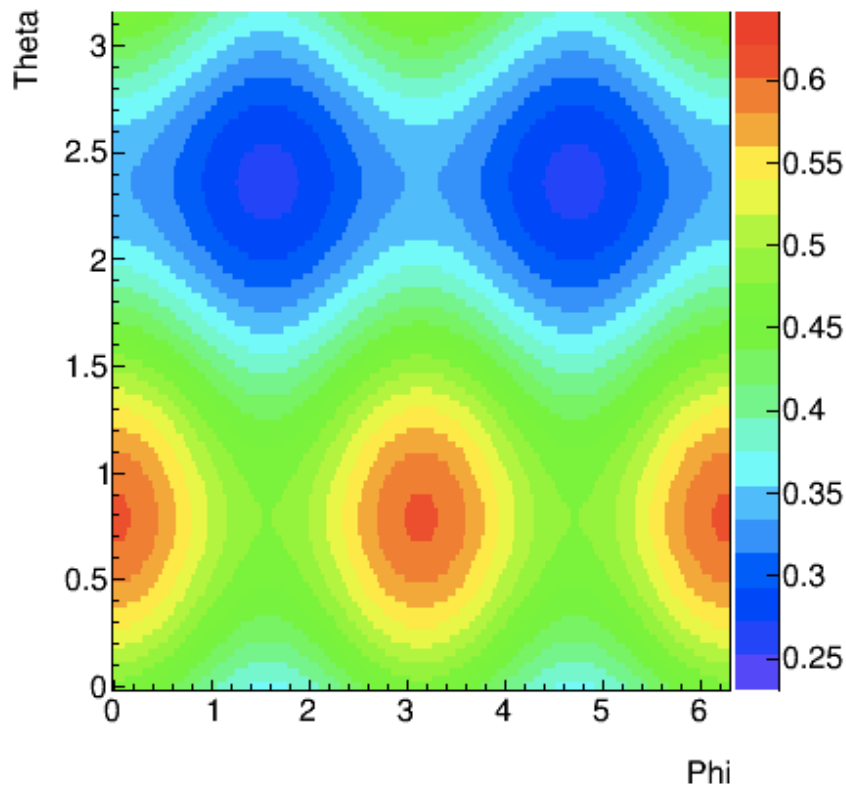
$P^{\text{det}}(x_{\text{true}})$       Probability to detect (=trigger) and select event  
6-D Interpolation from tabulated values -> fast

$P(\text{ev}_i | x_{\text{true}})$

# Detection Efficiency (1)



# Detection Efficiency (2)



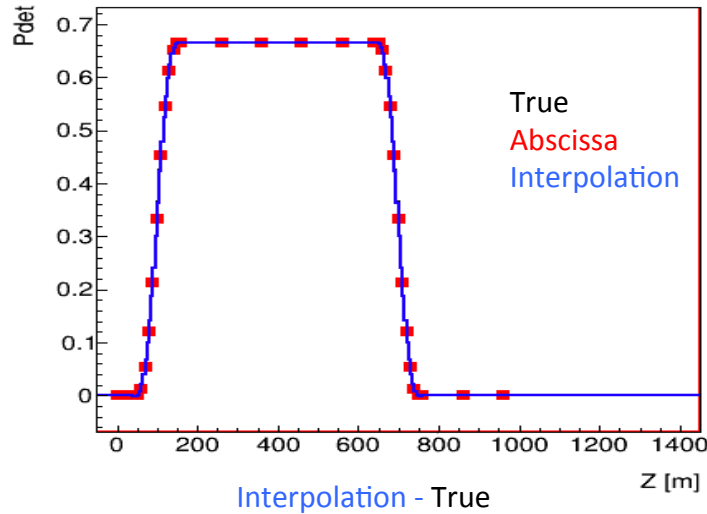


# What is Pdet?

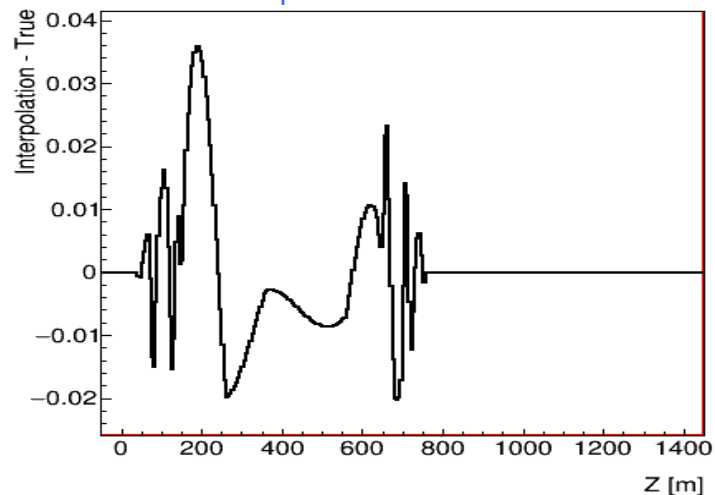
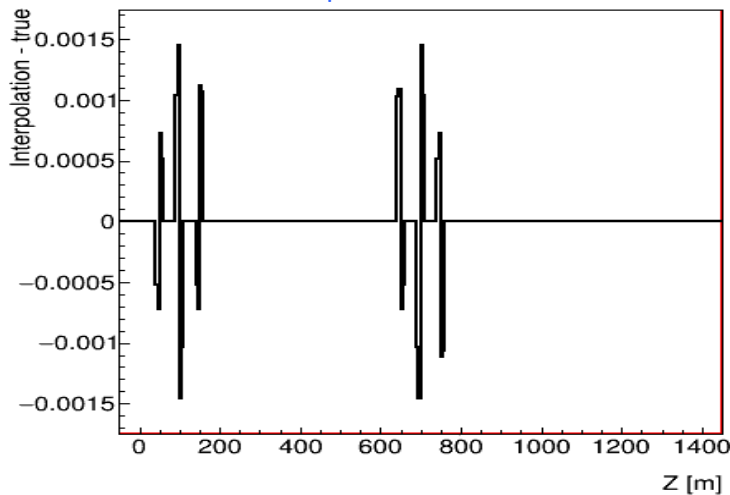
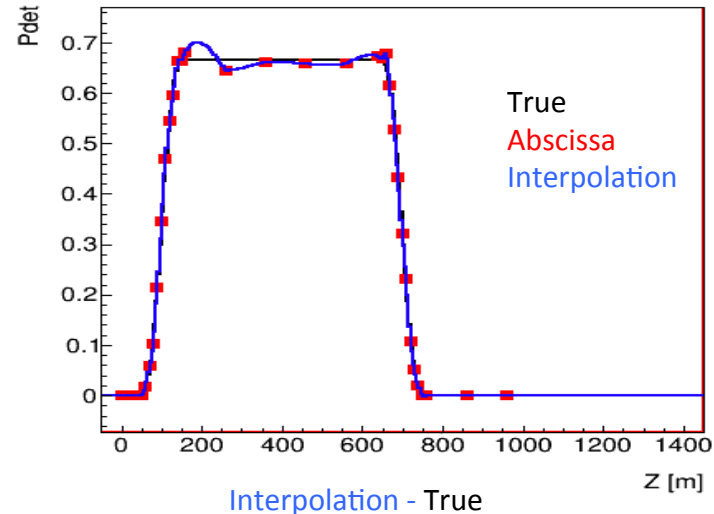
- Probability that an event:
  - Causes hits in detector: Jsirene
  - Leads to a trigger: JTriggerEfficiency
  - Is selected (reject atm. Muons): ??
- Get  $P_{\text{det}}(x_{\text{true}})$  by running MC events

# Statistical Fluctuations

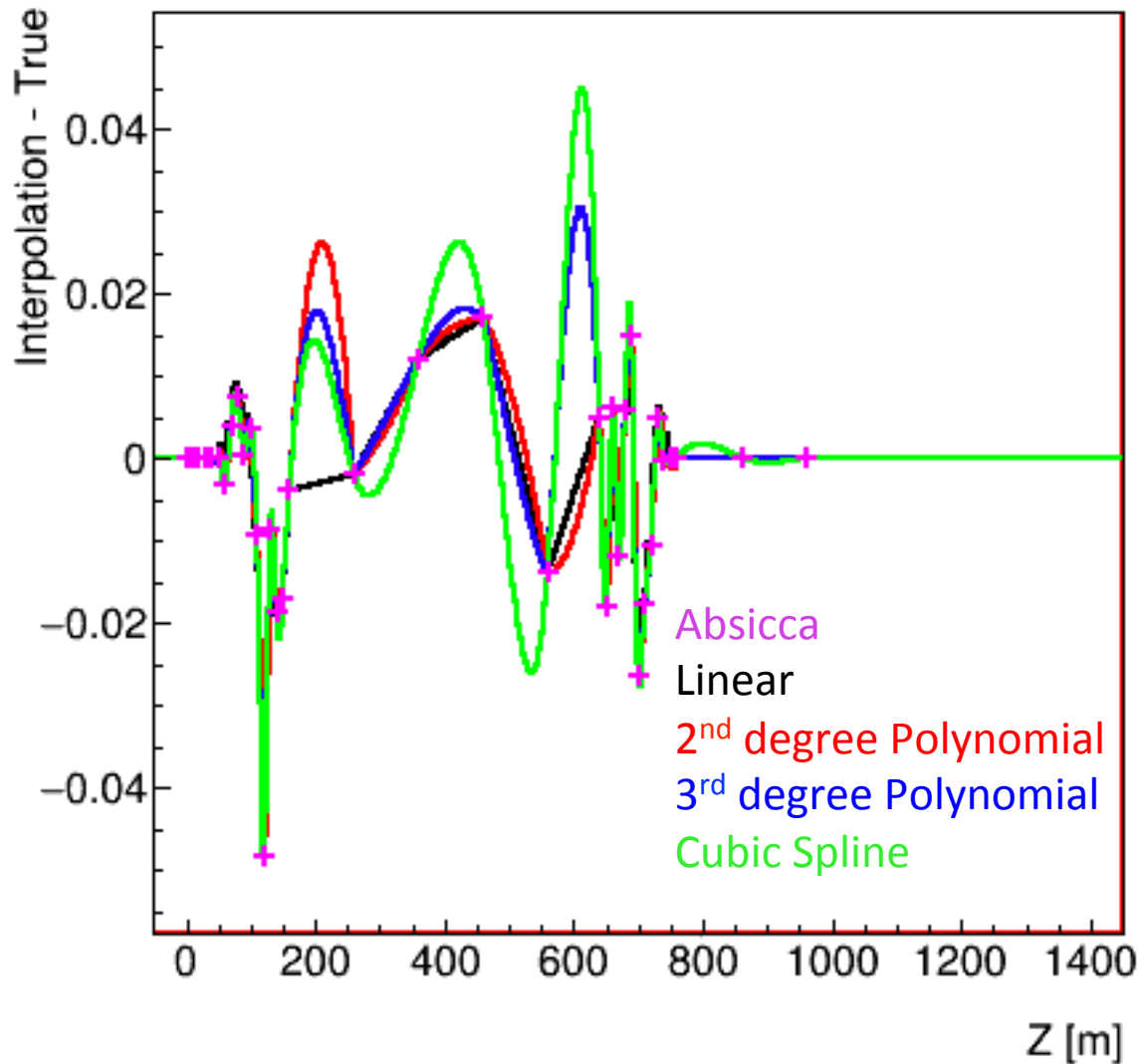
Ideal case: Infinite statistics



Realistic case: 1000 simulated events



# Different Interpolation Techniques

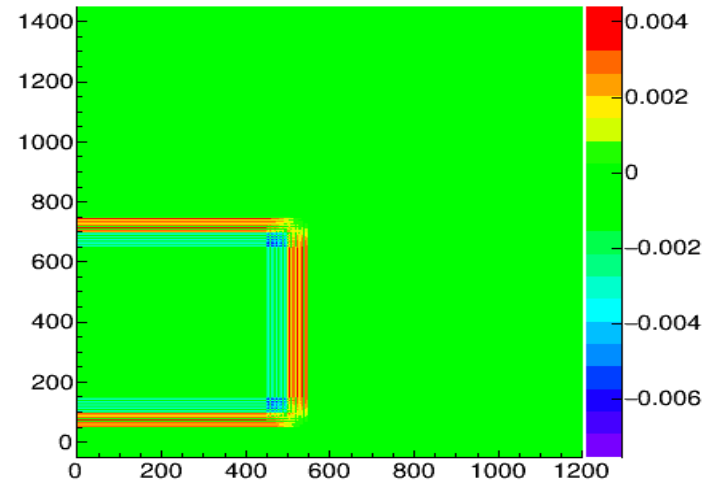
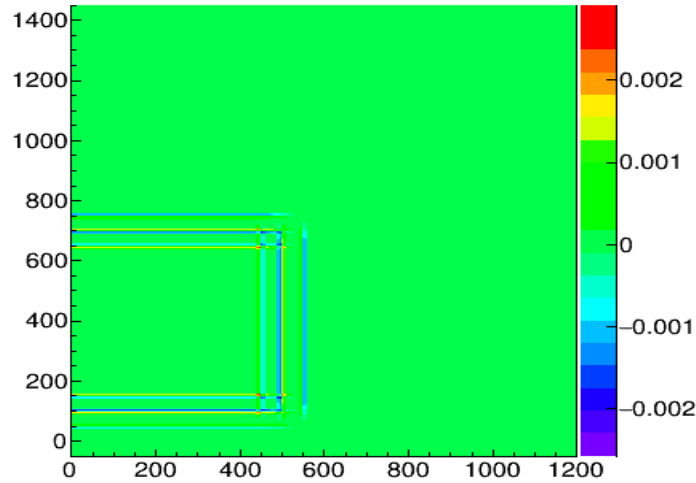


# Polynomial vs linear fit

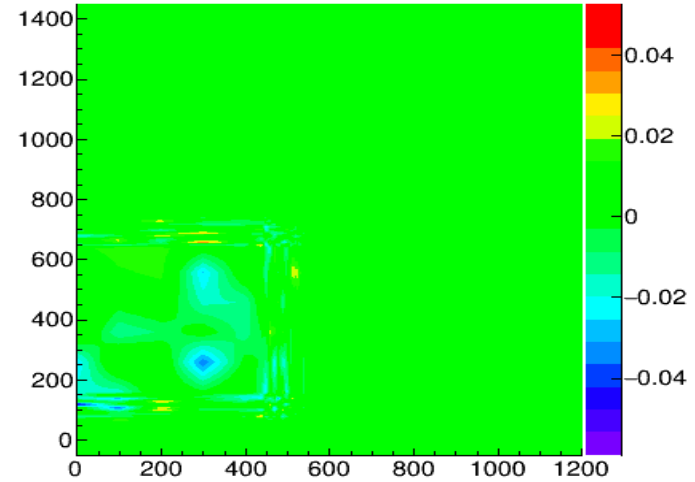
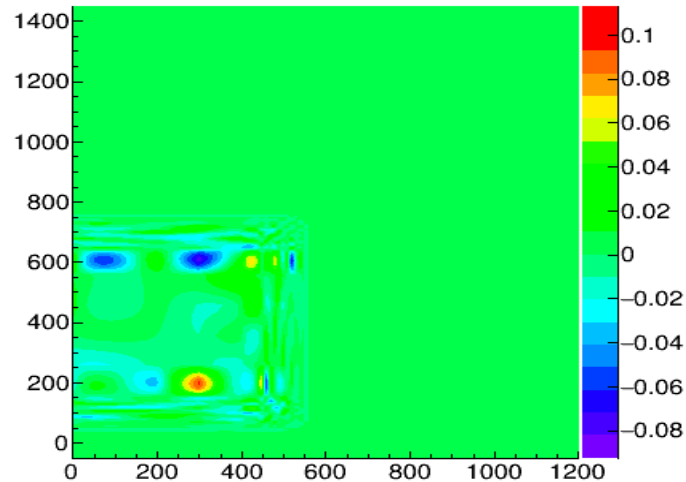
3<sup>rd</sup> degree polynomial

Linear fit

No stat. fluctuations



With stat. fluctuations



# Time Consumption

```
Scanning over 72000 Positions * 98 Directions * 1 Energy-bins = 7056000 points... Done in  
624169.543 ms elapsed  
623814.165 ms user  
    12.998 ms system  
99%CPU
```

3<sup>rd</sup> degree polynomial interpolation of 7 million points in 10 minutes

```
Scanning over 72000 Positions * 98 Directions * 1 Energy-bins = 7056000 points... Done in  
  
16068.632 ms elapsed  
16057.558 ms user  
    4.999 ms system  
99%CPU
```

Linear interpolation of 7 million points in 16 seconds

# Likelihood Ingredients

$$P(\text{data}|H) = \sum_i \left[ \log \int P(\text{ev}_i | x_{\text{true}}) \cdot P^{\text{det}}(x_{\text{true}}) \cdot \mu(x_{\text{true}} | H) dx_{\text{true}} \right] - \mu^{\text{tot}}(H)$$

$\mu(x_{\text{true}} | H)$       Number of expected background or signal events in our detector (can)

$P^{\text{det}}(x_{\text{true}})$       Probability to detect (=trigger) and select event

$P(\text{ev}_i | x_{\text{true}})$       Reconstruction, loop over PMTs.  $\text{Phit} * \text{Ptime} \rightarrow$  to do

# Conclusions

- New method seems promising
- Most ingredients in place
- ‘Reconstruction’ part to be done









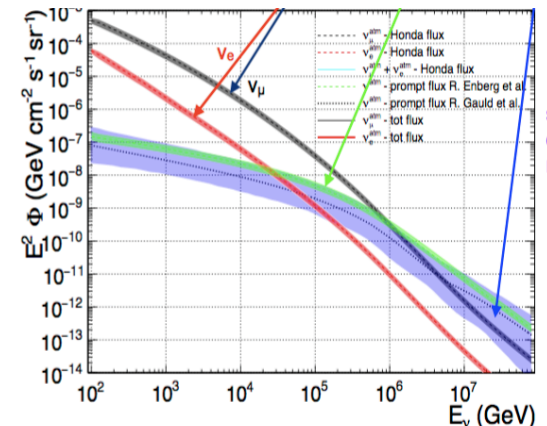
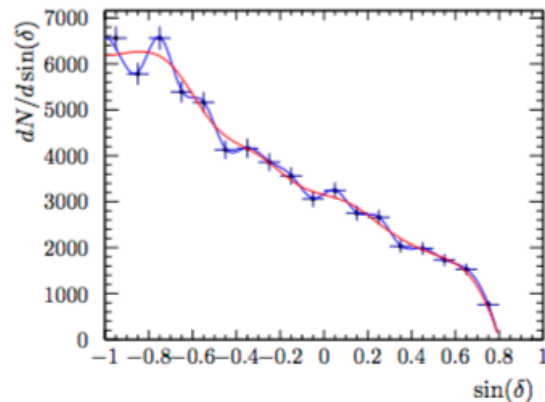
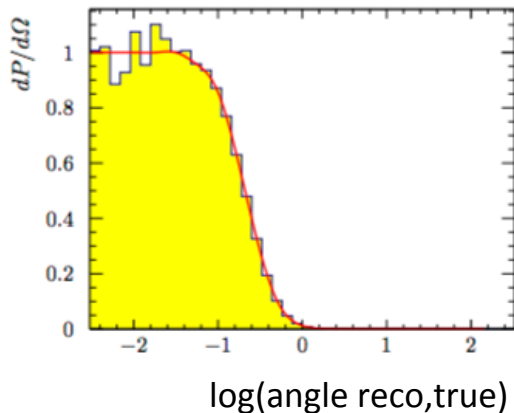
# Recap

$$\lambda = \log \left[ \frac{P(\text{data}|H_1)}{P(\text{data}|H_0)} \right]$$

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- New method:

$$P(\text{data}|H) = \sum_i \left[ \log \int P(ev_i | x_{true}) \cdot P^{det}(x_{true}) \cdot \mu(x_{true} | H) dx_{true} \right] - \mu^{tot}(H)$$

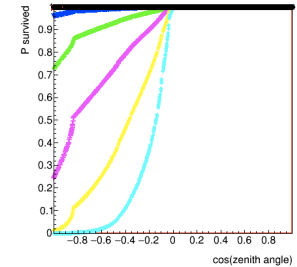
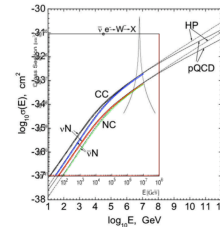
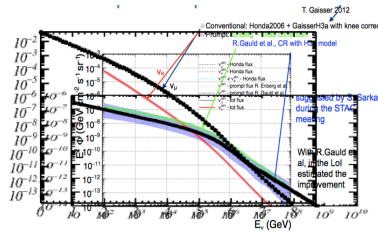
# Recap: Likelihood Ingredients

$$P(\text{data}|H) = \sum_i \left[ \log \int P(\text{ev}_i | x_{\text{true}}) \cdot P^{\text{det}}(x_{\text{true}}) \cdot \mu(x_{\text{true}} | H) dx_{\text{true}} \right] - \mu^{\text{tot}}(H)$$



$\mu(x_{\text{true}} | H)$

Number of expected background or signal events in our detector (can)



$P^{\text{det}}(x_{\text{true}})$

Probability to detect (=trigger) and select event



$P(\text{ev}_i | x_{\text{true}})$

Reconstruction, loop over PMTs.

