# Finding our way through BSM parameter spaces

#### Anders Kvellestad, University of Oslo

Nikhef, Amsterdam — 3 May 2018





- 1. Why are global fits necessary?
- 2. Why are global fits difficult?
- 3. GAMBIT and what it can do for you
- 4. GAMBIT physics results
- 5. Summary and outlook

# I. Why are global fits necessary?

- Lots of theories for BSM physics
- For each theory, a parameter space of varying phenomenology
- Many different experiments can constrain each theory

2HDM SUSY Composi GUT Higgs	te
⊖z∧ - No LHC signals - DM Higgs-like	
- Lots of LHC signals - DM Z-like Ol	













What to do when there are many parameters and many constraints? A **global fit**.

Theory 
$$\rightarrow f(X; \theta)$$
  
Experiment  $\rightarrow \mathcal{L}(\theta) = f(X_{data}; \theta)$   
 $\mathcal{L} = \mathcal{L}_{Collider} \mathcal{L}_{Higgs} \mathcal{L}_{DM} \mathcal{L}_{EWPO} \mathcal{L}_{Flavor} \dots$ 

## Global fits

 Calculate combined likelihood function including observables from collider physics, dark matter, flavor physics, +++

$$\mathcal{L} = \mathcal{L}_{collider} \mathcal{L}_{DM} \mathcal{L}_{flavor} \mathcal{L}_{EWPO} \dots$$

- Use sophisticated scanning techniques to explore likelihood function across the parameter space of the theory
- Test parameter regions in a statistically sensible way not just single points (parameter estimation)
- Test different theories the same way (model comparison)

## Global fits



 Use sophis function ac

 Test param single point

Test differe



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# 2. Why are global fits difficult?



### $\times$

[long calculation time per observable per parameter point]

#### $\times$

[huge number of points required to explore parameter space]





## Large number of observables

- Need many observables to constrain many parameters
- Observable calculations generally introduce additional parameters → nuisance parameters
- Typically need to interface several external tools
- Need consistent treatment of uncertainties across different calculations and codes
- Need to make observable calculations as reusable as possible



## Long time per observable

- Some observables require very time-consuming calculations (*e.g.* MC simulation of LHC searches)
- Sort likelihood calculations from quickest to slowest
- **Optimize** calculations as much as possible
- Parallelize calculations
- Make approximations when valid
   Typically requires expert knowledge

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Finding interesting parameter regions gets harder with increasing number of dimensions...



...so simply picking points «at random» will be highly inefficient...

...and it will mainly explore the **boundary** of the parameter space!



Need to use some **smart** sampling algorithms



How to tackle these challenges? How to avoid reinventing the wheel for every new analysis?

# 3. GAMBIT and what it can do for you

## The Global And Modular BSM Inference Tool

- A new and general framework for BSM global fits
- Fully open source
- · Modular design: can be extended with
  - new models
  - new likelihoods
  - new theory calculators
  - new scanning algorithms
- Use external codes (backends) as runtime plugins
  - Supported languages:
    - C, C++, Fortran, Python and Mathematica
- Two-level parallellization with MPI and OpenMP
- · Hierarchical model database
- Flexible output streams (ASCII, HDF5, ...)
- Many scanners and backends already included





## GAMBIT: The Global And Modular BSM Inference Tool

gambit.hepforge.org

EPJC **77** (2017) 784

#### arXiv:1705.07908

- Fast definition of new datasets and theoretical models
- Plug and play scanning, physics and likelihood packages
- Extensive model database not just SUSY
- Extensive observable/data libraries