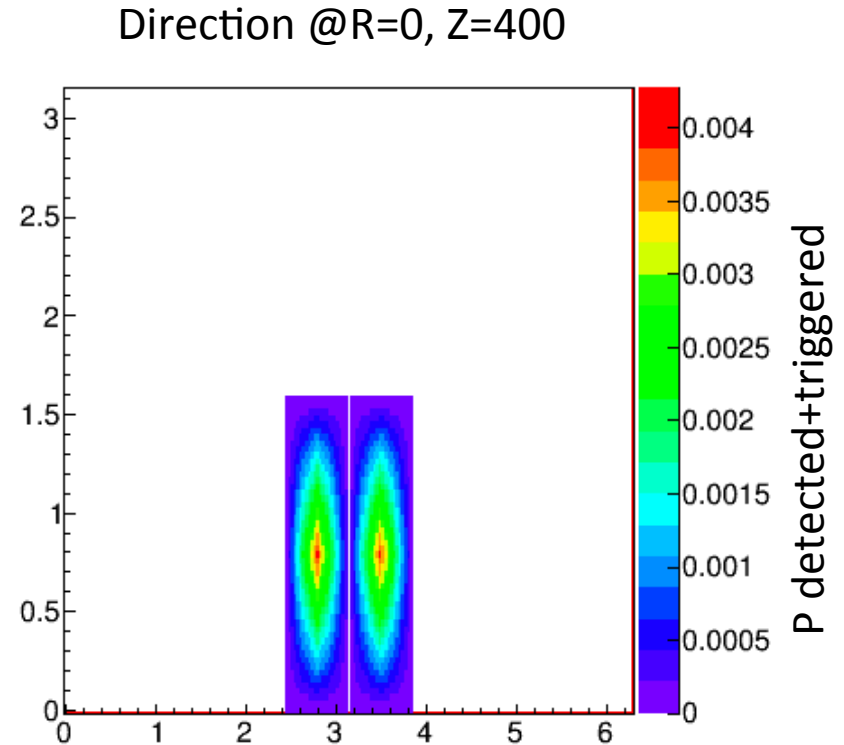
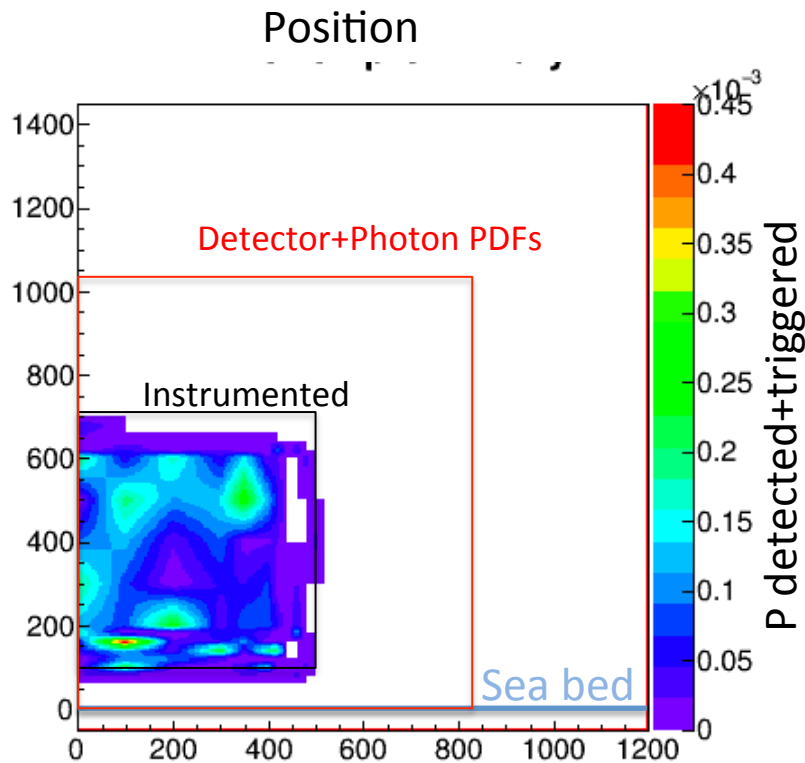
# Detection Efficiency

- For each neutrino energy, Bjorken- $\gamma$ , position, direction (6 parameters), DO:
- (Very fast) Monte Carlo generator:
  - Secondary particles
  - Photon propagation (JSirene)
  - Trigger
- Count fraction of trig. ev.
- Store in 6D interpolatable PDF table



# Detection Efficiency @ $10^2$ GeV

NC electron-neutrino (only single hadronic shower)

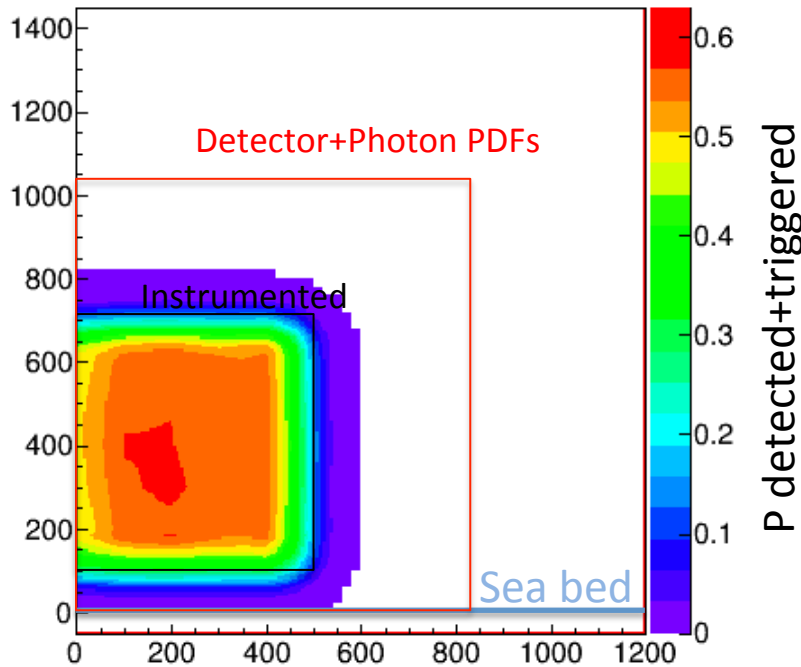




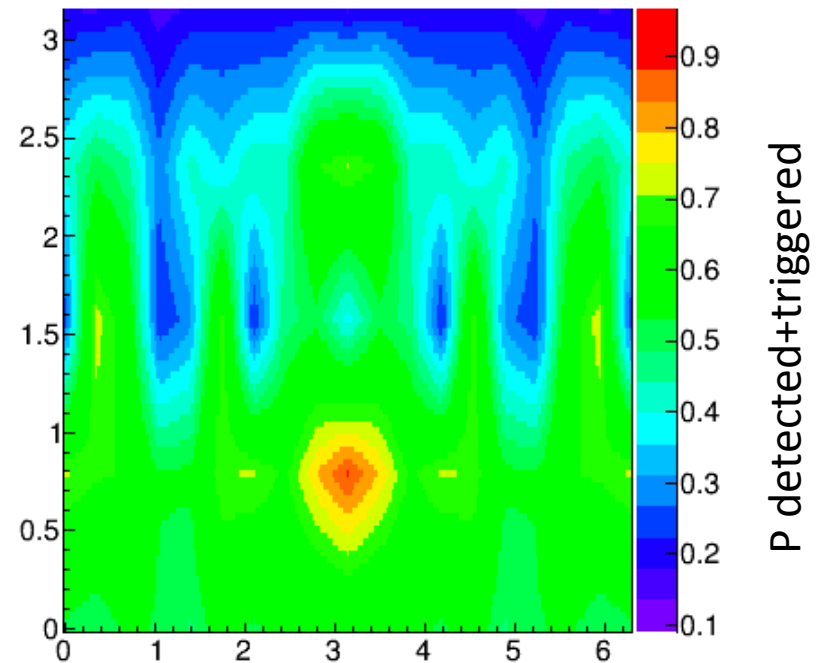
# Detection Efficiency @ $10^3$ GeV

NC electron-neutrino (only single hadronic shower)

Position



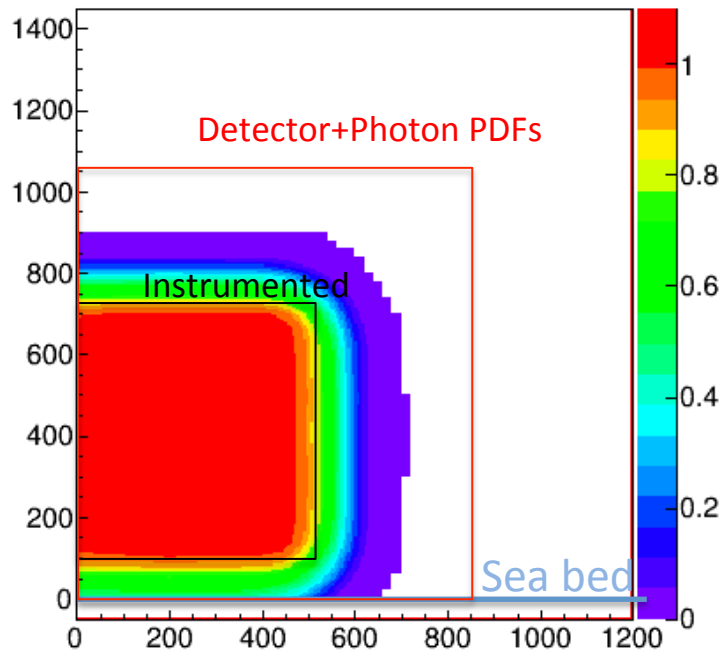
Direction @R=0, Z=400



# Detection Efficiency @ $10^4$ GeV

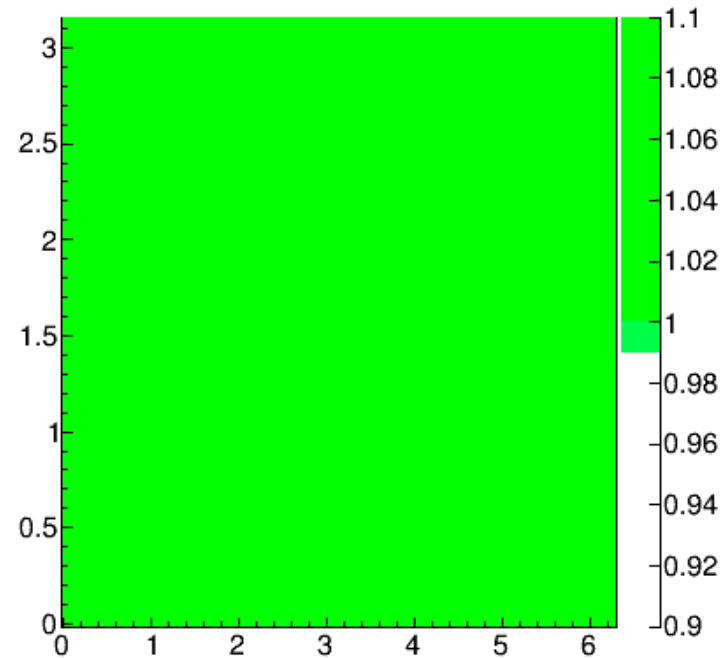
NC electron-neutrino (only single hadronic shower)

Position



P detected+triggered

Direction @R=0, Z=400

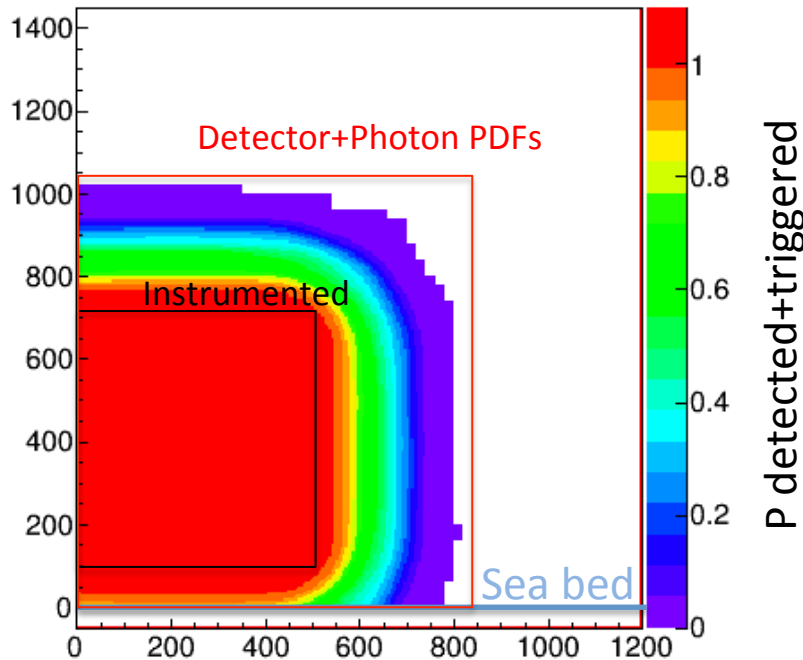


P detected+triggered

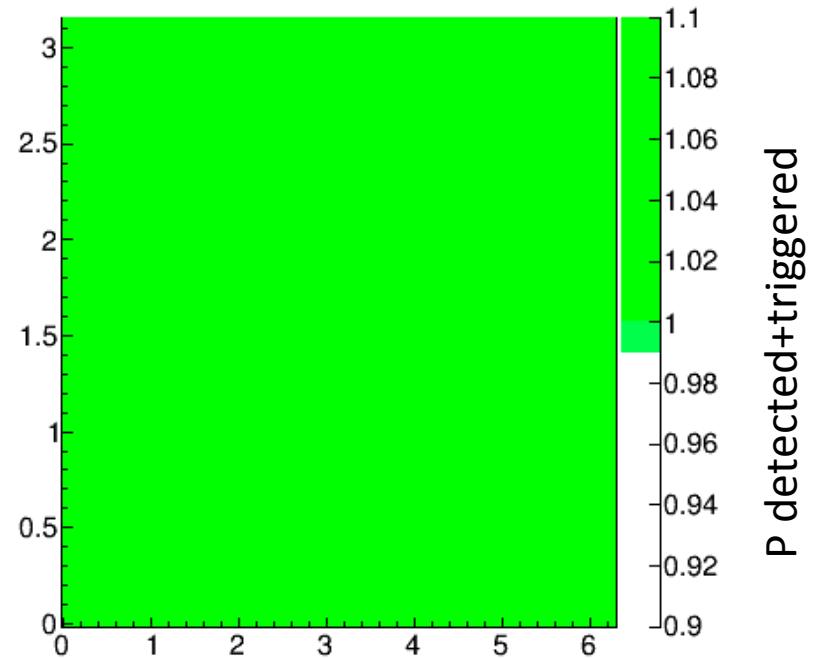
# Detection Efficiency @ $10^5$ GeV

NC electron-neutrino (only single hadronic shower)

Position



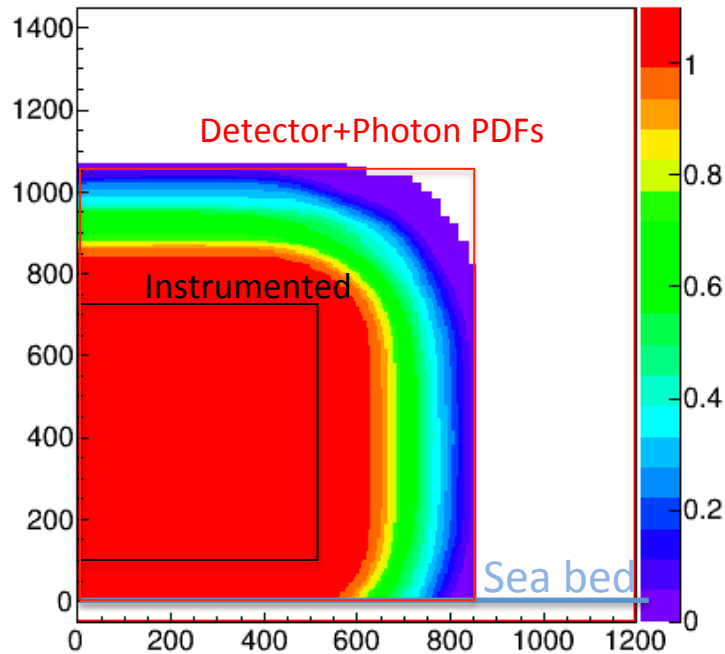
Direction @R=0, Z=400



# Detection Efficiency @ $10^6$ GeV

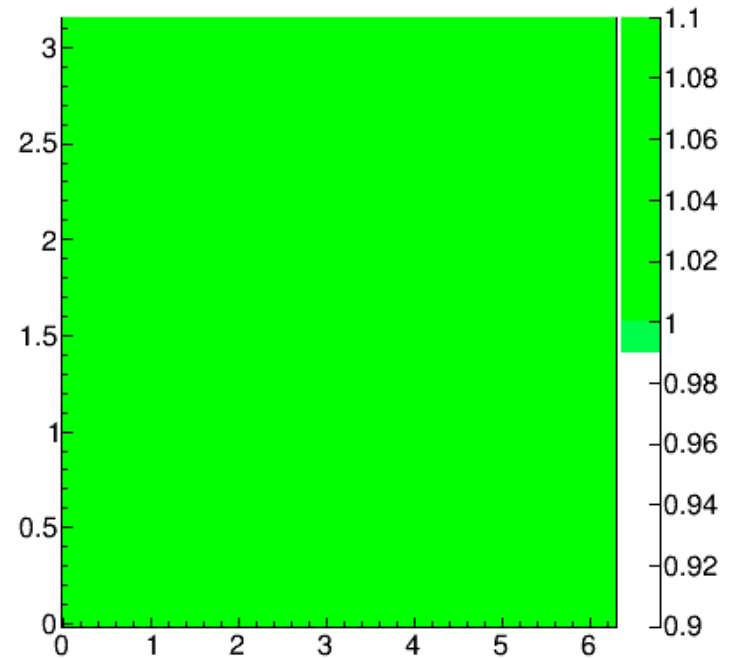
NC electron-neutrino (only single hadronic shower)

Position



P detected+triggered

Direction @R=0, Z=400

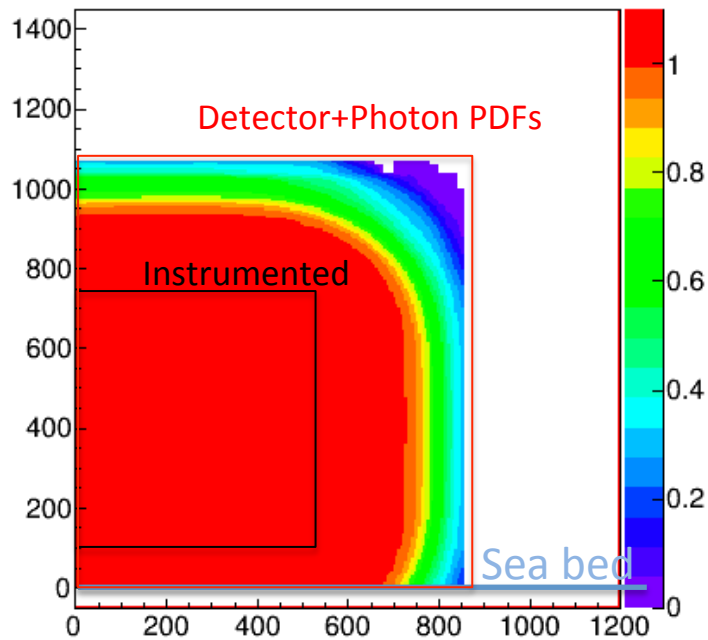


P detected+triggered

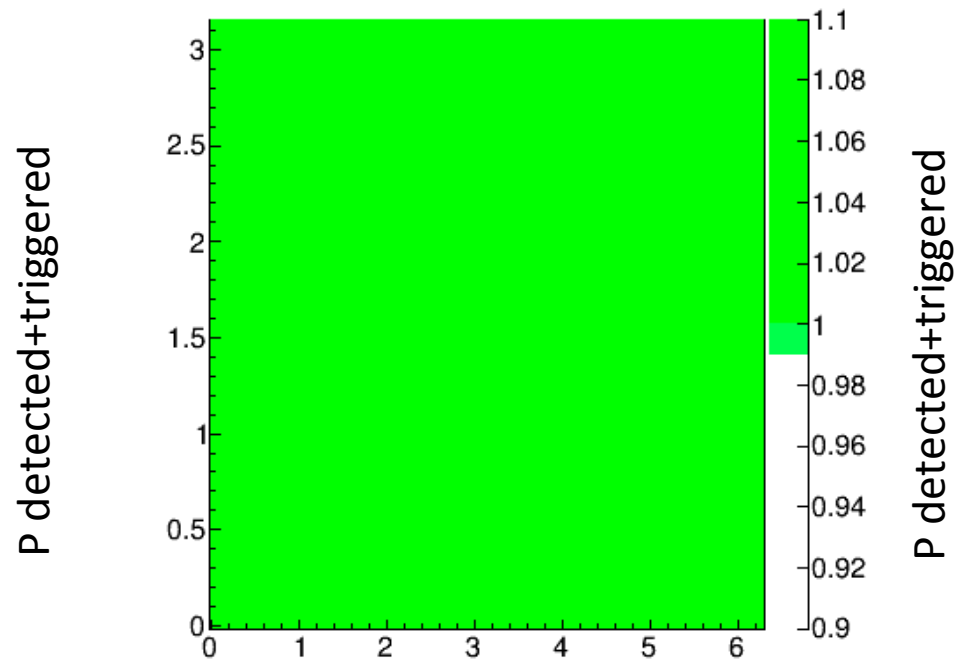
# Detection Efficiency @ $10^7$ GeV

NC electron-neutrino (only single hadronic shower)

Position



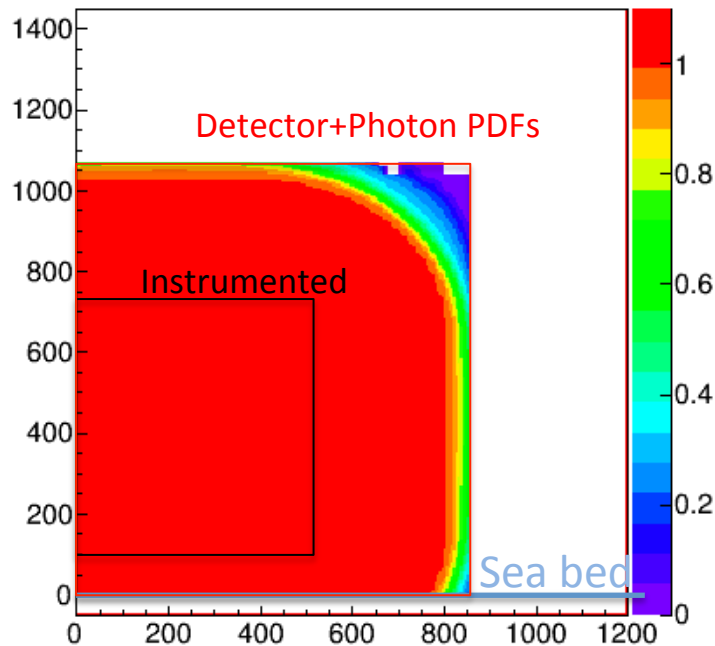
Direction @R=0, Z=400



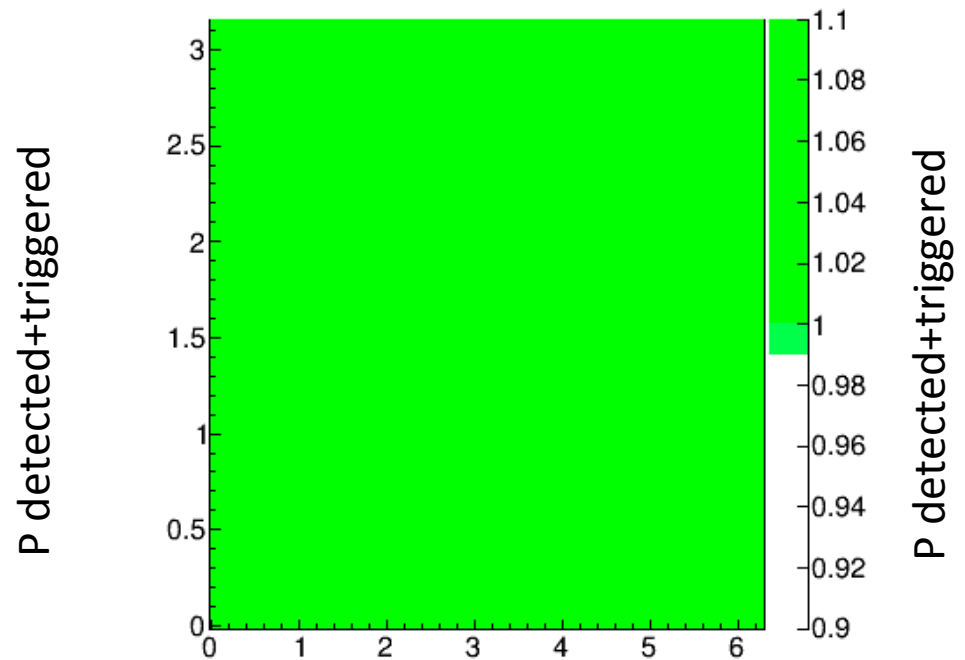
# Detection Efficiency @ $10^8$ GeV

NC electron-neutrino (only single hadronic shower)

Position



Direction @R=0, Z=400



# Likelihood Ingredients

$$P(\text{data}|H) = \sum_i \left[ \log \int P(\text{ev}_i | x_{\text{true}}) \cdot P^{\text{det}}(x_{\text{true}}) \cdot \mu(x_{\text{true}} | H) dx_{\text{true}} \right] - \mu^{\text{tot}}(H)$$



$\mu(x_{\text{true}} | H)$       Number of expected background or signal events in our detector (can)



$P^{\text{det}}(x_{\text{true}})$       Probability to detect (=trigger) and select event



$P(\text{ev}_i | x_{\text{true}})$       Probability to obtain measured event  $\text{ev}_i$   
**given** a certain neutrino hypothesis  $x_{\text{true}}$

# Event Probability D.F.

$$P(ev | x) = \prod_{\text{hit PMTs}} [P_i^{\text{hit}} \cdot P_i^{t \text{ 1st}}] \cdot \prod_{\text{non hit PMTs}} [1 - P_i^{\text{hit}}]$$

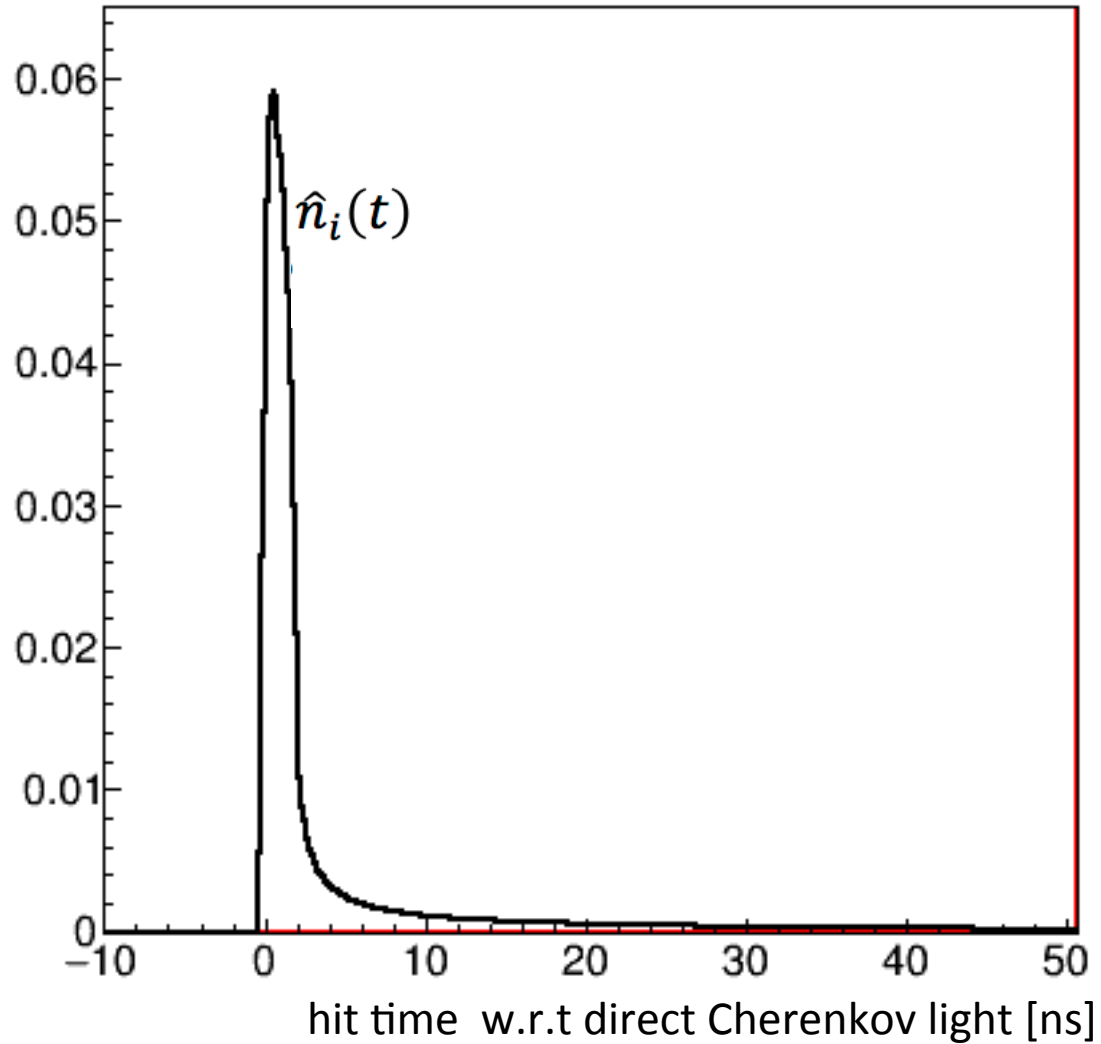
$$P_i^{\text{hit}} = 1 - \exp \left( - \int_{-\infty}^{\infty} \hat{n}_i(t) dt \right)$$

Expected number of photons from 40K and shower/track on PMT i at time t

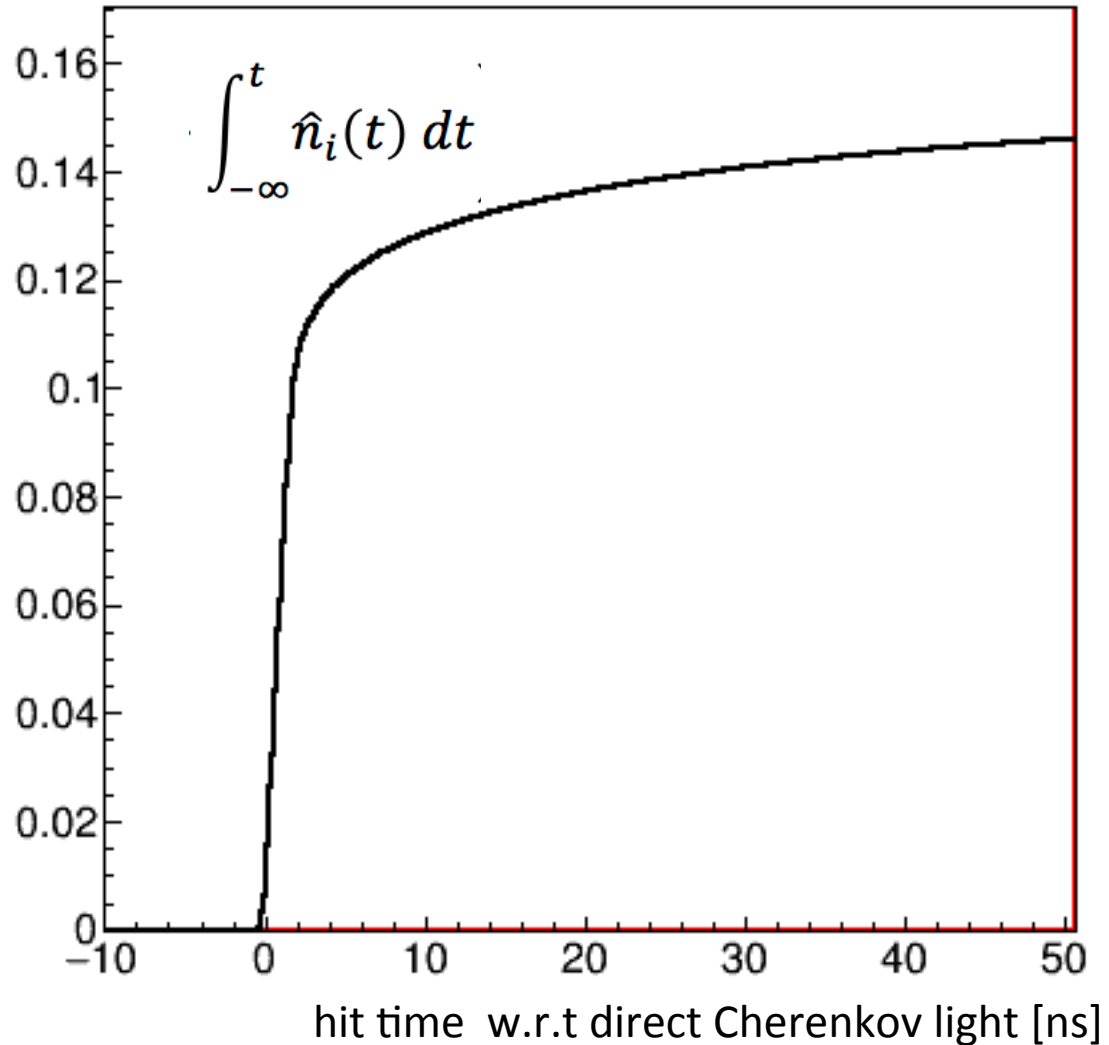
$$P_i^{t \text{ 1st}} \cdot P_i^{\text{hit}} = \underbrace{\exp \left( - \int_{-\infty}^t \hat{n}_i(t) dt \right)}_{\text{P not hit before t}} \cdot \underbrace{(1 - \exp(-\hat{n}_i(t)))}_{\text{P hit at t}}$$



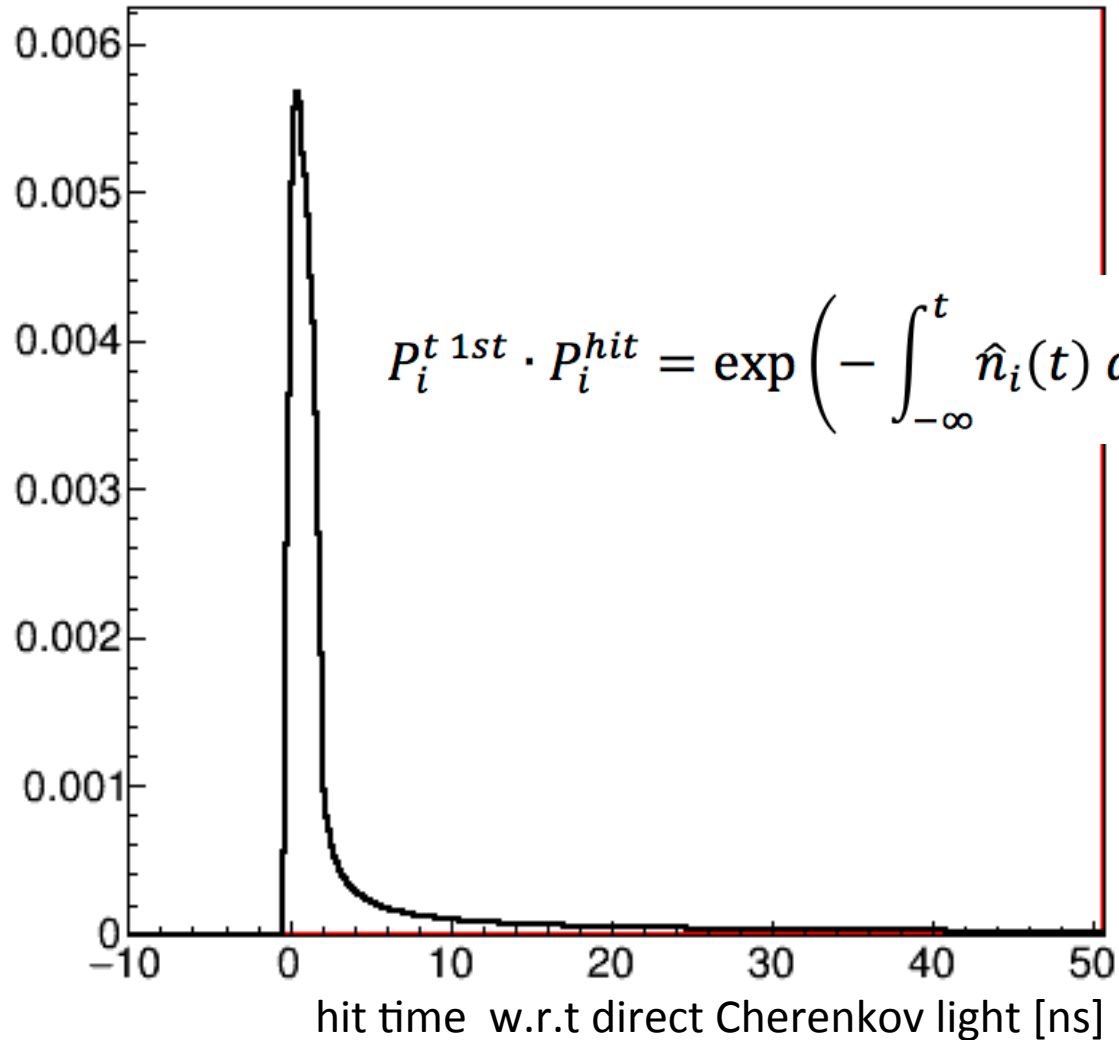
# Hit Time PDF



# Hit Time PDF



# Hit Time PDF



# Hits in ~~Theory~~ Practice

- Presence of  $^{40}\text{K}$  background hits

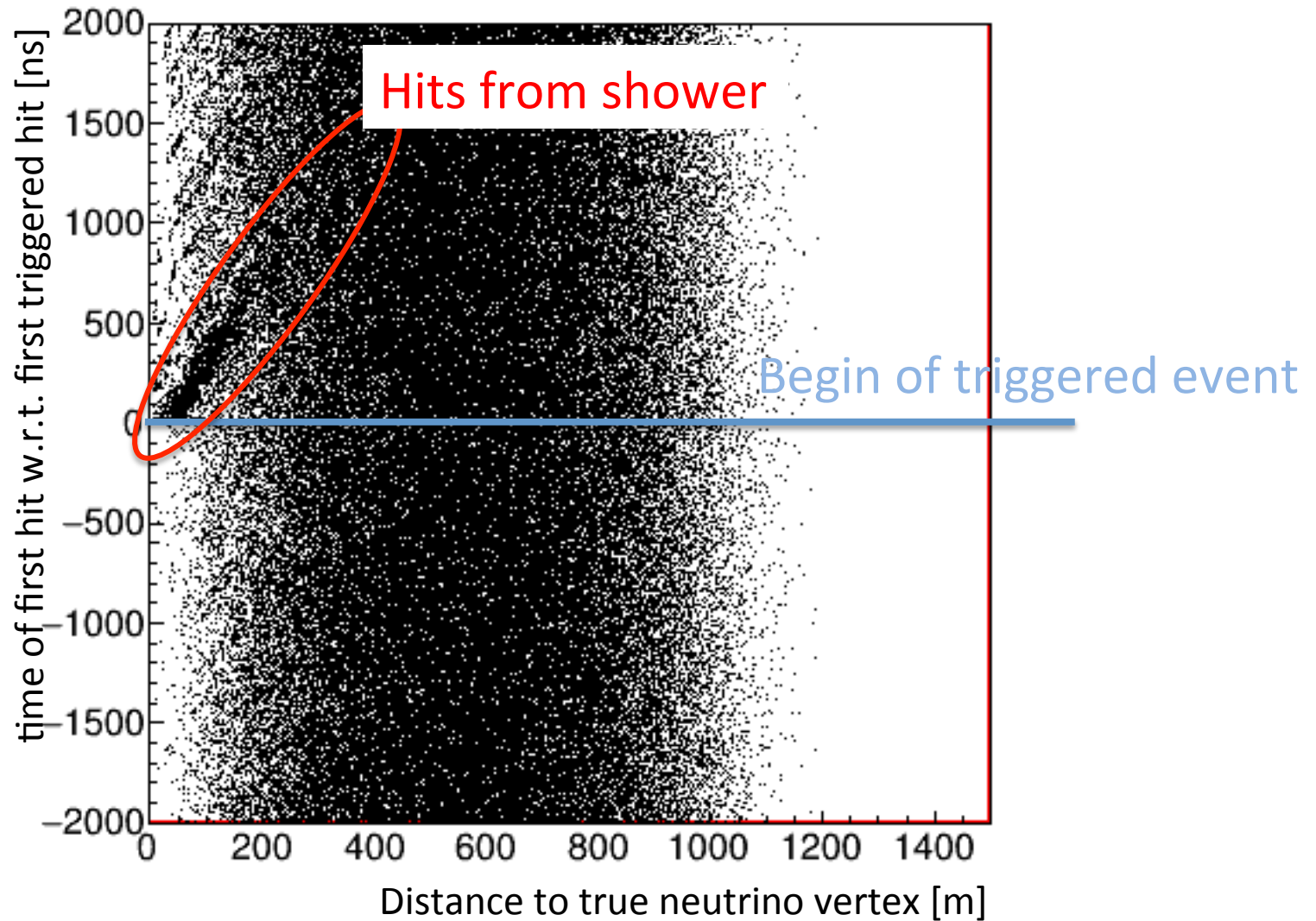
$$P_i^{1st} \cdot P_i^{hit} = \exp\left(-\int_{-\infty}^t \hat{n}_i(t) dt\right) \cdot (1 - \exp(-\hat{n}_i(t)))$$

- If all hit times are selected: signal will be overwhelmed by background
- Solution: only select hits in certain time window

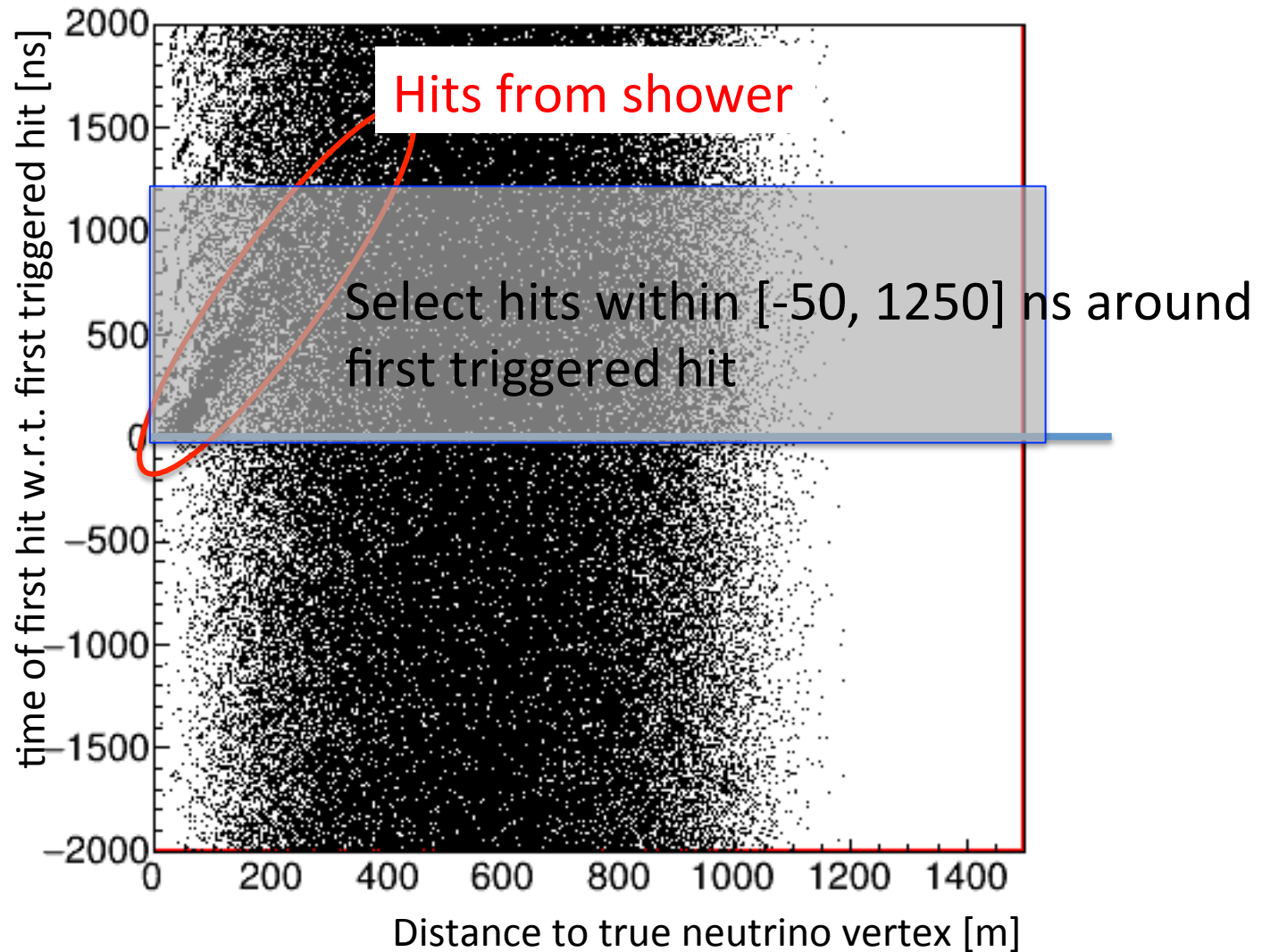
# Hit Selection Time Window

- Select Hits around expected hit time from given hypothesis
  - Advantage: Very pure selection
  - Drawback: biased selection
- Solution: Select hits around triggered event