ATLAS	F. Bernlochner, A. Buckley, P. Jackson, M. White
LHCb	M. Chrząszcz, N. Serra
Belle-II	F. Bernlochner, P. Jackson
Fermi-LAT	J. Conrad, J. Edsjö, G. Martinez, P. Scott
СТА	C. Balázs, T. Bringmann, M. White
$\mathbf{CMS}$	C. Rogan
IceCube	J. Edsjö, P. Scott
XENON/DARWIN	B. Farmer, R. Trotta
Theory	P. Athron, C. Balázs, S. Bloor, T. Bringmann,
	J. Cornell, J. Edsjö, B. Farmer, A. Fowlie, T. Gonzald
	J. Harz, S. Hoof, F. Kahlhoefer, S. Krishnamurthy,
	A. Kvellestad, F.N. Mahmoudi, J. McKay, A. Raklev,
	R. Ruiz, P. Scott, R. Trotta, A. Vincent, C. Weniger,

M. White, S. Wild

- Many statistical and scanning options (Bayesian & frequentist)
- *Fast* LHC likelihood calculator
- Massively parallel
- Fully open-source





What's in the box?

#### Core

Models

#### **Physics modules**

- ColliderBit: fast LHC sim, Higgs searches, LEP SUSY limits
- DarkBit: relic density, gamma ray signal yields, ID/DD likelihoods
- FlavBit: wide range of flavour observables & likelihoods
- SpecBit: spectrum objects, RGE running
- DecayBit: decay widths
- PrecisionBit: precision BSM tests

#### **Statistics and sampling**

ScannerBit: stats & sampling (Diver, MultiNest, T-Walk, ++)

#### Backends (external tools)

EPJC, arXiv:1705.07919 EPJC, arXiv:1705.07920 EPJC, arXiv:1705.07933

EPJC, arXiv:1705.07908

EPJC, arXiv:1705.07936

EPJC, arXiv:1705.07959

### Code structure



Code structure

- Basic building blocks: module functions
- A physics module: a collection of module functions related to the same physics topic
- Each module function has a single capability (what it calculates)
- A module function can have dependencies on the results of other module functions
- A module function can declare which models it can work with
- GAMBIT determines which module functions should be run in which order for a given scan (dependency resolution)

```
void function_name(double &result)
{
    ...
    result = ... // something useful
}
```

```
// Observable: BR(B -> tau nu)
#define CAPABILITY Btaunu
START_CAPABILITY
    #define FUNCTION SI_Btaunu
    START_FUNCTION(double)
    DEPENDENCY(SuperIso_modelinfo, parameters)
    BACKEND_REQ(Btaunu, (libsuperiso), double, (const parameters*))
    BACKEND_OPTION( (SuperIso, 3.6), (libsuperiso) )
    #undef FUNCTION
#undef CAPABILITY
```



## Dependency resolution



## Dependency resolution

User specifies the model, parameter space, observables and scanning technique 

> Type: double on: sigma\_SD\_p\_sim Module: DarkBi

equilibration time Sur

Type: double Function: equilibration\_time\_Sur Module: DarkBit

annihilation rate

Function: annihilation\_ra Module: DarkBi

from Felix Kahlhoefer

Type: double

capture\_rate\_Sun Type: double nction: capture\_rate\_Sun\_constant\_xs Module: DarkBit

nulike 1 0 0 init

Type: void

tion: nulike\_1\_0\_0\_init dule: BackendIniBit

ction: n

- GAMBIT then performs the *dependency resolution* 
  - Identification of all functions necessary to calculate requested observables
  - Dynamic adaptation to the user's system
  - Determination of the required inputs for each function \_
  - Construction of the optimum order of function evaluation
- A scan then consists of calling all necessary modules and external libraries in the required order for each parameter point

Hierarchical model database

- A **model** is a collection of named parameters
- Models can be **related** (e.g. MSSM9 is a parent of MSSM7)
- Points in child model automatically translated to ancestor models
- Ensures maximum reuse of calculations and minimizes risk of mistakes