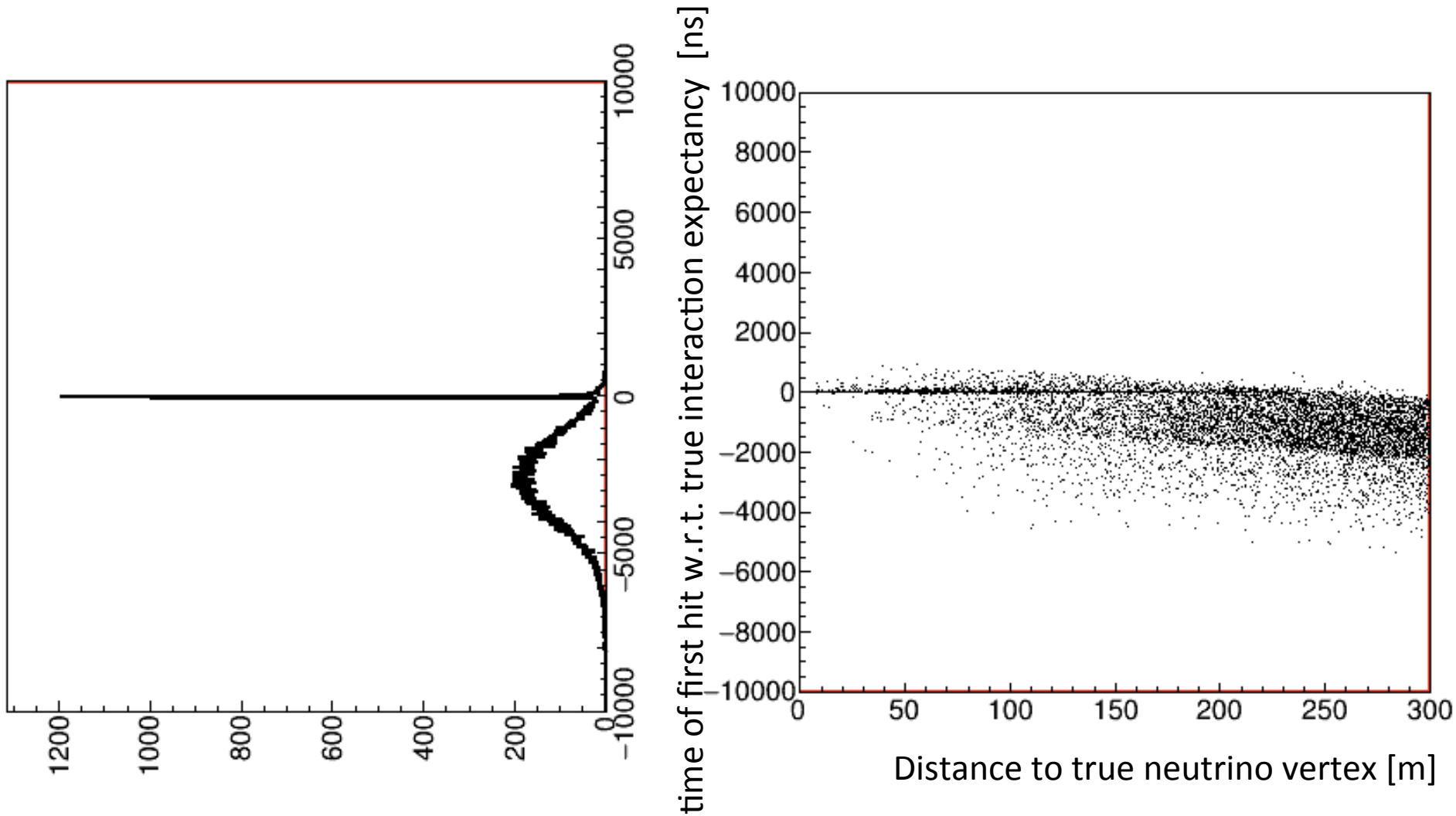
# Hit Times



# Hit Times

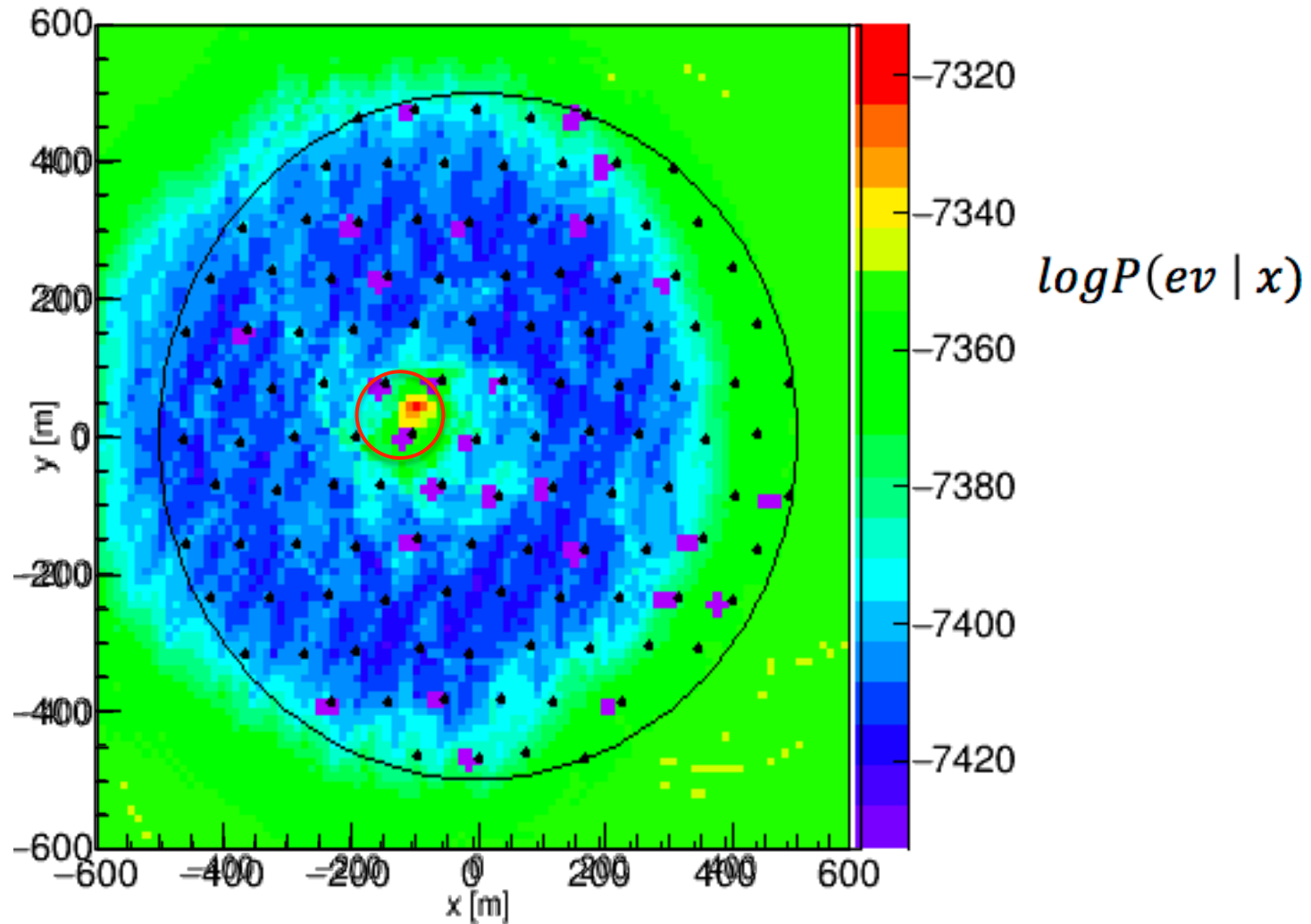


# Hit Times w.r.t. direct Cher. light



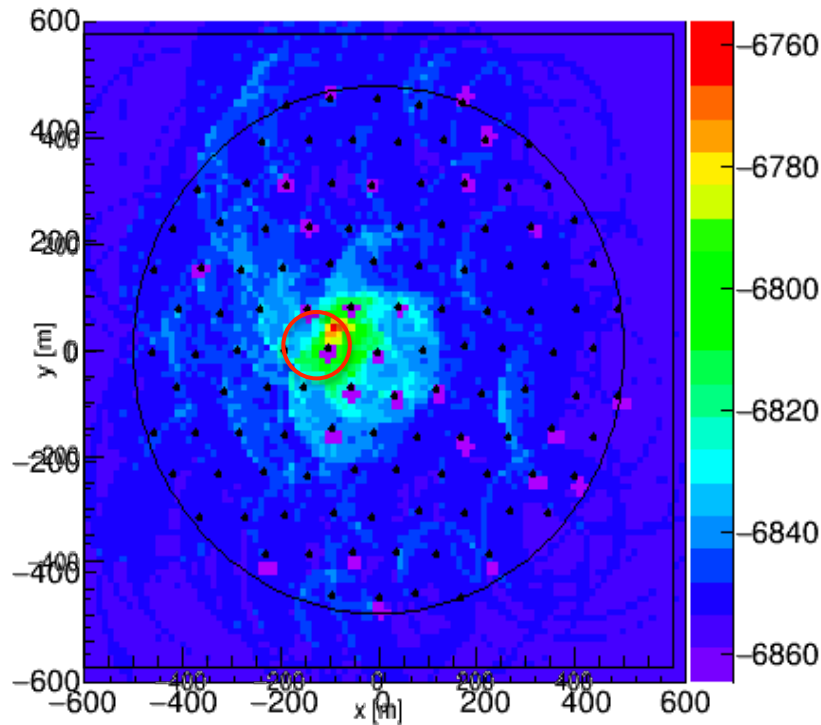


$$P(ev | x) = \prod_{\text{hit PMTs}} [P_i^{\text{hit}} \cdot P_i^{\text{t 1st}}] \cdot \prod_{\text{non hit PMTs}} [1 - P_i^{\text{hit}}]$$

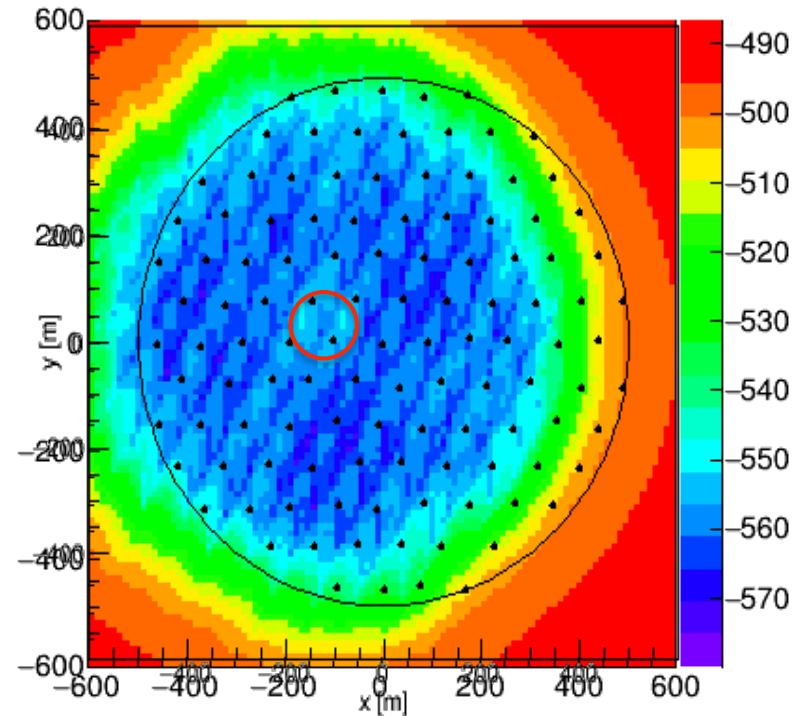


$$\log P(ev | x) = \sum_{\text{hit PMTs}} [\log (P_i^{\text{hit}}) + \log (P_i^{t \text{ 1st}})] + \sum_{\text{non hit PMTs}} [\log (1 - P_i^{\text{hit}})]$$

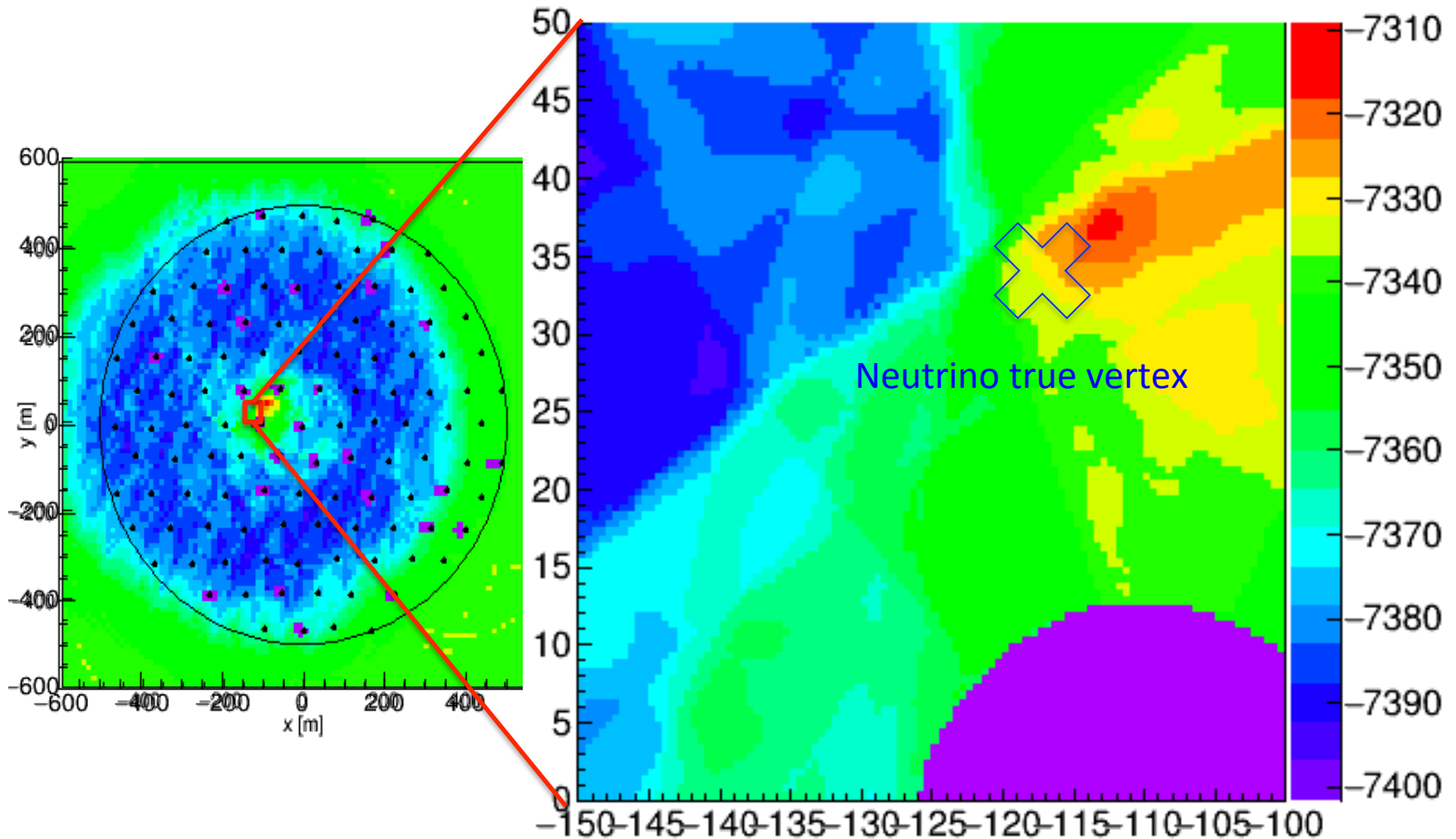
Hit PMTs



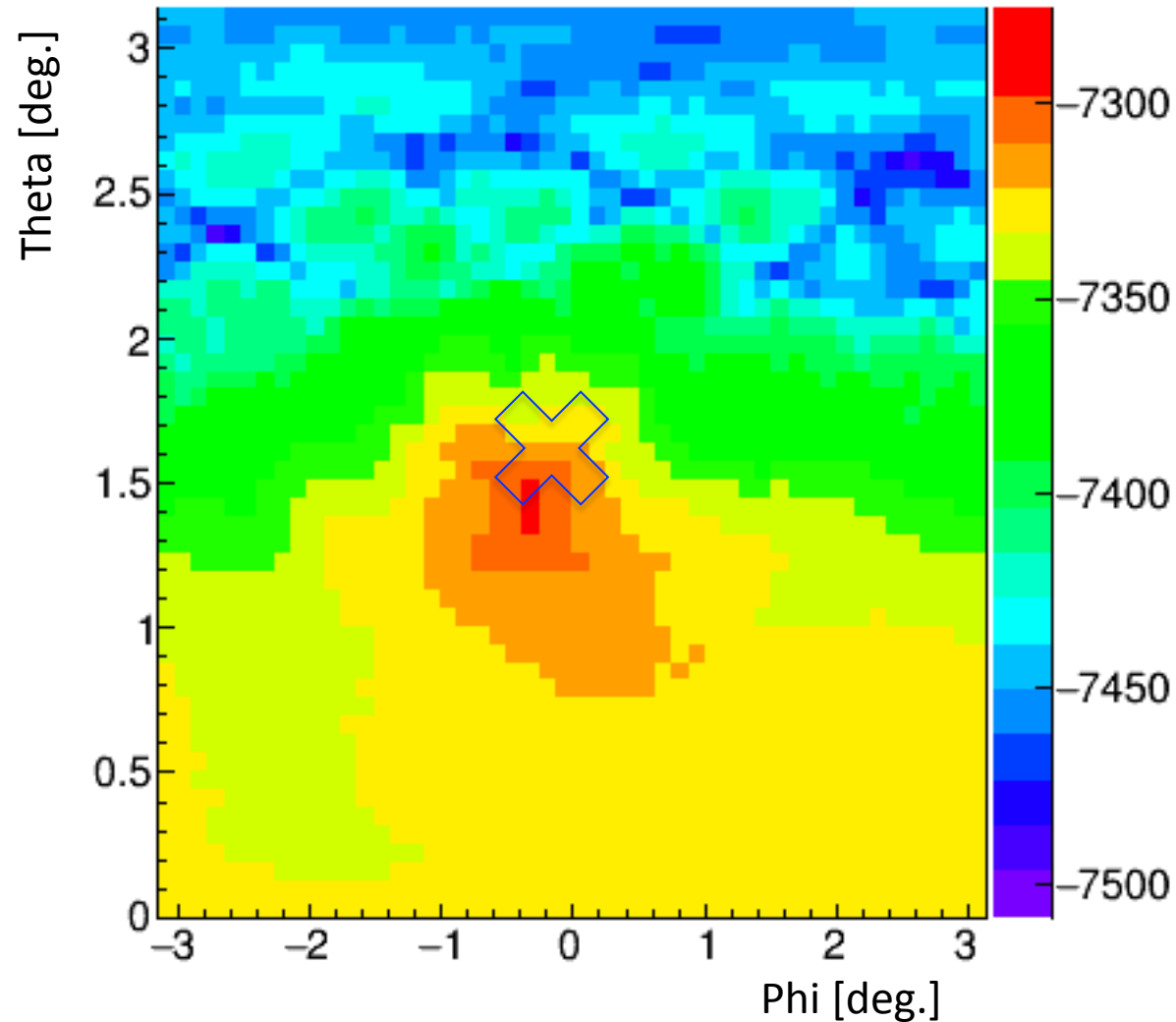
Not hit PMTs



# Event Probability: Position



# Event Probability: Direction



# Likelihood Ingredients

$$P(\text{data}|H) = \sum_i \left[ \log \int P(\text{ev}_i | x_{\text{true}}) \cdot P^{\text{det}}(x_{\text{true}}) \cdot \mu(x_{\text{true}} | H) dx_{\text{true}} \right] - \mu^{\text{tot}}(H)$$



$\mu(x_{\text{true}} | H)$

Number of expected background or signal events in our detector (can)



$P^{\text{det}}(x_{\text{true}})$

Probability to detect (=trigger) and select event



$P(\text{ev}_i | x_{\text{true}})$

Probability to obtain measured event  $\text{ev}_i$   
**given** a certain neutrino hypothesis  $x_{\text{true}}$

# How to solve the 8D integral?

$$P(data|H) = \sum_i \left[ \log \int P(ev_i | x_{true}) \cdot P^{det}(x_{true}) \cdot \mu(x_{true} | H) dx_{true} \right] - \mu^{tot}(H)$$

- Interaction vertex position (3D)
- Interaction time (1D)
- (Neutrino) Direction (2D)
- Neutrino Energy (1D)
- Bjorken-y (1D)

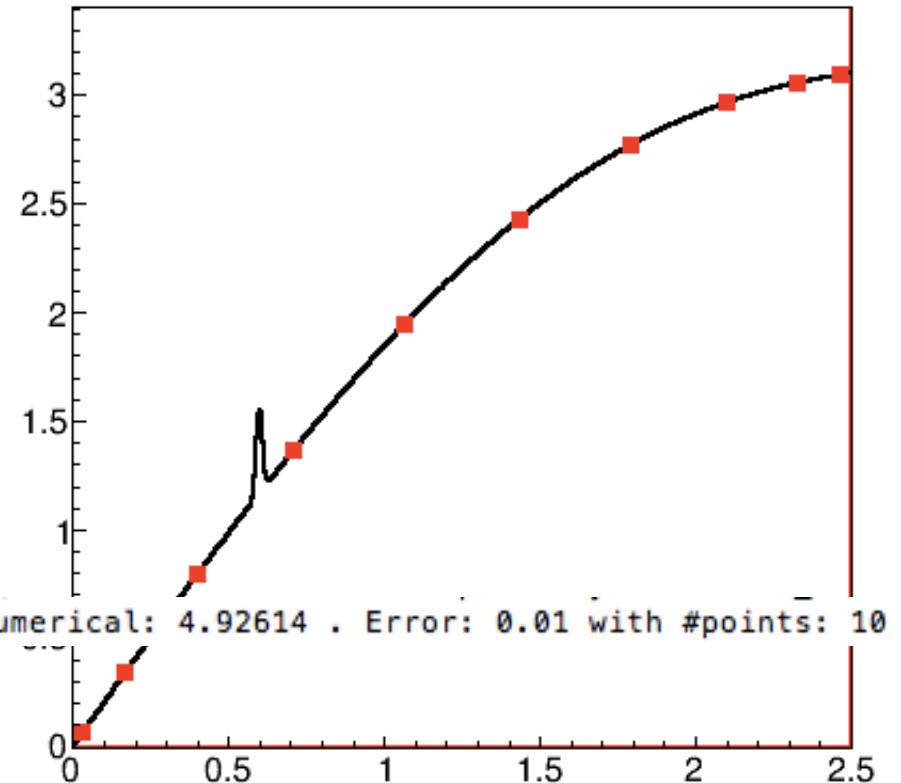
# How to solve the ~~8D~~ 6D integral?

$$P(\text{data}|H) = \sum_i \left[ \log \int P(\text{ev}_i | x_{\text{true}}) \cdot P^{\text{det}}(x_{\text{true}}) \cdot \mu(x_{\text{true}} | H) dx_{\text{true}} \right] - \mu^{\text{tot}}(H)$$

- Interaction vertex position (3)
- Interaction time (1)
  - Relatively easy once other params. are given?
- (Neutrino) Direction (2)
- Neutrino Energy (1)
  - Analytically?
- Bjorken-y (1)

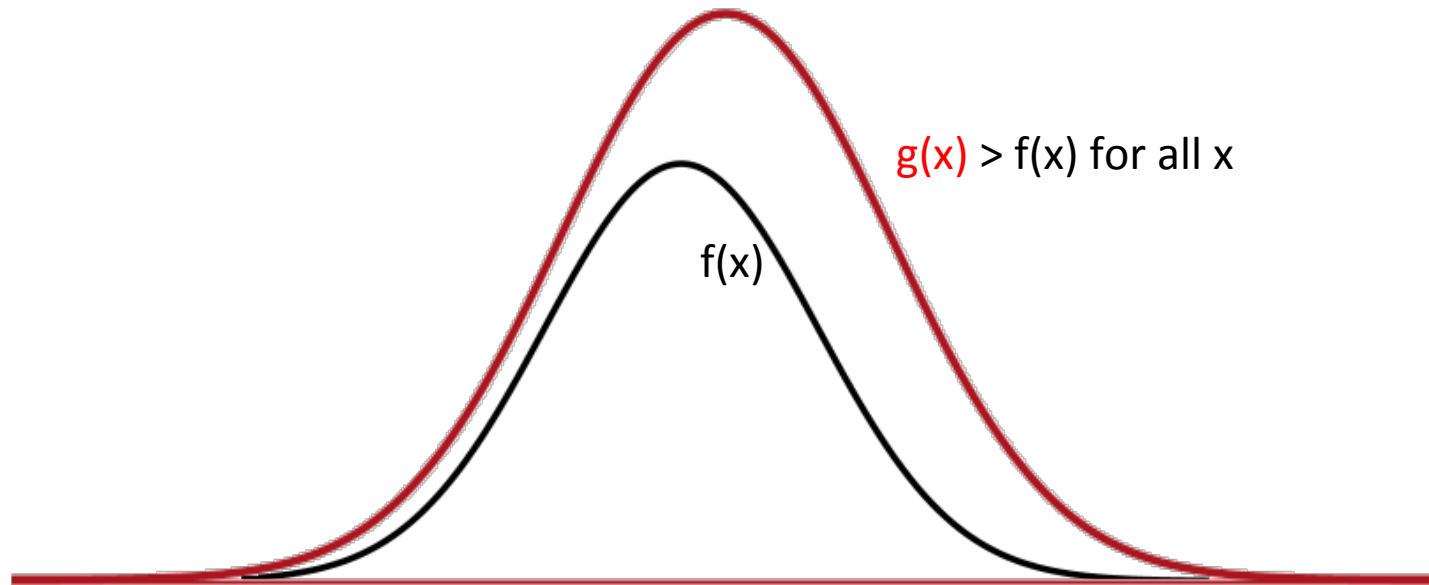
# Difficulties

- Event PDF is in general sharply peaked
  - ~1 degree (showers),  
~0.1 degree (tracks)
  - ~1m (showers)
- Algorithm generally misses this peak
- Each function evaluation takes time





# MC Integration Techniques (1)

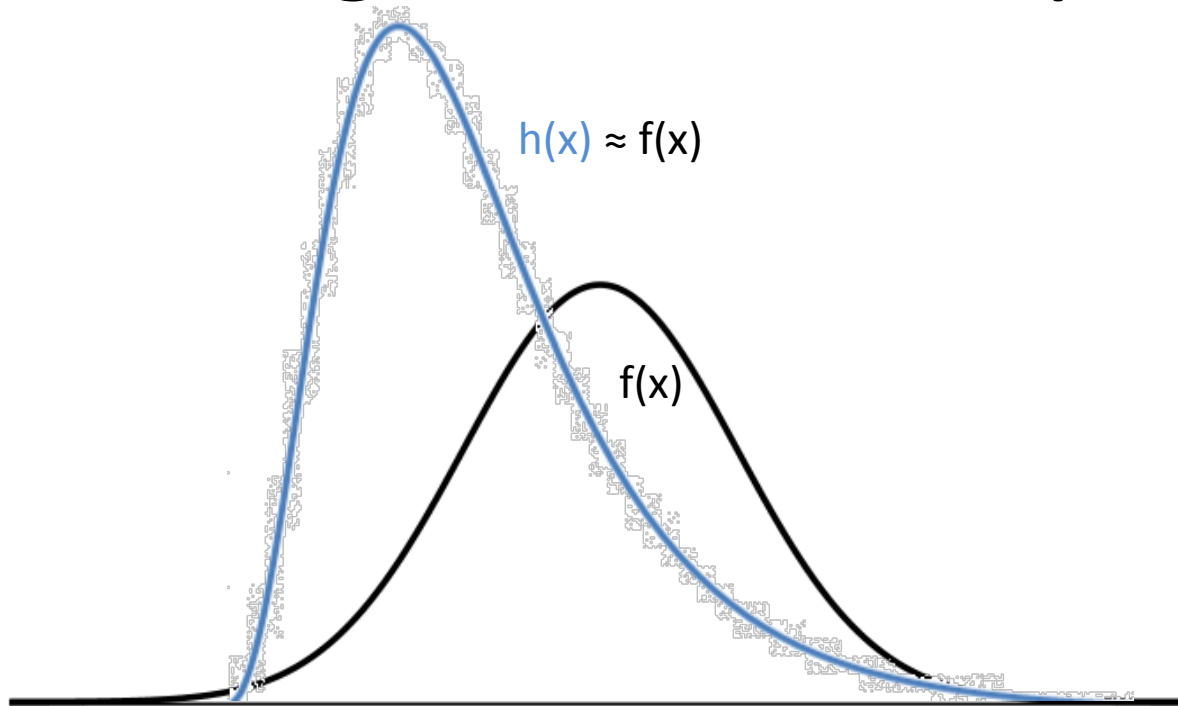


N times:

- 1) Random  $x$  from  $g(x)$
- 2) Random  $y$ ,  $0 < y < g(x)$
- 3) If  $y \leq f(x)$  {  $n++$  }

$$I = \int f(x) dx = n/N * \int g(x) dx$$

# MC Integration Techniques (2)

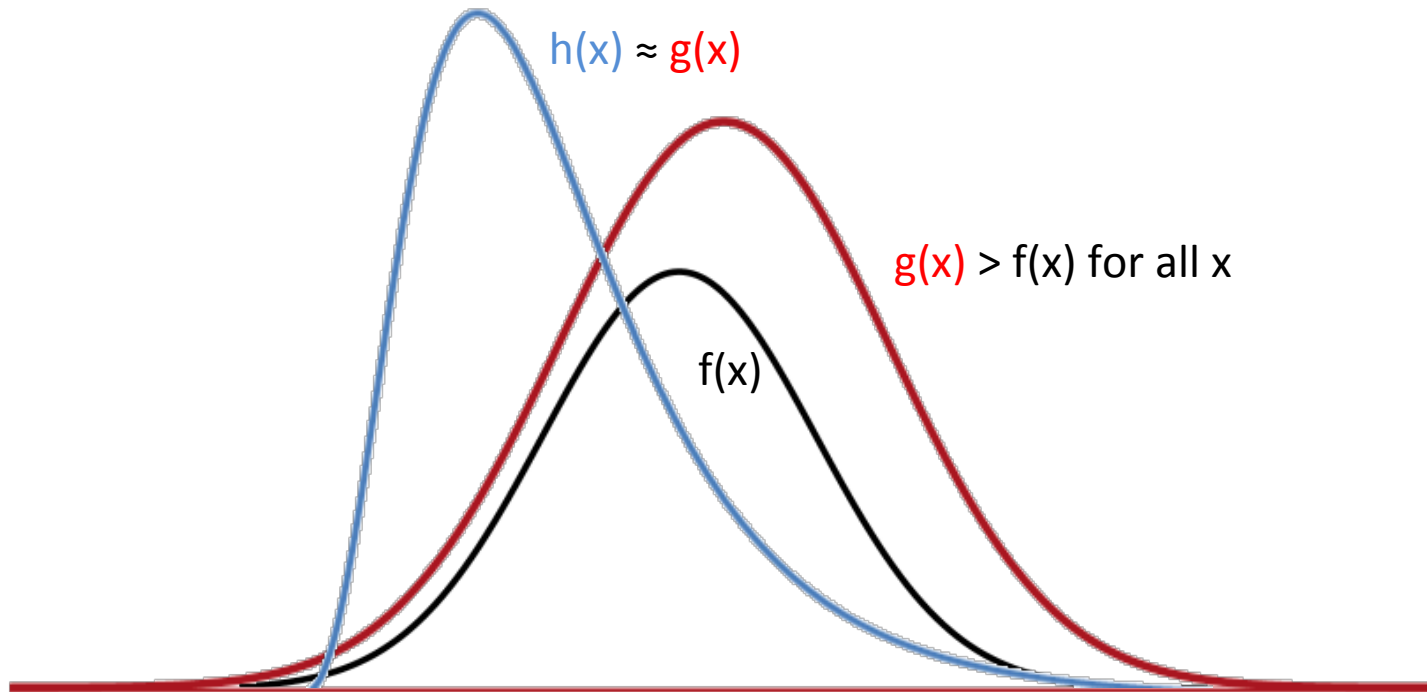


N times:

- 1) Random  $x$  from  $h(x)$
- 2)  $A += f(x)/h(x)$

$$I = \int f(x) dx = A/N * \int h(x) dx$$

# Combined

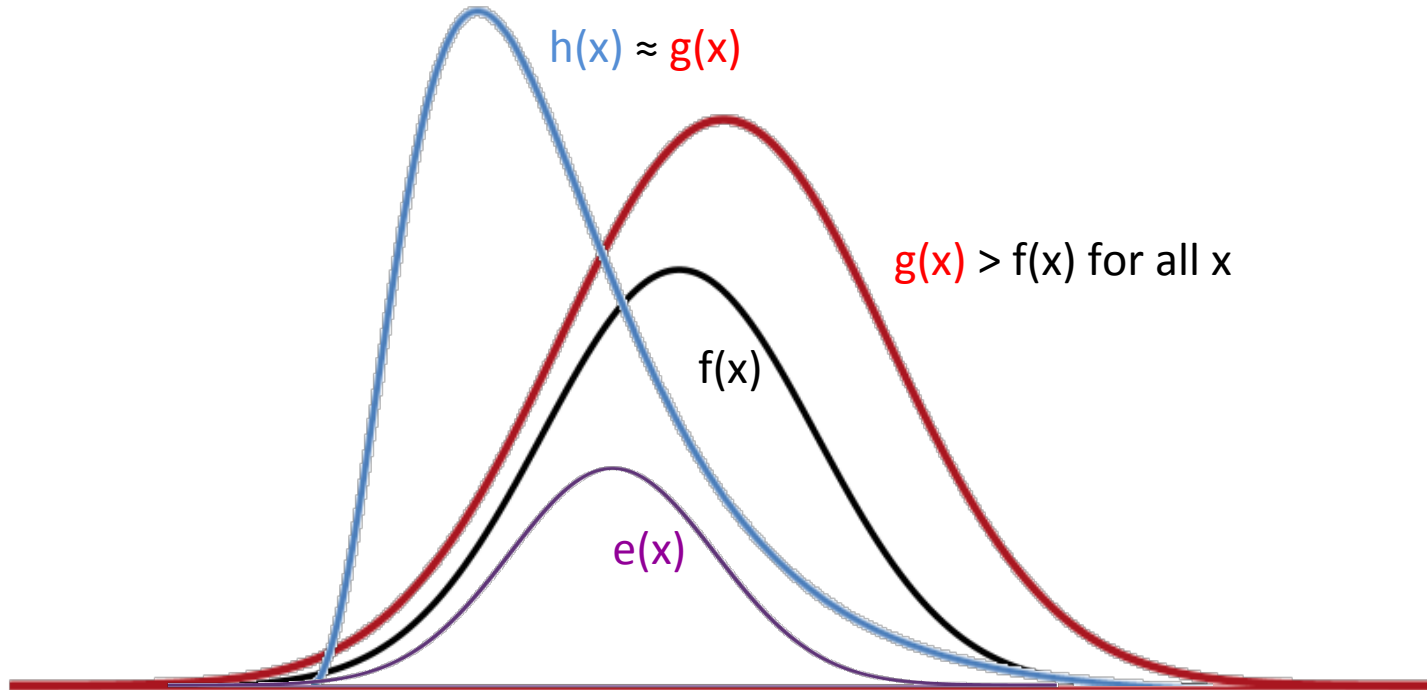


N times:

- 1) Random  $x$  from  $h(x)$
- 2)  $A += g(x)/h(x)$
- 3) Random  $y$ ,  $0 < y < g(x)$
- 4) If  $y \leq f(x)$  {  $n++$  }

$$I = \int f(x) dx = n/N^2 * A * \int h(x) dx$$

# Combined + Extended

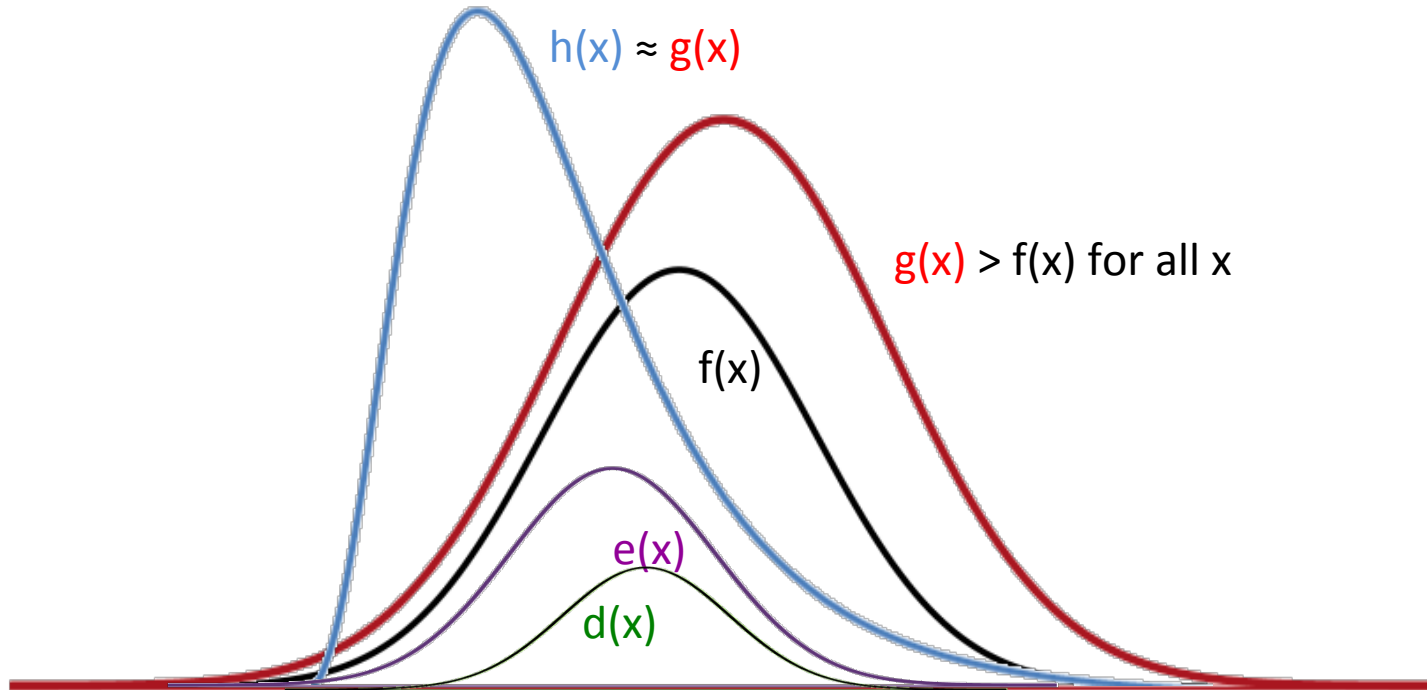


N times:

- 1) Random  $x$  from  $h(x)$
- 2)  $A += g(x)/h(x)$
- 3) Random  $y$ ,  $0 < y < g(x)$
- 4) If  $y \leq f(x)$  { if  $y \leq e(x)$  {  $n++$  } }

$$I = \int e(x) dx = n/N^2 * A * \int h(x) dx$$

# Combined + Extended



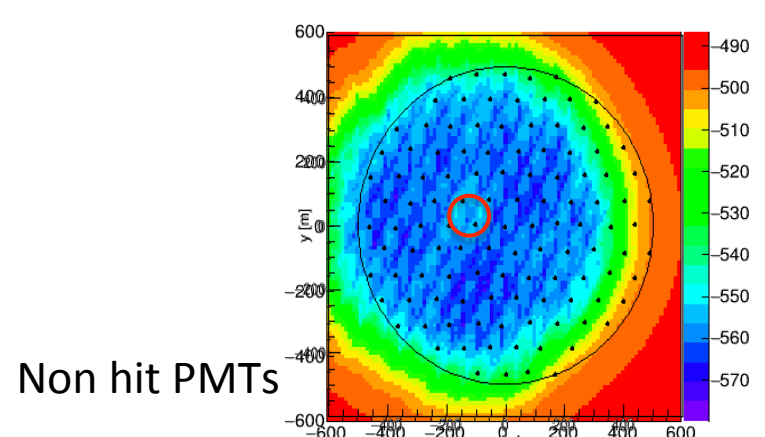
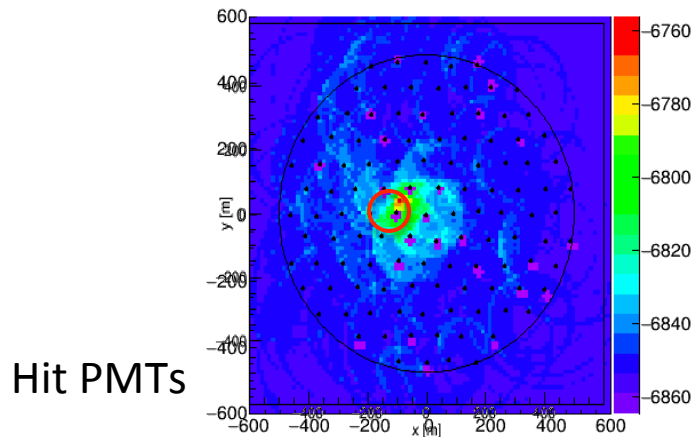
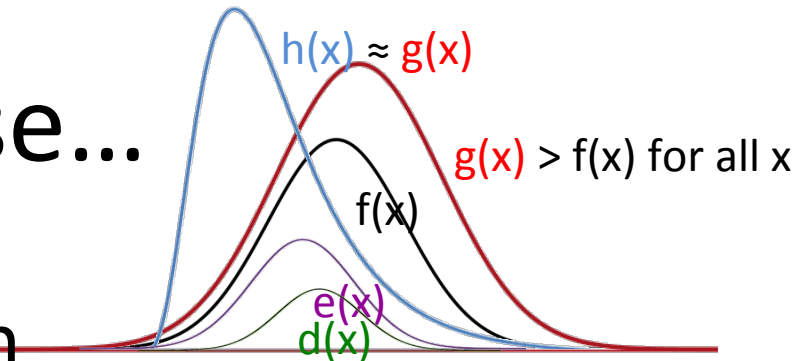
N times:

- 1) Random  $x$  from  $h(x)$
- 2)  $A += g(x)/h(x)$
- 3) Random  $y$ ,  $0 < y < g(x)$
- 4) If  $y \leq f(x)$  { if  $y \leq e(x)$  { if  $y \leq d(x)$  {  $n++$  } } }

$$I = \int d(x) dx = n/N^2 * A * \int h(x) dx$$

# In our case...

- $h(x)$ : some guiding function
- $g(x)$ :  $P(\text{ev} \mid x)$  over a small subset of PMTs
- $f(x)$ :  $P(\text{ev} \mid x)$  with slightly more PMTs
- $e(x)$ :  $P(\text{ev} \mid x)$  over a even more PMTs
- $d(x)$ :  $P(\text{ev} \mid x)$  with all PMTs



# In our case...

- $h(x)$ : some guiding function
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$$I = \int d(x) dx = n/N^2 * A * \int h(x) dx$$

# Guiding function

- Convenient choice: multivariate normal distribution
  - tracks: JPrefit PDF
  - Showers: ????



# Guiding function

- Convenient choice: multivariate normal distribution
  - tracks: JPrefit PDF
  - Showers: ????