## YAML files

#### Parameters

StandardModel SLHA2: *!import* include/StandardModel SLHA2 scan.yaml fixed value: -0.427 fixed value: -0.085 prior\_type: double log flat join ranges: [-1e4, -1e2, 1e2, 1e4] prior\_type: double\_log\_flat\_join ranges: [-1e4, -1e2, 1e2, 1e4] prior\_type: double log flat join ranges: [-1e4, -1e2, 1e2, 1e4] TanBeta: prior\_type: double\_log flat join ranges: [-1e8, -1e4, 1e4, 1e8] prior\_type: double\_log\_flat join ranges: [-1e8, -1e4, 1e4, 1e8] prior\_type: double\_log\_flat\_join ranges: [0, 0, 1e4, 1e8]

#### Printer:

printer: hdf5

options: output\_file: "MSSM7.hdf5" group: "/MSSM7"

Scanner

use\_scanner: de

scanners:

multinest:
 plugin: multinest
 like: LogLike
 nlive: 5000
 tol: 0.1
 updInt: 1

e: plugin: diver like: LogLike NP: 19200 convthresh: 1e-5 verbosity: 1

#### ObsLikes:

# LHC likelihoods
- purpose: LogLike
capability: LHC\_Combined\_LogLike

- purpose: LogLike capability: LHC\_Higgs\_LogLike
- # Dark matter likelihood
   capability: lnL\_oh2
  purpose: LogLike
- capability: lnL\_FermiLATdwarfs purpose: LogLike
- capability: XENON100\_2012\_LogLikelihood purpose: LogLike
- capability: XENONIT\_2017\_LogLikelihood purpose: LogLike
- capability: LUX\_2015\_LogLikelihood purpose: LogLike
- capability: LUX\_2016\_LogLikelihood purpose: LogLike
- capability: PandaX\_2016\_LogLikelihood purpose: LogLike
- capability: PIC0\_2L\_LogLikelihood purpose: LogLike
- capability: PIC0\_60\_F\_LogLikelihood purpose: LogLike
- capability: PIC0\_60\_2017\_LogLikelihood purpose: LogLike
- capability: SuperCDMS\_2014\_LogLikelihood purpose: LogLike
- capability: SIMPLE\_2014\_LogLikelihood purpose: LogLike
- capability: IC79\_loglike purpose: LogLike
- # Flavour physics likelihoods
   purpose: LogLike
  capability: b2ll\_LL

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v0: 235.0
### Backends

- A backend is an external code (C, C++, Fortran, Python, Mathematica)
- Connected to GAMBIT as a runtime plugin not linked at compile time, and not called via command line interface with file input/output
- GAMBIT module functions can request results from backends
- Backend functions are tagged according to what they calculate (e.g. "Omegah2")
  - Switching between different backends by changing one line in the YAML file
  - Ideal for comparing different theory codes
- Many codes already supported, and more to come
  - But you can always add a new interface yourself