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MASTER THESIS

**Reconstruction of High-energy Neutrino-induced  
Particle Showers in KM3NeT.**

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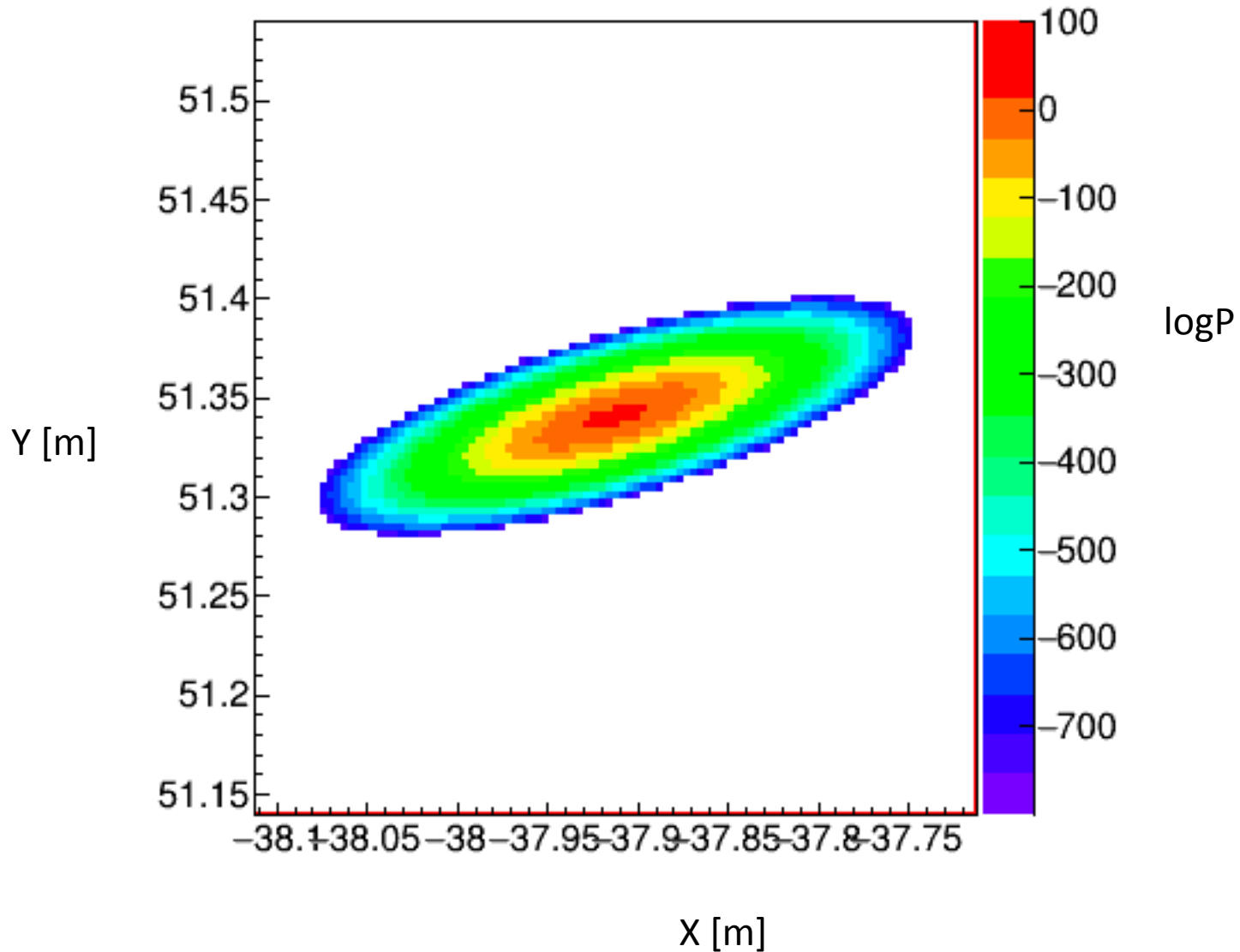
BY

[www.nikhef.nl/~kmelis/Masters\\_Thesis.pdf/Thesis.pdf](http://www.nikhef.nl/~kmelis/Masters_Thesis.pdf/Thesis.pdf)

# Shower Vertex PDF

- Basically a  $\text{Chi}^2$  distribution
  - Very sensitive to outliers (i.e.  $40\text{K}$  hits)
- Use first triggered hit on each DOM
- Hit clustering algorithm:
  - If many hits: iteratively remove worst hit
  - If #hits  $\leq 16$ : Try all combinations

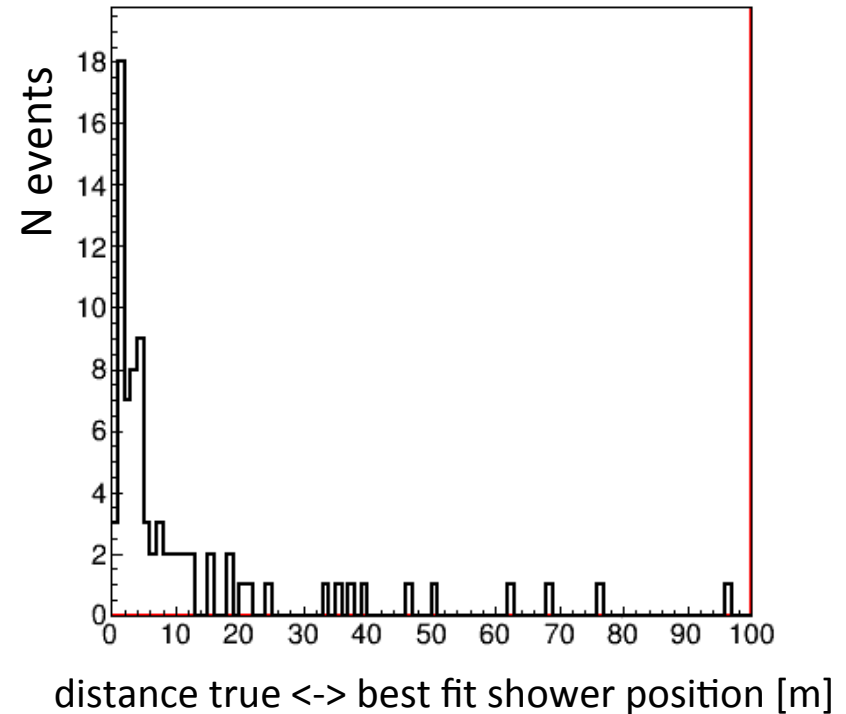
# Shower Vertex PDF



# Bonus: Shower Position Reconstruction


- Reasonable resolution:
  - median  $\sim 1\text{m}$
- Principle (cluster+ $\chi^2$ ) usable for tau double bang prefit?

Preliminary



# Conclusions

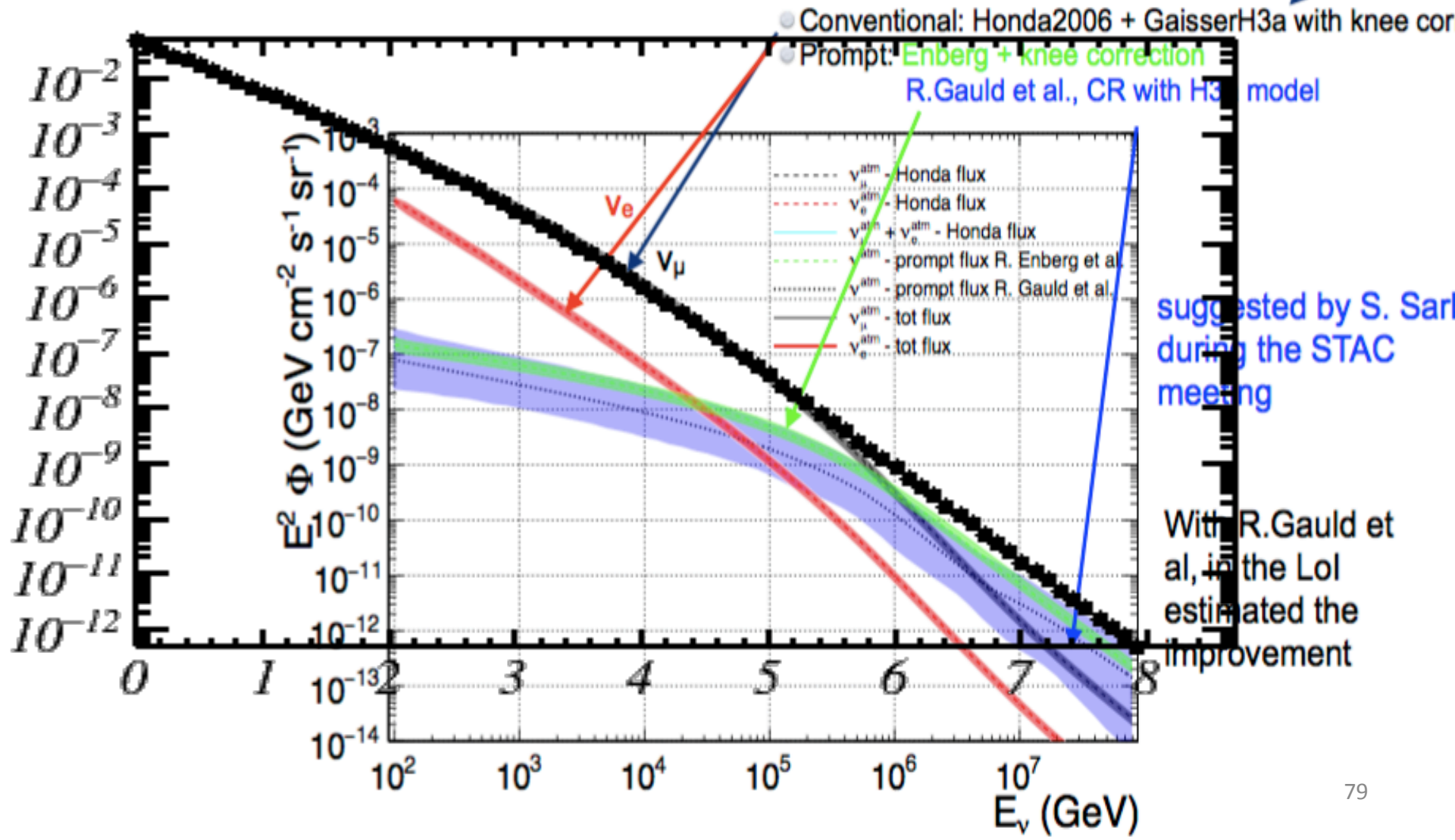


- Most ingredients seem
  - Neutrino background and signal fluxes
  - Detection efficiency tables
  - Event probability
- Integral evaluation seems feasible with MC techniques
-  **BONUS** :  
bij AH Willem's
  - Shower prefit (+tau double bang prefit?)
  - Very fast neutrino MC simulator

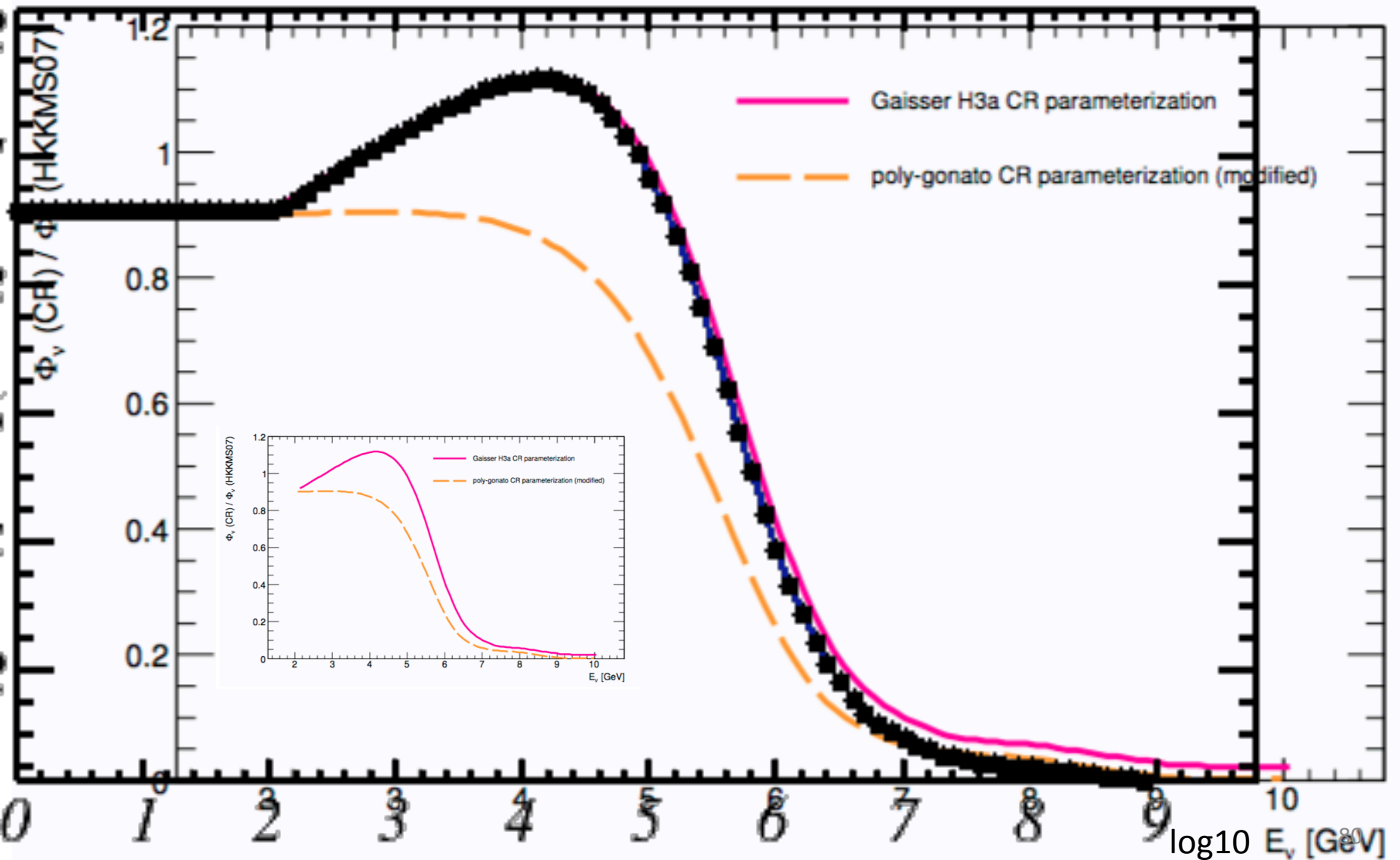
# Backup

# Honda extrapolated

T. Gaisser 2012



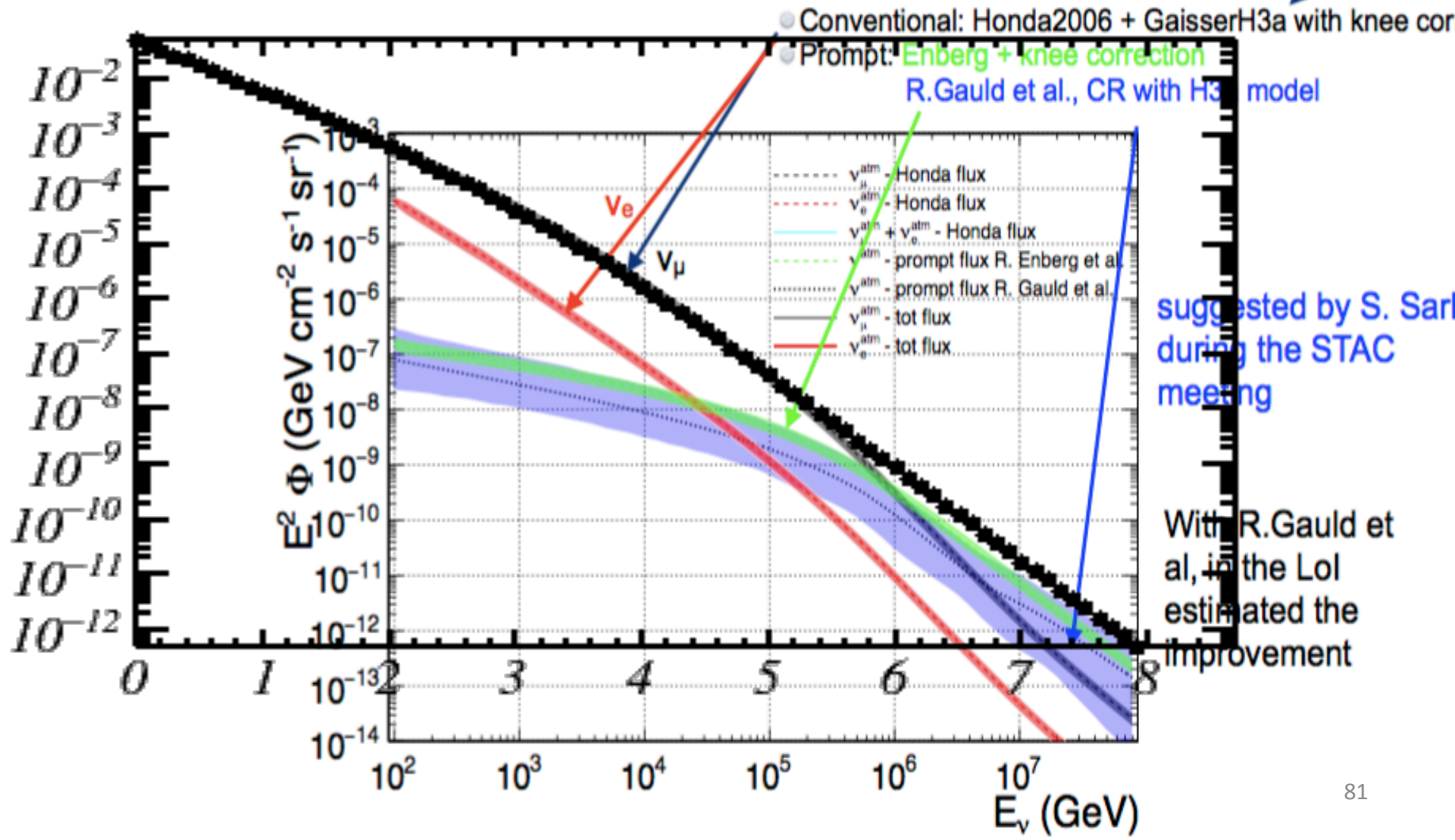
# Knee Correction (Gaisser H3a)





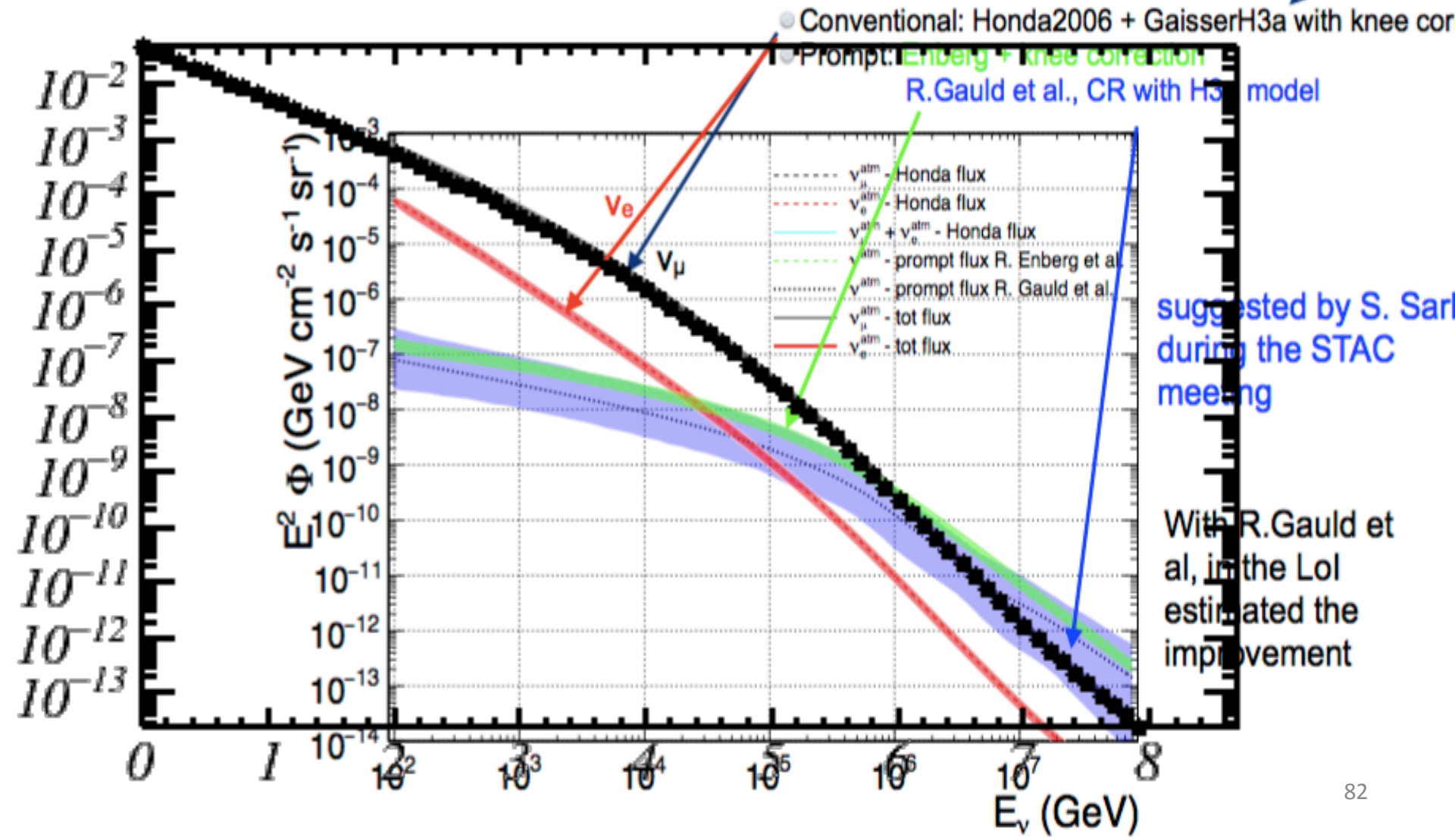
# Honda extrapolated

T. Gaisser 2012

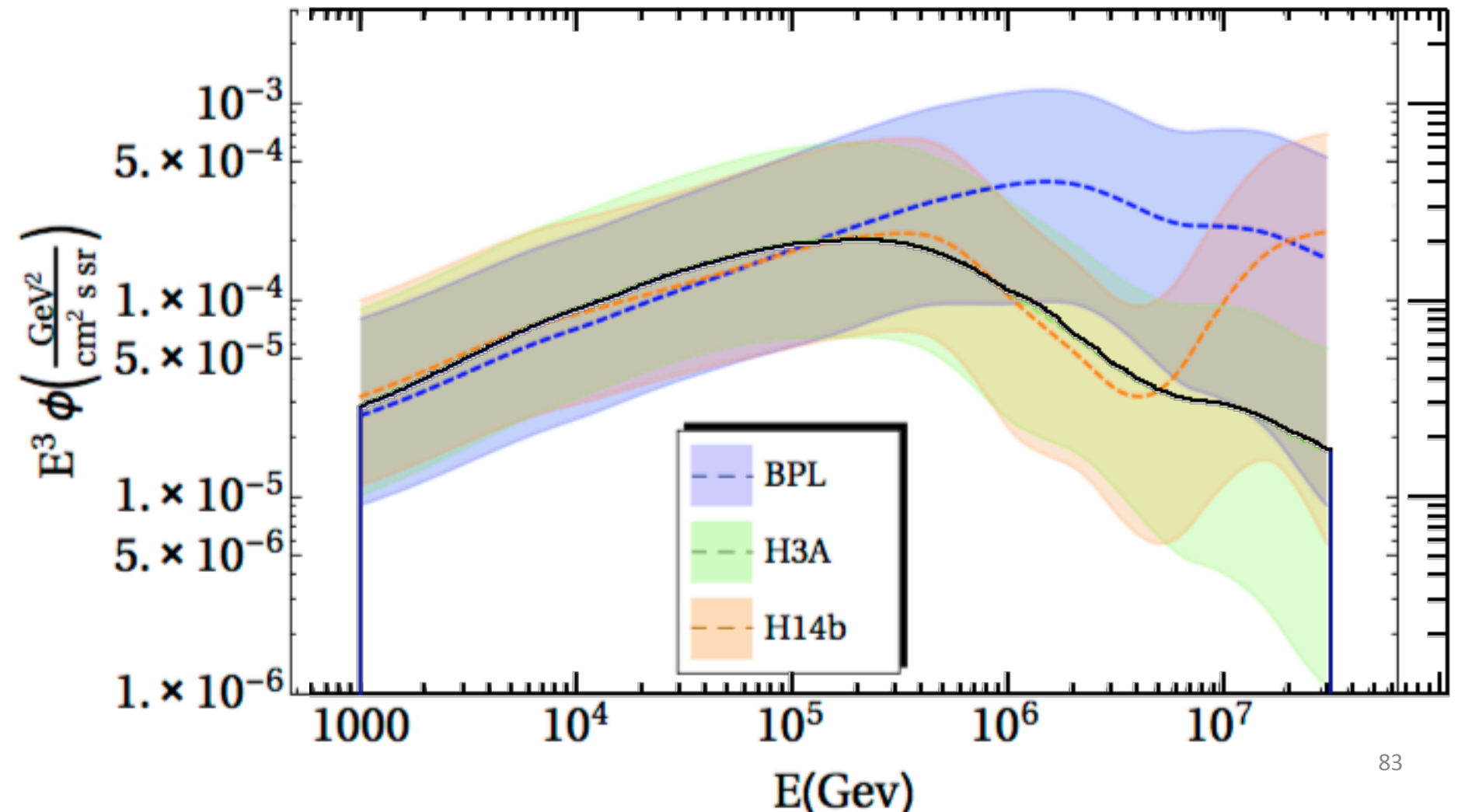


# Honda extrapolated + knee correction

T. Gaisser 2012

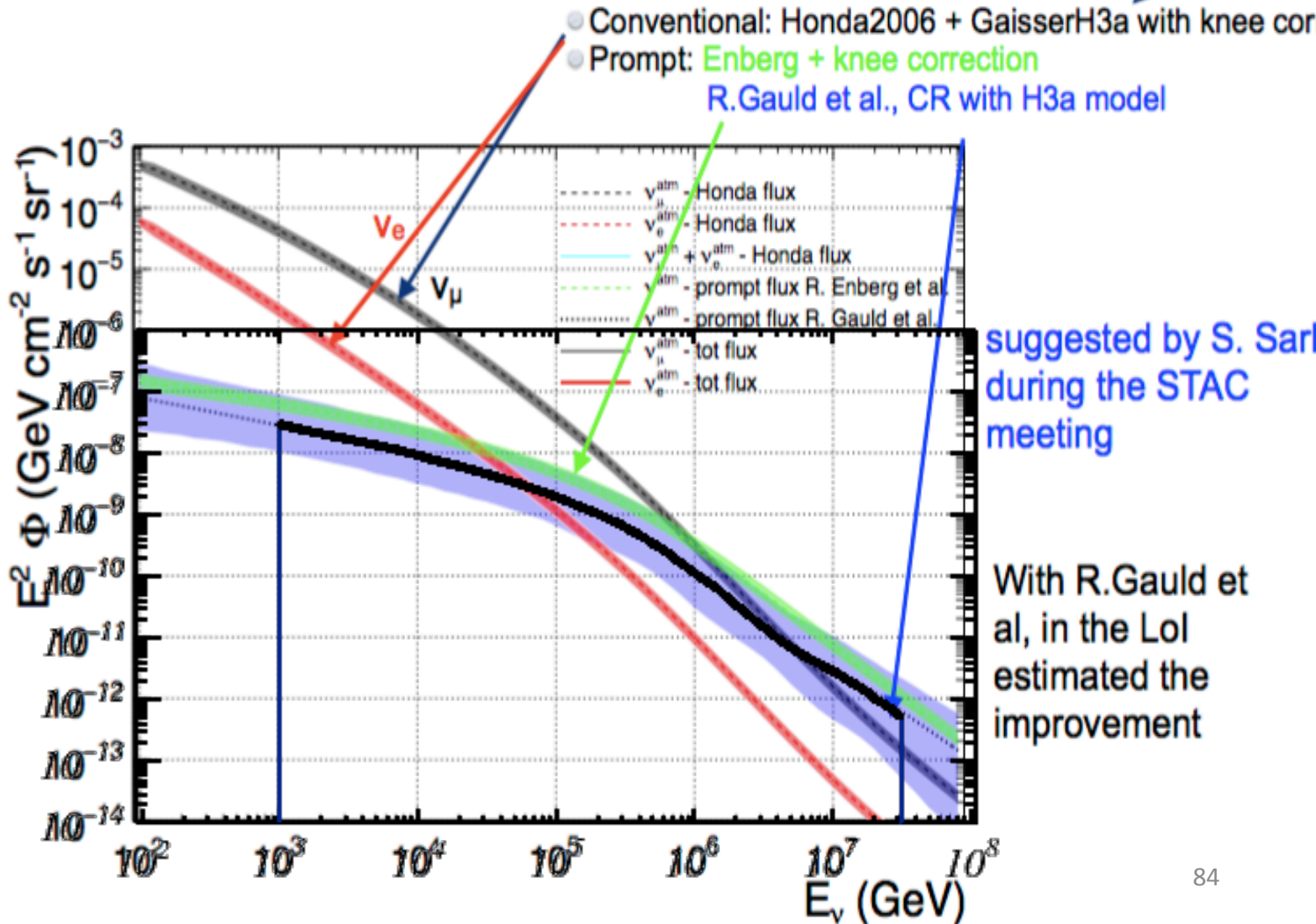


# Prompt: Gauld Flux (2016)



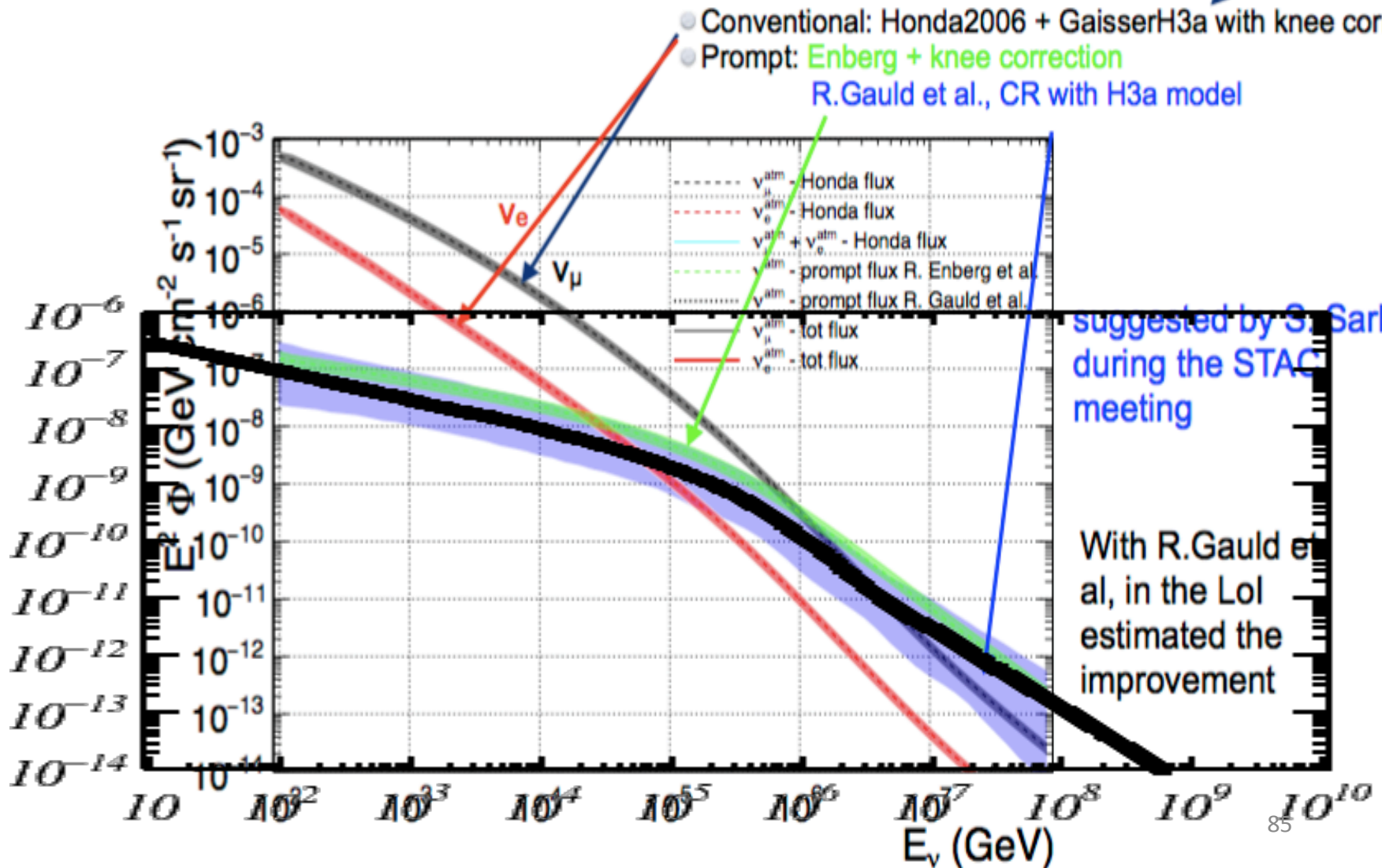
# Gauld 2016

T. Gaisser 2012



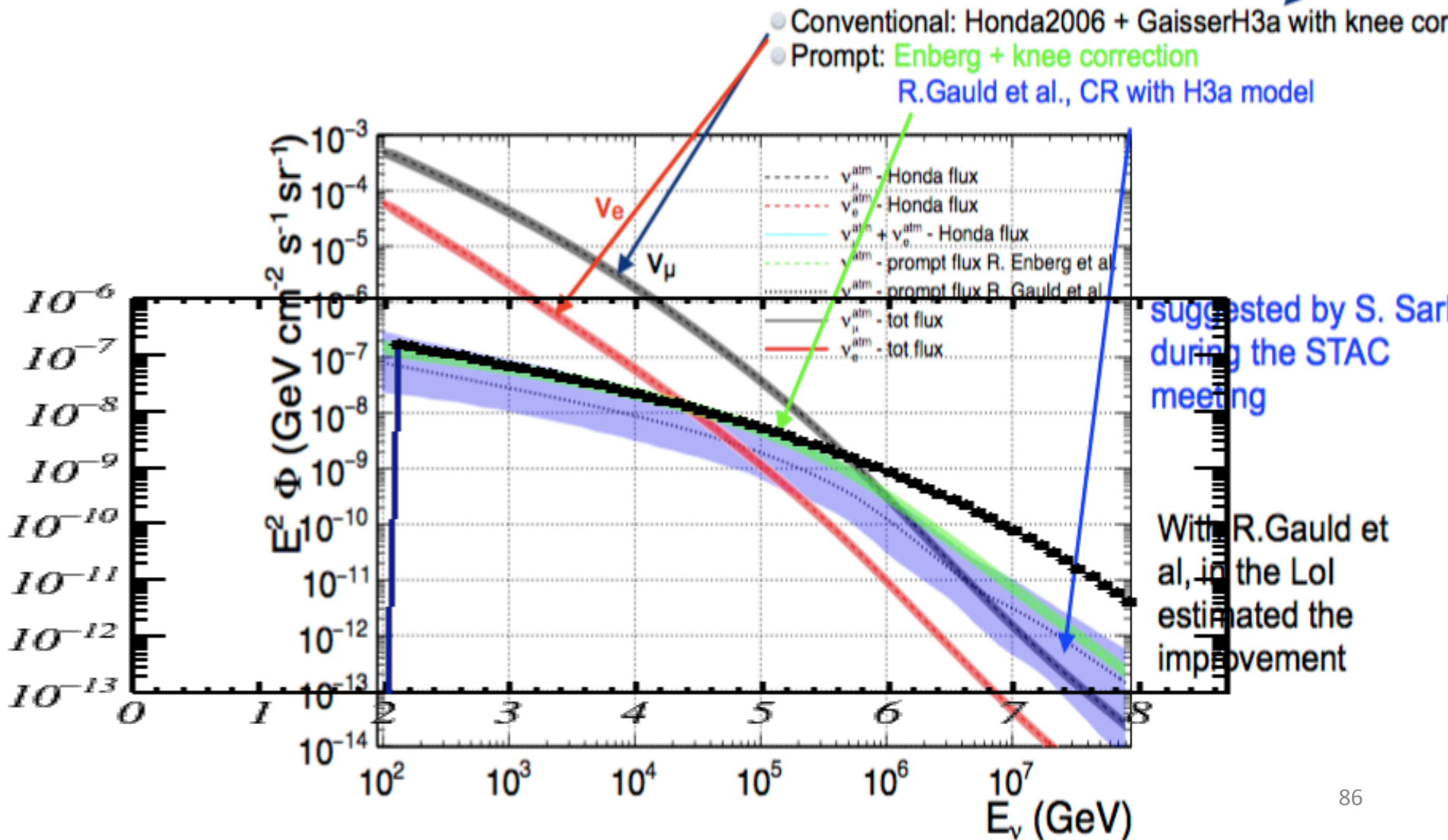
# Gauld 2016 extrapolated

T. Gaisser 2012



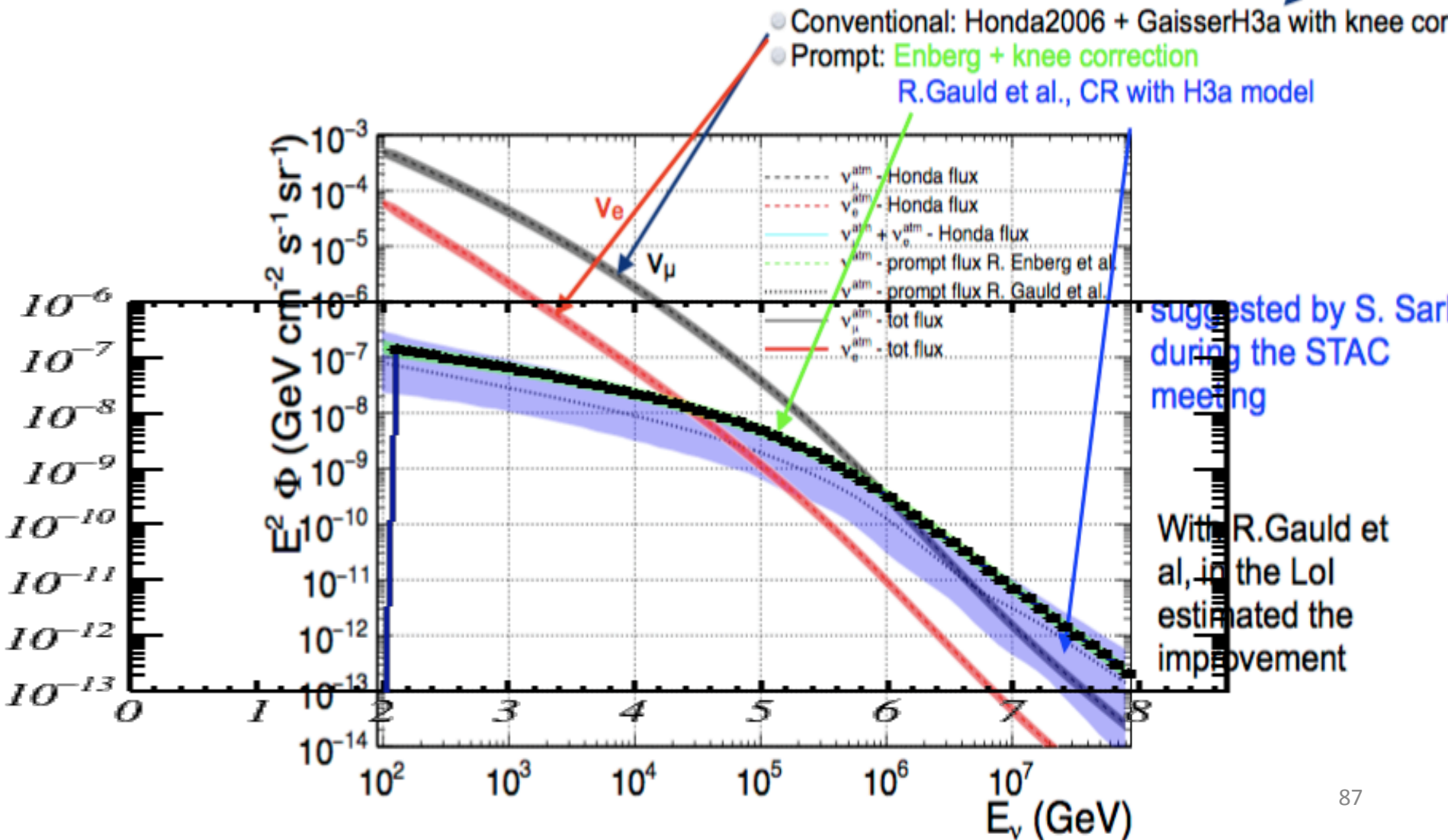
# Enberg extrapolated

T. Gaisser 2012

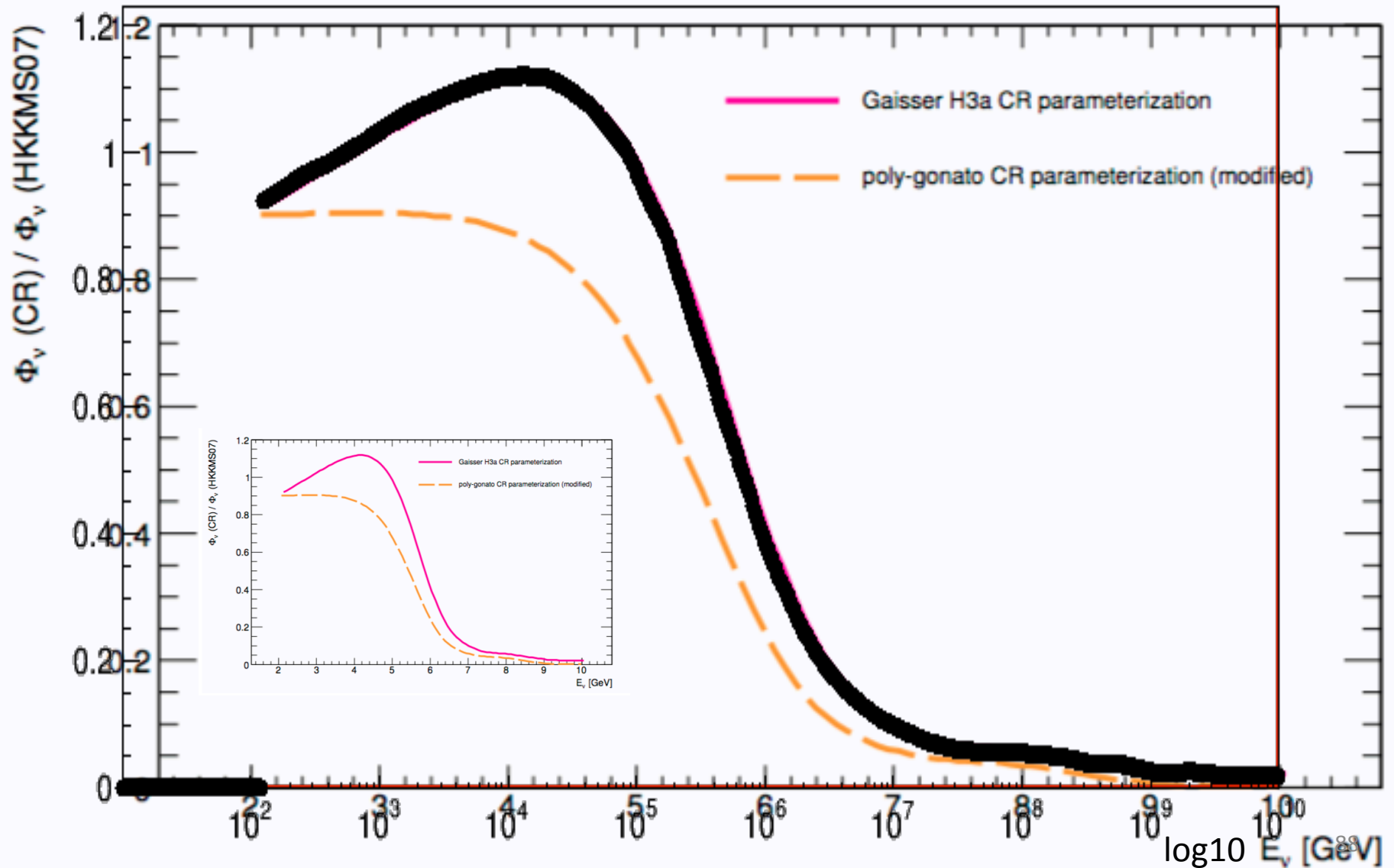