### Backends

BACKENDS	VERSION	PATH TO LIB	STATUS	#FUNC	#TYPES
DDCalc	1.0.0	Backends/installed/ddcalc/1.0.0/lib/libDDCalc.so	absent/broken	36	0
	1.1.0	Backends/installed/ddcalc/1.1.0/lib/libDDCalc.so	absent/broken	38	0
	1.2.0	Backends/installed/ddcalc/1.2.0/lib/libDDCalc.so	ок	39	0
DarkSUSY	5.1.3	Backends/installed/darksusy/5.1.3/lib/libdarksusy.so	ок	79	0
FeynHiggs	2.11.2	Backends/installed/feynhiggs/2.11.2/lib/libFH.so	absent/broken	14	0
	2.11.3	Backends/installed/feynhiggs/2.11.3/lib/libFH.so	ок	14	0
	2.12.0	Backends/installed/feynhiggs/2.12.0/lib/libFH.so	absent/broken	14	0
HiggsBounds	4.2.1	Backends/installed/higgsbounds/4.2.1/lib/libhiggsbounds.so	absent/broken	10	0
	4.3.1	Backends/installed/higgsbounds/4.3.1/lib/libhiggsbounds.so	ок	10	0
HiggsSignals	1.4	Backends/installed/higgssignals/1.4.0/lib/libhiggssignals.so	ок	12	0
LibFarrayTest	1.0	Backends/examples/libFarrayTest.so	ок	10	0
LibFirst	1.0	Backends/examples/libfirst.so	ок	8	0
	1.1	Backends/examples/libfirst.so	ок	15	0
LibFortran	1.0	Backends/examples/libfortran.so	ок	6	0
LibSecond	1.0	Backends/examples/libsecond/1.0/libsecond.py	ок	6	0
	1.1	Backends/examples/libsecond/1.1/libsecond.py	ок	б	0
MicrOmegas_MSSM	3.6.9.2	Backends/installed/micromegas/3.6.9.2/MSSM/libmicromegas.so	ок	18	0
MicrOmegas_SingletDM	3.6.9.2	Backends/installed/micromegas/3.6.9.2/SingletDM/libmicromegas.so	ок	16	0
Pythia	8.212	Backends/installed/pythia/8.212/lib/libpythia8.so	ок	0	28
	8.212.EM	Backends/installed/pythia/8.212.EM/lib/libpythia8.so	absent/broken	0	28
SPheno	3.3.8	Backends/installed/spheno/3.3.8/lib/libSPheno.so	ОК	282	0
SUSYHD	1.0.2	Backends/installed/susyhd/1.0.2/SUSYHD.m	Mathematica absent	3	O

### Scanners

- Trivial to switch between scanner algorithms
- · Choose the best scanner for your analysis
  - Profile likelihoods (frequentist)
  - Posterior distributions (Bayesian)
  - Evidence estimation (Bayesian)
  - Grid scans, post-processing, ...
- Ideal for comparing the performance of different scanners (see arXiv:1705.07959)



# GAMBIT

### Scan illustration



«All right, but apart from the physics likelihoods, two-level parallelization, dependency resolution, model hierarchy, dynamic backend system and efficient sampling algorithms, what has GAMBIT ever done for us?»

# 4. GAMBIT physics results



### GUT-scale MSSM results

# Parameters and scanning

- Profile likelihood analysis
- Combine samples from scans with different priors and scanners (Diver & MultiNest)
- Additional scans to improve sampling of co-annihilation regions
- In total for all three models:
  36 scans, ~280 million viable samples
- Vary 5 nuisance parameters (constrained by gaussian likelihoods)

Parameter	Minimum	Maximun	n Priors			
CMSSM						
$m_0$	$50{ m GeV}$	$10\mathrm{TeV}$	flat, log			
$m_{1/2}$	$50{ m GeV}$	$10\mathrm{TeV}$	$flat, \log$			
$A_0$	$-10\mathrm{TeV}$	$10\mathrm{TeV}$	flat, hybrid			
aneta	3	70	flat			
$\operatorname{sgn}(\mu)$	—	+	binary			
<b>NUHM1</b> – as per CMSSM plus						
$m_H$	$50{ m GeV}$	$10\mathrm{TeV}$	flat, log			
<b>NUHM2</b> – as per CMSSM plus						
$m_{H_u}$	$50{ m GeV}$	$10\mathrm{TeV}$	flat, log			
$m_{H_d}$	$50{ m GeV}$	$10\mathrm{TeV}$	flat, log			
 Parameter			Value(+Range)			
Varied			Value(±Italige)			
Strong couplin	nœ	$\sqrt{MS}(m-)$	0 1195(19)			
Strong coupling a		$\alpha_s  (m_Z)$	0.1100(10)			
Top quark pole mass		$m_t$	$173.34(2.28) \mathrm{GeV}$			
Local DM density		$ ho_0$	$0.2 - 0.8  { m GeV}  { m cm}^{-3}$			
Nuclear matri	ix el. (strange)	$\sigma_s$	$43(24)\mathrm{MeV}$			
Nuclear matri	ix el. (up + down	n) $\sigma_l$	$58(27) \mathrm{MeV}$			

# Likelihoods

- Nuisance parameter likelihoods (SM, local halo model, nuclear matrix elements)
- DM relic density as upper bound
- DM Indirect detection
  - Gamma rays: Fermi-LAT (dwarf spheriodal galaxies)
  - Neutrinos from DM annihilation in the Sun: IceCube79
- DM Direct detection:
  - · XENON100 (2012)
  - LUX (2016)
  - Panda-X (2016)
  - PICO (2015)
  - SuperCDMS (2014)
  - SIMPLE (2014)

- Electroweak precision observables
  - W mass
  - muon g-2
- 59 flavour observables
- Higgs mass and signal strengths
- SUSY cross section limits from LEP
- SUSY searches at LHC (simulated)
  - 0 lepton searches (Run I & II, ATLAS & CMS)
  - Stop searches (Run I, ATLAS & CMS)
  - 2 & 3 lepton searches (Run I, ATLAS & CMS)
  - Monojet search (Run I, CMS)





ıax



- We impose relic density likelihood as an upper limit
- Higgsino-dominated neutralino saturates relic density for masses ~1 TeV
- Can have combined higgsino co-annihilation and heavy Higgs funnel above 1 TeV



- Cross-section scaled according to predicted relic density
- Chargino co-ann. and Higgs funnel regions can be fully probed by future DD
- Preferred stop co-ann region difficult to probe for DD, ID and LHC (Hope to probe low-mass end of the stop-coann region at the LHC)
- Smallest cross-sections due to fine-tuned cancellations in tree-level matrix elements (Expect such cancellation to be spoiled by loop corrections)



### Weak-scale MSSM results

## Parameters and likelihoods

Parameter	Minimum	Maximum	Priors		
$A_{u_3}(Q)$	$-10\mathrm{TeV}$	$10\mathrm{TeV}$	flat, hybrid		
$A_{d_3}(Q)$	$-10\mathrm{TeV}$	$10\mathrm{TeV}$	flat, hybrid		
$M^2_{H_u}(Q)$	$-(10\mathrm{TeV})^2$	$(10 \mathrm{TeV})^2$	flat, hybrid		
$M_{H_{d}}^{2^{u}}(Q)$	$-(10\mathrm{TeV})^2$	$(10 \mathrm{TeV})^2$	flat, hybrid		
$m^2_{ ilde{f}}( ilde{Q})$	0	$(10\mathrm{TeV})^2$	flat, hybrid		
$M_2(Q)$	$-10\mathrm{TeV}$	$10\mathrm{TeV}$	split; flat, hybrid		
$ an \beta(m_Z)$	3	70	flat		
$\operatorname{sgn}(\mu)$	+		fixed		
Q	$1\mathrm{Te}$	eV	fixed		

- 7 MSSM parameters + 5 nuisance parameters
- Assume GUT-inspired relation on gaugino mass parameters:

$$\frac{3}{5}\cos^2\theta_{\rm W}M_1 = \sin^2\theta_{\rm W}M_2 = \frac{\alpha}{\alpha_{\rm s}}M_3$$

Same likelihoods as for the GUT-scale models

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•





- Best fit point in chargino co-annihilation region (chargino/neutralino mass ~260 GeV)
- Mass difference < 10 GeV (challenging for LHC)</li>
- Under-abundant relic density
- Entire chargino co-ann. and light Higgs funnel regions will be probed by future DD

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Anders Kvellest $\overline{a}d^0$ 

### Other models



# 5. Summary and outlook

# Summary and outlook

#### · GAMBIT is public - try it out!

- GAMBIT Community: a network of users & collaborators
- If you find a bug, please tell us (preferably via github)

#### • Help us extend GAMBIT

- Is your code useful for global fits? Why not create a GAMBIT interface?
- · Detailed instructions and examples in the manual and source code

#### First physics results

- Singlet DM
- · GUT-scale SUSY
- Weak-scale MSSM7

#### More results coming soon

Axions, Higgs portal dark matter, light EW-gauginos, right-handed neutrinos...