# Enberg extrapolated + knee correction

T. Gaisser 2012



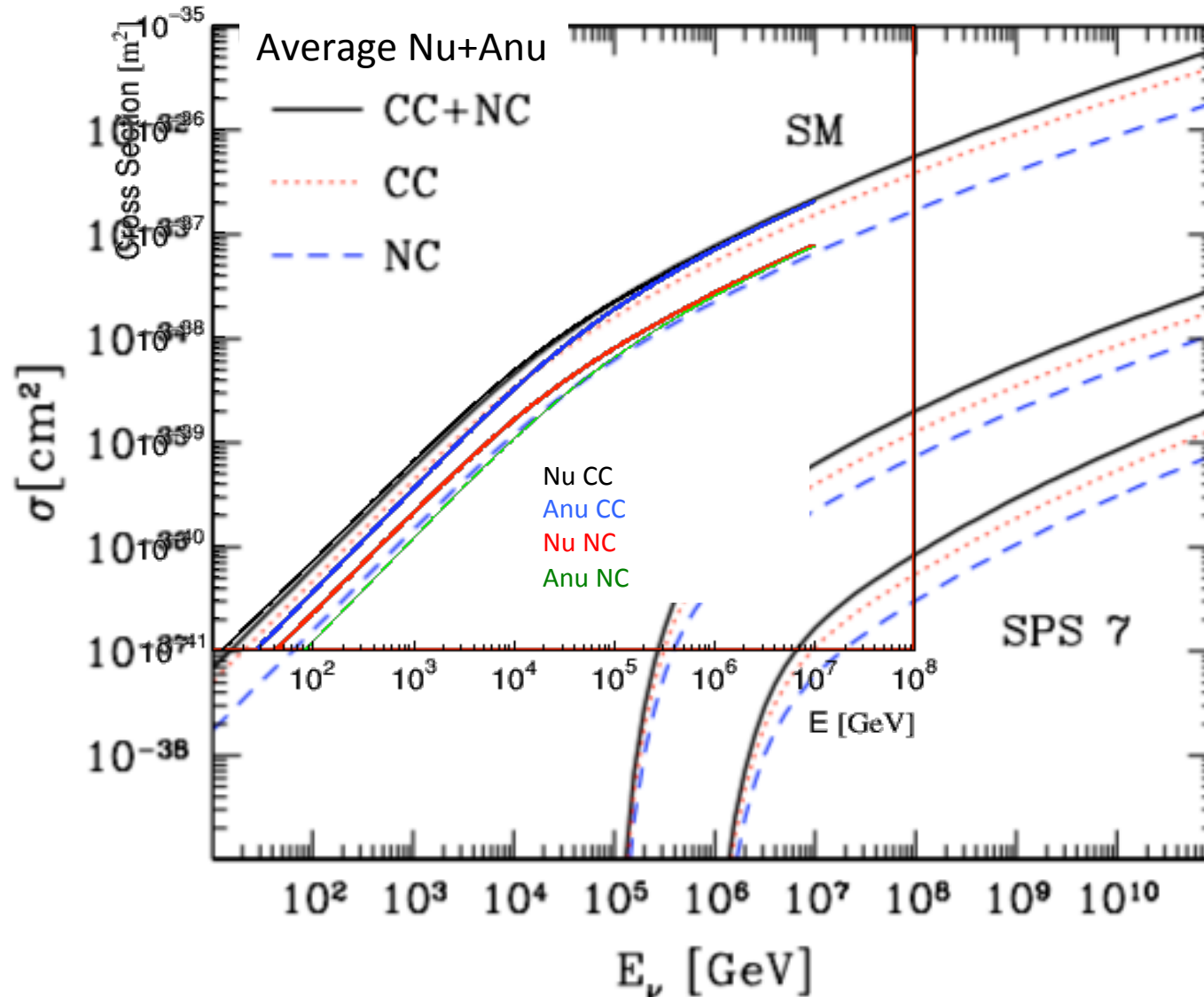
# Knee Correction (Gaisser H3a)



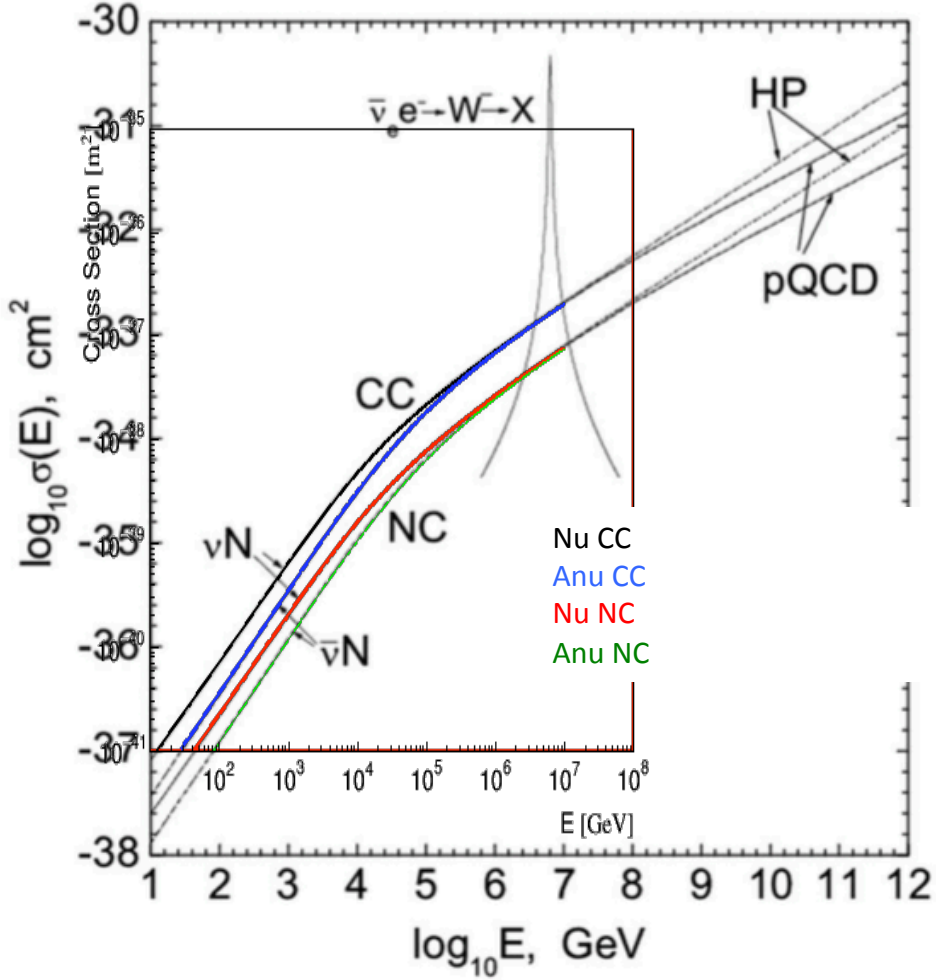




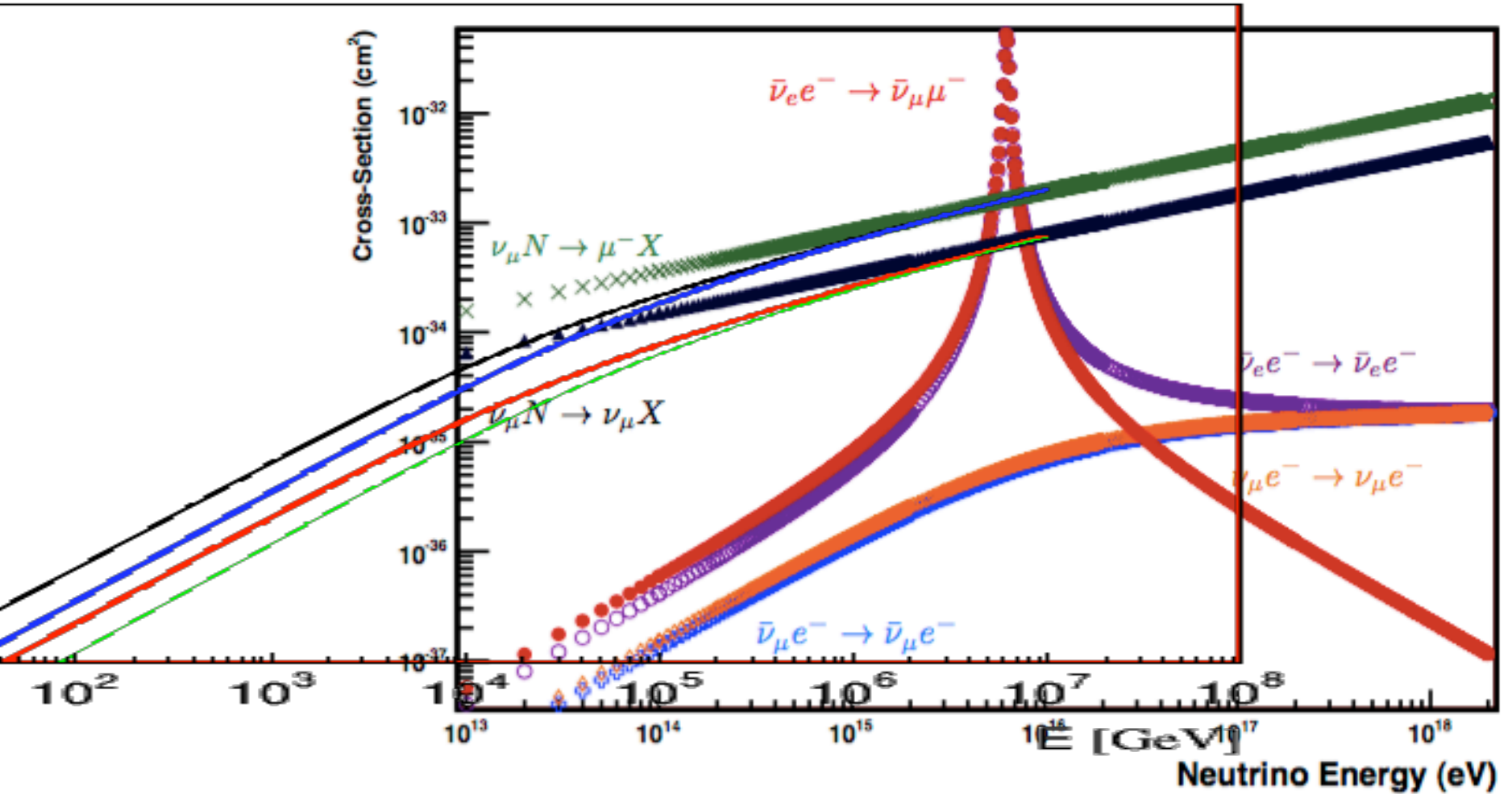
# Neutrino Cross Sections



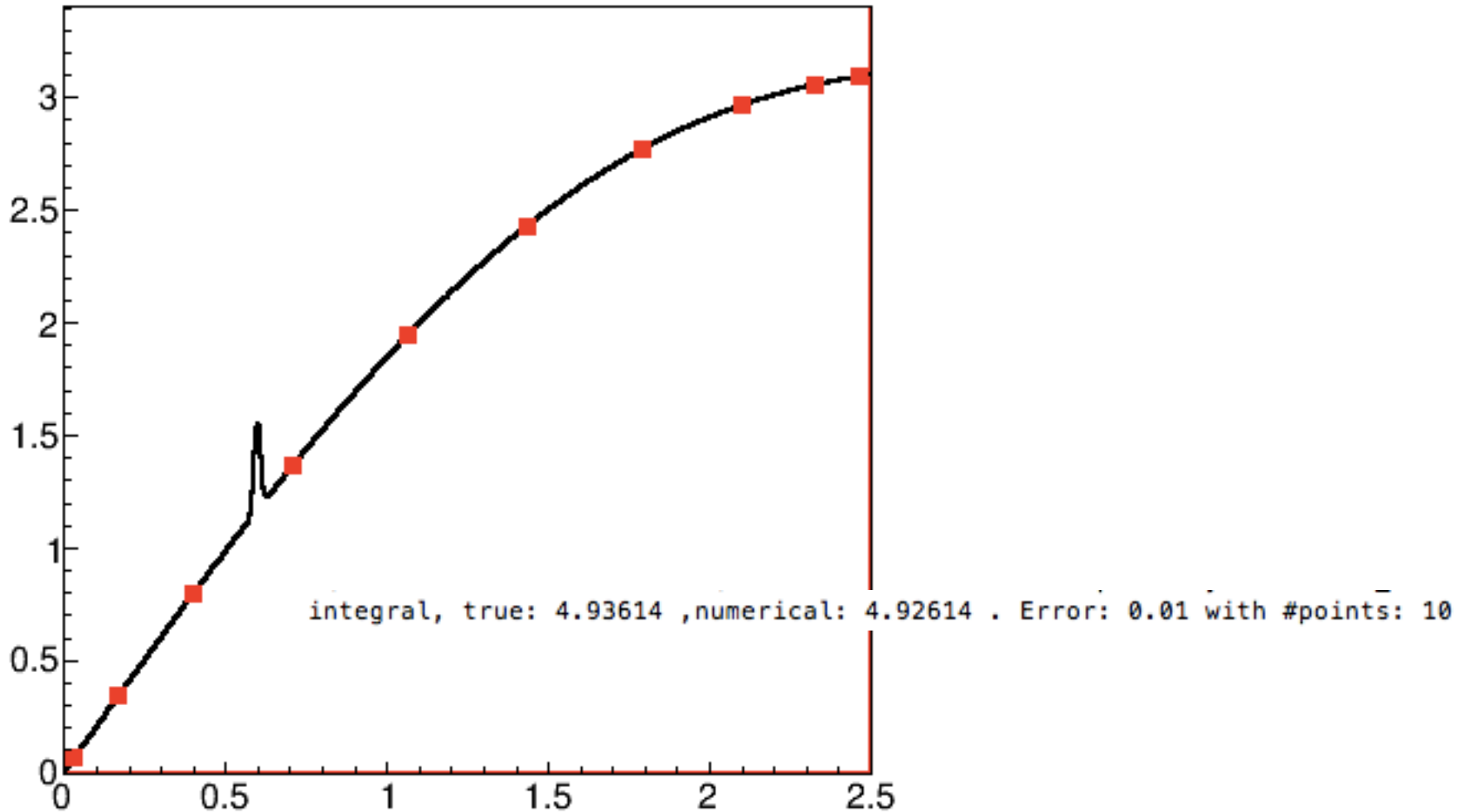
# Neutrino Cross Sections



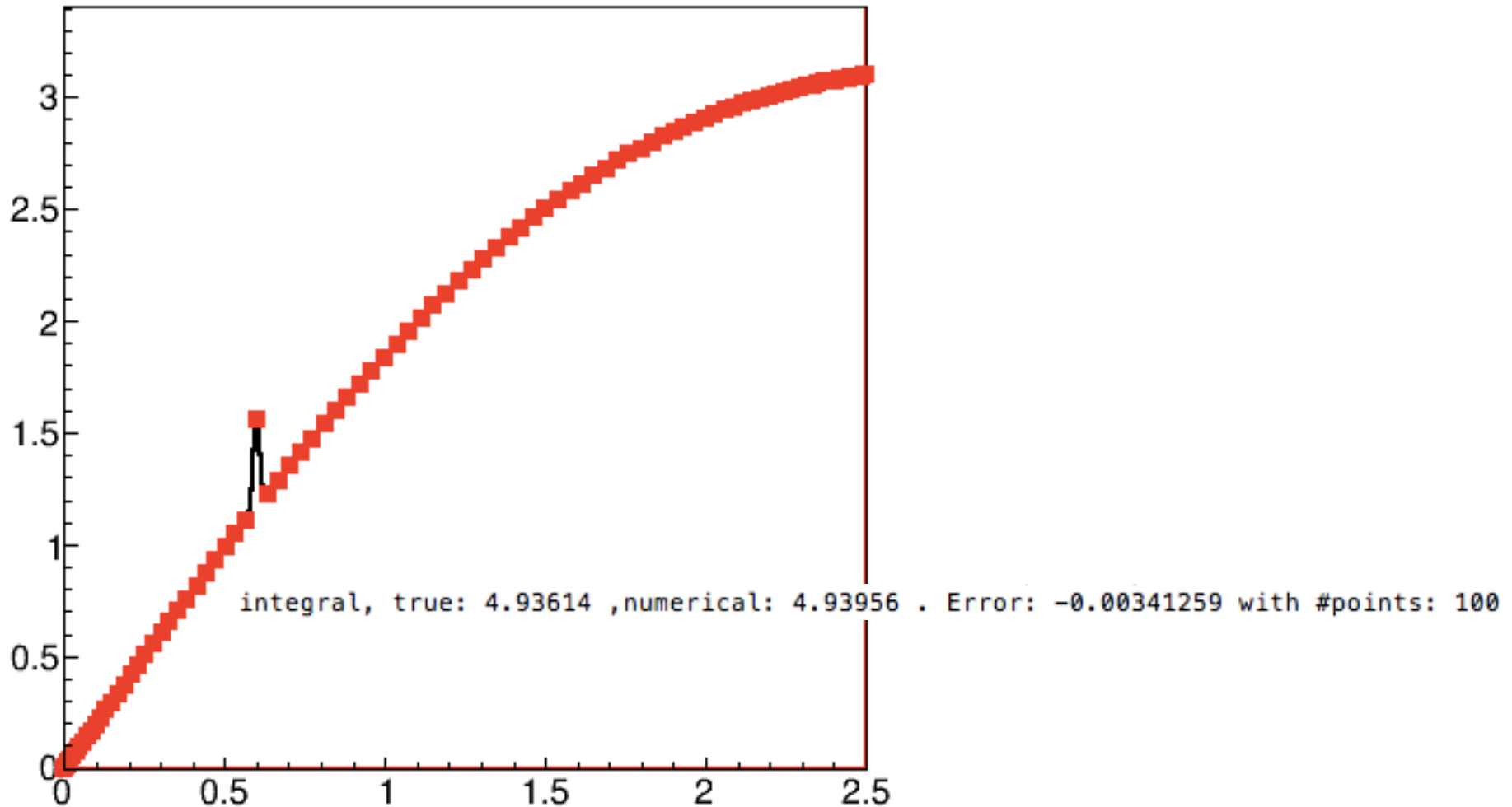
# Neutrino Cross Sections



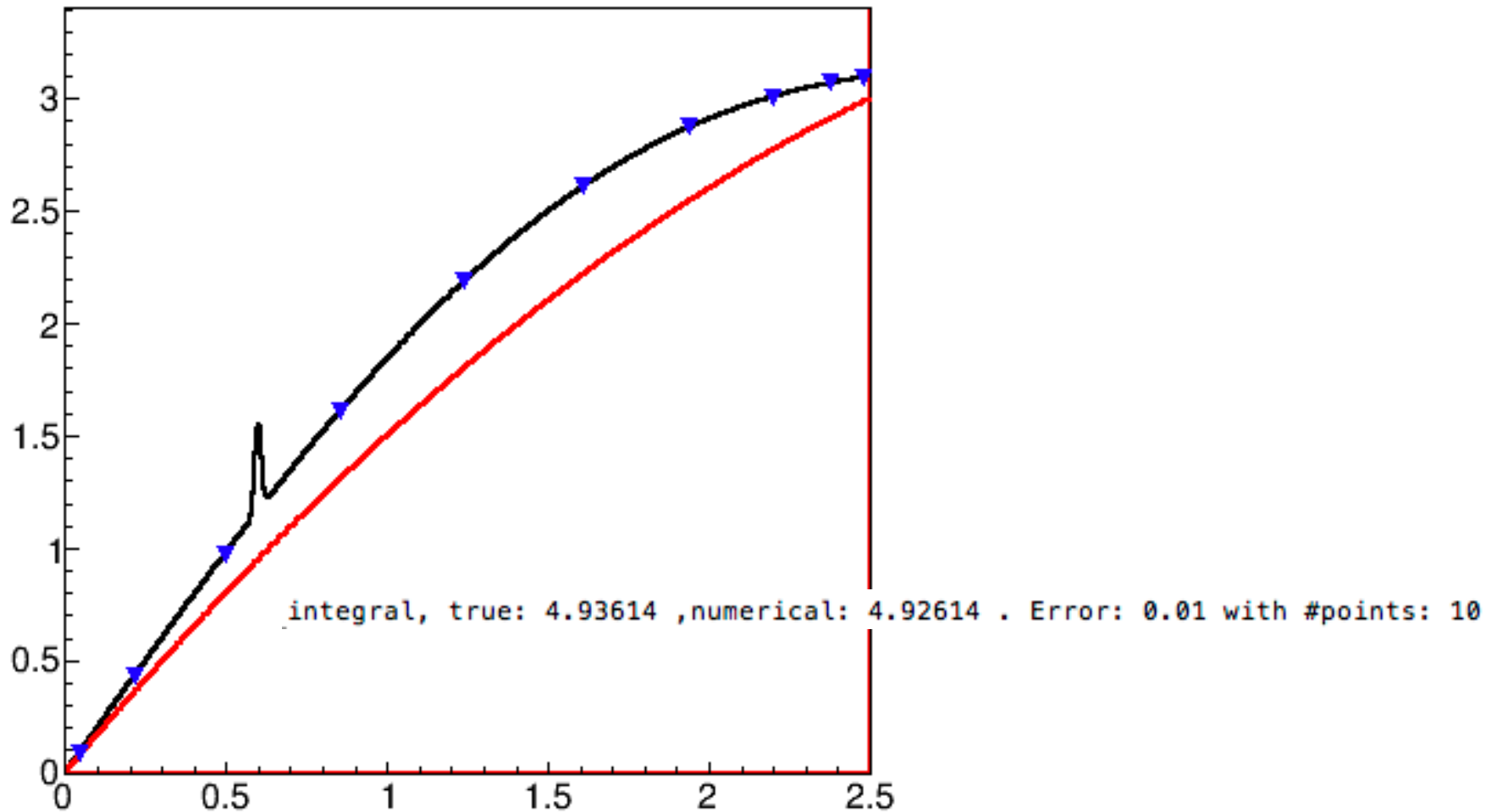
# Gaussian Quadrature



# Gaussian Quadrature



# Gaussian Quadrature



# Event Probability: Direction