### Future plans

- More models! More likelihoods!
- CosmoBit: cosmological models and observables
- · GAMBIT 2.0: Interface with Lagrangian-level tools for automatic code generation

# All results publicly available

### Results available on zenodo.cern.ch

- Parameter point samples (hdf5 files)
- GAMBIT input files for all scans
- Example plotting routines

### Links at gambit.hepforge.org/pubs



# Getting started with GAMBIT

### **Clone git repository from GitHub**

• github.com/patscott/gambit 1.1

### **Download tarballs**

<u>hepforge.org/downloads/gambit</u>

### **Pre-compilied version with Docker**

docker run -it jmcornell/gambit

### See quick start guide in arXiv:1705.07908

# Bonus material

# GAMBIT 2

### Extension to model building

- GAMBIT Universal Model (GUM) files
- Interface to Lagrangian-level tools
- Code generation for spectra, cross sections, ...



- 1. Add the model to the **model hierarchy**:
  - Choose a model name, and declare any parent model
  - Declare the model's parameters
  - Declare any translation function to the parent model

```
#define MODEL NUHM1
#define PARENT NUHM2
   START_MODEL
   DEFINEPARS(M0,M12,mH,A0,TanBeta,SignMu)
   INTERPRET_AS_PARENT_FUNCTION(NUHM1_to_NUHM2)
#undef PARENT
#undef MODEL
```

2. Write the translation function as a standard C++ function:

```
void MODEL_NAMESPACE::NUHM1_to_NUHM2 (const ModelParameters &myP, ModelParameters &targetP)
{
    // Set M0, M12, A0, TanBeta and SignMu in the NUHM2 to the same values as in the NUHM1
    targetP.setValues(myP,false);
    // Set the values of mHu and mHd in the NUHM2 to the value of mH in the NUHM1
    targetP.setValue("mHu", myP["mH"]);
    targetP.setValue("mHd", myP["mH"]);
}
```

3. If needed, declare that existing module functions work with the new model, or add new functions that do



### Adding a new observable/likelihood to GAMBIT

Adding a new module function is easy:

- 1. Declare the function to GAMBIT in a module's rollcall header
  - Choose a capability
  - Declare any **backend requirements**
  - Declare any **dependencies**
  - Declare any specific allowed models
  - other more advanced declarations also available

```
// A tasty GAMBIT module.
#define MODULE FlavBit
START MODULE
                                                 // Observable: BR(K->mu nu)/BR(pi->mu nu)
  #define CAPABILITY Rmu
  START CAPABILITY
                                                 // Name of a function that can compute Rmu
    #define FUNCTION SI_Rmu
    START_FUNCTION(double)
                                                 // Function computes a double precision result
    BACKEND_REQ(Kmunu_pimunu, (my_tag), double, (const parameters*)) // Needs function from a backend
   BACKEND OPTION( (SuperIso, 3.6), (my tag) )
                                                                     // Backend must be SuperIso 3.6
   DEPENDENCY(SuperIso_modelinfo, parameters)
                                                 // Needs another function to calculate SuperIso info
    ALLOW_MODELS(MSSM63atQ, MSSM63atMGUT)
                                                 // Works with weak/GUT-scale MSSM and descendents
    #undef FUNCTION
  #undef CAPABILITY
```

 Write the function as a standard C++ function (one argument: the result)



# Scalar singlet DM (2+13 parameters)

**GAMBIT** 1.0.0 **GAMBIT** 1.0.0 Profile likelihood ratio  $\Lambda$ 0 0 -1-1LHC (h decay  $\log_{10} \lambda_{hS}$  $\log_{10} \lambda_{hS}$ 0.6-20.4 $\mathcal{L}/\mathcal{L}_{\mathrm{ma}}$ -3-30.2Scalar singlet Scalar singlet Prof. likelihood Prof. likelihood AMBI 3.5505560 65 2.02.53.0 $\log_{10}(m_S/\text{GeV})$  $m_S$  (GeV)

(From Pat Scott)

Simplest BSM example:  $\mathcal{L}_S = -\frac{\mu_S^2}{2}S^2 - \frac{\lambda_{hs}}{2}S^2H^{\dagger}H + \dots$ 

All dark matter signals consistently scaled for predicted abundance

# Scalar singlet DM (2+13 parameters)

(from Felix Kahlhoefer)

### Assessing fine-tuning with Bayesian scans

- In case of a non-observation, experimental data will push WIMP models into more and more finely tuned regions of parameter space
- How do we assess whether WIMPs remain viable in spite of such tuning?
- Possible answer: Penalise fine-tuning with Bayesian statistics



## SUSY results

### **Definition of coloured regions**

- stau co-annihilation:  $m_{\tilde{\tau}_1} \leq 1.2 \, m_{\tilde{\chi}_1^0}$ ,
- stop co-annihilation:  $m_{\tilde{t}_1} \leq 1.2 \, m_{\tilde{\chi}_1^0}$ ,
- chargino co-annihilation:  $\tilde{\chi}_1^0 \ge 50\%$  Higgsino,
- $-A/H\text{-funnel: } 1.6 \, m_{\tilde{\chi}_1^0} \le m_{\text{heavy}} \le 2.4 \, m_{\tilde{\chi}_1^0},$

### GUT-scale results

Muon g-2





- Stop co-ann. region at large, negative trilinear coupling
- Small impact of (simple) check for charge- and colour-breaking minima



# MSSM7 results

### Chargino-netrualino mass plane



Fig. 8: Left: Profile likelihood in the  $\tilde{\chi}_1^{\pm} - \tilde{\chi}_1^0$  mass plane. Centre: Sub-regions within the 95% CL profile likelihood region, coloured according to mechanisms by which the relic density constraint is satisfied. The regions shown correspond to neutralino co-annihilation with charginos, stops or sbottoms, and resonant annihilation through the light or heavy Higgs funnels. Superimposed in red is the latest CMS Run II simplified model limit for  $\tilde{\chi}_1^{\pm} \tilde{\chi}_1^0$  production and decay with decoupled sleptons [210]. This limit should be interpreted with caution (see main text for details). Right: The same information as the central plot, but zoomed into the low-mass region. Note that, although the CMS limit appears to have excluded part of the chargino co-annihilation region, this is a binning effect. One should instead refer to the plot of the  $\tilde{\chi}_1^{\pm} - \tilde{\chi}_1^0$  mass difference in Fig. 7, which provides finer resolution on the mass difference in this region.

# MSSM7 results

### Stop/sbottom-netrualino mass planes



Fig. 10: Left: The profile likelihood ratio in the  $\tilde{b}_1 - \tilde{\chi}_1^0$  mass plane. Centre: Colour-coding shows mechanism(s) that allow models within the 95% CL region to avoid exceeding the observed relic density of DM. The regions shown correspond to neutralino co-annihilation with charginos, stops or sbottoms, and resonant annihilation through the light or heavy Higgs funnels. Right: The same information as the central plot, zoomed into the low-mass region.



Fig. 11: Left: The profile likelihood ratio in the  $\tilde{t}_1 - \tilde{\chi}_1^0$  mass plane. Centre: Colour-coding shows mechanism(s) that allow models within the 95% CL region to avoid exceeding the observed relic density of DM. The regions shown correspond to neutralino co-annihilation with charginos, stops or sbottoms, and resonant annihilation through the light or heavy Higgs funnels. Superimposed in red is the latest CMS Run II simplified model limit for stop pair production [211]. Right: The same information as the central plot, zoomed into the low-mass region.
## MSSM7 results

Muon g-2

